# agena >> 

## a programming language

primer and reference for version 2.36. 1
by alexander walz
January 29, 2023
agena Copyright 2006 to 2023 by alexander walz, rhineland.
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The latest release of Agena can be found at http://sourceforge.net/projects/agena.
This manual has been created with Lotus Word Pro 98 running on Sun Microsystems VirtualBox with Microsoft Windows 2000, yWorks yEd Graph Editor, and PDF Creator.

## Credits

## The Sources

Agena has been developed on the ANSI C sources of Lua 5.1, written by Roberto lerusalimschy, Luiz Henrique de Figueiredo, and Waldemar Celes. Used by their kind permission back in 2006.

## Chapter 7: Standard Library documentation

A substantial portion of Chapter 8 has been taken from the Lua 5.1 Reference Manual written by Roberto lerusalimschy, Luiz Henrique de Figueiredo, and Waldemar Celes. Used by kind permission.

## environ.anames

environ.anames has been invented by Joe Riel, put to the Maple community back in the early nineties.

## case of statement

The original code has been written by Andreas Falkenhahn and posted to the Lua mailing list on September 01, 2004. In Agena, the functionality has been extended to check multiple values in the of branches.

## skip statement

The skip functionality for loops has been written by Wolfgang Oertl and posted to the Lua Mailing List on September 12, 2005.
environ.globals base library function
The original Lua and C code for environ.globals has been written by David Manura for Lua 5.1 in 2008 and published on www.lua.org. The C source has been changed so that in Agena, C functions are no longer checked.
mkdir, chdir, and rmdir functions in the os library
These functions are based on code taken from the `lposix.c` file of the POSIX library written by Luiz Henrique de Figueiredo for Lua 5.0. These functions are themselves based on the original ones written by Claudio Terra for Lua 3.x.

## No automatic auto-conversion of strings to numbers

was inspired by Thomas Reuben's no_auto_conversion.patch available at lua.org.

## Kilobyte/Megabyte Number Suffix ('k', 'm')

taken from Eric Tetz's k-m-number-suffix.patch available at lua.org.

## Binary and octal numbers ('Ob', 'Oo')

taken from John Hind's Lua 5.1.4 patch available at lua.org.

## Integer division

taken from Thierry Grellier's newluaoperators.patch available at lua.org.
math.fraction
was originally written in ANSI C by Robert J. Craig, AT\&T Bell Laboratories.

The math library functions eps, epsilon, exponent, issubnormal, mantissa, math.frexp, math.nextafter, math.wrap, modf, round, zerosubnormal, cis, math.sincos, arctan, arctan2, sin, cos, +++ and -- operators
use a modified versions of $C$ functions that have originally been published by Sun Microsystems with the fdllibm IEEE 754 floating-point C library. See Appendix B3 for the licence.

## calc.diff

based on Conte and de Boor's `Coefficients of Newton form of polynomial of degree \(3^{`}\).

Advanced precision algorithm used in for/to loops, sumup, calc.fsum, linalg.trace, stats.amean, factory.count, stats.cumsum, and stats.sumdata.

The method to prevent round-off errors in iterations with non-integral step sizes has been developed by William Kahan and published in his paper `Further remarks on reducing truncation errors` as of January 1965. Agena in some cases uses a modified version of the Kahan algorithm developed by Kazufumi Ozawa, published in his paper `Analysis and Improvement of Kahan's

Summation Algorithm`. Especially the statistics function use the Kahan-Babuška variant described by Andreas Klein in his study `A generalized Kahan-Babuška-Summation-Algorithm `.

## calc.minimum, calc.maximum

use the subroutine calc.fminbr originally written by Dr. Oleg Keselyov in ANSI C which implements an algorithm published by G. Forsythe, M. Malcolm, and C. Moler, `Computer methods for mathematical computations`, M., Mir, 1980, page 202 of the Russian edition.

## bernoulli, besselj, bessely,euler, lambda

are completely or largely based on the functions originally written in FORTRAN by Shanjie Zhang and Jianming Jin, Computation of Special Functions, Copyright 1996 by John Wiley \& Sons, Inc. Used by Jianming Jin's kind permission.

## Graphics

The graphical capabilities of Agena in the Solaris, Linux, Mac, and Windows versions have been made possible through a Lua binding of Alexandre Erwin Ittner to the g2 graphical library which has been written by Ljubomir Milanovic and Horst Wagner.

## ADS package

The core ANSI C functions to create, insert, delete and close the database have been written by Dr. F. H. Toor.

## MAPM binding

Mike's Arbitrary Precision Math Library has been written by Michael C. Ring. See Appendix B6 for the licence.

The MAPM Agena binding is an adaptation of the Lua binding written by Luiz Henrique de Figueiredo, put to the public domain.

## Year 2038 fix for 32-bit machines

was written by Michael G. Schwern, and has been published under the MIT licence at http://github.com/schwern/y2038.

## gzip package

and its description of the binding has originally been written and published under the MIT licence by Tiago Dionizio for Lua 5.0.

## Internal string concatenation

Some internal initialisation routines use a C function written by Solar Designer placed in the public domain.

Functions arctan, expx2, gamma, Ingamma, calc.Ai, calc.Bi, calc.dawson, calc.dilog, calc.Ci, calc.Chi, calc.En, calc.fresnelc, calc.fresnels, calc.ibeta, calc.igamma, calc.igammc, calc.invibeta, calc.polylog, calc.Psi, calc.Si, calc.Shi, calc.Ssi, calc.zeta, stats.gammad, stats.gammadc, and stats.invnormald
use algorithms written in ANSI C by Stephen L. Moshier for the Cephes Math Library Release 2.8 as of June, 2000. Copyright by Stephen L. Moshier.
erf, erfc, inverf, inverfc, calc.intde, calc.intdei, calc.intdeo
These functions use procedures originally written in C by Takuya Ooura, Kyoto, Copyright(C) 1996 Takuya OOURA: "You may use, copy, modify this code for any purpose and without fee."
math.random

The algorithm used to compute random numbers has been written by George Marsaglia and published on en.wikipedia.org.

## io.anykey

The Linux version uses code written by Johnathon in 2008 which was published under the MIT licence.

## xBASE file support

The xbase package is a binding to xBASE functions written by Frank Warmerdam in ANSI C for the Shapelib 1.2.10 and 1.3.0 libraries. The Shapelib library has been published under the MIT licence.

## The net package

Most of the functions are based on Jürgen Wolf's $C$ examples published in his book `C von A bis Z`, 3rd Edition, Galileo Computing, Bonn, 2009.
`Beej's Guide to Network Programming, Using Internet Sockets`, written by Brian "Beej Jorgensen" Hall, was of great help. Some of the net functions use part of Mr. Hall's public domain code published in his tutorial. Copyright © 2009 Brian "Beej Jorgensen" Hall.

Studying the code of the LuaSocket 2.0.2 package, Copyright © 2004-2007 by Diego Nehab, and published under the MIT licence, was very worthwhile.

## strings.dleven

The implementation of Damerau-Levenshtein Distance is a blend of Code written by Lorenz and Anders Sewerin Johansen.

## utils.readxml

The original version of the core XML parser has been written in Lua 5.1 by Roberto Ierusalimschy, published on LuaWiki.
utils.decodeb64 and utils.encodeb64
The Base64 functions have been originally written in pure ANSI C by Bob Trower, Copyright (c) 2001, published under the MIT licence.

## printf

was taken from the compat.lua file shipped with the Lua 5.1 sources published under the MIT licence.
.. operator and \{\} indexing are based on code written by Sven Olsen, published in Lua Wiki/Power Patches.

## copy

The deep copying mechanism has originally been written by Kurt Jung and by Aaron Brown for Lua, and published in their book 'Beginning Lua Programming', Wiley Publishing, Indianapolis, Indiana, 2007, page 151.

## os.getenv, os.setenv, os.environ

have been written by Mark Edgar, Copyright 2007, published under the MIT licence, and were taken from http://lua-ex-api.googlecode.com/svn.

## bags package

The idea and its core implementation - ported to C - has been taken from the book `Programming in Lua` by Roberto lerusalimschy, 2nd Edition, Lua.org, p. 102.

## xml package

The xml package actually is the LuaExpat binding to the expat library with some few Agena-specific non-OOP modifications. LuaExpat 1.0 was designed by Roberto lerusalimschy, André Carregal and Tomás Guisasola as part of the Kepler Project which holds its copyright. The implementation was coded by Roberto lerusalimschy, based on a previous design by Jay Carlson.

LuaExpat development was sponsored by Fábrica Digital and FINEP.
bintersect, bminus, bisequal, stats.obcount
The algorithm for binary comparison has been taken from Niklaus Wirth's book, `Algorithmen und Datenstrukturen mit Modula-2`, 4th ed., 1986, p. 58.
linalg.mulrow, linalg.mulrowadd, stats.deltalist, stats.cumsum, stats.colnorm, stats.rownorm, stats.sumdata

These functions have been inspired by the deltaList, cumulativeSum, centralDiff, colNorm, rowNorm, mrow, and mrowdd functions available on the TI-Nspire ${ }^{\text {TM }}$ CXCAS.

## linalg.scale, stats.scale

is a port of function REASCL, included in the ALGOL 60 NUMAL package published by The Stichting Centrum Wiskunde \& Informatica (Stichting CWI) (legal successor of Stichting Mathematisch Centrum) at Amsterdam. Original authors:
T. J. Dekker, W. Hoffmann; contributors: W. Hoffmann, S. P. N. van Kampen.

## OS.now

uses $C$ routines of the IAU Standards of Fundamental Astronomy (SOFA) Libraries, See Appendix B5 for the licence.

Functions calc.clampedspline, calc.clampedsplinecoeffs, calc.interp, calc.neville, calc.newtoncoeffs, calc.nokspline, calc.noksplinecoeffs
use C++ routines (ported to C) provided or written by Professor Brian Bradie, Department of Mathematics, Christopher Newport University, VA, to the course `An Introduction to Numerical Analysis with Applications to the Physical, Natural and Social Sciences`. There have been no copyright remarks, so at least Agena's MIT licence is not applicable to the source files 'interp.c`and`interp.h`.

## stats.smallest

is based on N . Devillard's C implementation of an algorithm published in various books written by Niklaus Wirth, published for example in `Algorithmen und Datenstrukturen mit Modula-2`. Mr. Devillard put his code in the public domain.
strings.isiso* and strings.iso* functions
use ISO 8859/1 Latin-1 bit vector tables taken from the entropy utility ENT written by John Walker, January 28th, 2008, Fourmilab, put in the public domain.

## astro.moonriseset

Uses C functions Copyright © 2010 Guido Trentalancia IZ6RDB. This program is freeware - however, it is provided as is, without any warranty.

## astro.phase

Uses C functions taken from: http://www.voidware.com/moon_phase.htm. There have not been any copyright remarks.

## astro.sunriseset

Uses C functions written as DAYLEN.C, 1989-08-16. Modified to SUNRISET.C, 1992-12-01, (c) Paul Schlyter, 1989, 1992. Released to the public domain by Paul Schlyter, December 1992.

## astro.cdate \& astro.jdate

uses $C$ routines of the IAU Standards of Fundamental Astronomy (SOFA) Libraries, See Appendix B5 for the licence.

## strings.utf8size

of the core C code procedure has been written by mpezO, published at StackOverflow.

## strings.isutf8

of the core C code procedure has been written by written by Christoph, published on StackOverflow.
strings.isotolatin \& strings.isotoutf8
of the core C code procedures have been written by Nominal Animal published on StackOverflow.

## strings.glob

uses C code written by Arjan Kenter, Copyright 1995, Arjan Kenter.

## stats.sorted

uses an iterative Quicksort algorithm written by Nicolas Devillard in 1998, put to the public domain.
$/ \%, * \%,+\%,-\%, \% \%$ operators, math.dd, math.dms, math.splitdms, polar, stats.cdf, stats.numbcomb, stats.numbperm, and stats.pdf
have been inspired by the $\mathrm{TI}^{\text {TM }}-30$ ECO RS, $\mathrm{TI}^{\text {TM }}-30 \mathrm{X}$ Pro, Sharp ${ }^{\text {TM }}$ EL-W531XG and HP 35s pocket calculators.

## E, Exp

as a constant, defines the former Maple V Release 3 implementation of $\mathrm{E}=$ $\exp (1)=2.71828182845904523536$.

## Complex arithmetic

for various mathematical functions and operators has been implemented by primarily using Maple V Release 3, Maple V Release 4, and Maple 7.

## io.getclip and io.putclip

are based on C code written by banders7, published on Daniweb.

## try/catch statement

has been invented and written by Hu Qiwei for Lua 5.1 back in 2008, and has been extended for Agena.

## debug.getinfo

the 'a'/arity extension has been written by Rob Hoelz in 2012.
calc.polyfit \& calc.linterp uses $C$ code published by Harika in 2013 at http://programbank4u.blogspot.de.

## Review of the Agena interpreter at the Web

Many thanks to softpedia.com for the very kind critique and fine ranking.
linalg.det \& linalg.inverse
are based on C functions written by Edward Popko published on Paul Bourke's website at http://paulbourke.net/miscellaneous.
redo \& relaunch
have been inspired by the Ruby programming language.

## linalg.gsolve

is based on C functions written by Edward Popko and Alexander Evans; for the former see the link above, and for the latter the following address: http://www.dailyfreecode.com/code/basic-gauss-elimination-method-gauss-29 49.aspx.

## calc.simaptive and linalg.ludecomp

are based on C functions written by RLH, available at http://www.mymathlib.com, Copyright © 2004 RLH. All rights reserved.
$\sim=, \sim<>$, approx, qmdev
use methods developed by Donald Knuth.

## calc.Ei

uses a combination of C algorithms written by Stephen L. Moshier and RLH.

## linalg.rref

is based on a C\# function published at http://rose\#tacode.org.

## linalg.forsub

is based on an algorithm explained by Timothy Vismor found on his site http://vismor.com.

## cordic package

is based on a C package written by John Burkardt, taken from http://people.sc.fsu.edu/~jburkardt/c_src/cordic/cordic.c, with modifications using Maple V Release 4 and TI-Nspire CX CAS. Sources provided separately.
libusb binding
is based on lualibusbl - Lua binding for libusb 1.0, written by Tom N Harris. See: http://lualibusbl.googlecode.com.

## stats.extrema

is the Agena port of the `peakdet` function written by Eli Billauer for MATLAB.
mdf, xdf
have been inspired by the Sharp PC-1403H pocket computer.

## os.cpuload, os.drivestat, os.getenv, os.realpath \& os.setenv

are based mainly on procedures taken from Nodir Temirkhodjaev's LuaSys package.

## utils.readini

uses modified $C$ sources written by Nicolas Devillard for his iniparser 3.1 package.

## Various OS/2 operating system functions

have been made possible by the website http://www.edm2.com/os2api.

## Ilist and heaps packages

The C implementation of singly and doubly-linked lists and AVL trees has been accomplished by reading Michal Kottman's tip at nabble.com on how to code new data structures using Lua's userdata and how to anchor values into the registry. The algorithms themselves have originally been written in C by Martin Broadhurst.

## stats.dbscan \& stats.neighbours

The dbscan algorithm has been invented by Martin Ester, Hans-Peter Kriegel, Jörg Sander, and Xiaowei Xu, published at University of Munich. The Agena port is based on a Matlab implementation written by Peter Kovesi, Centre for Exploration Targeting, The University of Western Australia, with stats.neighbours a C-based split-off.

## hashes package

uses code published by RSA Data Security, Inc. Copyright (C) 1990. All rights reserved. For further credits, please see the hashes.c file in the Agena sources.
math.ceilpow2 and math.ilog 10
use code presented by Sean Eron Anderson at his `Bit Twiddling Hacks` webpage http://graphics.stanford.edu/~seander/bithacks.html.

## os.cdrom, os.ismounted, os.isremovable, os.isvaliddrive

The Windows versions are based on code published at MSDN, page http://support.microsoft.com/kb/165721\#. The Linux version of os.cdrom is based on Jürgen Wolf's C book `C von A bis Z`, 3rd Edition, Galileo Computing, Bonn, 2009. The OS/2 version of os.cdrom is based on code found on the OS/2 Hobbes FTP server at NMSU, left without any copyright remarks.

## os.terminate

The OS/2 version is largely based on Mark Kimes' public domain implementation.

## Os.monitor

The Linux version is based on Dave Drager+'s recommendation published at his blog.

## hypot2 and antilog ${ }_{n}$ operators

have been inspired by the Sinclair Scientific Programmable pocket calculator.
math.eps, stats.isall, stats.isany, and linalg.reshape functions have been inspired by Matlab.
stats.gmean
uses an algorithm taken from the COLT sources published by CERN, Geneva.
gdi.plotfn
has been improved by Slobodan from Serbia.

## oftype metamethod

to check structures at function invocation has been proposed by Slobodan from Serbia.
stats.durbinwatson, stats.standardise, and stats.sumdataln
have been inspired by the COLT package published by CERN, Geneva.
$\lll<$ and >>>> operators, bytes.arshift32, bytes.extract32, bytes.replace32
have been implemented using Lua 5.2 and 5.3 code and Rupert Tombs' arithmetic right-shift implementation.

## Chapter 6.24

is based on examples published at http://www.lua.org/pil/16.html.

## Exit and restart handling

via environ.onexit has been inspired by MuPAD 2.5.
with and related statements
are based on a Lua 5.1 power patch written by Peter Shook (`Unpack Tables by Name ').
math.dms
uses an algorithms proposed by user807566 on StackOverflow.

## case of boolean condition variant

has been inspired by the Go programming language.

## Numeric ranges in case/of clauses

have been inspired by the Fortran 90 programming language.
math.fma
for those platforms that do not provide a built-in fma C function, is based on a method proposed by Z boson on StackOverflow.

## math.signbit

for those platforms that do not provide a built-in signbit $C$ function, is based on a Sun Microsystems implementation.

## math.signbit

Its original version has been written by Jacob Rus for Lua, taken from: https://gist.github.com/jrus/3197011.

## math.wrap

Is based on Tim Cas' answer \#4633177 on StackOverflow and the restrictsymm function of the Julia programming language.

## Sinclair ZX Spectrum package

clones Spectrum ROM $Z 80$ assembler routines disassembled by Dr. Ian Logan and Dr. Frank O'Hara.

## math.eps

optionally uses a formula suggested by trashgod on StackOverflow to compute a small epsilon value that is suited for mathematical C double operations.

## dBASE version numbers

printed in the description of xbase.attrib have been taken from: http://stackoverflow.com/questions/3391525, answered by Les Paul.
round, mdf, and xdf
use an underlying C routine posted by Larry I Smith, see: https://bytes.com/topic/c/answers/521405-rounding-nearest-nth-digits.
math.cld, math.fld, math.flipsign, math.isqrt, math.Infact, and math.powmod
have been ported from or have been inspired by the corresponding functions written in the Julia programming language, published under the MIT licence.


#### Abstract

strings.appendmissing, strings.between, strings.chop, strings.chomp, strings.contains, strings.uncapitalise, strings.iswrapped, strings.wrap, and


 strings.wrapmissingare ports of StringUtils functions part of the Apache Commons Lang 3.5 API.
astro.hdate and os.date ('*sdn' format)
use C functions written by Scott E. Lee, see http://www.rosettacalendar.com.
hashes.mix64 and hashes.mix64to32
use Thomas Wang's C procedures, taken from gist.github/badboy/6267743.
times
is based on the corresponding Haskell function iterate.
for/until loops
have been inspired by COBOL.
math.sincos
uses Elliot Saba's sincos implementation.
math.accu
uses Julia Language's Kahan-Babuška-Neumaier compensated summation.
hashes.droot, hashes.parity, hashes.reflect
use Henry S. Warren's code published with his book `Hacker's Delight`.
hashes.pjw, hashes.rs, hashes.bp
are based on C functions written by Arash Partow.
map/@ extension to support function composition \& reduce
have been inspired by Slobodan's feedback and an excellent introduction to functional programming written by Mary Rose Cook.
bloom filter plus package
is based on C code created by Simon Howard, see Appendix B9 for ISC licence.
factory plus package
has been inspired by the `functools` package in Python 3.
strings.a64 and hashes.sha5 12
use C code from the musl-1.1.19 library, MIT licence.
? statement, prepend, linalg.iszero, linalg.isallones, thus indirectly satisfy have been inspired by the Axiom Computer Algebra System.

## getorset

has been inspired by the `getOrElseUpdate` operator in the Scala programming language.
if is operator and compound assignments, $+:=,:=$, etc.
have been inspired by Algol 68.
bytes.pack, bytes.packsize, bytes.unpack, tables.move, and the utf8 package have been taken from Lua 5.3.5 or Lua 5.4.0 RC 4 (utf8, move).

## GMP 6.1.2 port for OS/2

compiled by KO Myung-Hun has been used to compile the mp binding.

## dual package

uses definitions primarily found at blog.demofox.org and adl.stanford.edu.

## os.iterate

has been derived from listing published in `Programming in Lua` 2nd Ed., pp $271 \mathrm{f} .$, by Roberto Ierusalimschy.

## com package

is largely based on the LuaSys package v1.8, written by Nodir Temirkhodjaev.
assignments in conditions of while loops, if and case of statements
were inspired by Icon and C.

## duplicate parser warnings for duplicate local variable declaration

have originally been designed by Domingo Alvarez Duarte for Lua 5.1.
shift
has been written by StackOverflow user ryanpattison for Lua.
type anything and more or less constants
have been inspired by Maple.
erfcx, calc.scaleddawson, calc.w
use code written by Steven G. Johnson, October 2012, MIT licence.

## os.netuse, os.netsend \& os.netdomain

use code written by Antonio Escaño Scuri for the NTLua 3.0 package,
MIT licence.

## rings package

has been designed by Roberto lerusalimschy and Tomás Guisasola for Lua 5 as part of the Kepler Project. The implementation was originally coded by Tomás Guisasola. Rings development was sponsored by Fábrica Digital. MIT licence.
utils.decodeb85 and utils.encodeb85
The Base85 functions have been originally written in C by Rafa Garcia, Copyright
(c) 2016-2018, published under the MIT licence.
utils.decodea85 and utils.encodea85
The ASCll85 conversion functions have been written in C by Luiz Henrique de Figueiredo, placed in the public domain.
strings.pack, strings.packsize and strings.unpack
have been taken from Lua 5.4.4, Lua.org, PUC-Rio, MIT licence.

## bimaps package

has originally been written by Pierre 'catwell' Chapuis for Lua.
Copyright (C) 2013-2015 by Pierre Chapuis. MIT licence.

## heaps package

is based on a Lua package written by Geoff Leyland, New Zealand.
Copyright (c) 2008-201 1 Incremental IP Limited. MIT licence.

## aconv package

is based on the Lua-iconv 7 package for Lua 5.1, 2005-2011, MIT licence, written by Alexandre Erwin Ittner.

Finally, due to very kind help and feedback, in chronological order
Many thanks to the Lua team at PUC-Rio, Brazil, and to Agena users in Israel, Italy, Australia, Palestine, Poland, Serbia, the OS/2 community, and to users of other nations.

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Part One
Primer

Chapter One Introduction

## 1 Introduction

### 1.1 Abstract

Agena is a procedural programming language designed to be used in scientific, educational, linguistic, and many other applications, including scripting.

Agena provides real and complex arithmetic, graphics, efficient text processing, flexible data structures, intelligent procedures, package management, plus various multi-user configuration facilities.

Its syntax looks like very simplified Algol 68 with elements taken primarily from Maple, Lua and SQL. It has been implemented on the ANSI C sources of Lua 5.1 created by Roberto lerusalimschy, Luiz Henrique de Figueiredo, and Waldemar Celes.

Agena binaries are available for Solaris, Linux, Windows, OS/2, Mac OS X, Raspberry Pi , and DOS.

You may download Agena, its sources, and its manual from
http://sourceforge.net/projects/agena.

### 1.2 Features

Agena combines features of Lua 5, Maple, Algol 60, Algol 68, ABC, SQL, ANSI C and BASIC.

Agena provides all the common functionality found in imperative languages:

- statements,
- loops,
- conditions,
- procedures.

It also has extended programming features described later in this manual, such as:

- high-speed processing of extended data structures,
- fast string and mathematical operators,
- extended conditionals,
- abridged and extended syntax for loops,
- special variable increment, decrement and deletion statements,
- efficient recursion techniques,
- arbitrary precision mathematical libraries,
- a network package to exchange data over the Internet and LANs,
- easy-to-use package handling,
- and much more.

Like Lua, Agena is untyped and includes the following basic data structures: numbers, strings, booleans, tables, and procedures. In addition to these types, it
also supports Cantor sets, sequences, registers, pairs, complex numbers, linked lists, and multisets. With all of these types, you can build applications easily.

### 1.3 In Detail

Agena offers various flow control facilities such as

- if/elif/else conditions,
- case of/else conditions similar to C's switch/case statements,
- if operator to return alternative values,
- numerical for/from/to/downto/by loops with optional start, stop and step values, and automatic round-off error correction of iteration variables,
- combined for/while and for/until loops,
- for/in loops over strings and complex data structures,
- while and do/as loops similar to Modula's while and repeat/until iterators,
- do/od loops equal to the ones in Maple,
- a skip statement to prematurely trigger the next iteration of a loop,
- a break statement to prematurely leave a loop,
- a do nothing statement which does not do anything,
- fast and easy data type validation with the optional double colon facility in parameter lists.

Data types provided are:

- rational and complex numbers with extensions such as infinity and undefined,
- strings,
- booleans such as true, false, and fail,
- the null value depicting the absence of a value,
- multipurpose tables implemented as associative arrays to hold any kind of data, taken from Lua,
- Cantor sets as collections of unique items,
- sequences and registers, i.e. vectors, to internally store items in strict sequential order,
- pairs to hold two values or pass options to procedures,
- threads, userdata, and lightuserdata inherited from Lua.

For performance, most basic operations on these types have been built into the Agena kernel.

Procedures with full lexical scoping are supported, as well, and provide the following extensions:

- the << (args) -> expression >> syntax to easily define simple functions,
- user-defined types for procedures to allow individual handling,
- uder-defined types for tables, sets, sequences, registers and pairs,
- a facility to return predefined results,
- remember tables for high-speed recursion,
- closures which let functions remember their state, taken from Lua,
- the nargs system variable which holds the number of arguments actually passed to a procedure,
- metamethods to define operations for tables, sets, sequences, registers and pairs, inherited from Lua,
- OOP-style methods for tables,
- self-defined binary operators.

Some other features are:

- graphics in the Solaris, Mac, 32-bit Linux, Raspberry Pi, and Windows editions, provided by the gdi package,
- IPv4 networking with the Internet and LANs,
- functions to support fast text processing,
- configuration of user's environment via the Agena initialisation file,
- an easy-to-use package system also providing a means to both load a library and define short names for all package procedures at a stroke,
- the binio package to easily write and read files in binary mode,
- facility to store any data to a file and read it back later,
- undergraduate Calculus, Linear Algebra, and Statistics packages,
- enumeration and multiple assignment,
- transfer of the last iteration value of a numeric for loop to its surrounding block,
- scope control via the scope/epocs keywords,
- efficient stack programming facilities,
- bitwise operators,
- direct access to the file system,
- arbitrary precision mathematical libraries,
- dBASE, XML, CSV, INI, GZIP and TAR file support.

Agena includes all the packages that are part of Lua 5.1. Some of the very basic Lua library functions have been transformed to Agena operators to speed up execution of programmes. The Lua mathematical and string handling packages have been tuned and extended with new features.

Agena code is not compatible to Lua. Its C API, however, has been left unchanged and many new API functions have been added. As such, you can integrate any C package you have already written for Lua by just replacing the Lua- specific header files, see Chapter 17.

### 1.4 History

I have been dreaming of creating my own programming language for the last 35 years, with my first rather unsuccessful attempt on a Sinclair ZX Spectrum in the early 1980s.

Plans became concrete in 2005 when I learned Lua to write procedures for phonetic analysis and also learned ANSI C to transfer them into a C package. In autumn 2006 the first modifications of the Lua parser started with extensive modifications and extensions of the lexer, parser and the Lua Virtual Machine in summer 2007. Most of Agena's basic functionality had been completed in March

2008, followed by the first new data structure, Cantor sets, one month later, some more data structures, and a lot of fine-tuning and testing thereafter. Finally, in January 2009, the first release of Agena was published at Sourceforge.

Study of many books and websites on various programming languages such as Algol 68, Maple, Algol 60, and ABC, and my various ideas on the `perfect` language helped to conceive a completely new Algol 68-syntax based language with high-speed functionality for arithmetic and text processing.

You may find that at least the goal of designing a perfect language has not been met. For example, the syntax is not always consistent: you will find Algol 68-style elements in most cases, but also ABC/SQL-like syntax for basic operations with structures. The primary reason for this is that sometimes natural language statements are better to reminisce. I have stopped bothering about this inconsistency issue.

After almost four years of development, Agena 1.0 has been released in August 2010.

### 1.5 Origins

Most of all functionality stems from Lua, Maple and C. Some of my favourite additions to the Lua C sources include:

## Maple V Release 3 and later

- if/elif/else/fi, for/while, map, remove, select, selectremove, subs, with, readlib, package management, library.agn, agena.ini, read, save, substrings, Cantor sets and its operators, sequences, remember tables, in, nargs, op(s), restart, tables.indices, the linalg package, maybe all the pretty printers, argument type checks, :: type checks, and multiple :: type parameter checks, surely all mathematical functions and complex arithmetic, and much, much more.

The Maple language has been designed by Michael B. Monagan, Keith O. Geddes, K. M. Heal, George Labahn, and S. M. Vorkoetter for Waterloo Maple Inc./Maplesoft, Waterloo, Ontario. It is loosely based on Algol 68.

This is also why Agena looks a lot like Maple, and thus somewhat like:

## Algol 68

has many times been called the queen of all programming languages and Agena's

- case/of/esac control
has originally been introduced with Algol 68.


## Algol 60

- entier.

Algol 60 is the parent of Algol 68.

## Modula-2

- inc and dec.


## C

- printf, and most of Lua's system functions,
- compound operators such like c++, etc.

C actually is a descendent of Algol 68.

## COBOL

- for/until loops.


## Sinclair ZX Spectrum BASIC

- clear, cls, int.


## SQL and $\mathbf{A B C}$

- insert/into and thus indirectly create, delete/from, and pop/from.


## PL/I and REXX

- Some of the strings library functions have been taken from PL/I and REXX.


## Eiffel

- Checking the return type of procedures with the proc(...) :: <typename> statement has been taken from this language.


## Ada

- inspired the skip when and break when statements.


## Chapter Two

## Installing \& Running Agena

## 2 Installing and Running Agena

### 2.1 Sun Solaris 10

In Sun Solaris, and some of its forks, e.g. OpenSolaris, put the gzipped Agena package into any directory. Assuming you want to install the Sparc version, uncompress the package by entering:

```
> gzip -d agena-x.y.z-soll0-sparc-local.gz
```

Then install it with the Solaris package manager:

```
> pkgadd -d agena-x.y.z-sol10-sparc-local
```

This installs the executable into the /usr/local/bin folder and the rest of all files into /usr/agena. The/usr/agena/lib directory is called the `main Agena library folder`.

Make sure you have the expat, fontconfig, freetype, libg2, libgmp-10, jpeg, libgcc, libgd, libiconv, libintl, libncurses, libmpfr-6, libpng, readline, (lib)xpm, and zlib libraries installed. From the command line, type agena and press RETURN.


Image 1: Start-up message in Solaris
The procedure for OpenSolaris and Solaris for x86 CPUs is the same. The package always installs as smCagena.

### 2.2 Linux

On Debian based x86 distributions, install the 32-bit Stretch deb installer by typing:

```
> sudo dpkg -i --force-all agena-x.y.z-raspi.stretch.i386.deb
```

On Red Hat systems, install the rpm distribution by typing as root:

```
> rpm -ihv --nodeps agena-x.y.z-linux-i386.rpm
```

This installs the executable into the /usr/local/bin folder and the rest of all files into /usr/agena. The /usr/agena/lib directory is called the `main Agena library folder`.

Note that you must have the expat, fontconfig, freetype, libg2, libgmp-10, libjpeg62, libgcc, libgd (version 2.0.36 or earlier), libiconv, libintl, libmpfr-6, libncurses, libpng12, libreadline6, (lib)xpm, x11proto-xext-dev and zlib libraries installed before.

If you have no jpeg library installed on your system, also install libjpeg62. Warning: overinstalling libjpeg*turbo with libjpeg62 may totally corrupt your system, as happened on a Raspberry Pi.

From the command line, type agena and press RETURN.
The name of the Linux package is agena.

### 2.3 Windows

Just execute the Windows binary installer, and choose the components you want to install.

Make sure you either let the installer automatically set the AGENAPATH environment variable containing the path to the main Agena library folder (the default) or set it later manually in the Windows Control Panel, via the `System` menu.


Check the components you want to install and uncheck the components you don't want to install. Click Next to continue.

Select the type of install:
Or, select the optional components you wish to install:


Nullsoft Install Systern v2,46


Image 2: Leave the framed settings checked

WARNING: If your system environment variable PATH already consists of 8,000 or more characters, do NOT select the 'Append path to Agena binary to PATH' option, as this might corrupt the PATH setting.

You may start Agena either via the Start Menu, or by typing agena in a shell.


Image 3: Start-up message in Windows
If you do not have administrative rights to start the installer, or want to use the interpreter on a removable stick, download the portable version of Agena available at Sourceforge.net and study the readme.w32 file.

For the portable version:
In a NT shell, create a folder called 'agena' anywhere on your drive, change into this directory and decompress the archive into this folder presenving the subdirectory structure of the ZIP file.

Only if you use Windows 2000 or earlier: Now set the environment variable AGENAPATH, referring to the main Agena library `agena.lib` file. For example, if you install Agena into the folder c:\agena, the library files will reside in the c:\agena\lib subfolder, so enter the following statement:

```
set AGENAPATH=c:/agena/lib
```

Note the forward slashes in the path and the system variable name in capital letters.

In XP and later, Agena determines the path to the main Agena library automatically, provided you do not alter the subdirectory structure of the portable distribution.

### 2.4 OS/2 Warp 4, eComStation and ArcaOS

The WarpIN installer allows you to choose a proper directory for the interpreter, and then installs all files into it.

The dependencies are: WarpIN \& kLIBC \& ncurses; install using YUM:

```
yum install libc readline ncurses gmp
```

Make sure you either let the installer automatically set the environment variable called AGENAPATH containing the path to the main Agena library folder (the WarpIN default) by leaving the `Modify CONFIG.SYS' entry in the System Configuration window checked, or set it later by manually editing config.sys.

Just enter agena in a shell to run the interpreter, or double-click the Agena icon in the programme folder. Agena may require EMX runtime 0.9d fix 4 or higher in OS/2.

### 2.5 DOS

In DOS, create a folder called agena anywhere on your drive, change into this directory and decompress the agena.zip file into this folder preserving the subdirectory structure of the ZIP file.

Now set the environment variable agenapath in the autoexec.bat file. Use a text editor for this. For example, if you installed Agena into the folder c: \agena, and the library.agn file is in the lib subfolder, enter the following line into the autoexec.bat file:

```
set AGENAPATH=c:/agena/lib
```

Note the forward slash in the path and the variable name in capital letters.
Also append the path to the agena folder to the PATH system variable using backslashes, so that the entry looks something like this:

```
PATH C:\;C:\NWDOS;C:\AGENA\BIN
```

Although it is not necessary in FreeDOS 1.1 or later, at least with Novell DOS 7, you must install cwsdpmi.exe delivered with the DJPGG edition of GCC as a TSR programme before starting Agena. The binary can be found in the DJGPP distribution.

In order to always load this TSR when booting your computer, open the autoexec.bat file with a text editor. Assuming the cwsdPmi.Exe file is in the $\mathrm{c}: \backslash$ tools folder, add the following line:

```
loadhigh c:\tools\cwsdpmi.exe -p
```

Novell DOS's command line history works correctly on the Agena prompt.

### 2.6 Mac OS X 10.5 and above

Simply double-click the agena-x.y.z-mac.pkg installer in the file manager and follow the instructions. Do not choose an alternative destination for the package.

The Agena executable is copied into the /usr/local/bin folder, supporting files into /usr/agena, and the documentation to /Library/Documentation/Agena. The /usr/agena/lib directory is called the `main Agena library folder`.

Note that you may have to install the readline library before.
From the command line, type agena and press RETURN.

### 2.7 Agena Initialisation

When you start Agena, the following actions are taken:

1. The standard packages are initialised so that they become available to the user immediately.
2. All global values are copied from the _G table to its copy _origG, so that the restart function can restore the original environment if invoked.
3. The system variables libname and mainlibname pointing to the main Agena library folder and optionally to other folders is set by either querying the environment variable AGENAPATH or - if not set - checking whether the current working directory contains the string /agena or any other eligible folder name, building the path accordingly.

The main Agena library folder contains library files with file suffix agn written in the Agena language, or binary files with the file suffix so or dll originally written in ANSI C.

In UNIX, Mac OS X, and Windows, if the path could not be determined as described before, libname and mainlibname are by default set to /usr/agena/lib in UNIX and Mac OS X, and \%ProgramFiles\%\agena\lib in Windows, if these directories exist and if the user has at least read permissions for the respective folder. The libname variable is used extensively by the import and readlib functions that initialise packages. If it could not be set, many package functions will not be available.
4. Searching all paths in libname from left to right, Agena tries to find the standard Agena library library.agn and if successful, loads and runs it. The library.agn file includes functions written in Agena that complement the C libraries. If the standard Agena library could not be found, a warning message, but no error, is issued. If there are multiple library. agn files in your path, only the first one found is initialised.
5. The global Agena initialisation file - if present - with file name agena.ini is searched by traversing all paths in libname from left to right. As with library.agn, this file contains code written in Agena that an administrator may customise with pre-set variables, auxiliary procedures, etc. If the initialisation file does not exist, no error will be issued. If there are multiple Agena initialisation files
in your libname path, only the first one found is processed.
In UNIX based systems, the name of the initialisation file may also be .agenainit. If both an .agenainit and an agena.ini file exist, then .agenainit is read first.
6. The user's personal Agena initialisation file called agena.ini (optionally . agenainit in UNIX) - if present - is searched in the user's home folder and run. If this initialisation file does not exist, no error will be issued. After that the Agena session begins. See Appendix A6 for further details.

In UNIX based systems, if both the .agenainit and agena.ini files exist, then . agenainit is read first.
7. The path to the current user's home directory is assigned to the environ.homedir environment variable.

### 2.8 Installing Library Updates

Sometimes, library updates are provided at Sourceforge if library functions written in the Agena language have been patched or also if new functions written in the language have been developed.

For instructions on how to easily install such an update, have a look at the libupdate.readme file residing on the root of the agena-x.y.z-updaten.zip archive which can be downloaded from the Binaries Agena Sourceforge folder.

In general, the updates can be installed by just unpacking the respective ZIP archive into the main Agena folder.

A library update can be installed on every supported operating system, but you may need administrative rights.

## Chapter Three

Overview

## 3 Summary

Let us start by just entering some commands that will be described later in this manual so that you can get acquainted with Agena as fast as possible. In this chapter, you will also learn about some of the basic data types available.

On UNIX-based systems or DOS, type agena in a shell to start the interpreter. On OS/2 and Windows, either click the Agena icon in the programme folder or type agena in a shell.

### 3.1 Input Conventions in the Console Edition

Any valid Agena code can be entered at the console with or without a trailing colon or semicolon:

- If an expression is finished with a colon, it is evaluated and its value is printed at the console.
- If the expression ends with a semicolon or neither with a colon nor a semicolon, it is evaluated, but nothing is printed on screen.

You may optionally insert one or more white spaces between operands in your statements.

- To display results in the output window, pass the respective expression to the print function, e.g.:

```
print(exp(2*Pi*I)) Or a := 1; print(a);
```

You may optionally insert one or more white spaces between operands in your statements.

### 3.3 Getting Familiar

Assume you would like Agena to add the numbers 1 and 2 and show the result. Then type:

```
> print(1+2)
3
```

If you want to store a value to a variable, type:

```
> c := 25;
```

Now the value 25 has been stored to the name c, and you can refer to this number by the name c in subsequent calculations.

Assume that c is $25^{\circ}$ Celsius. If you want to convert it to Fahrenheit, enter:

```
> print(1.8*c + 32);
7 7
```

There are many functions available in the kernel and in various libraries. To compute the inverse sine, use the arcsin operator:

```
> print(arcsin(1));
1.5707963267949
```

The root function determines the $n$-th root of a value:

```
> print(root(2, 3));
1.2599210498949
```


### 3.4 Useful Statements

Instead of using print, you may also output results by entering an expression and completing it with a colon:

```
> root(2, 3):
1.2599210498949
```

The global variable ans always holds the result of the last statement you completed with a colon.

```
> ln(2*Pi):
1.8378770664093
```

> ans:
1.8378770664093

The console screen can be cleared by just entering the keyword cls:
> cls
The restart statement resets Agena to its initial state, i.e. clears all variables you defined in a session.

```
> restart
```

The bye statement quits a session - you can also press CTRL+C, alternatively.

```
> bye
```

If you would like to automatically run a procedure before restarting or quitting Agena, just assign this procedure to the name environ.onexit. See the description of the bye statement in Chapter 8 for more details.

If you prefer another Agena prompt instead of the predefined one, assign for example:

```
> _PROMPT := 'Agena$ '
Agena$_
```

You may put this statement into the initialisation file in the Agena library or your home folder, if you do not want to change the prompt manually every time you start Agena. See Appendix A6 for further detail.

```
Agena$ restart;
```


### 3.5 Assignment and Unassignment

As we have already seen, to assign a number, say 1, to a variable called a, type:

```
> a := 1;
```

Variables can be deleted by assigning null or using the clear statement. The latter also immediately performs a garbage collection.

```
> a := null:
null
> clear a;
> a:
null
```


### 3.6 Arithmetic

Agena supports both real and complex arithmetic with the + (addition), (subtraction), * (multiplication), / (division) and ^ (exponentiation) operators:

```
> 1+2:
```

3

Complex numbers can be entered using the I constant or the ! operator:

```
> exp(1+2*I):
-1.1312043837568+2.4717266720048*I
> exp(1!2):
-1.1312043837568+2.4717266720048*I
```


### 3.7 Strings

A text can be put in single or double quotes:

```
> str := 'a string':
a string
```

Substrings are extracted by passing an index or index range:

```
> str[3], str[3 to 6]:
s stri
```

Concatenation, search, and replacement:

```
>str := str & ' and another one, too':
a string and another one, too
> instr(str, 'another'):
14
> replace(str, 'and', '&'):
a string & another one, too
```

There are various other string operators and functions available.

### 3.8 Booleans

Agena features the true, false, and fail constants to represent Boolean values. fail may be used to indicate a failed computation. The operators $<,>,=,<>,<=$, and $>=$ compare values and return either true or false. The operators and, or, not, nand, nor, xor and xnor combine Boolean values.

```
> 1 < 2:
true
> true or false:
true
```

You can also do arithmetic with numbers and Booleans where true depicts 1 and false, fail or null 0 . Also, applying the unary minus operator to Booleans will convert them to either the numbers 0 or -1 .

### 3.9 Tables

Tables are used to represent more complex data structures. Tables consist of zero, one or more key-value pairs: the key referencing to the position of the value in the table, and the value the data itself.

```
tbl := [
    1 ~ ['a', 7.71],
    2 ~ ['b', 7.70],
    3 ~ ['c', 7.59]
];
```

To get the subtable ['a', 7.71] indexed with key 1, and the second value 7.71 in this first subtable, input:

```
> tbl[1]:
[a, 7.71]
> tbl[1, 2]:
7.71
```

The insert statement adds further values into a table.

```
> insert ['d', 8.01] into tbl
```

```
> tbl:
[[a, 7.71], [b, 7.7], [c, 7.59], [d, 8.01]]
```

Alternatively, values may be added by indexing:

```
> tbl[5] := ['e', 8.04];
> tbl:
[[a, 7.71], [b, 7.7], [c, 7.59], [d, 8.01], [e, 8.04]]
```

Of course, values can be replaced:

```
> tbl[3] := ['z', -5];
> tbl:
[[a, 7.71], [b, 7.7], [z, -5], [d, 8.01], [e, 8.04]]
```

Another form of a table is the dictionary, with indices that can be any kind of data not only positive integers. Key-value pairs are entered with tildes.

```
> dic := ['donald' ~ 'duck', 'mickey' ~ 'mouse'];
> dic['donald']:
duck
```


### 3.10 Sets

Sets are collections of unique items: numbers, strings, and any other data except null. Any item is stored only once and in random order.

```
> s := {'donald', 'mickey', 'donald'}:
{donald, mickey}
```

If you want to check whether 'donald' is part of the set, just index it or use the in operator:

```
> s['donald']:
true
> s['daisy']:
false
> 'donald' in s:
true
```

The insert statement adds new values to a set, the delete statement deletes them.

```
> insert 'daisy' into s;
> delete 'donald' from s;
> s:
{daisy, mickey}
```

Three operators exist to conduct Cantor set operations: minus, intersect, and union.

### 3.11 Sequences

Sequences can hold any number of items except null. All elements are indexed with integers starting with number 1. Compared to tables, sequences are twice as fast when adding values to them. The insert, delete, indexing, and assignment statements as well as the operators described above can be applied to sequences, too.

```
> s := seq(1, 1, 'donald', true):
seq(1, 1, donald, true)
> s[2]:
1
> s[4] := {1, 2, 2};
> insert [1, 2, 2] into s;
> s:
seq(1, 1, donald, {1, 2}, [1, 2, 2])
```


### 3.12 Pairs

Pairs hold exactly two values of any type, including null and other pairs. Values can be retrieved by indexing them or using the left and right operators. Values may be exchanged by using assignments to indexed names.

```
> p := 10:11;
> left(p), right(p), p[1], p[2]:
> p[1] := -10;
```


### 3.13 Conditions

Conditions can be checked with the if statement. The elif and else clauses are optional. The closing fi is obligatory.

```
> if 1 < 2 then
    print('valid')
e elif 1 = 2 then
    print('invalid')
else
    print('invalid, too')
> fi;
valid
```

The case statement facilitates comparing values and executing corresponding statements.

There are two flavours: The first checks an expression for certain values.

```
> c := 'agena';
```

```
> case c
    of 'agena' then
        print('Agena!')
    of 'lua' then
        print('Lua!')
    else
        print('Another programming language !')
> esac;
Agena!
```

The second one works exactly like the if statement but may improve code readability.

```
v := 1;
case
    of v > 0 then print(1)
        of v = 0 then print(0)
        else print(-1)
    esac;
1
```


### 3.14 Loops

A for loop iterates over one or more statements. It starts with an initial numeric value (from clause), and proceeds up to and including a given numeric value (to clause). The step size can also be given (step clause). The od keyword indicates the end of the loop body.

The from and step clauses are optional. If the from clause is omitted, the loop starts with the initial value 1 . If the step clause is omitted, the step size is 1 .

The current iteration value is stored to a control variable (i in this example) which can be used in the loop body.

```
> for i from 1 to 3 by 1 do
    print(i, i^2, i^3)
od;
\begin{tabular}{lll}
1 & 1 & 1 \\
2 & 4 & 8 \\
3 & 9 & 27
\end{tabular}
```

A while loop first checks a condition and if this condition is true or any other value except false, fail or null, it iterates the loop body again and again as long as the condition remains true. The following statements calculate the largest Fibonacci number less than 1000.

```
> a := 0; b := 1;
> while b < 1000 do
> c := b; b := a + b; a := c
> od;
> c:
987
```

A variation of while is the do/as loop which checks a condition at the end of the iteration. Thus the loop body will always be executed at least once.

```
> C := 0;
> do
> inc c
> as c < 10;
> C:
1 0
```

All flavours of for loops can be combined with a while condition. As long as the while condition is satisfied, i.e. is true, the for loop iterates.

```
> for x to 10 while ln(x) <= 1 do
print(x, ln(x))
od;
    0
    0.69314718055995
```

The skip statement starts another iteration of the loop immediately, thus skipping all of the following loop statements after the skip keyword for the current iteration.

The break statement quits execution of the loop and proceeds with the next statement right after the end of the loop. Thus the above loop could also be written as:

```
> for x to 10 do
> if ln(x) > 1 then break fi;
> print(x, ln(x))
od;
0
20.69314718055995
```

which of course is equivalent to

```
for x to 10 while ln(x) <= 1 do
    print(x, ln(x))
od
            0
            0.69314718055995
```

for loops can also be combined with a closing as or until condition. In this case, the loop body is always executed at least once. The loop is iterated as long as the as condition remains true or the until condition evaluates to false.

```
for x to 10 do
    print(x, ln(x))
as ln(x) <= 1
            0
            0.69314718055995
            1.0986122886681
for x to 10 do
    print(x, ln(x))
> until ln(x) > 1
```

```
1 0
0.69314718055995
1.0986122886681
```


### 3.15 Procedures

Procedures cluster a sequence of statements into abstract units which then can be run repeatedly.

Local variables are accessible to their procedure only and can be declared with the local statement.

The return statement passes the result of a computation.

```
> fact := proc(n) is
> local result;
    result := 1;
    for i from 1 to n do
        result := result * i
    od;
    return result
end;
fact(10):
3628800
```

A procedure can call itself.
If your procedure consists of exactly one expression, then you may use an abridged syntax if the procedure does not include statements such as if, for, insert, etc.

```
> deg := << (x) -> x * 180 / Pi >>;
```

To compute the value of the function at $\frac{\pi}{4}$, just input:

```
> deg(Pi/4):
4 5
```

Alternatively, you may use the def or the define statement, e.g. a function with two arguments can be defined as follows:

```
> define sum(x, y) -> x + y;
> sum(1, 2):
3
```

The -> assignment token is optional. Alternatively, you can also use an =or := sign or the is keyword.

### 3.16 Comments

You should always document your code so that you and others will understand its purpose if reviewed later.

A single line comment starts with a single hash. Agena ignores all characters following the hash up to the end of the current line.

```
> # this is a single-line comment
> a := 1; # a contains a number
```

A multi-line comment, also called `long comment`, starts with the token sequence \# / and ends with the closing /\# token sequence'.

```
> #/ this is a long comment,
> split over two lines /#
```

Alternatively, C comments are supported, as well:

```
> /* this is a one-line comment */
> /* this is a long comment,
> split over two lines */
```


### 3.17 Writing, Saving, and Running Programmes

While short statements can be entered directly at the Agena prompt, it is quite useful to write larger programmes in a text editor and save them to a text file so that they can be reused in future sessions.

Note that Agena comes with language scheme files for some common text editors. Look into the share/schemes subdirectory of your Agena installation.

Let us assume that a programme has been saved to a file called myprog.agn in the directory /home/alex in UNIX, or c:\Users \alex in OS/2, DOS or Windows. Then in UNIX, you can run it at the Agena prompt by typing:

```
> run '/home/alex/myprog.agn'
or in DOS-based systems:
> run 'c:/users/alex/myprog.agn' Or
> run 'c:\\users\\alex\\myprog.agn'
```

in DOS-based systems.

[^0]If you both want to start an Agena session and also run a programme from a shell, then enter:

```
$ agena -i /home/alex/myprog.agn
```

in UNIX or
$C: \backslash>a g e n a-i c: \backslash u s e r s \backslash a l e x \backslash m y p r o g . a g n$
in Windows. See Appendix A4 for further switches.

### 3.18 Using Packages

Many functions are included in additional packages which must at first be initialised so that the package functions can be used. Part II of this document indicates which packages are automatically initialised at Agena start-up and which packages have to be imported manually by the user.

For example, all statistics functions are included in the stats package which can be invoked with the import statement:

```
> import stats;
> stats.amean([1, 2, 3, 4]):
2.5
```

Shortcuts to the package functions can be defined by passing the alias option to the import statement.

```
> amean([1, 2, 3, 4]):
Error in stdin, at line 1:
    attempt to call global `amean` (a null value)
> import stats alias
Warning: iqr, sorted have been reassigned.
> amean([1, 2, 3, 4]):
2.5
```

If you want to define shortcuts to specific package functions only, pass their names right after the alias option:

```
> import stats alias amean, smm;
```

If you pass the as clause instead, it assigns an alias to a library name:

```
> import hashes as h;
> a := h.crc32('agena');
```

You may also have a look at the readlib and initialise functions described in Chapter 8.

Chapter Four
Data \& Operations

## 4 Data \& Operations

Agena features a set of data types and operations on them that are suited for both general and specialised needs. While providing all the general types inherited from Lua - numbers, strings, booleans, nulls, tables, and procedures - it also has four additional data types that allow very fast operations: sets, sequences, registers, pairs, and complex numbers.

| Type | Description |
| :--- | :--- |
| number | any integral or rational number, plus undefined and infinity |
| string | any text |
| boolean | booleans (e.g, true, false, and fail) |
| null | a value representing the absence of a value |
| table | a multipurpose structure storing numbers, strings, booleans, <br> tables, and any other data type |
| procedure | a predefined collection of one or more Agena statements |
| set | the classical Cantor set storing numbers, strings, booleans, and <br> all other data types available |
| sequence | a dynamically-sized vector storing numbers, strings, booleans, <br> and all other data types except null in sequential order |
| register | a fixed-size vector storing any value including null and featuring <br> a top position pointer to prevent access to elements above it |
| pair | a pair of two values of any type |
| complex | a complex number consisting of a real and an imaginary <br> number |
| userdata | part of system memory containing user-defined data; userdata <br> objects can only be created by changing the ANSI C sources of <br> the interpreter |
| lightuserdata | a value representing a C pointer; available only if you modify the <br> ANSI C sources of the interpreter |
| thread | a non-preemptive multithread object (a coroutine) |

Table 1: Available types
Tables, sets, sequences, registers, and pairs are also called structures in this manual.

You can determine the type of a value with the type operator which returns a string:

```
> type(0):
number
> type('a text'):
string
```

There is also a structure derived from both tables and sets: bags, see Chapter 10.8; also have a look on linked lists, see Chapter 10.7.

### 4.1 Names, Keywords, and Tokens

In Chapter 3, we have already assigned data - such as numbers and procedures to names, also called `variables`. These names refer to the respective values and can be used conveniently as a reference to the actual data.

A name always begins with an upper-case or lower-case letter or an underscore, followed by one or more upper-case or lower-case letters, underscores, single quotes or numbers in any order.

Since Agena is a dynamically typed language, no declarations of variable names are needed.

| Valid names | Invalid names |
| :--- | :--- |
| var | 1 var |
| - var | $1_{-}$ |
| var1 |  |
| - var1n |  |
| -1 |  |
| ValueOne |  |
| valueTwo |  |
| Value'One |  |

Table 2: Examples for valid and invalid names

The following keywords are reserved and cannot be used as names:

```
abs alias and antilo2 antilogl0 arccos arcsec arcsin arctan as assigned
atendof bea bottom break by bye case catch char cis clear cls conjugate
constant cos cosh cosxx create dec def define delete dict div do downto
duplicate elif else empty end entier enum esac esle even exchange exp
fail false feature fi filled first finite flip float for from global if
imag import in inc infinite infinity inrange insert int intdiv integral
intersect into invsqrt is keys last left ln lngamma local lower minus
mod mul muladd mulup nan nand nargs negate nonzero nor not notin numeric
od odd of onsuccess or pop proc procname qmdev qsumup real redo reg
relaunch reminisce restart return right rotate seq sign signum sin sinc
sinh size skip split sqrt square squareadd store subset sumup tan tanh
then to top trim true try type typeof unassigned undefined union until
upper when while with xnor xor xsubset yrt zero
anything boolean complex lightuserdata listing null number pair register
procedure sequence set string table thread userdata
integer nonnegative nonnegint posint positive
```

The following symbols denote other tokens:

```
+ - * ** / *% /% +% -% \ & && || ~ ~~ % %% ^ ^^ # = <> <= >= < > =
== ~= ~<> <<< >>> <<<< >>>> ( ) { } [ ] ; : :: :- -> @ @@ $ $$ , . .. ?
?- ` ++ -- +++ --- // \\ (/ \) | |- +:= -:= *:= /:= \:= %:= &:= &+ &- &*
&/ &\
```


### 4.2 Assignment

Values can be assigned to names in the following fashions:
[constant] name := value
[constant] name ${ }_{1}, \cdots$, [constant] name $_{k}:=$ value $_{1}, \cdots$, value ${ }_{k}$
[constant] name $_{1}, \cdots$, [constant] name $_{k}->$ value

In the first form, one value is stored in one variable, whereas in the second form, called `multiple assignment statement`, name ${ }_{1}$ is set to value ${ }_{1}$, name ${ }_{2}$ is assigned value $_{2}$, etc. In the third form, called the ` short-cut multiple assignment statement', a single value is set to each name to the left of the -> token.

First steps:

```
> a := 1;
> a:
1
```

An assignment statement can be finished with a colon to both conduct the assignment and print the right-hand side value at the console.

```
> a := 1:
1
```

$>\mathrm{a}:=\exp (\mathrm{a}):$
2.718281828459

Multiple assignments:

```
>a, b := 1, 2
> a:
1
> b:
2
```

If the left-hand side contains more names than the number of values on the right-hand side, then the excess names are set to null.

```
> c, d := 1
> C:
1
> d:
null
```

If the right-hand side of a multiple assignment contains extra values, they are simply ignored.

The multiple assignment statement can also be used to swap or shift values in names without using temporary variables.

```
> a, b := 1, 2;
> a, b := b, a:
2 1
```

A short-cut multiple assignment statement:

```
> x, y -> exp(1);
> x:
2.718281828459
> y:
2.718281828459
```

You can declare constants by putting the constant keyword in front of a variable name in an assignment. If you try to assign a new value to the constant later on in a session, the interpreter will issue an error:

```
> constant a := 1;
> a := 2;
Error at line 1: attempt to assign to constant `a` near `:=
```

You can declare multiple constants at a time:

```
> constant b, constant c := 2, 3;
> b := 0;
Error at line 1: attempt to assign to constant `b` near ` :=
> c := 0
Error at line 1: attempt to assign to constant `c` near `:=`
```

You can mix ordinary and constant declarations:

```
> a, constant b := 1, 2;
```

You should assign a value to a constant in one and the same declaration, otherwise you cannot use it:

```
> a, constant b := 1; # assign 1 to name a`, and no value to constant ` b`
> b := 0
Error at line 1: attempt to assign to constant `b`, near `:=
```

You can switch off this feature completely with the following statement:

```
> environ.kernel(constants = false);
```

On the interactive level, if you define one and the same constant multiple times in a body, for example a then or do body, Agena will just print a one-time warning message but will change this constant. When executing a script file, however, Agena will exit with a proper error message. This is due to the way the parser evaluates bodies on the command-line. Also, in closures (see Chapter 6.22) constants cannot be recognised, so if you try to change them, no error will be issued.

### 4.3 Enumeration

Enumeration with step size 1 is supported with the enum statement:
enum name ${ }_{1}\left[\right.$, name $\left._{2}, \ldots\right]$
enum name ${ }_{1}\left[\right.$, name $_{2}, \ldots$. . from value

All these values are constants, you cannot change them later on.
In the first form, name $1_{1}$ name $_{2}$, etc. are enumerated starting with the numeric value 1 .

```
> enum ONE, TWO;
> ONE:
1
> TWO:
2
```

In the second form, enumeration starts with the numeric value passed right after the from keyword.

```
> enum THREE, FOUR from 3
> THREE
3
> FOUR:
4
```


### 4.4 Deletion and the null Constant

You may delete the contents of one or more variables with one of the following methods: Either use the clear command,

```
clear name }\mp@subsup{1}{[, name 2, \cdots . , name }{k
```

```
> a := 1;
> clear a;
> a:
null
```

which also performs a garbage collection useful if large structures shall be immediately removed from memory, or set the variable to be deleted to null:

```
> b := 1;
> b := null:
null
```

The null value represents the absence of a value. All names that are unassigned evaluate to null. Assigning names to null quickly clears their values, but does not garbage collect them immediately.

The null constant has its own type: 'null'.

```
> type(null):
null
```

If you want to test whether a value is of type 'null', contrary to all other types, you have to put the type name in brackets:

```
> type(null) = 'null':
true
```

In all cases - whether using the clear statement or assigning to null - the memory freed is not given back to the operating system but can be used by Agena for values yet to be created.

There are two operators that quickly check whether a value is assigned or not: assigned and unassigned.

```
> assigned(v):
false
> unassigned(v):
true
```


### 4.5 Precedence

Operator precedence in Agena follows the table below, from lower to higher priority:

```
or xor nor xnor
and nand
< > <= >= = == ~= ~<> <> :: :- |
in notin subset xsubset union minus intersect atendof |-
& : @ $ $$
+ - || ^^ split &+ &- inc dec
* / % symmod roll \ && *% /% %% +% -% %% <<< >>> <<<<< >>>> &* &/ &\
    squareadd mul div intdiv mod
not - (unary minus) +++ ---
^ **
! and all self-defined binary operators and unary operators including ~~
```

As usual, you can use parentheses to change the precedence of an expression. The concatenation ( $\delta$ ), exponentiation (^, **), pair (:), mapping ( $($ ), and selection (\$) operators are right associative, e.g. $x^{\wedge} y^{\wedge} z=x^{\wedge}\left(y^{\wedge} z\right)$. All other binary operators are left associative.

```
> 1+3*4:
1 3
> (1+3)*4:
16
```


### 4.6 Arithmetic

### 4.6.1 Numbers

In the `real` domain, Agena internally only knows floating point numbers which can represent integral or rational numeric values. All numbers are of type number.

An integral value consists of one or more numbers, with an optional sign in front of it.

- 1
- -20
- 0
- +4

A rational value consists of one or more numbers, an obligatory decimal point at any position and an optional sign in front of it:

- -1.12
- 0.1
-. 1

Negative integral or rational values must always be entered with a minus sign, but positive numbers do not need to have a preceding plus sign.

You may optionally include one or more single quotes or underscores within a number to group digits:

```
> 10'000'000:
10000000
```

You can alternatively enter numbers in scientific notation using the e symbol.

```
> 1e4:
10000
>-1e-4:
-0.0001
```

If a number ends in the letter $\mathrm{K}, \mathrm{m}, \mathrm{G}, \mathrm{T}$ Or d , then the number is multiplied by 1,024 , $1,048,576\left(=1,024^{2}\right), 1,073,741,824\left(=1,024^{3}\right), 1,099,511,627,776\left(=1,024^{4}\right)$, or 12 , respectively. If a number ends in the letter $k, m, g, t$ or $d$, then the number is multiplied by $1,000,1,000,000,1,000,000,000,1,000,000,000,000$, or 12 respectively. If a number is appended by p, it is converted to percentage.

```
> 2k:
2000
> 1M:
1048576
> 12D:
144
```

Besides decimal numbers, Agena supports binary, octal, and hexadecimal numbers which may include `thousands` separators. They are represented by the first two letters 0 b or $0 \mathrm{~B}, 00$ or $00,0 \mathrm{x}$ or 0 x , respectively:

| System | Syntax | Examples (to decimal) |
| :---: | :---: | :---: |
| binary | 0b<binary number> or 0B<binary number> | $0 \mathrm{~b} 10=2$ |
| octal | 0o<octal number> Or 00<octal number> | $0010=8$ |
| hexadecimal (integer) | $0 x<$ hexadecimal number> Or OX<hexadecimal number> | $0 \times \mathrm{a}=10$ |
| hexadecimal (float) | 0x<int>.<frac> Or <br> 0x<int>.<frac>E Or <br> $0 x<i n t>p<i n t>$ Or <br> 0x<int>.<frac>P<int> | $\begin{aligned} & 0 \times 0.1=0.0625 \\ & 0 \times 0.1 \mathrm{E}=0.0625 \\ & 0 \times 223 \mathrm{p}-4=162.1875 \\ & 0 \times 1.921 \mathrm{FB} 54442 \mathrm{D} 18 \mathrm{P}+1= \\ & 3.1415926535898 \end{aligned}$ |

If you use only real numbers in your programmes, then Agena will calculate only in the real domain. If you use at least one complex value (see Chapter 4.6.5), then Agena will calculate in the complex domain.

Since Agena internally stores numbers in double or complex double precision，you will sometimes encounter round－off errors．For example，some values such as $\sqrt{2}$ or $\frac{1}{3}$ cannot be accurately represented on a machine．

The mapm package can be used in such situations as it provides arbitrary precision arithmetic．See Chapter 11.3 for more information．

Agena knows two representation for zero： 0 and -0 ，where -0 means something like zero but｀approached from｀$-\infty$ ．In relations， 0 and -0 are always the same，e．g． 0 $=-0 \Rightarrow$ true，and $0<-0 \Rightarrow$ false．In arithmetic，for example -1 ＊$-0 \Rightarrow-0$ ．To test for -0 ，use math．isminuszero．

## 4．6．2 Arithmetic Operations

Agena has the following arithmetical operators：

| Operator | Operation | Details／Example |
| :---: | :---: | :---: |
| ＋ | Addition | $1+2$ » 3 |
| － | Subtraction | $3-2$ » 1 |
| ＊ | Multiplication | 2 ＊ 3 》 6 |
| 1 | Division | 4 ／ 2 » 2 |
| $\wedge$ | Exponentiation with rational power | 2 ＾ 3 》 8 |
| ＊＊ | Exponentiation with integer power | 2 ＊＊ 3 》 8 |
| \％ | Modulus | $5 \% 2$ 》 1 |
| $\backslash$ | Integer division | 5 \2 » 2 |
| ＊\％ | Percents，percentage | 100 ＊\％ 2 》 2 |
| 1\％ | Percents，ratio | 100 ／ 2 » 5k |
| ＋\％ | Percents，add－on（premium） | 100 ＋\％ 2 》 102 |
| －\％ | Percents，discount | 100 －\％ 2 》 98 |
| ＠ | Conditional multiplication a＠b，returning a if $b=0$ ，and $a * b$ otherwise | $\begin{array}{lllll} 2 & @ & 0 & > & 2 \\ 2 & @ & 3 & > & 6 \end{array}$ |

Table 3：Arithmetic operators
The modulus operator is defined as $a \% b=a$－entier（a／b）＊b，the integer division as $a \backslash b=\operatorname{sign}(a)$＊sign（b）＊entier（abs（a／b））．

Agena has a lot of mathematical functions both built into the kernel and also available in the math，stats，linalg，and calc libraries．Table 4 lists some of the most common．

The mathematical procedures that reside in packages must always be entered by passing the name of the package followed by a dot and the name of the procedure．Use the import statement to activate the package before using these functions，e．g．to initialise the statistics package called stats，type：

```
> import stats;
```

Unary operators ${ }^{2}$ like $\mathbf{I n}$ ，exp，etc．can be entered with or without simple brackets．

| Procedure | Operation | Library | Example and result |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{\operatorname { s i n }}(\mathrm{x})$ | Sine（x in radians） | Kernel | sin 0 » |
| $\cos (x)$ | Cosine（x in radians） | Kernel | $\cos (0)$ 》 |
| $\tan (\mathrm{x})$ | Tangent（ x in radians） | Kernel | $\tan (1) \geqslant 1.557407$. |
| $\arcsin (x)$ | Inverse sine（ x in radians） | Kernel | $\arcsin (0)$ 》 0 |
| $\arccos (\mathrm{x})$ | Arc cosine（ x in radians） | Kernel | $\arccos (0)$ 》 1．570796．． |
| $\arctan (\mathrm{x})$ | Arc tangent（x in radians） | Kernel | $\arctan (\mathrm{Pi})$ 》 1．262627．． |
| $\sinh (\mathrm{x})$ | Hyperbolic sine | Kernel | $\sinh (0)$ 》 |
| $\cosh (x)$ | Hyperbolic cosine | Kernel | $\cosh (0)$ 》 1 |
| $\tanh (\mathrm{x})$ | Hyperbolic tangent | Kernel | $\tanh (0) \geqslant 0$ |
| abs（ X ） | Absolute value of $x$ | Kernel | abs（－1）＞1 |
| entier（x） | Rounds x downwards to the nearest integer | Kernel | $\begin{aligned} & \text { entier(2.9) " }{ }^{2} \\ & \text { entier (-2.9) }{ }^{2}-3-2 \end{aligned}$ |
| even（ x ） | Checks whether x is even | Kernel | even（2）＞true |
| $\exp (\mathrm{x})$ | Exponentiation $\mathrm{e}^{\mathrm{x}}$ | Kernel | $\exp (0)>1$ |
| Ingamma（x） | $\ln \Gamma \times$ | Kernel | exp（lngamma（3＋1））》 |
| $\operatorname{int}(x)$ | Rounds $x$ to the nearest integer towards zero | Kernel | $\begin{aligned} & \operatorname{int}(2.9)>2 \\ & \operatorname{int}(-2.9)>-2 \end{aligned}$ |
| $\ln (\mathrm{x})$ | Natural logarithm | Kernel | $\ln (1)$ 》 0 |
| $\boldsymbol{\operatorname { l o g }}(\mathrm{x}, \mathrm{b})$ | Logarithm of $x$ to the base b | Kernel | $\log (8,2)$ 》 3 |
| round（ $\mathrm{x}, \mathrm{d}$ ） | Rounds the real value x to the d－th digit | Base | ```round ( sqrt(2), 2) 》 1.41``` |
| $\boldsymbol{\operatorname { s i g n }}(\mathrm{X})$ | Sign of $x$ | Kernel | sign（－1）＞－1 |
| sqrit $(\mathrm{x})$ | Square root of $x$ | Kernel | sqrt（2）》 1．414213．． |
| sumup（［ $\cdots$ ］） | Sum | Kernel | sumup（［1，2，3］）》 6 |
| mean（［ $\cdot \cdot]$ ） | Arithmetic mean | stats | stats．mean（［1，2，3］）》2 |
| median（［ $\cdots$ ］） | Median | stats | $\begin{aligned} & \text { stats.median } \\ & [1,2,3,4])>2.5 \end{aligned}$ |

Table 4：Common mathematical functions
In addition，Agena can conduct bitwise operations on numbers．

| Operator | Operation | Details／Example |
| :---: | :---: | :---: |
| \＆\＆ | Bitwise｀and＇ | $7 \& \& 2$ 》 2 |
| ｜｜ | Bitwise｀or＇ | 1112 ＂ 3 |
| $\wedge$ | Bitwise｀exclusive－or｀ | $7{ }^{\wedge} 2$ » |
| $\sim \sim$ | Bitwise complement （bitwise｀not｀） | $\sim \sim 7$ »－8 |
| $\begin{aligned} & \lll, \\ & \ggg> \end{aligned}$ | Bitwise shift | $\lll$ conducts a left－shift（multiplication with 2），$\ggg$ a right－shift（division by 2）． |
| $\begin{aligned} & \lll<, \\ & \ggg> \end{aligned}$ | Bitwise rotation | $\lll<$ and $\ggg>$ rotate bits left－and rightwards． |
| nand | bitwise complement | Equivalent to $\sim \sim(a \& \& b)$ ． |

[^1]| Operator | Operation | Details / Example |
| :---: | :---: | :---: |
|  | and |  |
| nor | bitwise complement 'or' | Equivalent to $\sim \sim(a\|\mid b)$ |
| xnor | bitwise complement exclusive- 'or' | Equivalent to $\sim \sim(\mathrm{a} \wedge \wedge$ b) |
| getbit getbits | returns stored bits) | getbit(3, 1), getbits(3) |
| setbit setbits | sets bit(s) | $\operatorname{setbit}(3,1)$ » $1, \operatorname{setbits}(8, \operatorname{reg}(1,0,0))$ » 12 |

Table 5: Bitwise operators and functions
By default, the operators internally calculate with unsigned integers. You can change this behaviour to signed integers with environ.kernel:
> environ.kernel(signedbits = true);
The default is restored as follows:
> environ.kernel(signedbits = false);
Note that in order to return useful results $\sim \sim$, nand, nor and xnor should be used in signed mode only, regardless of the environ.kernel/signedbits setting.

### 4.6.3 Increment, Decrement, Multiplication, Division

Instead of incrementing or decrementing a value, say

```
> a := 1;
```

by entering a statement like

```
> a := a + 1:
2
```

you can use the inc and dec commands ${ }^{3}$ which are also around $10 \%$ faster:

```
inc name [, value];
```

dec name [, value];

If value is omitted, name is increased or decreased by 1.

```
> inc a;
> a:
3
```

[^2]```
> dec a;
> a:
2
> inc a, 2;
> a:
4
> dec a, 3;
> a:
1
```

Likewise, the mul and div statements multiply or divide their argument by a scalar, mod takes the modulus, and intdiv conducts an integer division, their defaults also being 1. negate flips a Boolean; with numbers, it converts 0 to 1 , and non-zero to 0.

It is advised that all inc, dec, mul, div, intdiv and mod statements are terminated by a semicolon unless the next token in the code is a keyword, so that the parser can discern them from the corresponding operators, see Chapter 4.6.8.

Alternatively, you may use mutate operators to express compound assignment:

| Operator | Operation | Equivalent |
| :---: | :--- | :--- |
| $+:=$ | addition | inc statement |
| $-:=$ | subtraction | dec statement |
| $*:=$ | multiplication | mul statement |
| $1:=$ | division | div statement |
| $\backslash:=$ | integer division | intdiv statement |
| $\%:=$ | modulus | mod statement |
| $\alpha:=$ | string concatenation | n/a |
| $@:=$ | conditional multiplication | n/a |

```
> a +:= 3; # equals to `a := a + 3` or `inc a, 3`
> a:
4
```

The suffix ++ and -- operators return the current value of a variable and subsequently increase or decrease the variable by one. Likewise, the prefix ++ and -- operators first increase or decrease a variable by one and then return the updates value. The operators work on indexed names, as well.

```
> c := 0;
> a := c++; # used as an expression
> print(a, c); # returns 0, 1
> c++; # used as a statement
> print(c)
2
```


### 4.6.4 Mathematical Constants

Agena features arithmetic constants mentioned in Appendix A9. All mathematical constants are protected and cannot be changed.

All mathematical functions and operators return the constant undefined instead of issuing an error if they are not defined at a given point:

```
> ln(0):
undefined
```

With values of type number, the finite function can determine whether a value is neither $\pm$ infinity nor undefined.

```
> finite(fact(1000)), finite(sqrt(-1)):
false false
```

The float function checks whether a value is a float and not an integer.

```
> float(1):
false
> float(1.1):
true
```


### 4.6.5 Complex Math

Complex numbers can be defined in two ways: by using the ! constructor or the imaginary unit represented by the capital letter i. Most of Agena's mathematical operators and functions know how to handle complex numbers and will always return a result that is in the complex domain. Complex values are of type complex.

```
> a := 1!1;
> b := 2+3*I;
> a+b:
3+4*I
> a*b:
-1+5*I
```

The following operators work on rational numbers as well as complex values: +, -, *, /, ^, **, =, <>, abs, arccos, arcsec, arcsin, arctan, conjugate, cos, cosh, entier, exp, flip, invsqrt, lngamma, ln, log, sign, sin, sinh, sqrt, tan, tanh, and unary minus. With these operators, you can also mix numbers and complex numbers in expressions. You will find that most mathematical functions are also applicable to complex values.

```
> c := ln(-1+I) + ln(0.5):
-0.34657359027997+2.3561944901923*I
```

The real and imaginary parts of a complex value can be extracted with the real and imag operators.

```
> real(c), imag(c):
\(-0.34657359027997\)
```


### 2.3561944901923

Three further functions may also be of interest: abs returns the absolute value of a complex number, argument returns its phase angle in radians, and conjugate computes the complex conjugate.

Note that the ! operator has the same precedence as unary operators like -, sin, cos, etc. This means that $-1!2=-1+2 *$, but also that $\sin 1!2=(\sin 1)!2$. Thus, it is advised that you use brackets when applying unary operators on complex values.

The setting environ.kernel(zeroedcomplex = true) makes Agena print complex values that are close to zero as just o in the output region of the console. Internally, however, complex values are not rounded by this or any other setting.

### 4.6.6 Comparing Values

Relational operators can compare both numeric and complex values. Whereas all relational operators work on numbers, complex numbers can only be compared for equality or inequality.

| Operator | Description | Complex values supported |
| :---: | :--- | :--- |
| $<$ | less than | no |
| $>$ | greater than | no |
| $<=$ | less than or equals | no |
| $>=$ | greater than or equals | no |
| $=$ | equals | yes |
| $<>$ | not equals | yes |
| in | in range | no |

```
> 1 < 2:
true
> 1 = 1:
true
> 1 <> 1:
false
```

The result true indicates that a comparison is valid, and false indicates that it is invalid. See Chapter 4.8 for more information.

Most computer architectures cannot accurately store number values unless they can be expressed as halves, quarters, eighths, and so on. For example, 0.5 is represented accurately, but 0.1 or 0.2 are not.

Since Agena is not a computer algebra system, you will sometimes encounter round-off errors in computations with numbers and complex numbers:

```
>0.2 + 0.2 + 0.2 = 0.6:
false
```

In such cases, the $\sim=$ operator or the approx function might be of some help since they compare values approximately.

```
>0.2 + 0.2 + 0.2 ~= 0.6:
true
>0.2!0.2 + 0.2!0.2 + 0.2!0.2 = 0.6!0.6:
false
> approx (0.2!0.2 + 0.2!0.2 + 0.2!0.2, 0.6!0.6):
true
```

To determine whether a number is part of a closed interval, use the in or inrange operators:

```
> 2 in 0 : 10:
true
```

You can use the +++ and --- operators to define open borders:

```
> inrange(1, +++1, ---10):
false
```

The unary zero operator checks whether a number or complex number is 0 or $0+1 * 0$; nonzero checks whether it is non-zero. The two operators are around $10 \%$ faster than the binary $=$ and $<>$ operators.

### 4.6.7 Range of Values

The following ranges apply to Agena numbers and complex numbers:

| Characteristic | Value |
| :--- | :--- |
| smallest representable number | $-1.797693134862315 \times 10^{308}$ |
| largest representable number | $+1.797693134862315 \times 10^{308}$ |
| largest positive integer without loss of <br> precision | $9.007199254741 \times 10^{15}$ |
| smallest subnormal (negative) positive <br> number | $(-) 4.9406564584124654 \mathrm{e}-324$ |
| largest subnormal (negative) positive <br> number | $(-) 2.2250738585072009 \mathrm{e}-308$ |

### 4.6.8 Adapting Basic Arithmetic Operators

There are six arithmetic binary operators that detect potential numeric overflow, underflow and division by zero and allow the user to invoke proper self-written functions that handle them: inc for addition, dec for subtraction, mul for multiplication, div for division and intdiv for integer division, plus mod for modulus.

These operators after checking possible exceptions call user-defined handlers that take the two operands plus the information on the kind of exception:

- addition: inc calls math.add,
- subtraction: dec calls math.subtract,
- multiplication: mul calls math.multiply,
- division: div calls math.divide,
- integer division: intdiv calls math.intdivide and
- modulus: mod calls math.modulo (not math.modulus !).


## Examples:

Division: the handler might look like this - math.intdivide and math.modulo may look similar, since the values for parameter kind are the same:

```
math.divide := proc(n, d, kind) is
    case kind
            # kind 0b0000 means no exception
        of 0b0000 then return n/d
            # kind 0b0001 means denominator is zero
        of 0b0001 then error('division by zero')
            # kind 0b0010 means very large value to be divided by value
            # close to 0
        of 0b0010 then error('underflow')
            # kind 0b1000 indicates both operands are close to 0
        of 0b1000 then return n/d
    esac
end;
> 1 div 0:
division by zero
```

A multiplication handler:

```
math.multiply := proc(a, b, kind) is
    case kind
        of 0b0000 then return a*b # kind 0b000 indicates no exception
                # kind 0b0010: very large value to be multiplied by value close
                # to zero
            of 0b0010 then error('underflow')
                # kind 0b0100: very large value to be multiplied by
                # very large value
            of 0b0100 then error('overflow')
                # kind 0b1000: both operands are close to zero
        of 0b1000 then return a*b
    esac
end;
```

```
> 1e308 mul 1e308:
overflow
```

Addition - and subtraction if this should make any sense, the possible values for kind are the same - could be handled like this (for subtraction redefine math.subtract):

```
math.add := proc(a, b, kind) is
    case kind
            of 0b0000 then return a + b # no exception
                # very large value to be added to (subtracted) value close to 0:
            of 0b0010 then return a + b
                # very large values to be added (or subtracted):
            of 0b0100 then error('overflow')
                # both operands are close to zero:
            of 0b1000 then return a + b
        esac
    end;
```

Agena is shipped with six default functions math.add, math.subtract, math.multiply, math.divide, math.intdivide and math.modulo that just conduct the requested operation and return the result, without issuing any error. You may overwrite them with alternatives of your choice.

The threshold that defines whether a value is `close to zero` can be set with environ.kernel/closetozero, which by default is DoubleEps, e.g.:

```
> environ.kernel(closetozero = 1e-20);
```

The type of numerical exception that occurred the last time one the six operators has been invoked can also be queried by calling environ.arithstate which returns the type of exception as a bit field, see all the case/of clauses above:

```
> 1e308 inc le308:
overflow
> environ.arithstate():
1
```

The description of environ.arithstate in Chapter 14.2 includes a complete list of all the numeric exceptions the six binary operators might encounter.

### 4.7 Strings

### 4.7.1 Representation

Any text can be represented by including it in single or double quotes:

```
> 'This is a string':
This is a string
```

Of course, strings - like numbers - can be assigned to variables.

```
> str := "I am a string.";
> str:
I am a string.
```

Strings - regardless whether included in single or double quotes - are all of type string,

```
> type(str):
string
```

and can be of almost unlimited length. Strings can be concatenated, characters or sequences of characters can be replaced by other ones, and there are various other functions to work on strings.

Multiline-strings can be entered by just pressing the RETURN key at the end of each line:

```
> str := 'Two
lines';
```

which prints as

```
> str:
```

Two
lines
A string may contain no text at all - called an empty string -, represented by two consecutive single quotes with no spaces or characters in between:
> ' ':

### 4.7.2 Substrings

You may obtain a specific character by passing its position in square brackets right after the string name. If you use a negative index $n$, then the $|n|$-th character from the right end of the string will be returned.

```
> str := 'I am a string.';
```

```
> str[1];
I
```

In general, parts of a string consisting of one or more consecutive characters can be obtained with the notation:

```
string[ start [ to end] ]
```

You must at least pass the start position of the substring. If only start is given then the single character at position start will be returned. If end is given too, then the substring starting at position start up to and including position end will be returned.

```
> str := 'string'
> str[3]:
r
> str[3 to 5]:
rin
> str[3 to 3]:
r
```

You may also pass negative values for start and/or end. In these cases, the positions are determined with respect to the right end of the string.

```
> str[3 to -1]:
ring
> str[3 to -2]:
rin
> str[-3 to -2]:
in
> str[-3]:
i
```


### 4.7.3 Escape Sequences

In Agena, a text can include any escape sequences ${ }^{4}$ known from ANSI C, e.g.:

- $\backslash \mathrm{n}$ : inserts a new line,
- \t: inserts a tabulator
- $\backslash$ b: puts the cursor one position to the left but does not delete any characters.

```
> 'I am a string.\nMe too.':
I am a string.
Me too.
> 'These are numbers: 1\t2\t3':
These are numbers: 1 2 3
```

[^3]```
> 'Example with backspaces:\b but without the colon.':
Example with backspaces but without the colon.
```

If you want to put a single or double quote into a string, put a backslash right in front of it:

```
> 'A quote: \'':
A quote: '
> "A quote: \"":
A quote: "
```

However, if a string is delimited by single quotes and you want to include a double quote (or vice versa), a backslash is not obligatory, e.g. "' agena ' $"$ is a valid string.

Likewise, a backslash is represented by typing it twice.

### 4.7.4 Concatenation

Two or more strings can be concatenated with the \& operator:

```
> 'First string, ' & 'second string, ' & 'third string':
First string, second string, third string
```

Numbers (but not complex ones) are supported, as well, so you do not need to convert them with the tostring function before applying \&:

```
> 1 & ' duck':
1 duck
```

Furthermore, the compound $\&:=$ concatenation operator appends a string to the contents of a string variable:

```
> a := 'In';
> a &:= 'Sight';
> a:
InSight
```


### 4.7.5 String Operators and Functions

Agena has basic operators useful for text processing:

| Operator | Return | Function |
| :---: | :---: | :---: |
| $s$ in $\dagger$ | number or null | Checks whether a substring $s$ is included in string $t$. If true, the position of the first occurrence of $s$ in $\dagger$ will be returned; otherwise null will be returned. |
| s atendof $\dagger$ | number or null | Checks whether a string $\dagger$ ends in a substring s. If true, the position of the position of $s$ in $\dagger$ will be returned; otherwise null will be returned. |
| replace(s, p, r) | string | Replaces all patterns $p$ in string $s$ with substring $r$. If $p$ is not in $s$, then $s$ will be returned unchanged. $p$ might also be the position (a positive integer) of the character to be replaced. |
| s split d | sequence of strings | Splits a string into its words with $d$ as the delimiting character(s). The items are returned as a sequence of strings. |
| size(s) | number | Returns the length of string s. If $s$ is the empty string, 0 will be returned. |
| abs(s) | number | Returns the numeric ASCII code of character s. |
| char( n ) | string | Returns the character corresponding to the given numeric ASCll code n. |
| lower(s) | string | Converts a string to lowercase. Western European diacritics are recognised. |
| upper(s) | string | Converts a string to uppercase. Western European diacritics are recognised. |
| tonumber(s) | number or complex value | Converts a string into a number or complex number. |
| tostring( n ) | string | Converts a number to one string. If a complex value is passed, the real and imaginary parts are returned separately as two strings. |
| trim(s) | string | Deletes leading and trailing spaces as well as excess embedded spaces. |

Table 7: String operators
Some examples:
> str := 'a string';
The character s is at the third position:

```
''s' in str:
3
```

Let us split a string into its components that are separated by white spaces:

```
> str split ' ':
seq(a, string)
str is eight characters long:
> size(str):
8
```

The ASCII code of the first character in str, a, is:

```
> abs(str[1]):
97
```

translated back to

```
> char(ans):
a
```

Put all characters in str to uppercase:

```
> upper(str):
```

A STRING

And now the reverse:

```
> lower(ans):
```

a string

The following functions can be used to find and replace characters in a string:


| Function | Functionality | Example |
| :---: | :---: | :---: |
|  | first match of the substring and returns the position where the pattern starts with respect to its left beginning. When searching from right to left, pattern matching is not supported. |  |
| atendof | Checks whether a string (right operand) ends in a substring (left operand). If true, the position will be returned; otherwise null will be returned. | $\begin{aligned} & \text { 'ing' atendof } \\ & \text { 'raining' } \\ & \text { " } 5 \end{aligned}$ |
| strings.find | Returns the first match of a substring (second argument) in a string (first argument) and returns the positions where the pattern starts and ends. An optional third argument specifies the position where to start the search. If it does not find a pattern, the function returns null. <br> The function supports pattern matching facilities described in Chapter 9.1.3. <br> See also: strings.mfind. which returns all occurrences. | ```strings.find( 'string', 'tr') » 2, 3 strings.find( 'string', 'tr', 3) " null strings.find( 'string', 't.') " 2, 3``` |
| replace | In a string (first argument) replaces all occurrences of a substring (second argument) with another one (third argument) and returns a new string. Pattern matching facilities are not supported. <br> A sequence of replacement pairs can be passed to the function, too. <br> See also strings.gsub. | ```replace(str, 'string', 'text') > text replace('string', seq('s':'S', 't':'T')) > STring``` |

Table 8: Search and replace functions and operators

For more information on these functions, check Chapter 9.1. See also the descriptions of strings.match and strings.gmatch.

The replace function can be used to find and replace characters in a string.

### 4.7.6 Comparing Strings

Like numbers, single or multiple character strings can be compared with the familiar relational operators based on their sorting order which is determined by your current locale.

```
> 'a' < 'b':
```

```
true
> 'aa' > 'bb':
false
```

If the sizes of two strings differ, the missing character is considered less than an existing character.

```
> 'ba' > 'b':
true
```


### 4.7.7 Patterns and Captures

Sometimes it my not suffice to just look for a fixed pattern, e.g. a simple substring, in a string. You may want to search for a pattern of different kinds of characters - e.g. both numbers and letters, or either letters or numbers, or a subset of them -, or of variable number of characters, or both of them.

Agena provides both character classes and modifiers to accomplish this. While common Regular Expressions are not supported, Agena offers quite similar facilities, all taken from Lua.

For performance reasons, you may use the following rule of thumb ${ }^{5}$ :

- If you would like to determine the start position of the very first match of a fixed pattern only, use the in operator, for in is the fastest.
- If you want to look as fast as possible only for the start position of the very first match of a `variable` pattern, using character classes and/or modifiers, or would like to give the position where to start the quickest search, use instr.
- If both the start and end position is needed, prefer strings.find. The instr function can also return the start and end position, with or without variable patterns, but may be slower than strings. find in most situations.

Character classes represent certain sets of tokens, e.g. the class \%d represents one digit, and \%a represents one upper-case or lower-case letter. Assume we would like to determine the position of the hour 00:00:00 in the following date/time string:

```
> date := '23.05.1949 00:00:00'
```

We could use the instr function to determine the start position of the hour,

```
> instr(date, '%d%d:%d%d:%d%d'):
12
```

or strings.find to get the start and end position of it.

```
> strings.find(date, '%d%d:%d%d:%d%d'):
12 19
```

[^4]strings.match extracts the hour.

```
> strings.match(date, '%d%d:%d%d:%d%d'):
00:00:00
```

For a complete list of all supported classes, please have a look at the end of this chapter or Chapter 9.1.3.

Character sets denote user-defined classes comprising any character class and/or single tokens, put in square brackets. For example, [01] may represent a binary, and [ $\% 1$-] any lower-case letter, white space or hyphen. A range of characters is represented by a hyphen, thus [A-Ca-c] represents one of the first three upper and lower case letters in the alphabet.

```
> instr('binary: 10', '[01]'):
9
```

A caret in front of a class indicates that a string should begin with this class, and a dollar trailing a class denotes that it should end in the given class.

```
> instr('1 is a number', '^[%l ]'):
null
> instr('1 is a number', '%l$'):
1 3
```

Patterns also support modifiers for repetition or optional parts. The plus sign indicates one or more repetitions of a class, the asterisk denotes zero or more repetitions, and the question mark zero or one occurrence.

```
> date := '23.05.1949 00:00:00'
> strings.find(date, '%d+.%d+.%d+'): # find the date 23.05.1949
1 10
> date := '23.05. 00:00:00'
> strings.find(date, '%d+.%d+.%d*'): # find 23.05., optionally the year
1
```

The single dot represents any occurrence of any character in a string, regardless whether the character is a cipher, a letter or special character. If you would like to search for one of the special characters *, +, -, ?, ., [, ], etc. in a string, just escape it with the percentage sign.

```
> instr(date, '%.'): # find the first dot in the date string
3
```

instr and strings.find also allow to switch off pattern matching by passing true as the last argument:

```
> instr(date, '.', true):
3
```

If a pattern is put in parentheses, one or more portions of a string matching this pattern are extracted from a string, to be optionally assigned to names. This feature is also called a capture. Two examples:

```
> strings.match('<id>1234</id>', '<id>(.*)</id>'):
1 2 3 4
> date := 'May 23, 1949 12:15:00';
> strings.find(date, '(%w+) (%d+), ?(%d+)'):
1 12 May 23 1949
> year, day, month := strings.match(date, '(%w+) (%d+), ?(%d+)'):
May 23 1949
> year, month, day:
May 1949 23
```

Another useful function is strings.gmatch which returns a function that iterates over all occurrences of a pattern in a string:

```
> f := strings.gmatch('1 10', '(%d+)'):
procedure(008E1278)
> f():
1
> f():
1 0
```

You may also use the wrapper function strings.gmatches which returns a sequence of all the substrings matching a given pattern.

```
> strings.gmatches('1 10', '(%d+)'):
seq(1, 10)
```

There is a small difference between the * and - modifiers for matching zero or more occurrences which may influence execution time significantly: while * looks for the longest match, - does for the shortest:

```
> strings.match('<p>a</p><p>2</p>', '<p>(.-)</p>'): # - shortest
a
> strings.match('<p>a</p><p>b</p>', '<p>(.*)</p>'): # * longest
a</p><p>b
```

With captures, and with captures only, strings.find not only returns the start and end position of the match, but also the match itself as a third return.

```
> strings.find('<p>a</p><p>b</p>', '<p>(.-)</p>'):
1 8 a
```

To check whether one of the characters is in a given set, use square brackets. In the next example, we check whether the first character in a pattern is either '1', '2' or '3', and the rest of the pattern is 'abc'.

```
> strings.match('2abc', '[123]abc'):
2abc
```

The pattern in the above example, e.g. its second argument, in general matches a substring in a string. If you would like to make sure that a pattern matches an entire string, put a caret in front of the pattern and a dollar sign at its end:

```
> strings.match('2abc', '^[123]abc$'):
2abc
```

Thus, since the string to be searched is longer,

```
> strings.match('y2abcy', '^[123]abc$'):
```

returns:
null
To recognise one or more ligatures and umlauts, along with one or more Latin letters, also just use square brackets and combine them with a modifier, here \%a:

```
> strings.match('Eckernförde, Schleswig-Holstein', '([äöüßÄÖÜ%a]*)'):
Eckernförde
```

Retrieve a value either residing in a conventional XML tag or its worst-case (though here invalid) SOAP variant:

```
> pattern := '<.*Data.*>(%a+)</.*Data>';
> str := strings.match(
> '<soap:Data attr=\'foo\'>value</soap:Data>',
> pattern);
> str:
value
> str := strings.match('<Data>value</Data>', pattern);
> str:
value
```

Summary ${ }^{6}$ of character classes and pattern modifiers:
$\left.\begin{array}{lll}\text { Classes } & . & \text { any character } \\ \% a & \text { letters a to } z \text { or A to Z }\end{array}\right]$

[^5]
### 4.8 Boolean Expressions

Agena supports the logical values true and false, also called `booleans`. Any condition, e.g. $a<b$, results to one of these logical values. They are often used to tell a programme which statements to execute and thus which statements not to execute.

Boolean expressions mostly result to the Boolean values true or false. Boolean expressions are created by:

- relational operators ( $>,<,=,==, \sim=, \sim<>,<=,>=,<>)$,
- logical names: true, false, fail, and null,
- in, subset, xsubset, and various functions.

Agena supports the following relational operators:

| Operator | Description | Example |
| :--- | :--- | :--- |
| $<$ | less than | $1<2$ |
| $>$ | greater than | $2>1$ |
| $<=$ | less than or equals | $1<=2$ |
| $>=$ | greater than or equals | $2>=1$ |
| $=$ | equals | $1=1$ |
| $==$ | strict equality for structures ${ }^{7}$ | $[1]==\quad[1]$ <br> $1==1$ |
| $\sim=$, | approximate equality/inequality for <br> real and complex numbers, and <br> structures | $1 \sim=1$ <br> $[1] \sim<>\quad[1]$ |
| $\sim<\gg$ | not equals | $1<>2$ |
| $<>$ |  |  |

Table 10: Relational operators
The logical operators and, or, nand, nor, xor, and xnor behave a little bit differently: They consider anything except false, fail, and null as true, and false otherwise. They return either the first or second operand, which can be any data - not just true or false - subject to the following rules:

| Operator | Description | Examples |
| :---: | :---: | :---: |
| and | Returns its first operand if it is or evaluates to false, fail or null, otherwise returns its second operand. | $\begin{aligned} & \text { true and } 1 \text { " } 1 \\ & \text { false and 1 } 1 \text { false } \\ & \text { true and false " false } \\ & \text { false and true " false } \end{aligned}$ |
| or | Returns its first operand if it is not or does not evaluate to false, fail, or null, otherwise it returns its second operand. | true or true " true true or false " true 2 or true » 2 <br> null or 2 » 2 |
| xor | With booleans: Returns the first operand if the second one evaluates or is false, fail, or null. It returns the second operand if the first operand evaluates to | ```true xor false» true true xor true » false false xor true " true 1 xor null " 1 1 xor 2 > 2``` |

[^6]| Operator | Description | Examples |
| :--- | :--- | :--- |
|  | false, fail, or null and if the second <br> operand is neither false, fail nor null. |  |
| With non-booleans: returns the first <br> operand if the second operand <br> evaluates to null, otherwise the second <br> operand will be returned. | not true » false <br> not false" true <br> not 1 » false <br> not null » true |  |
| not | Turns a true expression to false and vice <br> versa. | true nand false " true <br> 1 nand null » true |
| nand | Returns true if at least one operand in <br> false, otherwise returns false. | false nor false » true |
| nor | Returns true if both operands are false, <br> and false otherwise. | Returns true if both Boolean operands <br> are the same (where false and fail are <br> considered equal), and false otherwise. |
| xnor false xnor false » true |  |  |
| implies | Returns false if the first operand is true <br> and the second is false; otherwise <br> returns true. | false implies false <br> " true |

Table 11: Logical operators
As expected, you can assign Boolean expressions to names

```
> cond := 1 < 2:
true
cond := 1 < 2 or 1 > 2 and 1 = 1:
true
```

or use them in if statements, described in Chapter 5.

In many situations, the null value can be used synonymously for false.
The additional Boolean constant fail can be used to denote an error. With Boolean operators (and, or, not), fail behaves like the false constant, e.g. not(fail) = true, but remember that fail is always unlike false, i.e. the expression fail = false results to false.
true, false, and fail are of type boolean. null, however, has its own type: the string 'null'.

The and as well as or operators only evaluate their second argument if necessary, called short-circuit evaluation. Thus, the following statement does not issue an error:

```
> a := null
> if a :: number and a > 0 then print(ln(a)) fi
```

They are also handy to define defaults for unassigned names:

```
> a := null
> a := a or 0
> a:
0
```

You can add, subtract, multiply, divide and exponentiate numbers with true or false, where true in this context represents number 1 and false or fail number 0. Thus, for example, the expressions abs $(x>0) *_{x}$ and ( $x>0$ ) *x are equivalent expressions. You can even apply the four basic arithmetic operations on two booleans if deemed necessary.

### 4.9 Tables

Tables are used to represent more complex data structures. Tables consist of zero, one or more key-value pairs: the key referencing to the position of the value in the table, and the value the data itself.

Keys and values can be numbers, strings, and any other data type except null.
Here is a first example: Suppose you want to create a table with the following meteorological data recorded by Viking Lander 1 which touched down on Mars in 1976:

| Sol | Pressure in $\mathbf{~ m b}$ | Temperature in ${ }^{\circ} \mathbf{C}$ |
| :--- | :--- | :--- |
| 1.02 | 7.71 | -78.28 |
| 1.06 | 7.70 | -81.10 |
| 1.10 | 7.70 | -82.96 |

```
> VL1 := [
    1.02 ~ [7.71, -78.28],
    1.06 ~ [7.70, -81.10],
    1.10 ~ [7.70, -82.96]
];
```

To get the data of Sol 1.02 (the Martian day \# 1.2) input:

```
> VL1[1.02]:
[7.71, -78.28]
```

Tables may be empty, or include other tables - even nested ones.
You can control how tables are printed at the console in two ways: If the setting environ.kernel('longtable') is true (e.g. by entering the statement environ.kernel(longtable $=$ true), then each key~value pair is printed at a separate line. If the setting environ.kernel('longtable') is false, all key~value pairs will be printed in one consecutive line, as in the example above. Also, you can define your own printing function that tells the interpreter how to print a table (or
other structures). See Appendix A5 for further information on how to do this and other settings.

Stripped down versions of tables are sets, sequences and registers which are described later. Most operations on tables introduced in this chapter are also applicable to them.

### 4.9.1 Arrays

Agena features two types of tables, the simplest one being the array. Arrays are created by putting their values in square brackets:

$$
\left[\left[\begin{array}{l}
\text { value } \\
1
\end{array}[, \text { value } 2, ~ \cdots]\right]\right]
$$

```
> A := [4, 5, 6]:
[4, 5, 6]
```

The table values are 4,5 , and 6 ; the numbers 1,2 , and 3 are the corresponding keys or indices of table A, with key 1 referencing value 4 , key 2 referencing value 5, etc. With arrays, the indices always start with 1 and count upwards sequentially. The keys are always integral, so a in this example is an array whereas table vli in the last chapter is not.

To determine a table value, enter the name of the table followed by the respective index in square brackets:

```
tablename[key]
```

```
> A[1]:
4
```

Instead of using constants to index a table, you may also compute an index both in table assignments or queries. The following selects the middle element of A :

```
> l, r := 1, size A:
1
> A[(1+r)\2]:
5
```

If a table contains other tables, you may get their values by passing the respective keys in consecutive order. The two forms are equivalent:

```
tablename[key ][[key %][\cdots]
tablename[key 1, key2, ...]
```

```
> A := [[3, 4]]:
[[3, 4]]
```

The following call refers to the complete inner table which is at index 1 of the outer table:

```
> A[1]:
[3, 4]
```

The next call returns the second element of the inner table.

```
> A[1][2], A[1, 2]:
4 4
```

Tables may be nested:

```
> A := [4, [5, [6]]]:
[4, [5, [6]]]
```

To get the number 6, enter the position of the inner table [5, [6] ] as the first index, the position of the inner table [6] as the second index, and the position of the desired entry as the third index:

```
>A[2, 2, 1]:
6
```

With tables that contain other tables, you might get an error if you use an index that does not refer to one of these tables:

```
> A[1][0]:
Error in stdin, at line 1:
    attempt to index field `?` (a number value)
```

Here A [1] $^{2}$ returns the number 4, so the subsequent indexing attempt with $4[0]$ is an invalid expression. You may use the getentry function to avoid error messages:

```
> getentry(A, 1, 0):
null
```

Similarly, the .. operator allows to index tables even if its left-hand side operand evaluates to null. In this case, null will be returned, as well, with no error issued. It is twice as fast as getentry.

```
> create table A;
> A.b:
null
> A.b.c:
Error in stdin, at line 1:
    attempt to index field `b` (a null value)
> A..b..c:
null
```

A generalisation of the .. table field separator are curly braces.

```
> create table A;
> A[1]:
null
> A[1, 2]:
Error in stdin, at line 1:
    attempt to index field `?` (a null value)
> A{1, 2}:
null
```

Sublists of table arrays can be determined with the following syntax:

$$
\text { tablename[ } m \text { to } n \text { ] }
$$

Agena returns all values from and including index position $m$ to $n$, with $m$ and $n$ negative or positive integers or 0 . If there are no values between $m$ and $n$, an empty list will be returned. Table values with non-integral keys are ignored.

```
> A := [10, 20, 30, 40]
> A[2 to 3]:
[2 ~ 20, 3 ~ 30]
```

Tables can contain no values at all. In this case they are called empty tables with values to be inserted later in a session. There are two forms to create empty tables.
create table name ${ }_{1}\left[\right.$, table name $\left._{2}, \ldots\right]$ name $_{1}:=$ []

```
> create table B;
```

creates the empty table B,

```
> B := [];
```

does exactly the same.
You may add a value to a table by assigning the value to an indexed table name:

```
> B[1] := 'a';
```

$>B$ B:
[a]

Alternatively, the insert statement always appends values to the end of a table ${ }^{8}$ :
insert value ${ }_{1}\left[\right.$, value ${ }_{2}, \ldots$ ] into name

```
> insert 'b' into B;
> B:
[a, b]
```

To delete a specific key~value pair, assign null to the indexed table name:

```
> B[1] := null;
> B:
[2 ~ b]
```

The delete ${ }^{9}$ statement works a little bit differently and removes all occurrences of a value from a table.

```
delete value }\mp@subsup{1}{1}{[, value 2, \cdots .] from name
```

```
> insert 'b' into B;
> delete 'b' from B;
> B:
[]
```

In both cases, deletion of values leaves `holes` in a table, which are null values between other non-null values:

```
> B := [1, 2, 2, 3]
> delete 2 from B
> B:
[1 ~ 1, 4 ~ 3]
```

There exists a special sizing option with the create table statement which besides creating an empty table also sets the default number of entries. Thus you may gain some speed if you perform a large number of subsequent table insertions, since with each insertion, Agena checks whether there is enough space to accommodate further elements and allocates more space if necessary, which creates some overhead. The sizing option reserves memory for the given number of elements in advance, so there is no need for Agena to subsequently enlarge the table until the given default size has been exceeded.

[^7]Arrays with a predefined number of entries are created according to the following syntax:
create table name $_{1}\left(\right.$ size $\left._{1}\right)$ [, table name $_{2}\left(\right.$ size $\left.\left._{2}\right), \ldots\right]$

When assigning entries to the table, you will save at least $1 / 3$ of computation time if you know the size of the table in advance and initialise the table accordingly. If you want to insert more values later, then this will be no problem. Agena automatically enlarges the table beyond its initial size if needed.

```
> create table a(5);
> create table a, table b(5);
```


### 4.9.2 Dictionaries

Another form of a table is the dictionary with any kind of data - not only positive integers - as indices:

Dictionaries are created by explicitly passing key-value pairs with the respective keys and values separated by tildes, which is the difference to arrays:

$$
\left[\left[k e y_{1} \sim \text { value }_{1}\left[, \text { key }_{2} \sim \text { value }_{2}, \cdots\right]\right]\right]
$$

```
>A := [1 ~ 4, 2 ~ 5, 3 ~ 6]:
[1 ~ 4, 2 ~ 5, 3 ~ 6]
> B := [abs('p') ~ 'th']:
[231 ~ th]
```

Here is another example with strings as keys:

```
> dic := ['donald' ~ 'duck', 'mickey' ~ 'mouse'];
> dic:
[mickey ~ mouse, donald ~ duck]
```

As you see in this example, Agena internally stores the key-value pairs of a dictionary in an arbitrary order.

As with arrays, indexed names are used to access the corresponding values stored to dictionaries.

```
> dic['donald']:
duck
```

If you use strings as keys, a short form is:

```
> dic.donald:
duck
```

Further entries can be added with assignments such as:

```
> dic['minney'] := 'mouse';
```

which is the equivalent to

```
> dic.minney := 'mouse';
```

With string indices, an alternative to putting keys in quotes with the tilde syntax is:

$$
\left[\left[n a m e_{1}=\text { value } 1, n_{1}, \text { name }_{2}=\text { value }_{2}, \cdots\right]\right] \text { ] }
$$

Hence,

```
> dic := ['donald' ~ 'duck', 'mickey' ~ 'mouse'];
```

and

```
> dic := [donald = 'duck', mickey = 'mouse'];
```

are equal. You can also mix tilde ( ) and equals (=) assignments:

```
> dic := [donald = 'duck', mickey ~ 'mouse'];
```

If you want to enter the result of a Boolean equality check into a table, use the $==$ token instead of the $=$ sign:

```
> value := 1
> [value == 1, value <> 1]:
[true, false]
```

Dictionaries with an initial number of entries are declared like this:

```
create dict name, (size ) [, dict name=2(size}2), . . . ] 
```

You may mix declarations for arrays and dictionaries, so the general syntax is:
create $\{$ table | dict $\}$ name ${ }_{1}\left[\left(\right.\right.$ size $\left.\left._{1}\right)\right][$, \{table | dict $\}$ name $_{2}\left[\left(\right.\right.$ size $\left.\left._{2}\right)\right]$, . . ] $]$

Technically, tables consist of an array and a hash part. The array part usually stores all the elements in an array, the hash part the values of a dictionary. You can both pre-allocate the array and hash part of a table at once:
create table name, (arraysize $_{1}$, hashsize ${ }_{1}$ ) [, ...]

### 4.9.3 Table, Set and Sequence Operators

Agena features some built-in table, set and sequence operators which are described below. A `structure` in this context is a table, set or sequence.

| Name | Return | Function |
| :---: | :---: | :---: |
| c in A | Boolean | Checks whether the structure A contains the given value c. |
| filled A | Boolean | Determines whether a structure contains at least one value. If so, it returns true, else false. |
| empty A | Boolean | Checks whether a structure is empty. |
| $A=B$ | Boolean | Checks whether two structures A, B contain the same values regardless of the number of their occurrence and order; if $B$ is a reference to $A$, then the result is also true. |
| A $<>$ B | Boolean | Checks whether two structures $\mathrm{A}, \mathrm{B}$ do not contain the same values regardless of the number of their occurrence or order; if $B$ is a reference to $A$, then the result is false. |
| $A=B$ | Boolean | Checks whether two structures A, B contain the same number of elements and whether all key~value pairs in tables $A, B$ or entries in the sets, sequences or registers are the same; if $B$ is a reference to $A$, then the result is true. |
| $\operatorname{not}(\mathrm{A}==\mathrm{B})$ | Boolean | The negation of $\mathrm{A}==\mathrm{B}$. |
| $A \sim=B$ | Boolean | Like $==$, but checks the respective elements for approximate equality. Use environ.kernel/eps to change the setting for the accuracy threshold. |
| $\operatorname{not}(\mathrm{A} \sim=\mathrm{B})$ | Boolean | The negation of $A \sim=B$. |
| A subset $B$ | Boolean | Checks whether the values in structure $A$ are also values in B regardless of the number of their occurrence. The operator also returns true if $A=B$. |
| A xsubset B | Boolean | Checks whether the values in structure $A$ are also values in B. Contrary to subset, the operator returns false if $A=B$. |
| $A$ union $B$ | table, <br> set, seq, reg | Concatenates two tables, or two sets, or two sequences or registers $A, B$ simply by copying all its elements - even if they occur multiple times - to a new structure. With sets, all items in the resulting set will be unique, i.e. they will not appear multiple times. |
| A intersect $B$ | table, set, seq, reg | Returns all values in two structures $A, B$ that are included both in $A$ and in $B$ and returns them in a new structure. |


| Name | Return | Function |
| :---: | :---: | :---: |
| $A$ minus $B$ | table, <br> set, seq, <br> reg | Returns all the values in $A$ that are not in $B$ as a new structure. |
| copy A | table, <br> set, seq, reg | Creates a deep copy of structure A, i.e. if A includes other tables, sets, pairs, sequences or registers, copies of these structures are created, too. |
| join A | string | Concatenates all strings in the table, sequence or register A. |
| size $A$ | number | Returns the size of a table A, i.e. the actual number of key~value pairs in A. With sets, sequences and registers, the number of items will be returned. |
| sort(A) | table, seq, reg | This function sorts table, sequence or register $A$ in ascending order. It directly operates on $A$, so it is destructive. With tables, the function has no effect on values that have non-integer keys. Note that sort is not an operator, so you must put the argument in brackets. Please also see Chapter 7 for its derivatives: sorted, skycrane.sorted, stats.issorted, and stats.sorted. |
| unique $A$ | table, seq, reg | Removes multiple occurrences of the same value and returns the result in a new structure. With tables, also removes all holes ('missing keys`) by reshuffling its elements. This operator is not applicable to sets, since they are already unique. |
| sumup A | number | Sums up all numeric table, sequence or register values. If the structure is empty or contains no numeric values, null will be returned. Sets are not supported. |
| qsumup A | number | Raises each value in a table, sequence or register to the power of 2 and sums up these powers. If the structure is empty or contains no numeric values, null will be returned. Sets are not supported. |
| f @ A | table, seq, set, reg | Maps a function $f$ on all elements of structure A. |
| f \$ A | table, <br> set, seq, <br> reg | Selects all elements of a structure A that satisfy a condition given by function f . |
| f \$\$ A | Boolean | Checks whether at least one element in A satisfies the condition checked by function f . |

Table 12: Table, set, and sequence operators
Here are some examples - try them with sets, sequences and registers, as well:
The union operator concatenates two tables simply by copying all its elements even if they occur multiple times.

```
> ['a', 'b', 'c'] union ['a', 'd']:
[a, b, c, a, d]
```

intersect returns all values that are part of both tables as a new table.

```
> ['a', 'b', 'c'] intersect ['a', 'd']:
```

[a]

If a value appears multiple times in the structure at the left hand side of the operator, it is written the same number of times to the resulting structure.
minus returns all the elements that appear in the table on the left hand side of this operator that are not members of the right side table.

```
> ['a', 'b', 'c'] minus ['a', 'd']:
[b, c]
```

If a value appears multiple times in the structure at the left hand side of the operator, it is written the same number of times to the resulting structure.

The unique function

- removes all holes (‘missing keys`) in a table,
- removes multiple occurrences of the same value.
and returns the result in a new table. The original table is not overwritten. In the following example, there is a hole at index 2 and the value ' a ' appears twice.

```
> unique [1 ~ 'a', 3 ~ 'a', 4 ~ 'b']:
[b, a ]
```

You can search a table for a specific value with the in operator. It returns true if the value has been found, or false, if the element is not part of the table. Examples:

```
> 'a' in ['a', 'b', 'c']:
```

returns true.

```
> 1 in ['a', 'b', 'c']:
```

returns false. Remember that in only checks the values of a table, not its keys.

### 4.9.4 Table Functions

Agena has a number of functions that work on tables (and sequences and registers), for instance:

| Function | Description | Further detail |
| :---: | :---: | :---: |
| $\operatorname{map}(f, o)$ <br> $\operatorname{map}(f, g)$ | Maps a function $f$ onto all elements of structure o, or produces the function composition f @ g. | $f$ may be an anonymous function, as well. See also zip in Chapter 8. |
| purge(o, key) | Removes index key and its corresponding value from o. | All elements to the right are shifted down, so that no holes are created. |
| put(o, key, value) | Inserts a key ~ value pair into structure o . | The original element at position key and all other elements are shifted up one place. |
| select( $f, 0$ ) | Returns all the elements that satisfy the Boolean condition given by function $f$. | $f$ may be also an anonymous function. The remove function conducts the opposite operation. |
| subs( $0, x: V$ ) | Substitutes all occurrences of value $x$ in $o$ with value $v$. |  |
| binsearch(0, i) | Performs a binary search in a table. | With large tables, the function is much faster than the in operator. |

Table 13: Basic table library procedures
The map function is quite handy to apply a function with one or more arguments to all elements of a structure in one stroke:

```
> map(<< x -> x^2 >>, [1, 2, 3]):
[1, 4, 9]
```

The @ operator also maps a function on all elements of a structure. Contrary to map, it accepts univariate functions only, but is faster:

```
> << x -> x^2 >> @ [1, 2, 3]:
[1, 4, 9]
```

Likewise, the faster \$ operator selects all the elements of a structure that satisfy a condition checked by a univariate function.

```
> << x -> x > 1 >> $ [1, 2, 3]:
[2, 3]
```

Suppose we want to add a new entry 10 at position 3 of table $c^{10}$ :

```
> C := [1, 2, 3, 4]
> put(C, 3, 10)
```

[^8]```
> C:
[1, 2, 10, 3, 4]
```

Now we remove this new entry 10 at position 3 again:

```
> purge(C, 3)
> C:
[1, 2, 3, 4]
```

Determine all elements in c that are even:

```
> select(<< x -> even(x) >>, C):
[2 ~ 2, 4 ~ 4]
```

Or return all elements not even:

```
> remove(<< x -> even(x) >>, C):
[1 ~ 1, 3 ~ 3]
```

Note that remove and select do not alter the original structure passed as the second argument.
zip zips together two tables by applying a function to each of its respective elements.
> C :
$[1,2,3,4]$
> zip(<< (x, y) -> x + y >>, C, [10, 20, 30, 40]):
[11, 22, 33, 44]
For other functions, have a look at Part II of this manual and the Agena Quick Reference Excel sheet.

### 4.9.5 Table References

If you assign a table to a variable, only a reference to the table is stored in the variable. This means that if we have a table
$>A:=[1,2] ;$
assigning
> B := A;
does not copy the contents of $A$ to $B$, but only the address of the same memory area which holds table [1, 2], hence:

```
> insert 3 into A;
```

```
> A:
[1, 2, 3]
```

also yields:
> B :
[1, 2, 3]

Use copy to create a true copy of the contents of a table. If the table contains other structures, copies of these structures are also made (so-called `deep copies'). Thus copy returns a new table without any reference to the original one.

```
> B := copy(A);
> insert 4 into A;
> B:
[1, 2, 3]
```

With structures such as tables, sets, pairs, sequences or registers, all names to the left of an -> token will point to the very same structure to its right.
$>A, B->[]$
> $A[1]:=1$
> B :
[1]
Tables can also directly or indirectly contain themselves, in which case they are also called `cycles`. Just some few examples:

```
> A := []
> A := [A, A]
> A:
[[], []]
> A.A := A
> A:
[1 ~ [], 2 ~ [], A ~ circum_table(0236A460)]
```


### 4.9.6 Unpacking Tables by Name

There is syntactic sugar for the assignment statement to unpack named values, i.e. data indexed with string keys, from tables using the in keyword:

$$
\mathrm{key}_{1}\left[, \text { key }_{2}, \ldots\right] \text { in tablename }
$$

is equal to

$$
\text { key }_{1}\left[, \text { key }_{2}, . . \cdot\right]:=\text { tablename. } \text { key }_{1}\left[\text {, tablename. key }{ }_{2}, \ldots\right]
$$

A short example may suffice:

```
> zips := [duedo = 40210:40629,
    bonn = 53111:53229,
    cologne = 50667:51149];
> duedo, bonn in zips
> duedo, bonn, cologne:
40210:40629 53111:53229 null
```

The local statement, see Chapter 6.2, supports this sugar, as well. Read also Chapter 5.2.12 for a variant implemented available in the with statement.

### 4.9.7 Defining Multiple Constants Easily

The // ... <br> constructor allows to define a table of constant numbers and/or strings the simple way: items may not be separated by commas, and strings do not need to be put in quotes as long as they satisfy the criteria for valid variable names: names starting with a hyphen or letter, including diacritics - and keywords such like while, sqit, etc. do not have to be passed in quotes. Records are supported as well. Expressions like `sin(0)` etc. are not parsed and rejected. Example:

```
> a := // 0~0 1 2 3 zero one two three '2and3' sqrt ~ while \\:
[0 ~ 0, 1 ~ 1, 2 ~ 2, 3 ~ 3, 4 ~ zero, 5 ~ one, 6 ~ two, 7 ~ three,
8 ~ 2and3, sqrt ~ while]
```


### 4.10 Sets

Sets are collections of unique items: numbers, strings, and any other data except null. Their syntax is:

$$
\left\{\left[\text { item }\left[\text {, item }{ }_{2}, \cdots\right]\right]\right\}
$$

Thus, they are equivalent to Cantor sets: An item is stored only once.

```
>A}:={1, 1, 2, 2}
{1, 2}
```

Besides being commonly used in mathematical applications, they are also useful to hold word lists where it only matters to see whether an element is part of a list or not:

```
> colours := {'red', 'green', 'blue'};
```

If you want to check whether the colour red is part of the set colours, just index it as follows:

```
setname[item]
```

If an element is stored to a set, Agena returns true:

```
> colours['red']:
true
```

If an item is not in the given set, the return is false. Note that we can use the same short form for indexing values (without quotes) as can be done with tables.

```
> colours.yellow:
false
```

If you want to add or delete items to or from a set, use the insert and delete statements. The standard assignment statement setname [key] := value is also supported.
insert item ${ }_{1}\left[\right.$, item $\left.{ }_{2}, ~ . ..\right]$ into name
delete item ${ }_{1}$ [, item $\left.{ }_{2}, ~ . ..\right]$ from name

```
> insert 'yellow' into colours;
```

The in operator checks whether an item is part of a set - it is an alternative to the indexing method explained above, and returns true or false, too.

```
> 'yellow' in colours:
true
```

The data type of a set is set.

```
> type(colours):
set
```

You may predefine sets with a given number of entries according to the following syntax:
create set name ${ }_{1}\left[\left(\right.\right.$ size $\left.\left._{1}\right)\right]\left[\right.$ set name $_{2}\left[\right.$ size $\left._{2}\right)$ ], $\cdots$ ]

When assigning items later, you will save at least $90 \%$ of computation time if you know the size of the set in advance and initialise it with the maximum number of future entries as explained above. More items than stated at initialisation can be
entered anytime, since Agena automatically enlarges the respective set accordingly and will also reserves space for additional entries.

Sets are useful in situations where the number of occurrence of a specific item or its position does not concern. Compared to tables, sets consume around $40 \%$ less memory, and operations with them are $10 \%$ to $33 \%$ faster than the corresponding table operations.

Specifically, the more items you want to store, the faster operations will be compared to tables.

Note that if you assign a set to a variable, only a reference to the set is stored in the variable. Thus in a statement like A := \{\}; B := A, A and B point to the same set. Use the copy function if you want to create `independent` sets.

Sets can also include themselves, just an example:

```
>A := {}
>A := {A, A}:
{ {} }
```

If you want to know the number of occurrence of a unique element in a distribution, the bags package might be of interest, see Chapter 10.8.

The following operators operate on sets:

| Name | Return | Function |
| :--- | :--- | :--- |
| C in A | Boolean | Checks whether the set A contains the given value C. |
| filled A | Boolean | Determines whether a set contains at least one value. <br> If so, it returns true, else false. |
| empty A | Boolean | Checks whether a set is empty. |
| A = B | Boolean | Checks whether two sets A, B contain the same values; <br> if B is a reference to A, then the result is also true. |
| A <> B | Boolean | Checks whether two sets $A, B$ do not contain the same <br> values; if B is a reference to A, then the result is false. |
| A == B | Boolean | Same as =. |
| A subset B | Boolean | Checks whether the values in set $A$ are also values in B. <br> The operator also returns true if $A=B$. |
| A xsubset B | Boolean | Checks whether the values in set A are also values in B. <br> Contrary to subset, the operator returns false if A $=B$. |
| A union B | set | Concatenates two sets A, B simply by copying all its <br> elements to a new set. All items in the resulting set will <br> be unique, i.e. they will not appear multiple times. |
| A intersect B | set | Returns all values in two sets A, B that are included <br> both in A and in B as a new set. |
| A minus B | set | Returns all the values in A that are not in B as a new <br> set. |


| Name | Return | Function |
| :--- | :--- | :--- |
| copy A | set | Creates a deep copy of the set A, i.e. if A includes <br> other tables, sets, pairs, sequences or registers, copies <br> of these structures are built, too. |
| size A | number | Returns the size of a set A, i.e. the actual number of <br> elements in A. |
| f @ A | set | Maps a function fon all elements of a set A. <br> f \$ A set |
| Selects all elements in A that satisfy a given condition <br> checked by function $f$. |  |  |
| f\$ A | Boolean | Checks the elements in $A$ whether at least one satisfies <br> a given condition checked by function $f$. |

Table 14: Set operators

### 4.11 Sequences

Besides storing values in tables or sets, Agena also features the sequence, an object which can hold any number of items except null. You may sequentially add items and delete items from it. Compared to tables, insertion and deletion are twice as fast with sequences. Contrary to all other data structures, Agena automatically frees the memory occupied by a sequence if you remove values from it ${ }^{11}$.

Sequences store items in sequential order. As with tables, an item may be included multiple times. Sequences are usually indexed with positive integers in the same fashion as table arrays are, starting at index 1 . If you pass a negative index $n$, then the $|n|$-th value from the right end, i.e. the top of the sequence is determined. Non-integral indices are not allowed. As with tables, you can compute the index in assignments or queries.

Suppose we want to define a sequence of two values. You may create it using the seq operator.

```
seq([ item}1[, item2, ...]] ]
```

```
>a := seq(0, 1, 2, 3);
> a:
seq(0, 1, 2, 3)
```

You can access the items the usual way:

```
seqname[index]
```

```
> a[1]:
0
```

[^9]```
> a[2]:
1
```

If the index is larger than the current size of the sequence, an error will be returned ${ }^{12}$.

```
> a[5]:
Error, line 1: index out of range
```

Sublists of sequences can be determined with the following syntax:

## seqname[ $m$ to $n$ ]

Agena returns all values from and including index position $m$ to $n$, with $m$ and $n$ positive or negative integers. In case of a non-existing key, an error will be issued.

```
> a[2 to 3]:
seq(1, 2)
```

The way Agena outputs sequences can be changed by using the settype function.
In general, the settype function allows you to set a user-defined subtype for a sequence, set, table or pair.

```
> a := seq(0, 1);
> settype(a, 'duo');
> a:
duo(0, 1)
```

The gettype function returns the new type you defined above as a string:

```
> gettype(a):
duo
```

If no user-defined type has been set, gettype returns null.
Once the type of a sequence has been set, the typeof operator also returns this user-defined sequence type and will not return ' sequence' .

```
> typeof(a), gettype(a):
duo duo
```

This allows you to programme special operations only applicable to certain types of sequences.

The :: and :- operators can check user-defined types. Just pass the name of your type as a string:

[^10]```
> a :: 'duo':
true
> a :- 'duo':
false
```

Note that if a user defined-type has been given, the check for a basic type with the :: and :- operators will return also return true or false.

```
> a :: sequence:
true
> a :- sequence:
false
```

A user-defined type can be deleted by passing null as a second argument to settype.

```
> settype(a, null);
> typeof(a):
sequence
```

The create sequence statement creates an empty sequence and optionally allows to allocate enough memory in advance to hold a given number of elements (which can be inserted later). Agena automatically will extend the sequence, if the predetermined number of items is exceeded. The sequence and seq keywords are synonyms.

```
    create sequence name, [, seq name2, ...]
create sequence name, (size}\mp@subsup{)}{1}{}\mathrm{ [, seq name ( (size ), .. .]
```

Items can be added only sequentially. You may use the insert statement for this or the conventional indexing method.

```
> create sequence a(4);
> insert 1 into a;
> a[2] := 2;
> a:
seq(1, 2)
```

Note that if the index is larger than the number of items stored to it plus 1, Agena returns an error in assignment statements, since `holes` in a sequence are not allowed. The next free position in a is at index 3 , however a larger index is chosen in the next example.

```
> a[4] := 4
Error, line 1: index out of range
> a[3] := 3
```

Items can be deleted by setting their index position to null, or by applying delete, i.e. stating which items - not index positions - shall be removed. Note that all items to the right of the value deleted are shifted to the left, thus their indices will change.

```
> a[1] := null
>a:
seq(2, 3)
> delete 2, 3 from a
> a:
seq()
```

Thus concerning the insert and delete statements, we have the following familiar syntax:

```
insert item, [, item}\mp@subsup{2}{2}{\prime}...]] into name
delete item}1[\mathrm{ [, item2, . . ] ] from name
```

If you assign a sequence to a variable, only a reference to the sequence is stored in the variable. Thus sequences behave the same way as tables and sets do, i.e. in a statement like A $:=\operatorname{seq}()$; $B \quad:=A, A$ and в point to the same sequence in memory. Use the copy function if you want to create `independent` sequences.

```
> A := seq()
> B := A
> A[1] := 10
> B:
seq(10)
```

As with tables and sets, sequences can also reference to themselves:

```
> A := seq()
>A[1] := A
>A[2] := A
> A:
seq(circum_sequence(01E647D8), circum_sequence(01E647D8))
```

The following operators, functions, and statements operate on sequences:

| Name | Description | Example |
| :--- | :--- | :--- |
| $=$ | Equality check the Cantor way | $\mathrm{a}=\mathrm{b}$ |
| $==$ | Strict equality check | $\mathrm{a}==\mathrm{b}$ |
| $\sim=$ | approximate equality check | $\mathrm{a} \sim=\mathrm{b}$ |
| $<>$ | Inequality check the Cantor way | $\mathrm{a}<>\mathrm{b}$ |
| $::$ | Type check operator | $\mathrm{a}::$ sequence <br> $\mathrm{a}:: ~$ usertype $^{\prime}$ |


| Name | Description | Example |
| :---: | :---: | :---: |
| :- | Negation of type check operation | a :- sequence a :- 'usertype' |
| @ | Maps a function on all elements of a sequence. | f @ a |
| \$ | Selects all elements of A that satisfy a given condition. |  |
| \$\$ | Checks whether at least one element in A satisfies a condition. | f \$\$ a |
| insert | Inserts one or more elements. | insert 1 into a |
| delete | Deletes one or more elements. | $\begin{gathered} \text { delete 0, } 1 \\ \text { from a } \\ \hline \end{gathered}$ |
| bottom | Returns the item with key 1. | bottom a |
| top | Returns the item with the largest key. | top a |
| pop | as an operator works like top but also removes the item from the sequence | pop a |
| copy | Creates an exact copy of a sequence; deep copying is supported so that structures inside sequences are properly treated. | copy a |
| filled | Checks whether a sequence has at least one item. | filled a |
| empty | Checks whether a sequence is empty. | empty a |
| getentry | Returns entries without issuing an error if a given index does not exist. | getentry (a, 1, 3) |
| in | Checks whether an element is stored in the sequence, and returns true or false. See also binsearch. | 0 in seq(1, 0) |
| join | Concatenates all strings in a sequence in sequential order. | join(a) |
| pop | Pops the first or the last element from a sequence. | pop bottom from a pop top from a |
| size | Returns the current number of items. | size a |
| sort | Sorts a sequence in place. Please also see Chapter 7 for its derivatives: sorted, skycrane.sorted, stats.issorted, and stats.sorted. | sort (a) |
| type | Returns the general type of a sequence, i.e. sequence. | type a |
| typeof | Returns the user-defined type of a sequence, or the basic type if no special type has been defined. | typeof a |
| unique | Reduces multiple occurrences of an item in a sequence to just one. | unique a |
| unpack | Unpacks a sequence. See unpack in Chapter 8. | unpack (a) |
| nseq | Creates a new sequence and fills it with values | $\begin{gathered} \text { nseq }(\ll x \rightarrow x \\ \gg 1,10) \end{gathered}$ |
| map | Maps a function on all elements of a sequence. | $\begin{aligned} & \operatorname{map}\left(\ll x->x^{\wedge} 2\right. \\ & \ggg, \operatorname{seq}(1,2,3)) \end{aligned}$ |


| Name | Description | Example |
| :---: | :---: | :---: |
| zip | Zips together two sequences by applying a function to each of its respective elements. |  |
| intersect | Searches all values in one sequence that are also values in the other sequence and returns them in a new sequence. | $\begin{aligned} & \operatorname{seq}(1,2) \\ & \text { intersect } \\ & \operatorname{seq}(2,3) \end{aligned}$ |
| minus | Searches all values in one sequence that are not values in the other sequence and returns them as a new sequence. | $\begin{aligned} & \operatorname{seq}(1,2) \\ & \text { minus } \operatorname{seq}(2,3) \end{aligned}$ |
| subset | Checks whether all values in a sequence are included in the other sequence. | $\begin{aligned} & \text { seq(1) } \\ & \text { subset } \operatorname{seq}(1,2) \end{aligned}$ |
| union | Concatenates two sequences simply by copying all its elements. | $\begin{aligned} & \operatorname{seq}(1,2) \\ & \text { union } \operatorname{seq}(2,3) \end{aligned}$ |
| settype | Sets a user-defined type for a sequence. | settype(a, 'duo') |
| gettype | Returns a user-defined type for a sequence. | gettype (a) |
| setmetatable | Assigns a metatable to a sequence. | setmetatable <br> (a, mtbl) |
| getmetatable | Returns the metatable stored to a sequence. | getmetatable(a) |

Table 15: Basic sequence operators and functions
For more functions, consult the Agena Quick Reference Excel sheet. Also, you may have a look at the llist linked list package presented in Chapter 6.27, if you have to conduct a lot of insertions and/or deletions in a data structure.

The (/ ... <br>) constructor allows to define a sequence of constant numbers and/or strings the simple way: items may not be separated by commas, and strings do not need to be put in quotes as long as they satisfy the criteria for valid variable names(name starting with a hyphen or letter, including diacritics) or if they are keywords. Expressions like `sin(0) etc. are rejected.

Example:

```
> a := (/ 0 1 2 3 zero one two three '2and3' while \):
seq(0, 1, 2, 3, zero, one, two, three, 2and3), while]
```


### 4.12 Stack Programming

Sequences and sometimes table arrays can be used to implement stacks, and besides the insert/into statement to put an element to the top, an efficient statement is available to remove an item from the bottom or from the top of the stack:

## pop bottom from name

pop top from name

Both variants work on tables even if their integer keys are not distributed consecutively.

The bottom and top operators return the element at the bottom of the stack and the top of the stack, respectively. They both do not delete the element returned from the stack.

```
> stack := seq();
> insert 10, 11, 12 into stack;
> bottom(stack):
1 0
> top(stack):
1 2
> pop bottom from stack;
> pop top from stack;
> stack:
seq(11)
```

The rotate statement moves each element in a sequence or the array part of a table one position to the bottom (downwards) or to the top (upwards):

```
rotate bottom name
    rotate top name
```

The element at the bottom or the top is moved to the top or the bottom, respectively.

```
> s := seq(1, 2, 3);
> rotate bottom s;
> s:
seq(2, 3, 1)
> s := seq(1, 2, 3):
seq(1, 2, 3)
> rotate top s;
> s:
seq(3, 1, 2)
```

The pop operator - contrary to top - both returns the top element of a sequence or register and then removes it from the structure. With tables, it returns the value indexed by the largest integer key and then also removes it.

```
> pop(s):
2
> S:
seq(3, 1)
```

There are two other statements that work on sequences and registers only: The exchange statement swaps the two topmost elements, and the duplicate statement adds a copy of the current topmost element to the end of the structure.

```
> exchange s
> S:
seq(1, 3)
> duplicate s
> s:
seq(1, 3, 3)
```

You may try to use the put function to insert new values in the interior of a stack, shifting up other values to open space, and purge to delete values in the interior of a stack.

See also Chapter 14.6 for the six built-in number and character stacks.

### 4.13 More on the create Statement

You cannot only initialise any table arrays with the create statement, but also dictionaries, sets, and sequences with only one call and in random order, so the following statement is valid:

```
> create table a, dict b(10), set c, sequence d(100), table e(10);
> a, b, c, d, e:
[] [] {} seq() []
```


### 4.14 Pairs

The structure which holds exactly two values of any type (including null and other pairs) is the pair. A pair cannot hold less or more values, but its values can be changed. Conceived originally to allow passing options in a more flexible way to functions, it is defined with the colon operator:

```
item1 : item_
```

```
> p := 1:2
```

```
> p:
1:2
```

The left and right operators provide read access to its left and right operands; the standard indexing method using indexed names is supported, as well:

```
left [(] pair [)] right [(] pair [)]
```

```
> left(p), p[1]:
1 1
> right p, p[2]:
2 2
```

An operand of an existing pair can be changed by assigning a new value to an indexed name, where the left operand is indexed with number 1 , and the right operand with number 2 :

```
> p[1] := 2;
> p[2] := 3;
```

You can compute the index as long as the result evaluates to the integers 1 or 2, as well.

As with sequences, you may define user-defined types for pairs with the settype function which also changes the way pairs are output.

```
> typeof(p):
pair
> settype(p, 'duo');
> p:
duo(2, 3)
> typeof(p):
duo
> gettype(p):
duo
> p :: pair:
true
> p :: 'duo':
true
```

The only other operators besides left and right that work on pairs are equality $(=,==$, $\sim=$ ), inequality (<>, ~<>), ::, :-, type, typeof, and in.
$>p=3: 2:$
false

With pairs consisting of numbers, the in operator checks whether a left-hand argument number is part of a closed numeric interval given by the given right-hand argument pair.

```
> 2 in 0:10:
true
> 's' in 0:10:
fail
```

As with all other structures, if you assign a pair to a variable, only a reference to the pair is stored in the variable. Thus in a statement like $A:=a: b ; B:=A, A$ and $B$ point to the same pair. Use the copy function if you want to create 'independent` pairs.

Summary:

| Name | Description | Example |
| :---: | :---: | :---: |
| $=$, $==$, $\sim=$ | Equality checks (mostly same functionality) | $a=$ |
| <> | Inequality check | a <> b |
| :: | Type check operator | $\begin{aligned} & \text { a }:: \text { pair } \\ & \text { a }:: \text { 'udeftype } \end{aligned}$ |
| :- | Negation of type check operation | a :- pair <br> a :- 'udeftype' |
| @ | Maps a function on each operand. | f e a |
| copy | Creates an exact copy of a pair; deep copying is supported so that structures inside pairs are properly treated. | copy a |
| in | If the left operand $x$ is a number and if the left and right hand side of the pair $a: b$ are numbers, then the operator checks whether $x$ lies in the closed interval [a,b] and returns true or false. If at least one value $x, a, b$ is not a number, the operator returns fail. | 1.5 in 1:2 |
| left | Returns the left operand of a pair. | left (a) |
| right | Returns the right operand of a pair. | right (a) |
| type | With pairs, always returns 'pair'. | type (a) |
| typeof | Returns either the user-defined type of the pair, or the basic type ('pair') if no special type was defined for the pair. | typeof (a) |
| settype | Sets a user-defined type for a pair. | settype(a, 'duo') |
| gettype | Returns the user-defined type of a pair. | gettype (a) |
| setmetatable | Sets a metatable to a pair. | $\begin{aligned} & \text { setmetatable(p, } \\ & \text { mtbl) } \end{aligned}$ |
| getmetatable | Returns the metatable stored to a pair. | getmetatable (p) |

Table 16: Operators and functions applicable to pairs

### 4.15 Registers

Registers are memory-efficient, fixed-size Agena `sequences` that also store null's. They are not automatically extended if more values have to be added, but can be manually resized.

Registers allow to hide data: by changing the pointer to the top of a register using registers.settop, any values stored above (the position of) this pointer can neither be read nor changed by any of Agena's functions and operators. Registers are supported by most of the existing statements, operators and functions. Please also refer to Chapter 6.15 `Sandboxes`.

The concept of the fixed size and the top pointer is key to understanding and working with registers.

By default, the top pointer always refers to the very last element in a register - it is automatically changed only if an element is removed with the pop top or pop bottom statements, the pop operator or the purge function.

In general, registers can save memory if you know the precise number of values to be stored, or to be added or removed later, in advance. As such, they behave like C arrays storing any value without provoking faults. With respect to sequences, there usually are no performance gains with most operations - but since registers do not automatically shift elements, they are eight times faster when deleting items.

Let us first create a register with eight items:

```
> a := reg(1, 2, 3, 4, 5, 6, 7, 8):
reg(1, 2, 3, 4, 5, 6, 7, 8)
```

Read the first element:

```
> a[1]:
```

1

Set the first entry to null - contrary to other data structures, the size of register is not reduced, and no values are shiffed.

```
> a[1] := null;
> a:
reg(null, 2, 3, 4, 5, 6, 7, 8)
```

Now reset the pointer to the top of the register to the fourth element:

```
> registers.settop(a, 4);
> size(a):
4
> a:
reg(null, 2, 3, 4)
```

```
> a[5]:
In stdin at line 1:
    Error: register index 5 out of current range.
Stack traceback:
    stdin, at line 1 in main chunk
```

By changing the position of the top pointer beyond 4, we can read and change the values again:

```
> registers.settop(a, 8);
reg(null, 2, 3, 4, 5, 6, 7, 8)
```

When passing no elements to the reg operator, by default a register with sixteen slots is created.

```
> reg():
reg(null, null, null, null, null, null, null, null, null, null, null, null,
null, null, null, null)
```

But you can change this default to another value:

```
> environ.kernel(regsize = 8);
> reg():
reg(null, null, null, null, null, null, null, null)
```

Registers containing null's may issue errors with some functions or operators.
Changing the size of a register at runtime is easy:

```
> b := reg('a', 'b', 'c'):
reg(a, b, c)
```

register.extend enlarges a register to the given number of elements.

```
> registers.extend(b, 8);
> b:
reg(a, b, c, null, null, null, null, null)
```

register.reduce shrinks a register to the given number of elements.

```
> registers.reduce(b, 4);
> b:
reg(a, b, c, null)
```

Registers support metamethods and user-defined types. To hide the current size of the register as defined above, we could assign:

```
> size a:
```

8

```
> mt := [
    '__size' ~ proc(x) is
        return 0
    end
]
setmetatable(a, mt);
> size a:
0
```

| Name | Description | Example |
| :---: | :---: | :---: |
| $=$ | Equality check the Cantor way | $\mathrm{a}=\mathrm{b}$ |
| $=$ = | Strict equality check | $\mathrm{a}==\mathrm{b}$ |
| $\sim$ | Approximate equality check | $\mathrm{a} \sim=\mathrm{b}$ |
| <> | Inequality check the Cantor way | a <> b |
| :: | Type check operator | a :: register |
| :- | Negation of type check operation | a :- register |
| @ | Maps a function on all elements of a register. | f e a |
| \$ | Selects all elements of a that satisfy a given condition. | f \$ a |
| \$\$ | Checks whether at least one element satisfies a given condition. | f \$\$ a |
| insert | Inserts an element at the first position that holds a null value. | $\begin{gathered} \text { insert 0, } 1 \\ \text { into a } \end{gathered}$ |
| delete | Deletes one or more elements and replaces them with null. | $\underset{\text { drom } \begin{array}{c} \text { delete } \end{array}, \quad 1}{ }$ |
| bottom | Returns the item with key 1. | bottom a |
| top | Returns the item with the largest key. | top a |
| pop | as an operator works like top but also removes the item from the register. | pop a |
| copy | Creates an exact copy of a register; deep copying is supported so that structures inside register are properly treated. | copy a |
| filled | Checks whether a register has at least one item, including null. This is always true. | filled a |
| getentry | Returns entries without issuing an error if a given index does not exist. | getentry (a, 1, 3) |
| in | Checks whether an element is stored in the register, returns true or false. | 0 in reg (1, 0) |
| pop <br> bottom/ top | Pops the first or the last element from a register, shifting other elements to close the space, if necessary. Reduces the size of the register by one. | pop bottom from a pop top from a |
| size | Returns the number of `visible` elements. | size a |
| sort | Sorts a register in place. Please also see sorted. | sort(a) |


| Name | Description | Example |
| :---: | :---: | :---: |
| type | Returns the general type of a register, i.e. register. | type a |
| unique | Reduces multiple occurrences of an item in a register to just one. | unique a |
| unpack | Unpacks a register. See unpack in Chapter 8. | unpack (a) |
| duplicates | Finds duplicate elements. | duplicates(a) |
| map | Maps a function on all elements of a register. | $\begin{aligned} & \operatorname{map}\left(\ll x->x^{\wedge} 2\right. \\ & \gg, r \operatorname{reg}(1,2,3)) \end{aligned}$ |
| purge | Removes the value at the given position and shifts all elements to close the space. Also reduces the size of the register by one. |  |
| zip | Zips together two registers by applying a function to each of its respective elements. | $\begin{gathered} \text { zip }(\ll x, y \text { y } \quad \text {-> } \\ x+y=\gg, \\ \operatorname{reg}(1,2), \\ \operatorname{reg}(3,4)) \end{gathered}$ |
| intersect | Searches all values in one register that are also values in another register and returns them in a new register. | $\begin{aligned} & \text { reg }(1,2) \\ & \text { intersect } \\ & \text { reg }(2,3) \end{aligned}$ |
| minus | Searches all values in one register that are not values in another register and returns them as a new register. | $\begin{aligned} & \operatorname{reg}(1,2) \\ & \text { minus reg }(2,3) \end{aligned}$ |
| subset | Checks whether all values in a register are included in another register. | $\begin{aligned} & \text { reg(1) } \\ & \text { subset reg (1, 2) } \end{aligned}$ |
| xsubset | Checks whether all values in a register are included in another register. | $\begin{aligned} & \text { reg(1) } \\ & \text { xsubset reg }(1,2) \end{aligned}$ |
| union | Concatenates two registers simply by copying all its elements. | $\begin{aligned} & \text { reg }(1,2) \\ & \text { union } r e g(2,3) \end{aligned}$ |
| setmetatable | Assigns a metatable to a register. | setmetatable <br> (a, mtbl) |
| getmetatable | Returns the metatable stored to a register. | getmetatable(a) |
| registers. settop | Resets the top pointer to the given position, an integer. |  |
| registers. reduce | Shrinks the size of a register to the given value. |  |
| registers. extend | Enlarges the size of a register to the given value. |  |
| environ. kernel/ regsize | Sets the default size of newly created registers the given value, a non-posint. |  |

Table 17: Some operators and functions applicable to registers

### 4.16 Exploring the Internals of Structures

If you would like to know how a table, set, sequence, register or pair is represented internally, please have a look at the environ.attrib function explained in Chapter 14.2. It might help when debugging code.

The function returns the estimated number of bytes used by a structure, how many slots have been pre-allocated and how many are actually occupied, whether a user-defined type has been set, how many elements have been allocated to the array and hash parts of a table, etc.

### 4.17 Other Types

For threads, userdata, and lightuserdata please refer to the Lua 5.1 documentation and Chapter 6.30.

Agena supports the following metamethods with userdata: =, ==, $\sim=$, size, in, union, intersect, minus, sumup, and qsumup. '__index', '__writeindex','__gc', and '__tostring' are supported, as well.

Chapter Five

## Control

## 5 Control

### 5.1 Conditions

Depending on a given condition, Agena can alternatively execute certain statements with either the if or case statement.

### 5.1.1 if Statement

The if statement checks a condition and selects one statement from many listed. Its syntax is as follows:

```
if condition, then
    statements,
[elif condition_2 then
    statements_]
[onsuccess
    statements 3]
[else
    statements_]
fi
```

The condition may always evaluate to one of the Boolean values true, false or fail, or to any other value.


The elif, else, and onsuccess clauses are optional. While more than one elif clause can be given, only one else and one onsuccess clause is accepted.

If an if or elif condition results to true or any other value except false, fail or null, its corresponding then clause is executed. If all conditions result to false, fail or null, the else clause is executed if present - otherwise Agena proceeds with the next statement following the fi keyword.

If an onsuccess clause is given, and an if or elif condition results to true, the statements in this onsuccess branch are executed. This allows to move code common to all then clauses into one single branch, reducing code size. When
using both onsuccess and else clauses, the onsuccess clause must be put given before the else snippet.

## Examples:

The condition true is always true, so the string 'yes' is printed.

```
> if true then
    print('yes')
> fi;
yes
```

The next example demonstrates the behaviour if the condition is neither a Boolean nor null:

```
> if 1 then
    print('One')
> fi;
One
```

In the following statement, the condition evaluates to false, so nothing is printed:

```
> if 1 <> 1 then
    print('this will never be printed')
> fi;
```

An if statement with an else clause:

```
> if false then
    print('this will never be printed')
else
    print('this will always be printed')
> fi;
this will always be printed
```

An if statement with an elif clause:

```
> if 1 = 2 then
    print('this will never be printed')
< elif 1 < 2 then
print('this will always be printed')
> fi;
this will always be printed
```

An if statement with elif and else clauses:

```
> if 1 = 2 then
    print('this will never be printed')
elif 1 < 2 then
    print('this will always be printed')
else
    print('neither will this be printed')
> fi;
this will always be printed
```

Sometimes certain conditions may just be skipped with an empty statement, denoted by do nothing, to make the code more readable:

```
> if 1 = 2 then
> do nothing
< elif 1 < 2 then
    print('this will always be printed')
else
    print('neither will this be printed')
fi;
this will always be printed
```

One last example, this time demonstrating the optional onsuccess clause. As shown, both then statements include the same flag := true statement.

```
if 1 = 2 then
    print('this will never be printed');
    flag := true
elif 1 = 1 then
    print('this will always be printed');
    flag := true
else
    flag := false
fi;
this will always be printed
> flag:
true
```

So the two assignment statements may be moved into one onsuccess clause.

```
> if 1 = 2 then
    print('this will never be printed');
elif 1 = 1 then
    print('this will always be printed');
onsuccess
    flag := true
else
    flag := false
fi;
this will always be printed
> flag:
true
```

if and elif statements also support simple assignments in the conditions, as well.

```
> if flag := true then
    print('Output: ' & flag)
> fi;
Output: true
```

Only if the right-hand side of the assignment does neither result to false, fail nor null, will the corresponding then clause be executed.

You can also combine an assignment and a condition in the if clause:

```
> if c := 0, c >= 0 do
print(c)
od;
0
```


### 5.1.2 if Operator, Version One

The if operator checks a condition and returns the respective expression.
[with name ${ }_{1}, \ldots$ := expr $\left._{1}, \cdots[->]\right]$
if condition $n_{1}$ then expr $_{1}\left[\right.$ elif condition ${ }_{2}$ then expr $_{2}, \cdots$ ] else expr ${ }_{k}$ fi

The result is expression expr $r_{1}$ if condition ${ }_{1}$ is true or any other value except false, fail or null; and expr ${ }_{k}$ otherwise. You can also optionally add one or more elif clauses.

Example:

```
> x := if 1 = 1 then true else false fi:
true
```

which is the same as:

```
> if 1 = 1 then
> x := true
> else
    x := false
> fi;
```

The if operator only evaluates the expression that it will return. Thus the other expression which will not be returned will never be checked for semantic correctness, e.g. out-of-range indices, etc. You may nest if operators.

An optional preceding with clause allows to define one or more auxiliary variables that are local to this operator only:

```
> x := Pi;
> a := with n := 2*x -> if x < 0 then n else 2*n fi;
```

which is syntactic sugar for:

```
> x := Pi;
> scope
    local n := 2*x;
    a := if x < 0 then n else 2*n fi
    epocs;
```

The arrow token is optional. Multiple auxiliary variables are defined as follows:

```
> a := with m, n := x, 2*x -> if x < O then m else n fi;
```

The if operator cannot return multiple values, only one.

### 5.1.3 if Operator, Version Two

There is a second operator form, reminiscent to the if statement; for example:

```
> a := 10;
> sgn := if is a < 0 then # determines sign of `a'
> print('I am negative');
> [further statements ...]
    return -1
    elif a = 0 then
        print('I am zero');
        return 0
        else
        return 1
        fi;
sgn:
```

You may omit the elif and else clauses. Each clause may contain zero, one ore more statements, but it must always finish with the return expression which defines the resulting value ( $-1,0$ or 1 in the example above). In procedures, this special return expression does not cause a procedure to quit. Note that if the else clause is omitted, the operator returns null if no condition is met.

The operator returns exactly one value.

### 5.1.4 Short-cut Condition with ? and ?- Tokens

The question mark ? expresses a short-cut 'if` -like statement: if any condition preceding ? evaluates to true, exactly one statement right behind the token is executed, otherwise the statement is simply skipped. Likewise, the ?- token checks an expression and executes a one-line statement if it evaluates to false, fail or null.

```
> X := 0;
> x = 0 ? x := 1;
> x:
1
> x := 0;
> x <> 0 ?- x := 1;
> x:
1
```


### 5.1.5 case Statement

The case statement facilitates comparing values and executing corresponding statements. There exist two variants, the first one is:

```
case name
    [of value 11 [, value (2, ...] then statements,
    [of value 21 to value 22 then statements ]
    [of ...]
    [onsuccess ...]
    [else statementsk [esle]]
esac
```

```
> a := 'k';
> case a
    of 'a', 'e', 'i', 'o', 'u', 'y' then
        result := 'vowel'
    else
        result := 'consonant'
    esle
esac;
> result:
consonant
```

You can add as many of/then statements as you like. Fall through is not supported. This means that if one then clause is executed, Agena will not evaluate the following of clauses and will proceed with the statement right after the closing esac keyword. An else clause may be terminated by the esle token, but this is optional.

Instead of passing one or more individual values, you can also check whether a number $x$ or the first character of $a$ - non-empty - string $x$ is part of a range $a$ to $b$, i.e. $a \leq x \leq b$. One to range is accepted per of clause.

```
> a := 0;
> case a
    of -1 then result := -1
    of 0 to 10 then result := 10
    of 'a' to 'c' then result := 0
esac;
```

As with the if statement, if an onsuccess clause is given, and in case one of the conditions results to true, the statements in the onsuccess branch are executed. This allows to move code common to all then clauses into one single branch, reducing the code size.

If none of the of conditions is satisfied, and if an else clause is given, then the respective else statements are processed, otherwise Agena executes the code following the esac token.


The second variant is exactly equal to the if statement but may improve the readability of programme code.

With both variants, instead of the then keyword the -> token can be used.

### 5.1.6 case of Statement

A flavour of the if statement is the case of control. It may improve the readability of code.

There is no functional difference between if and case of statements.

Example:

```
> x := 0; flag := false;
> case
> of x < 0 then r := -1;
> of x = 0 then r := 0;
> onsuccess flag := true;
else r := 1 esle
> esac
> r, flag:
0 true
```

```
case
    of condition
    [of condition_ then statements 2]
    [of ...]
    [onsuccess ...]
    [else statementsk [esle]]
esac
```

case of statements also support simple assignments in the case of clause, and their optional of clauses, as well.


```
> case of flag := io.read() then
> print('Output: ' & flag)
> esac;
Agena
Output: Agena
```

Only if the right-hand side of the assignment does neither result to false, fail nor null will the then clause be executed.

### 5.2 Loops

Agena has three basic forms of control-flow statements that perform looping: while and for, each with different variations.

### 5.2.1 while Loops

A while loop first checks a condition and if this condition is true or any other value except false, fail or null, it iterates the loop body again and again as long as the condition remains true.

If the condition is false, fail or null, no further iteration is done and control returns to the statement following right after the loop body.

If the condition is false, fail or null right from the start, the loop is not executed at all.

```
while condition do
    statements
od
```

The programme flow is as shown in the diagram above.
The following statements calculate the largest Fibonacci number less than 1000.

```
> a := 0; b := 1;
> while b < 1000 do
> c := b;
> b := a + b;
> a := c
> od;
> C:
987
```

The following loop will never be executed since the condition is false:

```
> while false do
    print('never printed')
> od;
```

You can also conduct a simple assignment in the while condition. If an assignment is given in the while clause, its right-hand side is evaluated and stored to the left-hand side name. The result of the evaluation is then checked and either the loop body is executed - the result of the evaluation is neither false, fail nor null - or not.

This allows for shorter code: Instead of

```
> flag := true;
> while flag do
    flag := io.read();
    if flag = 'Z' then break fi
od
```

you can now simply write (no need to assign flag before):

```
> while flag := io.read() do
    if flag = 'Z' then break fi
> od
```

The variable assigned in the while clause is not local to the loop body but can be accessed later on the level that surrounds the loop. You may explicitly declare the variable local before.

You can also combine an assignment and a condition in the while clause. In this case, the assignment will be done only once and the condition will always be checked:

```
while c := 0, c < 3 do
    print(c++)
od;
C:
```

0
1
2
3

Variations of while are the do/as and do/until loops which check a condition at the end of the iteration, and thus will always be executed at least once.

In the do/as variant, as long as the condition evaluates to true, the loop body is executed.

```
> c := 0;
> do
> inc c
> as c < 10;
```


## do

statements
as condition
> $\mathrm{c}:$
10
do/until loops are iterated until the given condition is met.

```
> c := 0;
> do
> inc c
> until c > 10;
> c:
11
```

do/as and do/until support simple assignments in the respective condition.
Another flavour of the while loop is the infinite do/od loop which executes statements infinitely and can be interrupted with the break or return statements. See Chapter 5.2.10 for further information on the break statement. It is syntactic sugar for the while true do/od construct.

## do

statements
od

```
i := 0;
do
        inc i;
        if i > 3 then break fi;
        print(i)
    od;
1
2
3
```

for loops are used if the number of iterations is known in advance. There are for/to loops for numeric progressions, and for/in loops for table and string iterations.

### 5.2.2 for/to Loops

Let us first consider numeric for/to loops which use numeric values for control:

```
for name [from starf] [to stop]
    [by step] do
    statements
od
```


name, start, stop, and step are all numeric values or must evaluate to numeric values.

The statement at first sets the variable name to the value of start. name is called the control or loop variable. If start is not given, the start value by default is +1 .

When omitting the to clause, the loop iterates until the largest number representable on your platform has been reached. If left out, the step size is +1 .

The for loop then checks whether start $\leq$ stop. If so, it executes statements and returns to the top of the loop, increments name by step and then checks whether the new value is less or equal stop. If so, statements are executed again.

```
```

for i from 1 to 3 by 1 do

```
```

for i from 1 to 3 by 1 do
print(i, i^2, i^3)
print(i, i^2, i^3)
od;
od;
1
1
for i to 3 do
for i to 3 do
print(i, i^2, i^3)
print(i, i^2, i^3)
od;
od;
1 1
1 1
4 8
4 8
9 27

```
9 27
```

```
                        27
```

```
                        27
```

The control variable of a loop is always accessible to its surrounding block, so you may use its value in subsequent statements. This rule applies only to for/from/to-loops with or without a while, as or until extension, but not to for/in loops
described below. Note that within procedures, the loop control variable is automatically declared local, while on the interactive level it is global.

```
> for i while fact(i) < 1k do od
> i:
7
```

The following rules apply to the value of the control variable after leaving the loop:

1. If the loop terminates normally, i.e. if it iterates until the stop value has been reached, then the value of the control variable is its stop value plus the step size.
2. If the loop is left prematurely by executing a break statement ${ }^{13}$ within the loop, or if a for/while loop is terminated because the while condition evaluated to false (see Chapter 5.2.8), then the control variable is set to the loop's last iteration value before quitting the loop. There will be no increment with the loop's step size. The same applies to for/as and for/until loops (see Chapter 5.2.9).

Loops can count backwards if the step size is negative (see also the next chapter):

```
for i from 2 to 1 by -1 do
    print(i)
od
2
1
```

A special form is the to/do loop which does not feature a control variable and iterates exactly n times.

```
> to 2 do
> print('iterating')
> od
iterating
iterating
```

Agena automatically uses an advanced precision algorithm based on Neumaier summation if the step size is non-integral, e.g. $0.1,-0.01$. This mostly prevents round-off errors, thus avoids that the loop stops before the last iteration value - the limit - has been reached and that iteration values with round-off errors are returned. You may switch Agena into Kahan-Ozawa or Kahan-Babuška summation mode to use extended round-off prevention by issuing the statement in a session:

```
> environ.kernel(kahanozawa = true);
```

or

```
> environ.kernel(kahanbabuska = true);
```

[^11]As a further measure to prevent a loop stopping before the stop limit has been reached, numeric for loops with fractional step sizes automatically increase the stop limit by the value of the constant hEps. If a you pass a step size that is equals or less then hEps, Agena now issues an error. You can entirely switch off this math.Eps to zero, but only by calling environ.kernel:
> environ.kernel(hEps = 0);
Kahan-Babuška summation may be more accurate than Kahan-Ozawa summation. The speed loss with both algorithms compared to Neumaier is around 20 percent or more.

If the step size is an integer, e.g. 1000, 1, -1.0, then Agena does not use advanced precision to ensure maximum speed.

### 5.2.3 for/downto Loops

count from a start value down to a stop value, with a default countdown step size of (implicit minus) one. To count down, the optional step size should be positive.

```
for name from start downto stop [by step] do
    statements
od
```


### 5.2.4 for/in Loops over Tables

are used to traverse tables, strings, sets, and sequences, and also iterate over functions.

If null is passed after the in keyword, or if the value evaluates to null, then Agena does not execute the loop and continues with the statement following it.

Let us first concentrate on table iteration.

```
for key, value in tbl do
    statements
od
```

The loop iterates over all key~value pairs in table tbl and with each iteration assigns the respective key to key, and its value to value.

```
a := [4, 5, 6]
> for i, j in a do
print(i, j)
od
1 
3 6
```

There are two variations: When putting the token keys in front of the control variable, the loop iterates only over the keys of a table:

```
for keys key in tb/ do
    statements
od
```

Example:

```
> for keys i in a do
    print(i)
od
```



```
3
```

The other variation iterates on the values of a table only:

```
for value in tb/ do
    statements
od
```

```
for i in a do
    print(i)
od
```

4
5
6

The control variables in for/in loops are always local to the body of the loop (as opposed to numeric for loops). You may assign their values to other variables if you need them later.

You should never change the value of the control variables in the body of a loop the result would be undefined. Use the copy function to safely traverse any structure if you want to change, add, or delete its entries.

Because of the implementation of tables, please note that the keys in a table are not necessarily traversed in ascending order. You may want to iterate sequences or
linked lists (see Chapter 6.27).

### 5.2.5 for/in Loops over Sequences and Registers

All of the features explained in the last subchapter are applicable to sequences and registers, as well.

### 5.2.6 for/in Loops over Strings

If you want to iterate over a string character by character from its left to its right, you may use a for/in loop as well. All of the variations are supported.
for key, value in string do statements od
for value in string do statements od
for keys value in string do statements od

The following code converts a word to a sequence of abstract vowel, ligature, and consonant place holders and also counts their respective occurrence:

```
> str := 'æfter';
> result := '';
> c, v, l -> 0;
> for i in str do
> case i
> of 'a', 'e', 'i', 'o', 'u' then
result &:= 'V';
                inc v
            of 'å', 'æ', '\varnothing', 'ö' then
                result &:= 'L';
                inc l
            else
                result &:= 'C'
                inc c
    esac
> od;
```

```
> print(result, v & ' vowels', l & ' ligatures', c & ' consonants');
```

> print(result, v \& ' vowels', l \& ' ligatures', c \& ' consonants');
LCCVC 1 vowels 1 ligatures 3 consonants

```

\subsection*{5.2.7 for/in Loops over Sets}

All for loop variations support sets, as well. The only useful one, however, is the following:
```

> sister := {'swistar', 'sweastor', 'svasar', 'sister'}
> for i in sister do print(i) od;

```

\section*{svasar}
swistar
sweastor
sister

You may try the other loop alternatives to see what happens.

\subsection*{5.2.8 for/in Loops over Procedures}

The following procedure, called an iterator, returns a sequence of values multiplied by two. If state \(=n\), then the procedure returns null, quilting the for/in iteration. Note that the iterator in its first result n returns the next value of the loop control variable i. We use state to hold the number of iterations we wish to perform. See Chapter 6 which describes procedures in detail.
```

double := proc(state, n) is
if state > n then
inc n;
return n, 2*n
else
return null
fi
end;

```

In the following loop, 5 denotes the state and 0 the initial value.
```

for i, j in double, 5, 0 do
print(i, j)
od
2
4
6
8
1 0

```

Another means to iterate over procedures are closures, see Chapter 6.22. So far, here is just an example that you can use as a template for further experiments:
```

> iterate := proc(obj) is
local n := 0; \# with each call, counts up by one
return proc() is
inc n;
if n <= size obj then
return n, obj[n]
else
return null \# quit iteration
fi
end
end;
> f := iterate(seq(Pi, 2*Pi, 3*Pi));
> for i, j in f do
print(i, j)
ood;

```
```

1 3.1415926535898
6.2831853071796
3
9.4247779607694

```

You might also use the generic ipairs and pairs functions with for/in loops:
ipairs iterates table arrays, sequences, registers, strings and userdata that have an '__index ' metamethod, in a standard way:
```

> for i, j in ipairs(s) do
print(i, j)
> od;
1 3.1415926535898
2 6.2831853071796
3 9.4247779607694
> import numarray
> d := numarray.double(3)
> for i to 3 do d[i] := i*Pi od
> for i, j in ipairs(d) do
> print(i, j)
> od
1 3.1415926535898
2 6.2831853071796
3 9.4247779607694

```

To check whether a userdata features an '__index' entry in its associated metatable, just enter:
```

> getmetatable(d).__index:
procedure(01CE6DD0)

```
pairs allows to iterate all the keys and corresponding values of a dictionary, but as the following example shows, not surprisingly in a `random` fashion:
```

> t := [a = Pi, b = 2*Pi, c = 3*Pi]
for i, j in pairs(t) do
print(i, j)
> od
a 3.1415926535898
c 9.4247779607694
b 6.2831853071796

```

Take in mind that ipairs and pairs are much slower than iterating structures directly.


\subsection*{5.2.9 for/while and for/until Loops}

All flavours of for loops can be combined with a while condition. As long as the while condition is satisfied, the for loop iterates. To be more precise, before Agena starts the first iteration of a loop or continues with the next iteration, it checks the while condition to be true or any other value except false, fail or null. An example:
```

for x to 10
while ln(x) <= 1 do
print(x, ln(x))
od
0
0.69314718055995

```

Regardless of the value of the while condition, the loop control variables are always initiated with the start values: in the summary frame below, with for/to loops, a is assigned to \(i\) (or 1 if the from clause is not given); key and/or value are assigned with the first item in the table, set or sequence struct or the first character in string string. Likewise, the until condition quits a loop until it is satisfied.
for \(i\) [from \(a]\) [to b] [by step] (while|until) condition do statements od for [key,] value in struct (while|until) condition do statements od for keys key in struct (while|until) condition do statements od for [key,] value in string (while |until) condition do statements od for keys key in string (while|until) condition do statements od

The optional while and until clauses accept a simple assignment. In such a case, the right-hand side of the assignment is evaluated and stored to the left-hand side non-local name. The result of the evaluation is then checked and either the loop body is executed or not. Example:
```

> a := [10, 20, 4 ~ 30] \# the table has no index 3
for i to 4 while t := a[i] do \# since a[3] evaluates to null,
\# which is equal to false in this context, the loop quits with i = 3.
print(a[i], t)
od
10 10
20 20

```

\subsection*{5.2.10 for/as \& for/until Loops}

As with the optional while clause, all flavours of for loops can be combined with an as or an until condition.

In these cases, a loop is always iterated at least once, and after the first iteration is completed, Agena checks the given condition and decides whether to start the next iteration or to leave the loop.

In the following example, the for/as loop starts with \(i=0\) and since the first check to the as condition results to true, the next iteration with \(i=1\) is conducted. The next check to the as condition results to false, thus the loop quits.
```

> for i from 0 do
> print(i, 10^i)
> as 10^i < 10
0 1
1 10

```


The next loop iterates three times, until \(i=2\), since only then the until condition becomes true.
```

for i from 0 do
print(i, 10^i)
until 10^i > 10
1
1 0
1 0 0

```

\subsection*{5.2.11 Loop Jump Control}

Agena features statements to manipulate loop execution. skip and break are applicable to all loop types, whereas redo and relaunch work in for loops only.

The skip statement causes another iteration of the loop to begin at once, thus skipping all of the loop statements following it.

The break statement quits the execution of the loop entirely and proceeds with the next statement right after the end of the loop.
\(>a:=0 ;\)
while true do
while true do
    inc a;
    if \(a>5\) then break fi;
    if \(a<3\) then skip fi;
    print(a)
od;
4

There exists syntactical sugar for both the skip and the break statements: instead of putting these statements into if clauses, just add the when token along with a condition to the respective keyword.
```

> a := 0;
> while true do
inc a;
> break when a > 5;
skip when a < 3;
print(a)
od;

```
```

3
4

```

In for/to and for/in loops, the redo statement is similar to skip: it jumps back to the beginning of the loop but does not change the loop control variable in for/to loops or the index/value control variables in for/in loops. Thus, it restarts the current iteration. At restart, it checks an optional while condition, if present.
```

> flag := true;
for j in [10, 11, 12] do
print(j, flag);
if flag and j = 11 then
clear flag;
print(j, flag,
'jump back')
redo
fi;
until j > 12;

```
        true
        true
        false jump back
        false
        false

The relaunch statement completely restarts a for/to and for/in loop from its very beginning, i.e. resets the current control variable to its start value (from clause or first element, respectively).
```

flag := true;
for j in [10, 11, 12] do
print(j, flag);
if flag and j = 11 then
clear flag;
print(j, flag,
'restart')
relaunch
fi;
until j > 12;
10 true
11 true
1 1 null restart
10 null
11 null
12 null

```

\subsection*{5.2.12 Scope I: scope and epocs}

You can define the scope of local variables with the scope/epocs statement. Any variable declared local between the scope and epocs keywords exists only in this block, and they are not available outside of it:
```

scope
declarations and statements
epocs

```

An example:
```

> a := 2;
> scope
> local b := 3; \# b is local to the scope only
> c := a*b \# c is available outside the block
> epocs;
> print(a, b, c);
2 null 6

```

\subsection*{5.2.13 Scope II: with Statement}

The with statement allows to define a scope and assign one or more local variables in only one stroke. It is syntactic sugar to the scope statement only. The following example refers to the example in the preceding subchapter:
with name \(_{1}, \ldots:=\) expr \(_{1}, \cdots\) do declarations and statements od
```

> a := 2;
> with b := 3 do \# b is local, a and c are global
C : := a*b
> od;
> print(a, b, c);
2 null 6

```

Assign multiple local variables, in this case two variables:
```

> a := 2;
> with b, c := 3, 4 do
> d := a*b*c
> od;
> print(a, b, c, d);
2 null 6

```

\subsection*{5.2.14 with Statement for Dictionaries}

The with statement can also unpack table values, indexed by string keys, declare them local and then access them in the respective block. After leaving the block, all the values listed right between the with and in tokens are automatically written back to the table:
```

with key $_{1}\left[\right.$, key $\left._{2}, \cdots\right]$ in tablename do
statements
od

```
```

> zips := ['duedo' ~ 40210:40629,
> bonn = 53111:53229,
> cologne = 50667:51149];
> with duedo, cologne in zips do \# bonn has not been given here
> print(duedo, bonn, cologne);
cologne := null; \# cologne entry will be deleted from table zips
duedo := 40210:51149 \# duedo entry in zips will be changed
\# bonn entry will not be changed since not listed in the header
bonn := null
print(bonn, cologne, duedo)
> od;
40210:40629 null 50667:51149
null null 40210:51149
> zips:
[bonn ~ 53111:53229, duedo ~ 40210:51149]

```

Another flavour of the with statement has the following syntax:
```

with tablename do
statements
od

```

Within the body of this variant, the table tablename can be referenced by just an underscore. It also allows to actively change values in tablename. Example:
```

> zips := [duedo = 4000, bonn = 5300]
> with zips do
> print(_.bonn);
> _.bonn := 53111
> od
5 3 0 0
> zips:
[bonn ~ 53111, duedo ~ 4000]

```

\subsection*{5.2.15 Alternative to Closing Keywords}

You can use the end token instead of the closing fi, od, esac, yrt and epocs keywords, or mix both.

\section*{Example:}
```

if os.system()[1] in {'SunOS', 'Windows', 'Linux', 'Darwin'} then
if environ.kernel().is32bit then
readlib('fractals');
readlib('gdi');
readlib('gzip');
a, b := gzip.deflate('agena programming language');
if [gzip.inflate(a, b)] <> ['agena programming language', 26] then
print('error in gzip.in<br>deflate')
end;
try \# provoke segfaults
for i from 0 to 100 do
gzip.inflate(a, i)
od
end
end;
to 100 do readlib('net') end \# try crashing Agena at exit
fi;

```

Chapter Six

\section*{Programming}

\section*{6 Programming}

Writing effective code in a minimum amount of time is one of the key features of Agena. Programmes are usually represented by procedures. The words ‘procedure` and `function` are used synonymously in this text.

\subsection*{6.1 Procedures}

In general, procedures conflate a sequence of statements into abstract units which then can be repeatedly invoked.

Writing procedures in Agena is quite simple:
```

procname := proc([par1 [::type1] [, par2 [::type 2], . . ] ] ] ) [:: returntype] is
[local name 1 [, name 2, . . ]];
statements
end

```

All the values that a procedure shall process are given as parameters par \({ }_{1}\), etc. A function may have no, one or more parameters. A parameter may be succeeded by the name of a type (see Chapter 6.8.2), or a set of up to four types, that an argument must satisfy when the procedure is called.

If a type is given right after the parameter list, Agena checks whether the return of the procedure is of the given returntype, which may also be a user-defined type. The is keyword is obligatory.

A procedure usually uses local variables which are private to the procedure and cannot be accessed by other procedures or on the Agena interactive level.

Global variables are supported in Agena, as well. All values assigned on the interactive level are global, and you can also create global variables within a procedure. The values of global variables can be accessed on the interactive level and within any procedure.

A procedure may call other functions or itself. A procedure may even include definitions of further local or global procedures.

The result of a procedure will be returned through the return keyword which may be put anywhere in the procedure body, and which also immediately terminates execution of the procedure.
return [value [, va/ue \({ }_{2}, \cdots\) ] ]

As you can see, you may not only return a single result, but also multiple ones, or none at all.

Furthermore, a procedure will not return anything - not even the null value -
- if no return statement is given at all,
- if no values are given in the return statement.

The following procedure computes the factorial of an integer \({ }^{14}\) :
```

> restart;
> fact := proc(n) is
\# computes the factorial of an integer n
if n < 0 then return fail
elif n = 0 then return 1
else return fact(n-1)*n
fi
end;

```

It is invoked using the syntax:
```

funcname([arg}\mp@subsup{|}{1}{[, arg}\mp@subsup{\mp@code{g}}{2}{\prime}\cdots]]

```
```

> fact(4):
24

```
where the first parameter is replaced by the first argument arg \(_{1}\), the second parameter is substituted with arg \(_{2}\), etc.

When calling a function recursively, instead of writing out its real name, you may use the procname keyword, which in runtime is substituted by the name with which the procedure was invoked:
```

fact := proc(n) is
\# computes the factorial of an integer n
if n < O then return fail
elif n = 0 then return 1
else return procname(n-1)*n
fi
end;

```

A when clause can be added to a return statement that does not pass back any value including null. In this case, the execution of a function is being finished if the Boolean when condition has been satisfied, e.g. return when \(x\) <> 0 . return can be combined with both a when and with clause - for example
```

> return when x <> 0 with true;

```
is syntactic sugar for
```

> if x <> 0 then
> return true
> fi;

```

\footnotetext{
\({ }^{14}\) The library function fact is much faster.
}

Last of all, procedures can alternatively be defined as follows:
[local] proc procname( [par \(\left[::\right.\) type \(\left._{1}\right]\left[\right.\), par \(_{2}\left[::\right.\) type \(\left.\left._{2}\right], \cdots\right]\) ] [:: returntype] is [local [constant] name \({ }_{1}\) [, [constant] name \({ }_{2}, \ldots\) ]]; statements
```

end

```

Instead of the proc keyword, you can use the procname token. Thus, the factorial function can also be entered as follows:
```

proc fact(n) is
if n < 0 then return fail
elif n = 0 then return 1
else return procname(n-1)*n
fi
end;

```

\subsection*{6.2 Local Variables}

The function above does not need local variables as it calls itself recursively. However, with large values for n, the large number of unevaluated recursive function calls will ultimately cause stack overflows. So we should use an iterative algorithm to compute the factorial and store intermediate results in a local variable.

A local variable is known only to the respective procedure and the block where it has been declared. It cannot be used in other procedures, the interactive Agena level, or outside the block where the local variable has been declared.

A local variable can be declared explicitly anywhere in the procedure body, but at least before its first usage. If you do not declare a variable as local and assign values later to this variable, then it is global. Note that control variables in for loops are always implicitly declared local to either their surrounding (for/to loops) or inner block (for/in loops), so we do not need to explicitly declare them.

Local declarations come in different flavours:
local name \(_{1}\left[\right.\), name \(\left._{2}, \ldots\right]\)
local [constant] name 1 [, [constant] name \({ }_{2}, \ldots\). . \(:=\) value \(_{1}\) [, value \({ }_{2}, \ldots\). . ]
local [constant] name \({ }_{1}\left[\right.\), [constant] name \(\left.{ }_{2}, ~ \cdot . \cdot\right]\)-> value
local enum name \(_{1}\left[\right.\), name \(_{2}, \cdots\). ] [from value]
local key \(_{1}\left[\right.\), key \(\left._{2}, \ldots\right]\) in tablename

In the first form, name \(_{1}\), etc. are declared local.
In the second and third form, name \({ }_{1}\), etc. are declared local and, as opposed to the first form, followed by initial assignments of values to these names.

In the fourth form, name \(_{1}\), etc. are declared local and subsequently enumerated, i.e. assigned integers in ascending order, by default starting from 1, or the integer given in the optional from clause.

In the last form, table values are unpacked, equivalent to the assignment statement \(\mathrm{key}_{1}\), \(\mathrm{key}_{2}\), etc. : = tablename. \(\mathrm{key}_{1}\), tablename. \(\mathrm{key}_{2}\), etc., with \(\mathrm{key}_{1}\), \(\mathrm{key}_{2}\), etc. being automatically declared local.

By passing the constant keyword in front of a variable name, a variable will become a constant that cannot be changed later in a session. This feature works in procedures only, not on the interactive level.

Let us write a procedure to compute the factorial using a for loop. To avoid unnecessary loop iterations when the intermediate result has become so large that it cannot be represented as a finite number, we also add a clause to quit loop iteration in such a case.
```

> fact := proc(n) is
if n < O then return fail fi;
local result := 1;
for i from 1 to n do
result := result * i
if not finite(result) then break fi
od;
return result
end;
fact(10):
3628800

```

Since result has been declared local it does not exist on the interactive level:
```

> result:
null

```

There is a shortcut to create local structures - tables, sets, and sequences:
```

create local <structure> name, [, <structure> name 2, . . .]

```
where <structure> might be the keyword table, set or sequence. You can declare different local structures with one create local statement.

A useful function is environ.globals which determines global variable assignments inside procedures and helps to find those positions where a local declaration has been forgotten.

\subsection*{6.3 Global Variables}

Global variables are visible to all procedures and the interactive level, such that their values can be queried and altered everywhere in your code.

Using global variables is not recommended. However, they are quite useful in order to have more control on the behaviour of procedures. For example, you may want to define a global variable _EnvMoreInfo that is checked in your procedures in order to print or not to print information to the user.

Global variables can be depicted with the global statement. It checks whether the given variable or variables have not been declared local before its execution and issues an error otherwise.
```

fact := proc(n) is
if n < O then return fail fi;
local result := 1;
global _EnvMoreInfo;
for i from 1 to n do
result := result * i
if result = infinity then
if _EnvMoreInfo then print('Overflow !') fi;
break
fi
od;
return result
end;

```

We should assign _EnvMoreInfo any value different from null, fail or false in order to get a warning message at runtime.
```

> _EnvMoreInfo := true;
> fact(10000):
Overflow !
infinity

```

\subsection*{6.4 Changing Parameter Values}

You can change the values of procedure parameters within a procedure. Thus, an alternative to the abs operator might be:
```

> myAbs := proc(x) is
if x < 0 then
x := -x
fi;
return x
end;
myAbs(-1):
1

```

\subsection*{6.5 Optional Arguments}

A function does not have to be called with exactly the number of parameters given at procedure definition. You may also pass less or more values. If no value is passed for a parameter, then it is automatically set to null at function invocation. If you pass more arguments than there are actual parameters, excess arguments are ignored.

For example, we can control whether a warning message is printed during function execution by passing an optional argument:
```

> fact := proc(n, warning) is
if n < O then return fail fi;
local result := 1;
for i from 1 to n do
result := result * i
if result = infinity then
if warning then print('Overflow !') fi;
break
fi
od;
return result
end;
fact(10000):
infinity

```

In this example, the option must be any value other than null, false or fail to get the effect.
```

fact(10000, true):
Overflow !
infinity

```

A variable number of arguments can be passed by indicating them with a question mark in the parameter list and then querying them with the varargs system table in the procedure body. The ? token can be used within in the procedure body as a shortcut to the varargs table.
```

varadd := proc(?) is
local result := 0;
for i to size ? do
inc result, ?[i]
od;
return result
end;
> varadd(1, 2, 3, 4, 5):
15

```

You may determine the number of arguments actually passed in a procedure call by querying the system variable nargs inside the respective procedure. A variant of the above procedure might thus be:
```

varadd := proc(?) is
local result := 0;
for i to nargs do
inc result, ?[i]
od;
return result
end;
> varadd(1, 2, 3, 4, 5):
15

```

Note: With OOP-style methods, nargs will also count the method itself.

Let us build an extended square root function that either computes in the real or complex domain. By default, i.e. if only one argument is given, the real domain is taken, otherwise you may explicitly set the domain using a pair as a second argument.
```

xsqrt := proc(x, mode) is
if nargs = 1 or mode = 'domain':'real' then
return sqrt(x)
elif mode = 'domain':'complex' then
return sqrt(x + 0*I)
else
return fail
fi
end;
> xsqre(-2):
undefined
> xsqrt(-2, 'domain':'real'):
undefined

```

If the left-hand value of the pair in a function call shall denote a string, you can spare the single quotes around the string by using the = token which converts the left-hand name to a string \({ }^{15}\).
```

> xsqrt(-2, domain = 'complex'):
1.4142135623731*I

```

You can mix optional arguments and the variable-arguments feature in parameter lists, with the question mark always the last item in the list:
```

> xsqrt := proc(x, mode, ?) is
> ...
> end;

```

Finally, if you would like to define defaults for missing arguments, just use the binary or operator as shown below as it returns the first operand if it is non-null, and it returns the second operand if the first is null:
```

> f := proc(x) is
x := x or 0;
return x
end;
f():
0

```

\footnotetext{
\({ }^{15}\) If you need a Boolean equality check in a function call, such like \(\mathrm{f}(\mathrm{a}=\mathrm{b})\), use the isequal function or the \(==\) operator, like \(f(\) isequal \((a, b))\) or \(f(a==b)\).
}

\subsection*{6.6 Passing Options in any Order}

We can use variable arguments along with pairs in order to pass one or more optional arguments in any order.
```

> f := proc(?) is
local bailout, iterations := 2, 128; \# default values
for i to nargs do
case left(?[i])
of 'bailout' then
bailout := right(?[i]);
of 'iterations' then
iterations := right(?[i]);
else
print 'unknown option'
esle
esac
od;
print('bailout = ' \& bailout, 'iterations = ' \& iterations)
end;
> f();
bailout = 2 iterations = 128
> f('bailout':10);
bailout = 10 iterations = 128
> f('iterations':32, 'bailout':10);
bailout = 10 iterations = 32

```

Again, the quotes around the option name (the left-hand side of the pair) can be spared by giving the \(=\) token which converts the name to a string.
```

> f(bailout = 10, iterations = 32);
bailout = 10 iterations = 32

```

Sometimes, implementing checks on options may take a substantial amount of programming time, so please have a look at the checkoptions, copyadd and the opt* functions which may save up to \(20 \%\) of code. You might consult Chapter 8 for further details.

\subsection*{6.7 Type Checking}

Although Agena is untyped, in many situations you may want to check the type of a certain value passed to a function. Agena has four facilities for this:
1. the type operator determines the basic type of its argument;
2. the typeof operator returns a basic or user-defined type;
3. the :: operator checks for a basic or user-defined type;
4. the :- operator checks whether a value is not of a given basic or user-defined type:

Basic or user-defined types can optionally be specified in the parameter list of a procedure by means of the preceding :: token so that they will be checked at
procedure invocation, see Chapter 6.8.2. Furthermore, the type or types of return of a procedure may be given right after the parameter list, see Chapter 6.8.3.

The following basic types are available in Agena:
```

boolean, complex, lightuserdata, null, number, pair, procedure,
register, sequence, set, string, table, thread, userdata.

```

These names are reserved keywords, but with the exception of the null constant evaluate to strings so that they can be compared with the result of the type operator:

\section*{type(va/ue)}
```

> type(1):
number
> type(1) = number:
true

```

If you want to check for the null type, put the null token in quotes:
```

> a := null;
> type(a) = 'null':
true

```

The :: and :- operators check whether their arguments are or are not of a specific type - or user-defined type - and return true or false. They are speed-optimised and around \(20 \%\) faster than comparing the return of the type operator with a type name.
```

value :: typename
value :- typename

```

Examples:
```

> 1 :: number:
true
> '1' :- number:
true

```

In case of user-defined types, the type name must always be a string, in quotes. See Chapter 6.12 for more information. The :: and :- operators can also isolate numbers further by passing the tokens integer, posint, nonnegint, positive, negative, or nonnegative, see Chapter 6.8.2 for further information.
```

> -1 :: nonnegative:

```
false

\subsection*{6.8 Error Handling}

\subsection*{6.8.1 The error Function}

The error function immediately terminates procedure execution, and prints an error message if given.
error('error string')
```

> fact := proc(n) is
> if n :- number then
> error('Error: number expected')
f fi;
if n < O then return null
elif n = 0 then return 1
else return fact(n - 1)*n
fi
end;
> fact('10'):
Error: number expected
Stack traceback:
stdin, at line 3, at line 1

```

\subsection*{6.8.2 Type Checks in Procedure Parameter Lists}

You may specify permitted types in the parameter list of a procedure by using double colons:
```

> fact := proc(n :: number) is
if n < O then return null
elif n = 0 then return 1
else return fact(n - 1)*n
fi
end;
> fact('10'):
Error in stdin:
invalid type for argument \#1: expected number, got string.

```

This form of type checking is more than twice as fast as the if/type/error combination. If the argument is of the correct type, Agena executes the procedure, otherwise it will issue an error. Agena will also throw an error if the argument is not given:
```

> fact()
Error in stdin:
missing argument \#1 (type number expected).

```

Finally, argerror is a little bit smarter than error for it automatically indicates the type of an argument actually passed to a procedure in its error message.
```

> a := 1;

```
```

> if a :- string then
argerror(a, 'myproc', 'expected a string')
> fi
Error in `myproc`: expected a string, got number.

```

Furthermore, you may specify a set of one to five permissible basic types for any parameter with the set notation:
```

> sec := proc(x :: {number, complex}) is
> return 1/cos(x)
> end;

```

Besides the basic types number, complex, string, table, set, pair, sequence and register, you can also pass the following keywords to further isolate numbers:
\begin{tabular}{|l|l|}
\hline Keyword & Check for \\
\hline integer & a number that represents a signed integer \\
\hline posint & a number that represents a positive integer \\
\hline nonnegint & a number that represents a non-negative integer \\
\hline positive & checks for a positive number (float or integer) \\
\hline negative & checks for a negative number (float or integer) \\
\hline nonnegative & checks for a non-negative number (float or integer) \\
\hline
\end{tabular}

Note that in Agena there is only one type that represents floats and integers: type number. The above mentioned five numeric `types` are only supported in parameter lists and by the :: and :- operators.

Finally, there are three pseudo-types:
- anything stands for any type, including 'null'. If given in a parameter list, then Agena checks whether the corresponding argument of any type, even 'null', has been passed in a function call - if not, an error will be issued. The pseudo-type can also be passed as the right operand to the :: and :- operators;
- listing identifies a table, sequence or register in the parameter list of a procedure. The type can be passed as the right operand to :: and :-, as well.
- basic identifies a number, string, Boolean or null, and is recognised in parameter lists and the :: and :- operators.

Examples that summarise these special types:
```

> proc f(x :: anything) :: listing is
> return x
> end;
> f()
Error in stdin:
missing argument \#1 (of type anything).
Stack traceback:
stdin, in `f`
stdin, at line 1 in main chunk

```
```

> f(1)
Error in stdin at line 2:
Error in `return`: result of type listing expected, got number.
Stack traceback:
stdin, at line 2 in `f`
stdin, at line 1 in main chunk
> f([1]):

```
[1]

\subsection*{6.8.3 Checking the Type of Return of Procedures}

Agena can check whether all returns of a procedure are of one given type by specifying this return type right after its parameter list.
```

> fact := proc(n :: number) :: number is
if n < 0 then return undefined
elif n = O then return 1
else return fact(n-1)*n
fi
end;
fact(10):
3628800

```

If one of the returns is not of the return type, the procedure issues an error.
```

> fact := proc(n :: number) :: number is
> if n < 0 then return undefined
> elif n = 0 then return 1
> else return 'don\'t know'
fi
end;
> fact(10):
Error in stdin, at line 5:
return` value must be of type number, got string.
Stack traceback:
stdin, at line 5, at line 1

```

The `virtual' types integer, posint, nonnegint, positive, negative and nonnegative can also be queried, see previous subchapter.

You can define up to five basic types that are allowed to be returned by putting them in curly brackets, just like in parameter lists:
```

> f := proc(x) :: {number, complex} is return 'a' end
> f()
In stdin at line 1:
Error in `return`: unexpected type string in return.

```

If you would like to automatically check structures for proper content at function invocation, please have a look at the end of Chapter 6.19.

There are further functions for error handling:

\subsection*{6.8.4 The assume Function}
assume checks a Boolean relation. If the relation is valid, it returns true and continues execution of the procedure. In case of an invalid relation, it bails out of the procedure and prints an error message. The second argument to assume is optional; if not given, the text `assumption failed` is printed, and 'error string' otherwise.
assume(relation [, 'error string' ])
```

> assume(1 = 1, '1 is not 1'):
true 1 is not 1
> assume(1 <> 1, '1 is 1'):
Error in `assume`: 1 is 1.
Stack traceback: in `assume
stdin, at line 1 in main chunk

```

\subsection*{6.8.5 Trapping Errors with protect/lasterror}
protect traps any error that might occur, but does not terminate a function call. In case of no errors, it returns all results of the call. But if there was an error, it returns the error message as a string and also sets the global variable lasterror to this error message. In case of a successful call, lasterror will always be null.
protect takes the name of the function to be executed as its first argument, and all its arguments \(a, b\), etc. as optional arguments:
\(\operatorname{protect}(f[, a[, b, \cdots]])\)

Thus, if a function has no arguments, simply pass the expression protect (f).
```

> iszero := proc(x) is
if x <> 0 then
error('argument must be zero')
else
return true
fi
end;

```

Now call iszero in protected mode:
```

> protect(iszero, 0):
true

```
```

> lasterror:
null
> protect(iszero, 1):
argument must be zero
> lasterror:
argument must be zero

```

To conveniently check whether an error occurred you might enter:
```

> protect(iszero, 0) = lasterror:
false
> protect(iszero, 1) = lasterror:
true

```

\subsection*{6.8.6 Trapping Errors with the try/catch Statement}

Instead of intercepting errors with protect and lasterror, you may use the try/catch statement:
```

try
statements,
[catch [errvar then]
statements_]
yrt

```

Any statements statements \({ }_{1}\) - one or more - are put right after the try keyword. If an error occurs in one of these statements, Agena immediately will jump to the catch clause if present, ignoring any subsequent statements in statements. If there is no catch clause, execution will immediately continue with the statement right after the yrt token, regardless of whether an error occurred or not, also ignoring all subsequent commands in statements \({ }_{1}\).

If a catch clause is given, then in case of an error the error message is stored to the local variable errvar, and after that all the statements statements 2 following the then keyword are processed. errvar does not need to be declared, it is implicitly local to the catch clause only. You may also do without specification of an error variable - in this case the error message is automatically stored to the local lasterror variable, and the then keyword must be left out.

Examples:
```

try
error('Oops !');
print('Invalid index !')
yrt;

```

As shown above, due to the immediate jump out of the try body, the print function is not called. In the next example, the error message is stored to the variable message, and in the catch clause it is then printed at the console.
```

> try
> error('Oops !');
print('Invalid index !')
catch message then
print('The error was: ' \& message);
> yrt;
The error was: Oops !
> message:
null

```

Now we do not specify an error variable in the catch clause:
```

> try
error('Oops !');
> print('Invalid index !')
> catch
> print('The error was: ' \& lasterror);
> yrt;
The error was: Oops !

```

\subsection*{6.8.7 Trapping Errors with pre and post clauses}

Instead of writing long special error treatment code when checking arguments or the return of a function, you may use the pre and post clauses:

The pre clause, placed right before the is keyword, checks a condition and issues an error if it is not met:
```

> golden := proc(n :: number) \# approximation of golden ratio
> pre isint(n) and n > -1 is \# if n < 0 or float, quit with an error
> if n = 0 then return 1 fi;
> return 1.0 + 1.0/procname(n - 1);
> end;
> golden(-1):
In stdin at line 2:
Error in pre-condition: posture not satisfied.

```

It is faster than checking arguments with calls to the assume function.
The post clause in return statements checks a condition and issues an error if it is not met:
```

> proc(x :: number) is
[...]
\# issue an error if x <> 1, and return x otherwise
return post x <> 1 with x
end;

```

A function can include both pre and post conditions.

\subsection*{6.9 Multiple Returns}

As stated before, a procedure can return no, one, or more values. Just specify the values to be returned:
```

> f := proc() is
> a := 2;
> return 1, a
> end;
> f():
1 2

```

There are two ways to refer to these multiple returns in subsequent statements. If you assign the return to only one variable, e.g.
```

> m := f():
1

```
the second return is lost, so enter:
```

> m, n := f();
> m:
1
> n:
2

```

A function may return a variable number of values, so it might be useful to put them in a sequence, register or table:
```

> seq(f()):
seq(1, 2)

```

Sometimes a procedure shall return the first result of a computation only. In this case, put the call that results into multiple returns into brackets. math.fraction returns three values: the numerator, the denominator, and the accuracy, in this order. Let us write a numerator function that only returns the first result of math.fraction.
```

numerator := proc(x :: number) is
return (math.fraction(x))
end;
numerator(0.1):

```
1

The ops function returns all its arguments after argument number index, an integer.
ops(index, \(\arg _{1}\left[, \arg _{2}, \ldots\right]\) )

The following statement determines the denominator and the accuracy.
```

> ops(2, math.fraction(0.1)):
10 0

```

To return only the first result, the denominator, put the call to ops in brackets.
```

> denominator := proc(x :: number) is
> return (ops(2, math.fraction(x)))
> end;
> denominator(0.1):
10

```
unpack returns all elements in a table or sequence:
```

> squared := proc(t :: table) is
local result := << x -> x^2 >> @ t;
return unpack(result)
end;
> squared([1, 2, 3, 4]):
1 4 4 9 16

```

Alternatively, unpack accepts the positions of the first to the last element to be returned as its second and third argument. If only the second argument is given, all elements in a structure from the given position up to the end are passed back.
unpack(structure [, beginning [, end]] )
```

> squared := proc(t :: table, ?) is
local result := << x -> x^2 >> @ t;
return unpack(result, unpack(?))
end;
> squared([1, 2, 3, 4], 2):
4 9 16
squared([1, 2, 3, 4], 2, 3):
4

```

\subsection*{6.10 Procedures that Return Procedures}

Besides returning numbers, strings, tables, etc., procedures can also return procedures. As an example, the function polygen
```

polygen := proc(?) is
local s := seq(unpack(?));
return proc(x) is
local r := bottom(s);
for i from 2 to size s do
r := r*x + s[i]
od;
return r
end
end;

```
returns a procedure that evaluates a polynomial of degree n from the given coefficients \(c_{n}, c_{n-1}, \cdots, c_{2}, c_{1}\) :
\[
\ll(x)->c_{n}{ }^{*} x^{n-1}+c_{n-1}{ }^{*} x^{n-2}+\cdots+c_{2}{ }^{*} x+c_{1} \gg
\]

In the following example, polygen creates the polynomial \(3 x^{2}-4 x+1\) as a procedure.
```

> f := polygen(3, -4, 1)
> f(2):
5

```

\subsection*{6.11 Shortcut Procedure Definition}

If your procedure consists of exactly one expression, then you may use an abridged syntax if the procedure does not include statements such as if/then, for, insert, etc.

```

    << [c] [par1 [:: type, ] [, par, [:: type 2], . . ]] [)]
    [ with var1 [, \cdots] := val1 [,\cdots]]]-> expr 1[, expr 2, \cdots] >>>
    ```

As you see, optional basic and user-defined types can be specified in the parameter section.

Let us define a simple factorial function.
```

> fact := << (x :: number) -> exp(lngamma(x + 1)) >>;
fact(4):
24

```

Brackets around parameters are optional if at least one parameter is given, even if you specify types.
```

> isInteger := << x -> int(x) = x >>;
> isInteger(1):
true
> isInteger(1.5):
false
> one := << () -> 1 >>; \# with no parameters, use empty bracket pair

```

Optional arguments and the ? notation are supported.
One or more local variables can be defined by the with clause put in front of the expression that computes the result:
```

> fact := << (x :: number)
> with n := 1
> -> exp(lngamma(x + n)) >>;
> fact(4):
24

```

Short-cut procedures can return multiple results:
```

> f := << x -> x, x+1, x+2 >>
> f(0):
0 1 2

```

\subsection*{6.12 User-Defined Procedure Types}

The settype function allows to group procedures \(\operatorname{proc}_{1}\), proc \(_{2}, \cdots\), by giving them a specific type (passed as a string) just as it does with sequences, tables, sets, and pairs.
settype(proc 1 [, proc \(_{2}, ~ \cdots\) ], 'your_proctype')

User-defined procedures can be queried with the typeof operator which returns a string.
```

> f := << x -> 1 >>;
> settype(f, 'constant');
> typeof(f):
constant
> type(f): \# only returns the basic type
procedure

```

The :: and :- operators can also validate a user-defined procedure type. Pass the name of the user- defined type as a string:
```

proc, :: 'your_proctype'
proc, :- 'your_proctype'

```
```

> f :: 'constant':
true
> f :- 'constant':
false

```

Note that the type operator only checks for basic types.

An alternative to typeof is the gettype function. If a user-defined type has set for a value, then it returns its name as a string, otherwise, it returns null.

If you want to check whether user-defined types have been passed to a
procedure, use the double colon notation in the parameter list.
Suppose you have defined a type called triple:
```

> t := [1, 2, 3]
> settype(t, 'triple')
> sum := proc(x :: triple) is
> return sumup(x)
> end
> sum(t):
6

```

\subsection*{6.13 Scoping Rules}

In Agena, variables live in blocks or `scopes`. A block may contain one or more other blocks. A local variable is visible only to the block in which it has been declared and to all blocks that are part of this block. Thus, variables declared local in inner blocks are not accessible to the outer blocks or outside the procedure in which they are hosted.

Procedures, if- and case-statements, while-, do- and for-loops create blocks, or more precisely, a block resides between:
1. then and elif, else or fi keywords - in if statements;
2. then and of, else or esac keywords - in case statements;
3. do and as -in do/as loops;
4. do and od-in for and while and do/od loops;
5. is and end - in procedures;
6. scope and epocs - in scope blocks (including the with statement; see below).

As an example, variables declared as local in the then clauses of an if-statement live only in the respective then part. The same applies to variables declared locally in else clauses.
```

> f := proc(x) is
if x > 0 then
local i := 1; print('inner', i)
else
local i := 0; print('inner', i)
fi;
print('outer', i) \# i is not visible
end;
> f(1);
inner 1
outer null

```

Variables declared as local in for- or while-loops are only accessible in the bodies of these loops. The loop control variables of for/to-loops are automatically declared local to their surrounding block, while control variables of for/in-loops are implicitly declared local to the respective loop bodies.
```

> f := proc(x) is
while x < 2 do
local i := x
inc x
print('inner', i)
od;
print('outer', i) \# i is not visible
end;
> f(1);
inner 1
outer null

```

A special scope can be declared with the scope and epocs statements:

\section*{scope \\ dec/arations \& statements epocs}

The next example demonstrates how it works:
```

> f := proc() is
local a := 1;
scope
local a := 2;
writeline('inner a: ', a);
epocs;
writeline('outer a: ', a);
> end;
> f()
inner a: 2
outer a: 1

```

The scope statement can also be used on the interactive level to execute a sequence of statements as one unit. Compare
```

> print(1);
1
> print(2);
2
> print(3);
3

```
with
```

scope
print(1);
print(2);
print(3)
epocs;

```
1
2
3

\subsection*{6.14 Access to Loop Control Variables within Procedures}

As already mentioned, the control variable of a for/to loop is always local to the body surrounding the loop.
```

> mandelbrot := proc(x, y, iter, radius) is
local i, c, z;
z := x!y;
C := z;
for i from 0 to iter while abs(z) < radius do
z := z squareadd c \# = z^2 + c
od;
return i \# return the last iteration value
end;

```

The procedure counts and returns the number of iterations a complex value \(z\) takes to escape a given radius by applying it to the formula \(z=z^{\wedge} 2+c\).
```

> mandelbrot(0, 0, 128, 2):
1 2 9

```

The following example demonstrates that local variables are bound to the block in which they have been declared.
```

f := proc() is
local i;
for i to 3 do
local j;
for j to 3 do od;
print(i, j)
od;
print(i, j)
end;
f()
14
2 4
3 4
null

```

\subsection*{6.15 Sandboxes}

By default, every procedure has access to the full Agena environment, i.e. to all of Agena's functions, packages, and all the other values. You might want to limit this access, for example if one of your procedures offers services on the Internet, or you want a procedure maintain its own environment.

Here, the environ.setfenv function comes into play. It initialises the environment a function can use.

Example 1: Give access to all functions except the os package.
First copy Agena's environment represented by the system table _G to a new table so that altering this new table will not effect Agena's normal environment:
```

> _newG := copy(_G); \# copy can also duplicate cycles like _G

```

Delete the os package from this new environment:
```

> delete os from _newG;

```

Define a function that tries to determine the current working directory:
```

> curdir := proc() is
> return os.chdir()
> end;

```

Set the environment excluding the os package:
```

> environ.setfenv(curdir, _newG);
> curdir():
Error in stdin, at line 2:
attempt to index global `os` (a null value) with a string value
Stack traceback:
stdin, at line 2, at line 1

```

Example 2: Give access only the specific functions.
Let us redefine curdir: it will only access a redefined print function and all of the functions of the os package. curdir cannot call any other function.
```

> curdir := proc() is
print(os.chdir())
> end;
> environ.setfenv(curdir,
> ['print' ~ << x -> print('cwd is ' \& x) >>, 'os' ~ os])
> curdir():
cwd is C:/agena/src

```

To determine the current environment used by a function, use environ.getfenv:
```

> environ.getfenv(curdir):
[os ~ (...), print ~ procedure(01D4BA18)]

```

Please see Chapter 14.2 (environ.getfenv, environ.setfenv, environ.isselfref) for further features.

To hide data in a sandbox, please have a look at registers - explained in Chapter 4.15

\subsection*{6.16 Altering the Environment at Run-Time}

Besides using a special environment (see preceding subchapter), a procedure can also create new variables and put them into Agena's standard environment.

Why should one do so ? Consider the utils.decodexml function. It converts an XML string into a table consisting of key-value pairs, the keys being the XML tags, and the values the corresponding data. XML allows to use name spaces, so that tags might look like <soap:body>, etc.

So, XML data like
```

> str := '[soap:body](soap:body)
> <orderid>123</orderid>
> </soap:body>'

```
is converted to
```

> order := utils.decodexml(str):
[soap_body ~ [orderid ~ 123]]

```

To read the order number, one might just enter:
```

> order.soap_body.orderid:
1 2 3

```

Unfortunately, especially the SOAP standard allows one to define ones own name space, so that the following is also equivalent and valid XML data:
```

> str := '<s:body>
> <orderid>123</orderid>
> </s:body>'
> order := utils.decodexml(str):
[s_body ~ [orderid ~ 123]]

```

In this case you would have to write a new statement to get the order ID since fetching it with
```

> order.soap_body.orderid:
Error in stdin, at line 1:
attempt to index field `soap_body` (a null value)

```
will not work. Fortunately, Agena stores all values in the _G system table, with its keys being strings representing the variable names, and the entries the values of the these variables. So flexible code to read data from XML code featuring different name spaces might look like this:
```

> str := '<s:body>
> <orderid>123</orderid>
> </s:body>'
> order := utils.decodexml(str):
[s_body ~ [orderid ~ 123]]
> tag := tables.indices(order)[1]:
s_body
> prefix := tag[1 to ('_' in tag) - 1]:
S

```
```

> _G['order'][prefix \& '__body'].orderid:
1 2 3

```

Likewise, defining new variables within code can be done like this:
```

> _G['jpl'] := ['Jet Propulsion Laboratory']
> jpl:
[Jet Propulsion Laboratory]

```

\subsection*{6.17 Packages}

\subsection*{6.17.1 Writing a New Package}

Let us write a small utilities package called helpers including only one main and one auxiliary function. The main function shall return the number of digits of an integer.

Package procedures are usually stored to a table, so we first create a table called helpers. After that, we assign the procedure ndigits and the auxiliary aux. is Integer function to this table.
```

> create table helpers, helpers.aux;
> helpers.aux.isInteger := << x -> int(x) = x >>; \# aux function
> helpers.ndigits := proc(n :: number) is
> if not helpers.aux.isInteger(n) then
error('Error, argument is not an integer')
fi;
return if n = 0 then 1 else entier(ln(abs(n))/ln(10) + 1) fi
end;

```

Now we can use our new package.
```

> helpers.ndigits(0):
1
> helpers.ndigits(-10):
2
> helpers.ndigits(.1):
Error, argument is not an integer
Stack traceback: in `error`
stdin, at line 3, at line 1

```

To save us a lot of typing, we can assign a short name to this table procedure.
```

> ndigits := helpers.ndigits;
> ndigits(999):
3

```

Save the code listed above to a file called helpers.agn in a subfolder called helpers in the Agena main directory. In order to use the package again after you
have restarted Agena, use the run function and specify the full path.
```

> restart;
> run 'd:/agena/helpers/helpers.agn'
> helpers.ndigits(10):
2

```

You may print the contents of the package table at any time:
```

> helpers:
[aux ~ [isInteger ~ procedure(0044A6E0)], ndigits ~ procedure(0044A850)]

```

\subsection*{6.17.2 The initialise Function}

The initialise function, besides loading the package in a convenient way, automatically assigns short names to all package procedures so that you may use the shortcuts instead of the fully written function names.

In order to do this, you must first prepend or append the location of the directory containing your new package to the libname system variable, or execute Agena in the directory containing your package. You may do this by adding the following line to your personal Agena initialisation file (see Chapter A6), assuming that the helpers.agn file has been stored to the folder \(d\) :/agena/helpers.
libname \(\&:=\) ';d:/agena/helpers';
Alternatively, you may save the helpers.agn file into the lib folder of your Agena distribution if you do not want to modify libname.

Now in the interactive level, type:
```

> restart;

```
libname and some few other system variables are not reset by the restart statement because restart deliberately does not touch the contents of these specific system variables.
```

> initialise 'helpers'
ndigits
> ndigits(1); \# same as helpers.ndigits(1)

```

You may also want with to print a start-up notice at every package invocation by assigning a string to the table field `packagename.initstring`. Put the following line into the helpers.agn file after the create table statement, save the file and restart Agena:
```

> helpers.initstring := 'helpers v1.0 as of June 11, 2013\n\n';

```
```

> restart;
> initialise 'helpers'
helpers v1.0 as of June 11, 2013

```
ndigits

Since you may not want that short names are set for certain, especially auxiliary functions, their procedure names should be defined as follows: `packagename.aux.procedurename`, e.g. helpers.aux.isInteger.

The contents of the helpers.agn file should finally look like this:
```

create table helpers, table helpers.aux;
helpers.initstring := 'helpers v1.0 as of June 11, 2013\n\n';
helpers.aux.isInteger := << x -> int(x) = x >>; \# aux function
helpers.ndigits := proc(n :: number) is
if not helpers.aux.isInteger(n) then
error('argument is not an integer')
fi;
if n = 0 then
return 1
else
return entier(ln(abs(n))/ln(10) + 1);
fi;
end;

```

Save the file again and restart Agena.
```

> restart;
> initialise 'helpers'
helpers v1.0 as of June 11, 2013
ndigits

```

You can also define a package initialisation routine. It will automatically be run by the initialise statement after the package has been found and initialised successfully. The name of the initialisation routine must be of the form `packagename.aux.init`, e.g.:
```

> helpers.aux.init := proc() is
> writeline('I am being run')
> end;

```

Of course, you must create a `packagename.aux table before defining the initialisation function.

Instead of using initialise to load a package, you may use the import/alias statement - see Chapter 3.18-so
```

> initialise 'helpers';

```
is equivalent to
> import helpers alias;

\subsection*{6.18 Remember Tables}

Agena features remember tables which store the results of previous calls to Agena or C library procedures or contain a list of predefined results, or both. If a function is called again with the same argument(s), then the corresponding result will be returned from the table, and the procedure body is not executed, resulting in significantly better execution times. Remember tables are called rtables or rotables for short.

All functions to create, modify, query, and delete remember tables are available in the rtable package.

There are two types of remember tables:
- Standard Remember Tables, called `rtables`, that can be automatically updated by a call to the respective function; they may be initialised with a list of precomputed results (but do not need to).
- Read-only Remember Tables, called `rotables`, that cannot be updated by a call to the respective function. Rotables should be initialised with a list of precomputed results.

\subsection*{6.18.1 Standard Remember Tables}

A standard remember table is suited especially for recursively defined functions. It may slow down functions, however, if they have remember tables but do not rely much on previously computed results.

By default, no procedure contains a remember table. It must explicitly be created either by including the feature reminisce statement as the very first line in a procedure body, or by calling the rable.init function right after the procedure has been defined. A remember table may optionally be filled with default values with the rtable.put function. Since those functions are very basic, a more convenient facility is the rable.remember function which will exclusively be used in this chapter.

In order for an rtable to be automatically updated, the respective function must return its result with the return statement (which may sound profane). If a function is called with arguments that are not already known to the remember table, then the return statement adds these arguments and the corresponding result or results to the rtable.

Let us first try the feature reminisce variant, which may suffice in most cases. Just add this statement right after the is token in a procedure that computes Fibonacci numbers:
```

> fib := proc(n) is
feature reminisce; \# creates a read-write remember table
if n = 0 or n = 1 then return n fi; \# exit conditions
return procname(n - 2) + procname(n - 1)
end;
> fib(50):
20365011074

```

Now let us use the functions of the rtable package to administer remember tables.
Two examples: We want to define a function \(f(x)=x\) with \(f(0)=\) undefined.
First a new function is defined without using the feature reminisce phrase:
```

> f := proc(x) is return x end;

```

Only after the function has been created in such a way, the remember table can be set up. The rtable.remember function can be used to initialise rtables, explicitly set predefined values into them, and add further values later in a session.
```

> import rtable alias;
> remember(f, [0 ~ undefined]);

```

The rtable has now been created and a default entry add to it so that calling f with argument 0 returns undefined and not 0 .
```

> f(1):
1
> f(0):
undefined

```

If the function is redefined, its remember table is destroyed, so you may have to initialise it again.

Fibonacci numbers, as already shown above, can be implemented recursively and run with astonishing speed using itables.
```

> fib := proc(n) is
> assume(n >= 0);
> return procname(n - 2) + procname(n - 1)
> end;

```

The call to assume assures that n is always non-negative and serves as an ‘emergency brake` in case the remember table has not been set up properly.

The rtable is being created with two default values:
```

> remember(fib, [0~0, 1~1]);

```

If we now call the function,
```

> fib(50):
20365011074

```
the contents of the rtable will be:
```

> remember(fib):
[[22] ~ [28657], [39] ~ [102334155], [17] ~ [2584], [5] ~ [8], [27] ~
[317811], [50] ~ [20365011074], [3] ~ [3], [0] ~ [1], [46] ~ [2971215073],
[41] ~ [267914296], [1] ~ [1], etc.]

```

If a function has more than one parameter or has more than one return, remember requires a different syntax: The arguments and the returns are still passed as key~value pairs. However, the arguments are passed in one table, and the returns are passed in another table.
```

> f := proc(x, y) is
> return x, y
> end;
> remember(f, [[1, 2] ~ [0, 0]]);
> a, b := f(1, 2);
> a:
0
b b:
0

```

Please check Chapter 14.4 for more details on their use.

\subsection*{6.18.2 Read-Only Remember Tables}

If you do not want a function updating its remember table each time it is called with new arguments and results, you may use a read-only remember table, called `rotable` for short. Rotables are initialised with a list of precomputed results.

The function itself cannot implicitly enter new entries to its remember table via the return statement; it can only do so via a call to the rtable.put function or a utility that is based on rtable.put, called rtable.defaults. This gives you full control on the contents and the amount of data stored in a remember table - and thus on the speed of your procedure.

Assume you want to define a procedure that computes factorials \(n\) !, and that does not compute the results for \(n<11\), but retrieves the results from an rotable instead.

A function might look like this:
```

fact := proc(x :: number) is
if x :: nonnegint then \# is x an integer and non-negative ?
return exp(lngamma(x + 1))
else
return undefined
fi
end;

```

The defaults function can set up the rotable and enter precomputed values into it.
```

> \# set precompiled results for 0! to 10! to fact
> defaults(fact, [
> 0~1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800
> ]);

```

The factorial function is significantly faster when called with arguments that are in the rotable than if there would be no such value cache, because it would have to re-compute the results instead of just reading them.

Let us look into the remember table:
```

> defaults(fact):

```
```

[[2] ~ [2], [1] ~ [1], [8] ~ [40320], [9] ~ [362880], [10] ~ [3628800],

```
[[2] ~ [2], [1] ~ [1], [8] ~ [40320], [9] ~ [362880], [10] ~ [3628800],
[0] ~ [1], [4] ~ [24], [5] ~ [120], [6] ~ [720], [3] ~ [6], [7] ~ [5040]]
```

[0] ~ [1], [4] ~ [24], [5] ~ [120], [6] ~ [720], [3] ~ [6], [7] ~ [5040]]

```

You can also easily add further argument \(\sim\) result pairs with the rable.defaults function:
```

> defaults(fact, [11 ~ 39916800]);
> defaults(fact):
[[2] ~ [2], [1] ~ [1], [8] ~ [40320], [9] ~ [362880], [10] ~ [3628800], [0]
~ [1], [11] ~ [39916800], [4] ~ [24], [7] ~ [5040], [6] ~ [720], [3] ~ [6],
[5] ~ [120]]

```

A read-only remember table can be deleted by passing null as a second argument to defaults.

Please note that in a function featuring a remember table, the respective return statements should not include calls to other functions than the function itself. Instead, use auxiliary variables and use them in the return statements.

\subsection*{6.18.3 Functions for Remember Table Administration}

For completeness, here is a list of all the functions to administer remember tables:
\begin{tabular}{|c|c|}
\hline Procedure & Details \\
\hline rtable.forget(f) & Empties the remember table of function f but does not delete the table so that it will continue collecting results with the next call to f. Read-only remember tables cannot be emptied. The memory previously occupied by cached function arguments and results can be reused for other purposes \\
\hline rtable.get(f) & Returns the remember table of function f . \\
\hline rtable.init(f) & Initialises a standard remember table for the function f. \\
\hline rtable.roinit(f) & Initialises a read-only remember table for the function f. \\
\hline \begin{tabular}{l}
rtable.put( \\
f, [arguments], [returns])
\end{tabular} & Adds function argument(s) and the corresponding return(s) to the remember table of procedure f . \\
\hline rable.purge(f) & Deletes the remember table of function f entirely. The function empties the remember table before deleting it. It also enforces an immediate garbage collection. If you want to use a new remember table with the function, you have to initialise it with rtable.init or rtable.roint again. \\
\hline rtable.mode(f) & Returns the string 'ttable' if a function f has a standard remember table, 'rotable' if it has a read-only remember table, and 'none' if it has no remember table at all. \\
\hline
\end{tabular}

Table 18: Functions for administering remember tables

\subsection*{6.19 Overloading Operators with Metamethods}

One of the many useful functions inherited from Lua 5.1 are metamethods which provide a means to use existing operators to tables, sets, sequences, registers, pairs, and userdata.

For example, complex arithmetic could be entirely implemented with metamethods so that you can use already existing symbols and keywords such as + or abs with complex values and do not have to learn names of new functions \({ }^{16}\). This method of defining additional functionality to existing operators is also known as `overloading`.

Adding such functionality to existing operators is very easy. As an example, we will define a constructor to produce complex values and three metamethods for adding complex values with the + token, determining their absolute value with the standard abs operator, and pretty printing them at the console.

\footnotetext{
\({ }^{16}\) For performance reasons, complex arithmetic has been built directly into the Agena kernel.
}

At first, let's store a complex value \(z=x+y i\) to a sequence of size 2 . The real part is saved as the first value, and the imaginary part as the second.
```

> cmplx := proc(a :: number, b :: number) is
create local sequence r(2);
insert a, b into r;
return r
end;

```

To define a complex value, say \(z=0+i\), just call the constructor:
```

> cmplx(0, 1):
seq(0, 1)

```

The output is not that nice, so we would like Agena to print cmplx(0, 1) instead of \(\operatorname{seq}(0,1)\). This can be easily done with the settype function:
```

> cmplx := proc(a :: number, b :: number) is
create local sequence r(2);
insert a, b into r;
settype(r, 'cmplx');
return r
end;
> cmplx(0, 1):
cmplx(0, 1)

```

Adding two complex values does not work yet, for we have not yet defined a proper metamethod.
```

> cmplx(0, 1) + cmplx(1, 0):
Error in stdin, at line 1:
attempt to perform arithmetic on a sequence value

```

Metamethods are defined using dictionaries, called `metatables`. Their keys, which are always strings, denote the operators to be overloaded, the corresponding values are the procedures to be called when the operators are applied to tables, sets, sequences (which are used in this example), registers or pairs. See Appendix A2 for a list of all available method names. To overload the plus operator use the '__add' string.

Assign this metamethod to any name, cmplx_mt in this example.
```

cmplx_mt := [
'__add' ~ proc(a, b) is
return cmplx(a[1]+b[1], a[2]+b[2])
end
]

```

Next, we must attach this metatable cmplx_mt to the sequence storing the real and imaginary parts with the setmetatable function. We have to extend the constructor by one line, the call to setmetatable:
```

cmplx := proc(a :: number, b :: number) is
create local sequence r(2);
insert a, b into r;
settype(r, 'cmplx');
setmetatable(r, cmplx_mt);
return r
end;

```

Try it:
```

> cmplx(0, 1) + cmplx(0, 1):
cmplx(0, 2)

```

Add a new method to calculate the absolute value of complex numbers by overloading the abs operator.
```

> cmplx_mt.__abs :=<< (a) -> hypot(a[1], a[2]) >>;

```

The metatable now contains two methods.
```

> cmplx_mt:
[___add ~ procedure(004A64D0), ___abs ~ procedure(004D2D30)]
> z := cmplx(1, 1);
> abs(z):
1.4142135623731

```

It would be quite fine if complex values would be output the usual way using the standard \(\mathrm{x}+\mathrm{yi}\) notation. This can be done with the '-_tostring' method which must return a string.
```

> cmplx_mt.__tostring := proc(z) is
return if z[2]<0 then z[1]\&z[2]\&'i' else z[1]\&'+'\&z[2]\&'i' fi
> end;
> z:
1+1i

```

To avoid using the \(\mathbf{c m p l x}\) constructor in calculations, we want to define the imaginary unit \(\mathrm{I}=0+\mathrm{i}\) and use it in subsequent operations. Before assigning the imaginary unit, we have to add a metamethod for multiplying a number by a complex number.
```

cmplx_mt.__mul := proc(a, b) is
if typeof(a) = 'cmplx' and typeof(b) = 'cmplx' then
return cmplx(a[1]*b[1]-a[2]*b[2], a[1]*b[2]+a[2]*b[1])
elif type(a) = number and typeof(b) = 'cmplx' then
return cmplx(a*b[1], a*b[2])
fi
end;

```
and also extend the metamethod for complex addition.
```

cmplx_mt.__add := proc(a, b) is
if typeof(a) = 'cmplx' and typeof(b) = 'cmplx' then
return cmplx(a[1]+b[1], a[2]+b[2])
elif type(a) = number and typeof(b) = 'cmplx' then
return cmplx(a+b[1], b[2])
fi;
end;
> i := cmplx(0, 1);
> a := 1+2*i:
1+2i

```

Until now, the real and imaginary parts can only be accessed using indexed names, say \(z[1]\) for the real part and \(z[2]\) for the imaginary part. A more convenient - albeit not that performant - way to use a notation like z.re and z.im in both read and write operations is provided by the '__index' and '__writeindex' metamethods, respectively.

The _index metamethod for reading values from a structure obj works as follows:
- If the structure is a table, then Agena will automatically call the metamethod if the lookup obj[key] results to null.
- If the structure is a set, then Agena will automatically call the metamethod if the lookup obj[key] results to false.
- If the structure is a sequence or register, then the metamethod is called if the lookup obj[key] would result to an index-out-of-range error.

The \(\qquad\) writeindex ' metamethod for writing values to a structure works as follows:
- If the structure is a table, sequence or pair, then the metamethod is always called.
- The metamethod is also supported by the insert statement.

The procedures assigned to the '__index' and '__writeindex' keys of a metatable should not include calls to indexed names, for in some cases this would lead to stack overflows due to recursion (the respective metamethod is called again and again). Instead, use the rawget function to directly read values from a structure, and the rawset function to add values into a structure.

Let us first define a global mapping table for symbolic names to integer keys:
> cmplx_indexing := [re ~ 1, im ~ 2];
Now let us define the two new metamethods. Both will accept expressions like a.re and a[1]. In the following read procedure the argument x represents the complex value, and the argument \(y\) is assigned either the string 're' or 'im'. Thus, cmplx_indexing['re'] will evaluate to the index 1, and cmplx_indexing['im'] to index 2.
```

cmplx_mt.__index := proc(x, y) is \# read operation
if type(y) = string then \# for calls like `a.re` or `a.im`
return rawget(x, cmplx_indexing[y])
else
return rawget(x, y) \# for calls like `a[1]` or `a[2]`
fi
end;

```

In the write procedure, argument x will hold the complex value, y will be either 're' or 'im', and \(z\) is assigned the component - a rational number -, i.e. x.re \(:=z\) or x.im := z.
```

cmplx_mt.__writeindex := proc(x, y, z) is \# write operation
if type(y) = string then
rawset(x, cmplx_indexing[y], z)
else
rawset(x, y, z) \# for assignments like `a[1] := value`
fi
end;

```

You can now use the new methods.
```

> a:
1+2i
> a.re:
1
> a.im := 3;
> a:
1+3i

```

Note that while arithmetic metamethods can be applied on mixed types, for example the above defined complex number and a simple Agena number, relational operators cannot compare values of different types. Instead, Agena in this case just returns false with the equality operators \(=,==\), and \(\sim=\); and issues an error with relational operators that compare for order.

Using the '__writeindex' metamethod, it is quite easy to write-protect structures. In the following example, we will create a procedure that accepts a table, write-protects it and returns it. The metamethod:
```

readonly_mt := [
'__writeindex' ~
proc(t, k, v) is error('Error, structure is read-only.') end
]

```

A constructor that simplifies creating read-only structures:
```

> readonly := proc(t :: table) is
setmetatable(t, readonly_mt);
return t
end;
> moons := readonly(['Phobos', 'Deimos']);

```

Adding further values to the table, or changing an existing one, now will not work.
```

> insert 'Mars' into moons;
Error, structure is read-only.
Stack traceback: in `error`
> moons:
[Phobos, Deimos]

```

Using one and the same global table to define metamethods for various variables may be appropriate to save memory, but modification of the metatable itself may have unwanted effects.
```

> readonly_mt.__writeindex := proc(t, k, v) is rawset(t, k, v) end;
> insert 'Mars' into moons;
> moons:
[1 ~ Phobos, 2 ~ Deimos, Mars ~ Mars]

```

Finally, to protect values already assigned to a table, we could define:
```

> readonly_mt := [
__writeindex =
proc(t, k, v) is
if rawget(t, k) <> null then
error('Error, structure is read-only.')
else
rawset(t, k, v)
fi
end
]
> create table t;
> setmetatable(t, readonly_mt)
> t[1] := 0
> t[1] := 1
Error, structure is read-only.

```

To protect metatables from tampering, use the \(\qquad\) metatable method and set it to any value except null.
```

readonly_mt := [
__metatable = false,
__writeindex =
proc(t, k, v) is error('Error, table is read-only') end
];
readonly := proc(t :: table) is
setmetatable(t, readonly_mt);
return t
end;
> moons := readonly(['Phobos', 'Deimos']);

```
```

> setmetatable(moons, [
> __writeindex =
>
> );
Error in `setmetatable`: cannot change a protected metatable.
Stack traceback: in `setmetatable`
stdin, at line 1 in main chunk

```

A structure with a '__call' key in its metatable can also be called like a function.
```

readonly := proc(t :: table) is
setmetatable(t, [
__call = proc(t) is
for i, j in t do print(i, j) od
end]);
return t
end;
> moons := readonly(['Phobos', 'Deimos']);
moons();
Phobos
Deimos

```

To close this chapter, metamethods can also be used to automatically check the contents of structure passed at function invocation, and also to extend the :: and :operators.

Let us assume we would like to write a procedure that sums up all numbers in a set:
```

> s := {1, 2, 3, 4, 5};

```

We create a metatable first,
```

> create table mt;

```
and then assign a proper evaluation procedure to the \(\qquad\) oftype metamethod that makes sure that the set consists of numbers only.
```

mt.__oftype := proc(x) is
if type x = set then
for i in x do
if i :- number then return false fi
od;
return true
else
return false
fi
end

```

We assign the metatable to the set,
```

> setmetatable(s, mt);

```
and first try out the extended :: and :- operators.
```

> s :: set:
true

```

If an invalid member is inserted into the set,
```

> insert 'a' into s;

```
the type check fails:
```

> s :: set:
false
> s :- set:
true

```

Now we use the type evaluator in a procedure call:
```

> sum := proc(x :: set) is
> local s := 0; for i in x do inc s, i od; return s
> end;
> sum(s):
In stdin:
argument \#1 does not satisfy type check metamethod

```

The '__oftype ' metamethod works as follows: it first checks whether the structure (a table, set, sequence, register, pair) or userdata at the left-hand side matches the basic or user-defined type given at the right-hand side. If true, then Agena checks whether the structure has an attached '__oftype' metamethod and then runs it. The validator function must either return true if the criteria have all been met, or false, fail or null otherwise.

Note that in the validator mt.__oftype definition given above, we use the type operator instead of the :: operator in the first if statement since otherwise Agena would issue a stack overflow error.

The \(\qquad\) oftype metamethods also work if a return type has been specified.

In some packages, for example list and numarray, metamethods are included in the binary C library file and can be accessed through the so-called registry, via the debug.getregistry function. You may want to use this function to add further self-defined metamethods written in the Agena language.

For example, the _in metamethod of the numarray package is defined in the Agena source file lib/numarray.agn, and not in the C library file.
```

numarray.aux.mt := [
__in = proc(x, a) is
return numarray.whereis(x, a, 1, Eps) <> null
end
]

```

The metatable stored to the registry can be read by a call to registry.get. Just insert all of your own metamethod procedures by individually adding them, but do not directly assign your metamethod table to the result of registry.get('numarray').
```

scope
\# protect against sandboxing (prevent errors at initialisation)
if registry.get :: procedure then
\# get the internal registry metatable for numarrays
local _mt := registry.get('numarray');
if _mt :: table then
\# include each metamethod function step-by-step
for i, j in numarray.aux.mt do
_mt[i] := j
od
fi
fi
epocs;

```

Never modify or delete existing metamethods, as this will lead to undefined behaviour.

Note: The delete statement supports metamethods: it passes the data to be deleted as its key and null as the value to the __writeindex metamethod. To protect values stored to structures you might define:
```

readonly_mt.__writeindex := proc(t, k, v) is
if unassigned v or assigned rawget(t, k) then
error('cannot delete or modify value')
else
rawset(t, k, v)
fi
end;

```

The pop, rotate, duplicate, and exchange statements issue an error if a given structure features a __writeindex metamethod. This prevents read-only structures from being modified.

\subsection*{6.20 Memory Management, Garbage Collection, and Weak Structures}

Agena includes a garbage collector that sweeps all structures, procedures, userdata, and threads (called `objects` in this subchapter) that no longer have valid references in your programme - i.e. are inaccessible. Agena can then use the space for new objects. Numbers, complex numbers, strings and booleans are never collected.

Consider the following code: Let us assign a table to a name.
```

> s := []

```

Now s refers to a memory address so that Agena can access the table.
```

> environ.pointer(s):

```
008F0F38

If we reassign \(s\), a different empty table is assigned to it.
```

> s := []

```

This newly created table is stored to another part of the memory.
```

> environ.pointer(s) :
008A4188

```

Since the first table at memory position 008FOF38 can no longer be accessed, it unnecessarily occupies space. The garbage collector regularly looks for unreferenced objects and removes them.

Besides automatic garbage collection, the user can also invoke it manually, if deemed necessary, or even stop and restart it by calling environ.gc.

Sometimes it may be necessary to immediately clear values occupying a large amount of space. In this case assign null to it, so that the next automatic collection cycle can free it. If necessary call environ.gc for immediate collection. As a shortcut, you could also use the clear statement which conducts both nulling a value and collecting it.

If a table, set, sequence, procedure, userdata or thread is included in another table or sequence, the garbage collector does not collect it if its reference should have become invalid.
```

> restart
> t := []
> v := [1]; insert v into t
> v := [2]; insert v into t
> environ.gc()

```
[1] is still part of the table.
```

> t:
[[1], [2]]

```

If you do not want this to happen, declare the table or sequence 'weak` by using the '__weak' metamethod. With tables, you can either declare its keys weak by passing the string ' \(k\) ', or its values weak with the string 'v', or both with 'kv'. With sequences, simply use use the string ' v '.

If the collector meets a weak key that has become inaccessible, it removes the key-value pair. If the collector meets a weak value that has become inaccessible, it removes the key-value pair.
```

> t := []
> setmetatable(t, ['__weak' ~ 'v'])
> v := [1]; insert v into t
> v := [2]; insert v into t
> environ.gc()
> t:
[2 ~ [2]]

```

Do not change the '__weak' field after it has been assigned to an object, as the behaviour would be undefined. The insert and delete statements will reject manipulation of weak tables and sequences.

\subsection*{6.21 Extending Built-in Functions}

You may redefine existing built-in functions if you want to change their behaviour or extend its features. You can either write a completely new replacement from scratch or use the original function in your modified version. Your new procedure can then be called with the same name as the original one.

Note that only Agena functions written in C or in the language itself can be redefined, and that operators cannot.

In Agena, each mathematical function \(f\) works as follows: if a number \(x\), which by definition represents a value in the real domain, is passed to them, then the result \(f(x)\) will also be in the real domain. If \(x\) is a complex value, then the result will be in the complex domain.

Suppose that you want to automatically switch to the complex domain if a function value in the real domain could not be determined, i.e. if \(\mathrm{f}(\mathrm{x})=\) undefined. An example is:
```

> root(-2, 2):
undefined

```

On the interactive level enclose the new procedure definition with the scope and epocs keywords. This is necessary because on the interactive level, each statement entered at the prompt has its own scope and thus local variables cannot be accessed in the statements thereafter.

The new function definition might be:
```

scope
\# save the original function in a `hidden` variable
local oldroot := root;

```
```


# \# define the substitute

root := proc(x, n) is \# new definition
local result := oldroot(x, n);
if result = undefined then \# switch to complex domain
result := oldroot(x+0*I, n)
fi;
return result
end;
epocs;

```

The original function root is stored to the local oldroot variable so that the user can no longer directly access it.
```

> root(-2, 2):
8.6592745707194e-017+1.4142135623731*I

```

If you wish to permanently use your redefined functions, just put them into the initialisation file, located either in the lib folder of your Agena installation, or your home directory. See Appendix 6 for further information.
Since files have their own `scope`, the scope and epocs keywords are no longer needed (but can be left in the file).

\subsection*{6.22 Closures: Procedures that Remember their State}

A procedure can remember its state. This state is represented by the function's local variables which survive and retain their values even after the call to the procedure has finished. Such procedures are also called `closures`.

So with successive calls, the procedure can access these values again and re-use them.

Let us define an iterator function that returns an element of a table one after the other:
```

> traverse := proc(o :: table) is
local count := 0;
return proc() is
inc count;
return o[count]
end
end;

```

The traverse procedure is called a `factory` for it creates and returns the closure which we assign to the name iterator:
```

> tbl :=['a', 'b', 'c'];
> iterator := traverse(t.bl);

```

The iterator function remembers its state and can be called like 'normal` functions:
```

> iterator():
a

```

What happened? The call to traverse with the table tbl = ['a', 'b', 'c'] as its only argument initialised the variable count and assigned it to 0 . The table you passed is also stored to the closure's internal state since technically, parameters are local variables. With the first call to iterate, count was incremented from 0 to 1 , so that the first element of the table, i.e. tbl [1], could be returned thereafter.
```

> iterator():
b
> iterator():
C

```

Since the table now has no more elements left (count \(=4\) ), the iterator now returns null, since tbl [4] = null.
```

> iterator():
null

```

You can define more than one closure with a factory at the same time, each being completely independent from the others:
```

> iterator2 := traverse(['a', 'b', 'c']);
> iterator2():
a
> iterator2():
b
> iterator3 := traverse(['a', 'b', 'c']);
> iterator3():
a

```

In Chapter 5, we have already introduced for/in loops that can iterate over functions. There are various ways to accomplish this.

In general, one or two loop control variables are given to the left of the in keyword, followed by the function and up to two further variables to its right.

Example 1: With function next, iterate table tbi and pass null as the initialiser to get its first entry. The respective values in tbl are assigned to loop control variable i:
```

> tbl := [10, 20, 30, 'a' ~ 40];
> for i in next, tbl, null do \# equivalent to `for i in tbl do`
print(i)
od;
10
20
30
4 0

```

Example 2: Same as Example 1 but with two control variables \(k\), v storing the respective table key and value, in this order.
```

for k, v in next, tbl, null do
print(k, v)
od;
10
20
3 30
a 40

```

Example 3: Retrieve only the table keys.
```

for keys k in next, tbl, null do
print(k)
od;

```
1
2
3
a
for/in loops iterate over factories, as well. Just some examples:
```

> gmatch := proc(s) is
> local c, p := 0, strings.gmatch(s, '%a+'); \# p is assigned a factory
> return proc() is
local word := p();
return when word = null with null;
inc c;
return c, word \# return position and word
end
end;
> s := 'hello world from Agena';
> f := gmatch(s);
> for i in f do
> print(i)
> od;
hello
world
from
Agena
f := gmatch(s);
> for k, v in f do
> print(k, v)
> od;
1 hello
2 world
3 from
4 Agena
f := gmatch(s);
> for keys k in f do
print(k)
od;

```


\subsection*{6.23 Self-defined Binary Operators}

A procedure f of two arguments \(\mathrm{x}, \mathrm{y}\)
```

> plus := proc(x, y) is return x + y end;

```
can be called like a binary operator through the syntax x f y :
```

> 1 plus 2:

```
3

When using a function as a binary operator, it has always the highest precedence.

\subsection*{6.24 OOP-style Methods on Tables}

Agena supports OOP-style methods. For a table object representing a bank account,
```

> account := ['balance' ~ 0];

```
define the following method (please note the two @ tokens):
```

> proc account@@deposit(x) is
> inc self.balance, x;
return self.balance
end;

```

The name self always refers to the table object, here account. Call the method using two e characters:
```

> account@@deposit(100)

```

Query the object.
```

> account:
[balance ~ 100, deposit ~ procedure(016D6820)]

```

Let us define a method for withdrawing an amount of money. Instead of the proc statement, we will now use the standard := assignment:
```

> account@@withdraw := proc(x) is
if x < O then error('Error, value must be non-negative.') fi;
dec self.balance, x;
return self.balance
end;

```

To set up new accounts that inherit the methods and characteristics associated with the account object, assign the metatable of the account object to the freshly created account using the setmetatable function, and force Agena to search for the methods or its balance stored to account by proper indexing (i.e. self.__index
:= self). Thus, we use the account object as a prototype inherited by individual accounts. To explore the metatable of an object, call getmetatable.
```

> proc account@@new(o) is
O := o or []; \# if not given, create object with its initial
\# balance taken from the current state of `account`
setmetatable(o, self); \# assign metatable of `account` object
\# (i.e. `self`) to new table
self.__index := self; \# inherit methods from `account` object
return o
end;
> a := account@@new();
> a.balance:
100

```

Set up a new account with its initial balance set to zero:
```

> b := account@@new(['balance' ~ 0]);

```

Pay into the bank 200 currency units.
```

> b@@deposit(200):
200

```

If you want to create a different class of accounts, e.g. accounts on credit that own all the features of account but do not allow any overdraft, just assign an account object to it by calling the new method (do not just assign account to creditaccount):
```

> creditaccount := account@@new();

```
and overwrite the withdraw method:
```

> proc creditaccount@@withdraw(x :: number) is
> if x < O then error('Error, value must be non-negative.') fi;
if x > self.balance then error('Error, not enough credit.') fi;
dec self.balance, x;
return self.balance
end;
> c := creditaccount@@new();
> c@@withdraw(1000):
Error, not enough credit.

```

Since b is an unlimited account, we can withdraw money as much as we want, as its withdraw metamethod has not been replaced.
```

> b@@withdraw(1000):
-800

```

\subsection*{6.25 Assigning Tables to Procedures}

As an alternative to storing values into the registry (see Chapter 6.31) or using closures (Chapter 6.22), you can assign a table to a procedure with the store
feature. The table will remain active during the entire Agena session and you can read from or write values to it in subsequent calls to the function.
This feature is thrice as fast as interacting with the registry, but only half as fast as closures. The table can be accessed through the store keyword which can also be indexed:
```

> f := proc() is
feature store;
store[1] := Pi;
store.count := (store.count or 0) + 1;
return store, store[1], store.count
end;
> f()
[3.1415926535898, 1] 3.1415926535898 1

```

To get access to the internal store, call debug.getstore which returns its reference. You can both inspect this table as well as inject values into the store. In the following example we define a sine function with precomputed coefficients:
```

> zxsine := proc(x :: number) is \# ZX Spectrum SIN emulation
feature store; \# activate the internal store
local w, z;
x *:= 0.5/Pi;
x -:= entier(x + 0.5);
w := 4*x;
if w > 1 then
w := 2 - w
elif w < -1 then
W := - W - 2
fi;
z := 2*W*W - 1;
return w*(store[1] + z*(store[2] + z*(store[3] + z*(store[4] +
z*(store[5] + z*store[6])))))
end;
_coeffs := // 1.267162131 -0.284851843 0.18226552e-1 -0.546208e-3
> 0.9480e-5 -0.112e-6 <br>;

```

To get a reference to the store, execute:
```

> _store := debug.getstore(zxsine);

```

Insert coefficients to the store,
```

> for i in _coeffs do
> insert i into _store
> od;

```
and do some cleanup thereafter:
```

> _store, _coeffs -> null;

```

Voila:
```

> zxsine(Pi/4):
0.70710678125

```

Of course, you can mix store tables with remember tables. For another example, see Chapter 6.31.

\subsection*{6.26 Summary on Procedures}

The following diagram tries to summarise all features of a procedure.


\subsection*{6.27 I/O}

Agena features various functions to deal with files, to read lines and write values to them. Keyboard interaction is supported, too, as is interaction with other applications. Most of the functions have been taken from Lua. All the functions for input/output are included in the io and the binio packages.

Read and write access to files usually is conducted through file handles. At first, a file is opened for read or write operations with the io.open function. Then you apply the respective read or write functions and finally close the file again by calling io.close.

\subsection*{6.27.1 Reading Text Files}

Open a file and store the file handle to the name fh:
```

> fh := io.open('d:/agena/src/change.log'):
file(7803A6F0)

```

Read the first ten characters:
```

> io.read(fh, 10):
Change Log

```

Read the next ten characters:
```

> io.read(fh, 10):
for Agena

```

Close the file:
```

> io.close(fh):
true

```

Besides file handles, many I/O functions also accept file names. For example, the io.lines procedure reads in a text file line by line. It is usually used in for loops. The respective line read is stored to the loop key, the loop value is always null. The function opens and closes the file automatically.
```

> for i, j in io.lines('d:/agena/lib/agena.ini') do
> print(i, j)
> od
execute := os.execute; null
getmeta := getmetatable; null
setmeta := setmetatable; null

```

\subsection*{6.27.2 Writing Text Files}

To write numbers or strings into a file, we must first create the file with the io.open function. The second argument ' \(w\) ' tells Agena to open it in `write` mode.
```

> fh := io.open('d:/file.txt', 'w');

```

As mentioned above, io.open returns a file handle to be used in subsequent I/O operations.
```

> io.write(fh, 'I am a text.');

```

If you would like to include a newline, pass the ' \(\backslash n\) ' string,
```

> io.write(fh, 'Me ', 'too.', '\n');

```
or use the io.writeline function which automatically adds a newline to the end of the input. The next statement writes the number \(\pi\) to the file.
```

> io.writeline(fh, Pi);

```

After all values have been written, the file must be closed with io.close.
```

> io.close(fh);

```

The statements presented above produce the file contents:
```

I am a text.Me too.
3.1415926535898

```

We can append text to a file we have already created. In order to append - and not to overwrite existing - text, use the 'a' switch in the call to io.open \({ }^{17}\). Using the 'w' switch would replace the text already existing with the new one. See Chapter 12.1 for further options accepted by io.open.

Tables, sets or sequences cannot be written directly to files, they must be iterated using loops so that their keys and values - which must be numbers, booleans or strings - can be stored separately to the file thereafter. The same applies to pairs: use the left and right operators to write their components.

The following statements write all keys and values of a table to a file. The keys and values are separated by a pipe '।', and a newline is inserted right after each key \(\sim\) value pair. Note that you can mix numbers and strings.
```

> a := [10, 20, 30];
> file := io.open('d:/table.text', 'w');
> for i, j in a do
> io.write(file, i, '|', j, '\n')
> od;
> io.close(file);

```

Hint: To create UNIX text files on DOS-like systems, such as DOS, OS/2, Windows, just open the text file in binary mode, e.g. io.open('d:/table.text', 'wb'). This avoids carriage return control codes to be added to the file with each line break.

See Chapter 12.1 for a description of all io package functions.
If you have trouble with character encoding, the converters strings.tolatin, strings.toutf8, strings.diamap or the aconv package might help you.

\subsection*{6.27.3 Keyboard Interaction}

The io.read function allows to enter values interactively via the keyboard when called with no argument. Use the RETURN key to complete the input. The value returned by io.read is a string. If you would like to enter and process numbers thereafter, use the tonumber function to transform the string into a number.
```

> a := io.read();
10

```

\footnotetext{
\({ }^{17}\) See Chapter 12.1 for further options accepted by io.open.
}
```

> a:
10
> type(a):
string
> tonumber(a)^2:
100

```

All available keyboard functions are:
\begin{tabular}{l|l|}
\hline Procedure & Details \\
\hline io.anykey & Checks whether a key has been pressed and returns true or false. \\
\hline io.getkey & \begin{tabular}{l} 
Waits until a key is pressed and returns its ASCll value. This function is \\
not available on all platforms.
\end{tabular} \\
\hline io.read & \begin{tabular}{l} 
If called with no arguments, reads one or more characters from the \\
keyboard until the RETURN key is being pressed. The return is a string.
\end{tabular} \\
\hline
\end{tabular}

Table 19: Functions to read the keyboard

\subsection*{6.27.4 Default Input, Output, and Error Streams}

Agena provides aliases to the standard input, output, and error channels known from C:
- io.stdin, the standard input stream, used to input data, usually the keyboard,
- io.stdout, the standard output stream, used to output data, usually the console,
- io.stderr, the standard error stream, used for error messages and diagnostics, usually the console.

Examples:
```

> io.writeline(io.stdout, 'Okay');
Okay
> io.writeline(io.stderr, 'Not okay');
not okay

```

\subsection*{6.27.5 Locking Files}

Agena allows files to be locked so that only the current process can read or write data to them. This feature prevents corruption to files during write operations or reading invalid data when other programmes try to access them. See io.lock and io. unlock in Chapter 12.1 for further information.

\subsection*{6.27.6 Interaction with Applications}

You can call another application, pass data to it and receive data from the application with the io.popen function. The function returns a file handle, so that you can receive the information returned (from the stdout channel of the called programme) for further processing.

To get a listing of all files in the current directory, enter:
```

> p := io.popen('ls'):
file(77602960)
> io.readlines(p):
[ads.c, agena.c, etc.]

```

Finally, close the connection.
```

> io.close(p)

```

If you pass the 'w' option to io.popen as a second argument, you can send further data to the external programme:
```

> p := io.popen('cat', 'w')
> io.write(p, 'Hello ')
> io.write(p, 'World\n')
> io.close(p)
Hello World

```

If you want to receive data from the stderr channel, or suppress output at the Agena console, include the respective redirection instruction, which may vary among operating systems, in the first argument to io.popen.

\subsection*{6.26.7 CSV Files}

Comma-separated value files can be read and written conveniently by utils.readcsv and utils.writecsv. This function provides various options to further process the data being read. See Chapter 16.1 for further details.

\subsection*{6.27.8 XML Files}

XML files are imported and converted to Agena data structures with utils.readxml or xml.readxmI. XML files can be created with utils.encodexml and io.write. Chapter 16.1 and 12.5 offers further information on how to do this.

\subsection*{6.27.9 dBASE III/IV Files}

The xbase package can read and write dBASE III/V-compatible files. See Chapter 12.3 for details.

\subsection*{6.27.10 INI Files}

The utils.readini and utils.writeini functions deal with traditional INI initialisation files.

\subsection*{6.28 Linked Lists}

With large tables, sometimes it may be very costly to insert or delete an element with the put and purge functions because all elements after the insert or deletion position must either be shifted up- or downwards. This is also true with sequences and registers.

In addition, iterating a table with the for/in statement does not ensure that the keys are traversed in ascending order \({ }^{18}\).

In these cases you may use the llist package implementing linked lists which store elements in a sequential order and where each value also links to its successor (and predecessor). Just take a look at the examples at the end of this subchapter.

The benefit of using linked list in these situations is a speed increase of at least 600 \%, but may be very much larger.

To see how a linked list works, let us create one manually. First, establish a root which indicates the end of the list.
```

> list := null;

```

Now we insert the numbers \(-2,-1\) and 0 into this list, so that it contains the elements \(0,-1,-2\), in this order.
```

> list := ['data' ~ -2, 'next' ~ list];
> list := ['data' ~ -1, 'next' ~ list];
> list := ['data' ~ 0, 'next' ~ list];

```

To traverse the list, we use a new reference so that the original list is not changed:
```

> l := list;
while l do
print(l.data)
l := l.next
od;
0
-1
-2

```

To insert an element somewhere in the list, we enter:
```

> l := list;
> while l do
if l.data = -1 then
l.next := ['data' ~ -1.5, 'next' ~ l.next];
break
fi;
l := l.next
od;
18 See skycrane.iterate.

```
```

> l := list;
> while l do
> print(l.data)
> l := l.next
> od;
0
-1
-1.5
-2

```

It may often be useful to add further information to a linked list to save unnecessary traversal, e.g. the position of the element or the predecessor.

Instead of implementing singly- or doubly-linked lists yourself, use the llist package. First initialise it,
> import llist
and create an empty list.
```

> L := llist.list():
llist()

```

Now add O to it
```

> llist.append(L, 0);

```
and also put -2 to its beginning.
```

> llist.prepend(L, -2);
> L:
llist(-2, 0)

```

Insert -1 at position 2. As you see, the original element at this position is not deleted but shifted to open space.
```

> llist.put(L, 2, -1):
> L:
llist(-2, -1, 0)

```

To delete an element at a position, enter:
```

> llist.purge(L, 2):
> L:
llist(-2, 0)

```

The size operator determines the number of all elements in a linked list.
```

> size L:

```
2

To determine a specific element, index it as usual:
```

> [1]
-2

```

Passing an index that does not exist, simply results to null.
Finally, to replace an element, use a usual assignment statement.
```

> L[2] := -1
> L:
llist(-2, -1)

```

You may have a look at unrolled singly-linked lists, which are also provided by the llist package for high-speed processing. The ulist functions have the same name as those for llists, and almost the same syntax, so here is just a small example:
```

> import llist \# _not_ `import uliist`
> a := ulist.list(64) \# 64 slots per node
> for i to 11 do ulist.append(a, i) od \# fill ulist with numbers 1 to 11
> ulist.put(a, 5, 100); \# insert 100 at position 5
> a := ulist.dump(a); \# convert ulist into a sequence and dump it
> \# from memory
> print(a)
seq(1, 2, 3, 4, 100, 6, 7, 8, 9, 10, 11)

```

Finally, functions to work on doubly-linked lists are available in table dlist. Read and write access to elements in doubly-linked lists is around twice as fast as for singly-linked lists:
```

> l := dlist.list('Algol 68', 'Maple', 'Lua', 'SQL');
> dlist.append(l, 'Agena'); \# add new entry to the end of the list
> l[-1]:
Agena
> dlist.prepend(l, 'Agena'); \# add new entry to the start of the list
> 1[1]:
Agena
> dlist.purge(l, 1); \# delete first entry
> 1[1]:
Algol 68
> dlist.purge(l, -1); \# delete last entry
> l[-1]:
SQL

```
```

> \# insert a new value into the middle of the list, shifting elements into
> \# open space
> dlist.put(l, 3, 'Agena');
> dlist.toseq(l):
seq(Algol 68, Maple, Agena, Lua, SQL)
> f := dlist.iterate(l); \# iterate through the list
> f():
Algol 68
(etc.)

```

\subsection*{6.29 Numeric C Arrays}

Agena numbers can alternatively be processed using numeric C arrays. The numarray package supports C doubles, signed 4 -byte integers (int32_t), and unsigned chars. See Chapter 10.6 for further details.

While C numeric arrays consume less memory than Agena's built-in structures, operations are slower.

\subsection*{6.30 Userdata and Ligthuserdata}

Some Agena packages such as linked lists and numarrays implement data structures by so-called userdata, i.e. C structures that are garbage-collected by the interpreter provided that a '_-gc' metamethod exists.

Likewise, lightuserdata are pointers to any \(C\) objects but programmers writing \(C\) libraries have to implement their own garbage collection procedures.

To the ordinary programmer writing code exclusively in the Agena language, userdata and lightuserdata are irrelevant as this kind of data can only be accessed through functions written in C .

\subsection*{6.31 The Registry}

The registry is an interface between Agena and its C virtual machine which mainly stores values needed by userdata, metatables of libraries written in C , open files, and loaded libraries. It can also be used to exchange data between the C environment and Agena, or between Agena functions in general. See Chapter 6.25 for a faster alternative if you know that a function does not need to exchange data with other functions.
debug.getregistry gives full access to the registry but should be used carefully. It is recommended to revert to the functions of the registry package to read, add or delete registry data or to modify C library metatables, and to exclude the debug library from sandboxes (see Chapters 6.15, 7.40 and 7.53).

Registry entries indexed by integral keys refer to data occupied by userdata objects, which for example are used by the llist and numarray libraries. The registry library, however, does not expose these values to Agena.

Following is an example how you can use this feature:
```

watch := proc(x) is
local id, t, val;
t := time();
\# create light userdata as registry key
id := 'baselib_watch';
unassigned registry.get(id) ? registry.anchor(id, 0);
if x then \# any argument given ? -> initialise / reset the clock
registry.anchor(id, 0);
return
fi;
val := registry.get(id); \# get old time (in seconds)
if val = O then \# start clock
registry.anchor(id, t); \# assign a new value to registry
t := 0
else \# return elapsed time and set clock to current time
t -:= val;
registry.anchor(id, time())
fi;
return t
end;

```

In comparison, an implementation using an internal store table would be:
```

watch := proc(x) is
feature store;
local id, t, val;
val := store[1]; \# get old time (in seconds)
unassigned val ? store[1] := 0; \# initialise with the first call
t := time();
if x then \# reset the clock but do not turn it on again
store[1] := 0;
return
fi;
if val = 0 then \# start clock
store[1] := t;
t := 0
else \# return elapsed time and set clock to current time
t -:= val;
store[1] := time()
fi;
return t
end;

```

\section*{Part Two}

Reference

Chapter Seven

\section*{The Libraries}

\section*{7 The Libraries}

The standard libraries taken from the Lua 5.1 distribution provide useful functions that are implemented directly through the C API. Some of these functions provide essential services to the language (e.g., next and getmetatable; others provide access to `outside` services (e.g., l/O); and others could be implemented in Agena itself, but are quite useful or have critical performance requirements that deserve an implementation in C (e.g., sort) .

The following text is based on Chapter 5 of the Lua 5.1 manual and includes all the new operators, functions, and packages provided by Agena.

Lua functions which were deleted from the code are not described. References to Lua were not deleted from the original text. If an explanation mentions Lua, then the description also applies to Agena.

All libraries are implemented through the official C API and are provided as separate C modules. Currently, Agena has the following standard libraries:
- the basic library,
- package library,
- string library,
- table library,
- mathematical library,
- two input and output libraries,
- operating system library,
- environmental libraries,
- debug facilities.

Except for the basic and the package libraries, each library provides all its functions as fields of a global table or as methods of its objects. Agena operators have been built into the kernel (the Virtual Machine), so they are not part of any library.

\section*{Chapter Eight}

\section*{Basics}

\section*{8 Basics}

The basic library provides some core functions to Agena. If you do not include this library in your application, you should check carefully whether you need to provide implementations for some of its facilities.

For logical operators, please see Chapter 4.8.
Summary of functions:
Checks
\$\$, abs, alternate, assigned, assume, binsearch, filled, has, isequal, rawequal, recurse, satisfy, whereis.

\section*{Extraction}
\$, bottom, columns, descend, duplicates, getentry, left, max, min, next, ops, rawget, recurse, right, top, unique, unpack, values.

Types
checkoptions, checktype, float, gettype, isboolean, iscomplex, isint, isnegative, isnegint, isnonnegint, isnonposint, isnumber, isnumeric, ispair, isposint, ispositive, isseq, isstring, isstructure, istable, nan, nonneg, optboolean, optcomplex, optint, optnonnegative, optnonnegint, optnumber, optposint, optpositive, optstring, settype, type, typeof.

Counting
countitems, size.

\section*{Data Manipulation}
@, augment, getbit, map, move, prepend, purge, put, rawset, reduce, remove, select, selectremove, setbit, sort, sorted, subs, toreg, toseq, toset, totable, zip.

\section*{Data Generation}
iterate, tables.new, sequences.new, registers.new.
Error Handling
argerror, error, protect, xpcall.

\section*{Libraries}
readlib, with.

Files
read, save.
Output
print, printf, write, writeline.
Parsing
load, loadfile, loadstring.

Cantor Operations
bintersect, bisequal, bminus.
Metatables
getmetatable, setmetatable.
Miscellaneous
bye, clear, restart, time.
f @ obj
f @ g
In the first form, the operator maps a function f to all the values in table, set, sequence, register, string or pair obj. f should be a univariate function and return only one value. The type of return is the same as of obj. If obj has metamethods or user-defined types, the return will also have them.

If obj is a string, f is applied on all of its characters from the left to right. The return is a sequence of function values.

Examples:
```

> << x -> x^2 >> @ [1, 2, 3]:
[1, 4, 9]
> << x -> x > 1 >> @ [1, 2, 3]:
[false, true, true]

```

In the second form, the function creates the composition of two functions f @ \(\mathrm{g}=\) \(f(g(x))\) and returns it is a new function ( \(£\) @ \(g)(x)\). \(f\) and \(g\) may be univariate or multivariate and also return multiple results.

Example:
```

> \# first take root, then negate
> h := << x -> -x >> @ << x -> sqrt x >>
> h(2):
-1.4142135623731

```

See also: @ and \$\$ operators, map, reduce, remove, select, subs, times, zip.

\section*{f \({ }^{\text {S }} \mathrm{obj}\)}

Returns all values in table, set, sequence or register obj that satisfy a condition determined by function f . f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.
```

> << x -> x > 1 >> \$ [1, 2, 3]:
[2, 3]

```

If present, the function also copies the metatable and user-defined type of obj to the new structure.

Please note that if obj is a table, the return might include holes. With obj a register, all values up to the current top pointer are evaluated, and the size of the returned register is equal to the number of the elements in the return.

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

\section*{f \(\mathbf{\$} \mathbf{\$}\) obj}

Checks whether at least one element in table, set, sequence or register obj satisfies the condition defined by function \(f\) and returns true or false. \(f\) should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.
```

> << x -> x < 1 >> \$\$ [1, 2, 3]:
false
```

Please note that if obj is a table, the return might include holes. With obj a register, all values up to the current top pointer are evaluated.

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.
abs (x)
If $x$ is a number, the abs operator will return the absolute value of $x$. With complex numbers, the magnitude $\sqrt{\operatorname{real}(\mathrm{X})^{2}+\mathrm{imag}(\mathrm{X})^{2}}$ is evaluated (see also: cabs).

If x is a Boolean, it will return 1 for true, 0 for false, and -1 for fail.
If x is null, abs will return -2 .
If x is a string of only one character, abs will return the ASCll value of the character as a number. If x is the empty string or longer than length 1 , the function returns fail.

```
alternate (x, y)
```

Returns x if y evaluates to null, else returns y . This is equivalent to if $\mathrm{y}=$ null then x else ${ }_{y}$ fi, which is not equal to ${ }_{y}$ or x .

See also: or operator.

```
argerror (x, procname, message)
```

Receives any value $x$, the name of procedure procname (a string) where $x$ did not satisfy anything, the error message text message, and appends the user-defined type or if not defined the basic type of $x$. Thus it returns the error message: 'Error in procname: message, got <type of $x>$.'.

The function is written in Agena and included in the lib/library.agn file.
See also: error.

## assigned (obj)

This Boolean operator checks whether any value different from null is assigned to the expression obj. If obj is already a constant, i.e. a number, boolean including fail, or a string, the operator always returns true. If obj evaluates to a constant, the operator also returns true. See also: unassigned.

```
assume (obj [, message])
```

Issues an error when the value of its argument obj is false (i.e., null or false); otherwise, returns all its arguments. message is an error message; when absent, it defaults to 'assumption failed'.
augment (obj1, obj2 [, ...])
Joins two or more tables, sequences or registers obj1, obj2 together horizontally. The arguments must either be tables, sequences or registers only. All structures must be of the same size. The type of return is determined my the type of the arguments.

The function is written in Agena and included in the lib/library.agn file.
See also: columns, linalg.augment.
beta ( $\mathrm{x}, \mathrm{y}$ )
Computes the Beta function. x and y are numbers or complex values. The return may be a number or complex value, even if $x$ and $y$ are numbers. The Beta function is defined as: $\operatorname{Beta}(\mathrm{x}, \mathrm{y})=\frac{\Gamma \mathrm{x} * \Gamma \mathrm{y}}{\Gamma(\mathrm{x}+\mathrm{y})}$, with special treatment if x and y are integers.

```
binsearch (o, x [m [, l [, r]]])
```

Performs a binary search for x in the sorted table, sequence or register o. You may optionally specify the left border 1 and the right border r in $\circ$ where to search for x , by default 1 is 1 and $r$ is size $\circ$. The very first element in $\circ$ to be checked is given by $m$ which by default is $(1+r) \backslash 2$.

The function returns true on success or false otherwise. The second return is the index position of the last element checked before the function returns.

You may have to sort o before invoking the function, otherwise the result would be incorrect.

See also: in operator.

```
bintersect (obj1, obj2 [, option])
```

Returns all values of table, sequence or register obj1 that are also values in table or sequence obj2. obj1 and obj2 must be of the same type. The function performs a binary search in obj2 for each value in obj1. If no option is given, obj2 is sorted before starting the search. If you pass an option of any value then obj2 should already have been sorted, for no correct results would be returned otherwise.

With larger structures, this function is much faster than the intersect operator.
The function is written in Agena and included in the lib/library.agn file.
See also: bisequal, bminus.
bisequal (obj1, obj2 [, option])
Determines whether the tables, sequences or registers obj1 and obj2 contain the same values. The function performs a binary searches. If no option is given (any value), obj1 and obj2 are sorted before starting the search. If you pass an option of any type then obj1 and obj2 should already have been sorted, for no correct results would be returned otherwise.

With larger structures, this function is much faster than the = operator.
The function is written in Agena and included in the lib/library.agn file.
See also: bintersect, bminus.

```
bminus (obj1, obj2 [, option])
```

Returns all values of table, sequence or register obj1 that are not values in table, sequence or register obj2. obj1 and obj2 must be of the same type. The function performs a binary search in obj2 for each value in obj1. If no option is given, obj2 is sorted before starting the search. If you pass the option then obj2 should already have been sorted, for no correct results would be returned otherwise.

With larger structures, this function is much faster than the minus operator.
The function is written in Agena and included in the lib/library.agn file.
See also: bintersect, bisequal.

## bottom (obj)

With the table array, sequence or register obj, the operator returns the element at index 1 . If obj is empty, it returns null.

See also: top.

## bye

Quits the Agena session. No arguments or brackets are needed. If a procedure has been assigned to the name environ.onexit, then this procedure is automatically run before exiting the interpreter. The function also conducts a final garbage collection fully closes the state of the interpreter before leaving. An example:

```
> environ.onexit := proc() is print('Tschüß !') end
> bye
Tschüß !
```

checkoptions (procname, obj, option [, ...] [, true])

Checks options passed to a given procedure, saving many lines of code in procedures.

Since an option such like delimiter='; ' in a function call is actually passed as the pair 'delimiter':';' you have to make sure that `real` pairs containing data (but not options) are not included in the call to checkoptions. See Chapter 6.6.

Its first argument procname - a string, not the function reference - is the name of the procedure in which the check takes place.

Its second argument obj - a table - represents the arguments to be checked.
The third to last arguments are pairs. The respective left operand (a string) will be checked whether one of the right operands of the pairs in obj is of the type passed as the right operand (a string or a basic type). See examples below.

The evaluation of obj works as follows: If an entry in obj is not a pair, it is not evaluated, ignored and not returned in the resulting table. But if the entry is a pair, it checks whether the left-hand side is a string, i.e. the name of an option. It then checks whether its right hand side is of the given type in anything passed to option or further options of type pair. By default, If an option in obj cannot be found in option or further options of type pair, an error will be issued. But if the very last argument is the Boolean value true, no error will be issued and the `unknown` option is part of the resulting table.

If successful, the return is a table where the respective left-hand side in obj is the key and the respective right-hand side in obj is the respective entry. Please play around with this new function, or have a look at the lib/skycrane.agn file in your local Agena installation, function skycrane.scribe. User-defined types are properly handled.

Thus:

```
> checkoptions('myproc', [1, 'neil':'armstrong'], neil=string):
> # 'neil' must be a string, number 1 will be skipped as not being a pair
[neil ~ armstrong]
> checkoptions('myproc', ['neil':'armstrong'], neil=boolean):
Error in `myproc`: boolean expected for neil option, got string.
> checkoptions('myproc', ['neil':'armstrong', 'james':'lovell'],
> neil=string, true):
[james ~ lovell, neil ~ armstrong]
```

checktype (obj, main, sub)

Checks whether the structure obj is a table, set, pair, sequence or register, and whether it is of the type given by main (a string), and whether all its elements are of type sub (a string). It returns true or false. User-defined types are supported.

The function is written in Agena and included in the lib/library.agn file.
cleanse (t)
Empties a table, set or register and returns the emptied structure. With a register, sets all its places to null and returns the modified register. With tables, sets and sequences, the memory previously occupied can be reused by the interpreter.
clear v1 [, v2, $\cdots$ ]
Deletes the values in variables v1, v2, ..., and performs a garbage collection thereafter in order to clear the memory occupied by these values.
columns (obj, p [, …] [, 'structure'])
Extracts the given columns $p$ (etc.) from the two-dimensional table, sequence or register obj. The type of return is determined by the type of obj and is either a structure of structures if the option 'structure' is given, or a multiple return of structures.

The function is written in Agena and included in the lib/library.agn file.
See also: ops, select, unpack, values, linalg.column, utils.readscv.

```
copy (obj [, option])
```

The function copies the entire contents of a table, set, pair or sequence obj into a new structure. If obj contains structures itself, those structures are also copied (by a 'deep copying' method). Structures included more than once are properly aggregated to one single reference to save memory space. Metatables and user-defined types are copied, too.

With tables, if the 'array' option is given, then the function returns just the array part of obj. Likewise, the ' hash' option only extracts the hash part of obj.

If the option is 'nometa', then metatables and user-defined types will not be copied regardless of the data type of obj.

The type of return is determined by the type of obj.
The function also treats cycles (structures that directly or indirectly reference to themselves), correctly.

See also: copyadd.

```
copyadd (obj [, \cdots.])
```

Copies all elements in table, set, sequence or register obj and any further optional arguments into a new structure and returns it. The result is of the same type as obj.

With tables, the array and hash parts are copied 1:1, i.e. the elements in the array part of obj are copied to the array part with the same keys, and the elements in the hash part of obj are copied to the hash part of the new table, with the same keys, too.

For performance reasons, substructures are not deep-copied.
The function may be used when in an expression there is a call to unpack or any other function returning multiple values, which is followed by one or more subsequent values, as in this situation multiple values returned by any function get truncated to the first value if it's not the last trailing expression.

Compare for example:

```
> f := proc(x, y) is
> return math.sincos(x), y
> end;
> f(0, E):
0 2.718281828459
versus
> f := proc(x, y) is
    return unpack(copyadd([math.sincos(x)], y))
end;
f(0, E):
0 1 2.718281828459
```

The function is written in Agena and included in the lib/library.agn file.
See also: copy, tables.include, insert statement.

```
countitems (item, obj)
countitems (f, obj [, \cdots.]])
```

In the first form, counts the number of occurrences of an item in the structure (table, set, sequence or register) obj.

In the second form, by passing a function $£$ with a Boolean relation as the first argument, all elements in the structure obj that satisfy the given relation are counted. If the function has more than one argument, then all arguments except the first are passed right after the name of the object obj.

The return is a number. The function may invoke metamethods.
See also: select, bags package.
descend (f, obj, [, ...] [, option])
Returns all elements in the structure obj (a table, set, sequence or register) that satisfy a given condition expressed by function $£$. The function can be multivariate and must return either true or false. The optional second and all further arguments of f may be passed as the third, etc. argument.

With tables, all the entries and keys are scanned.
With sequences and registers, only the entries (not the keys) are scanned.
The function performs a recursive descent if it detects tables, sets, registers or sequences in obj so that it can find elements in deeply nested structures. Pairs, however, are ignored.

If obj is a table and the option skiphash=true has been passed, then the function ignores all non-numeric keys and their corresponding values, i.e. ignores the hash part of a table.

The function returns a structure with its type depending on the type of obj with all the hits in no more than two levels, an example:

```
> s := seq(1, 2, 3, [1, 2, 3], seq(1, 2, 2, 4, {2, 4, 5}));
> descend(<< x -> x = 2 >>, s):
seq(2, [2], seq(2, 2), {2})
> # return all elements greater or equal 3
> ge := proc(x, y) is # x greater or equal y ?
> try
    return x >= y
        catch # avoid comparisons of numbers with other data types
            return false
        yrt
    end;
> descend(ge, s, 3):
seq(3, [3], seq(4), {4, 5})
```

descend issues an error if obj is unassigned.
See also: has, recurse, satisfy, select.

```
duplicates (obj [, option])
```

Returns all the values that are stored more than once to the given table, sequence or register obj, and returns them in a new table, sequence or register. Each duplicate will be returned only once. If option is not given, the structure is sorted before evaluation since this is needed to determine all duplicates. The original structure is left untouched, however.

If a value of any type is given for option, the function assumes that the structure has been already sorted. The values in obj should either be strings or numbers if no option is given, otherwise the function will fail.

The function is written in Agena and included in the lib/library.agn file.

## empty (obj)

This Boolean operator checks whether a table, set, register, sequence or string obj does not contain any item and returns true if so; otherwise it returns false.

See also: filled.

```
error (message [, level])
```

Terminates the last protected function called and returns message as the error message. error never returns.

Usually, error adds some information about the error position at the beginning of the message. The level argument specifies how to get the error position. With level 1 (the default), the error position is where the error function was called. Level 2 points the error to where the function that called error was called; and so on. Passing a level 0 avoids the addition of error position information to the message.

See also: argerror.

## eval (...)

Just returns the value represented by its arguments. See also: identity.

```
everyth (n, k)
everyth (obj, k)
```

In the first form, returns the Agena equivalent $\mathrm{n} \% \mathrm{k}=0$, a Boolean.
In the second form, returns every given k-th element in the table, sequence or register obj in a new structure. The type of return is determined by the type of the first argument. With tables, only the array part is traversed.
_G

A global variable (not a function) that holds the global environment (that is, _G._G = _G). Agena itself does not use this variable; changing its value does not affect any environment, nor vice-versa. (Use setfenv to change environments.)

```
filled (obj)
```

This Boolean operator checks whether a table, set, register, sequence or string obj contains at least one item and returns true if so; otherwise it returns false.

See also: empty.

```
getbit (x, pos)
```

Checks for the bit at position pos $\in[1,32]$ in the integer $x$, and either returns true or false.

See also: getbits, getnbits, setbit, setbits, setnbits, bytes.tobytes, numarray.getbit.

```
getbits (x [, any])
```

Returns all 32 bits in the integer $x$, and returns a register of size 32 with values true or false. If any second argument is given, the register is filled with zeroes or ones instead of booleans.

See also: getbit, getnbits, setbit, setbits, setnbits, numarray.getbit.
getnbits (x, pos, nbits)
From the 32-bit integer $x$, starting from bit position pos from the right, retrieves nbits bits and returns a decimal value. pos should be in [1,32].

```
getentry (obj [, ki, \cdots., kn])
```

Returns the entry obj $\left[k_{1}, \ldots, k_{n}\right]$ from the table, sequence or register obj without issuing an error if one of the given indices $k_{i}$ (second to last argument) does not exist. It conducts a raw access and thus does not invoke any metamethods.

If obj $\left[k_{1}, \cdots, k_{n}\right]$ does not exist, null will be returned. If only obj is given, it is simply returned.

See also: .. operator, \{\} indexing, getorset.
getmetatable (obj)
If obj does not have a metatable, returns null. Otherwise, if the obj's metatable has a '__metatable' field, returns the associated value. Otherwise, returns the metatable of the given obj.

See also: setmetatable.

```
getorset (obj, ki, \cdots, k
```

Returns the non-null element at index $\operatorname{obj}^{[ }\left[\mathrm{k}_{1}, \mathrm{k}_{2}, \ldots, \mathrm{k}_{\mathrm{n}}\right]$, where obj is a table, sequence or register. If any index position is invalid, the function returns null.

If $\circ \mathrm{obj}\left[\mathrm{k}_{1}, \mathrm{k}_{2}, \ldots, \mathrm{k}_{\mathrm{n}}\right]=$ null, then the function assigns $\circ \mathrm{obj}\left[\mathrm{k}_{1}, \mathrm{k}_{2}, \ldots, \mathrm{k}_{\mathrm{n}}\right]:=\mathrm{v}$ and returns v .

See also: getentry.

```
gettype (obj)
```

Returns the type - set with settype - of a function, sequence, set, pair or userdata obj as a string. If no user-defined type has been set, or any other data type has been passed, null will be returned.

See also: settype, typeof.

## has (obj, x)

Checks whether the structure obj (a table, set, sequence, register or pair) contains element x . If obj and x are strings, checks whether at least one character in obj matches one of the characters in x .

With tables, all the entries are scanned. If x is not a number then the indices of the table are searched, too.

With sequences and registers, only the entries (not the keys) are scanned. With pairs, both the left and the right item is scanned. The function performs a deep scan so that it can find elements in deeply nested structures.

The function return true if x could be found in obj, and false otherwise. If obj $<>\mathrm{x}$ and if obj is a number, boolean, complex number, string, procedure, thread, userdata or lightuserdata, has returns fail.

See also: descend, in, recurse, satisfy.

```
identity (...)
```

Returns its arguments. See also: eval, unpack.

```
initialise (packagename [, false])
initialise (packagename , key1, key2, ... [, false])
```

Assigns short names to package procedures such that:

```
name := packagename.name
```

The function works as follows:

- In both forms, initialise first tries to load and run the respective Agena package. The package may reside in a text file with file suffix .agn, or in a C dynamic link library with file suffix .so in UNIX and .dll in Windows, or both in a text file and in a dynamic link library. The function first tries to find the package in the current working directory and if it failed, in the path pointed to by mainlibname; if this fails, too, it traverses all paths in libname from left to right until it finds at least the C DLL or the Agena text file, or both. If a package consists of both the C DLL and an Agena text file, then they both must reside in the same folder.
- If the function does not find the package, an error will be returned.
- Next, initialise tries to find a package initialisation procedure. If a procedure named 'packagename.init` is present in your package then it is executed if the package has been found successfully.
- In the first form, if only the string packagename is given, short names to all functions residing in the global table packagename are created.

If you do not want initialise to assign short names for certain functions, their names should be in the format packagename.aux.procedurename, e.g. math.aux.errormessage.

Note that if packagename. name is not of type procedure, a short name is not created for this object.

- If you would like to display a welcome message, put it into the string packagename.initstring. It is displayed with an empty line before and after the text. An example:
agenapackage.initstring := 'agenapackage v0.1 for Agena as of $\backslash$
May 23, 1949\n';
- In the second form, you may specify which short names are to be assigned by passing them as further arguments in the form of strings. Contrary to the first form, short names are also created for tables stored to table packagename.

As opposed to the first version, initialise does not print any short names or welcome messages on screen.

- Further information regarding both forms:

The function returns a table of all short names assigned.
If the global environment variable environ.withverbose is set to false, no
messages are displayed on screen except in case of errors. If it is set to any other value or null, a list of all the short names loaded and a welcome message is printed.

If a short name has already been assigned, a warning message is printed. If a short name is protected (see table environ.withprotected), it cannot be overwritten by initialise and a proper message is displayed on screen. You can control which names are protected by modifying the contents of environ.withprotected.

For information on which folders are checked and how to add new directories to be searched by initialise, see readlib.

Note that initialise executes any statements (and thus also any assignment) included in the file packagename.agn.

The function is written in Agena and included in the lib/library.agn file.
If the last argument is the Boolean false, initialise does not print the assigned shortcuts at the console.

Note: the import/alias statement is an interface to the initialise function but does not require package names to be put into quotes. For example,

```
> initialise 'stats';
```

is equivalent to
> import stats alias;

See also: readlib, run, register, and import/alias statement.

```
ipairs (obj)
```

Returns three values: an iterator function, the table, sequence, register, string or userdata obj, and 0 , so that the construction

```
for i, v in ipairs(obj) do body od
```

will iterate over the pairs (1,obj[1]), (2,obj[2]), $\cdots$, up to the first integer key absent from the data structure.

If you pass userdata, for example a numarray, it must feature a metatable with an '_index' metamethod. Otherwise an error will be issued.

If there is nothing more to iterate, the iterator returns nulls.
See next for the caveats of modifying the table during its traversal; and also: pairs, factory.iterate, skycrane.iterate.

```
Example:
> import numarray
> d := numarray.double(3)
> d[1] := Pi; d[2] := 2*Pi; d[3] := 3 *Pi;
> f := ipairs(d):
procedure(00410A30)
> idx, val := f(d, 0): # pass 0 to start the iteration
1 3.1415926535898
> idx, val := f(d, idx):
2 6.2831853071796
> idx, val := f(d, idx):
3 9.4247779607694
> idx, val := f(d, idx): # nothing left
null null
```

isboolean (...)
Checks whether the given arguments are all of type boolean and returns true or false.

```
iscomplex (...)
```

Checks whether the given arguments are all of type complex and returns true or false.

```
isequal (obj1, obj2)
```

Equivalent to obj1 $=$ obj2 and returns true or false.
The function is written in Agena and included in the lib/library.agn file.

## isint (...)

Checks whether all of the given arguments are integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: finite, float.

## isnegative (...)

Checks whether all of its arguments are negative numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnegint, isposint, isnonneg, ispositive.

```
isnegint (...)
```

Checks whether all of the given arguments are negative integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

```
isnonneg (...)
```

Checks whether all of its arguments are zero or positive numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnegint, isposint, isnegative, ispositive.

```
isnonnegint (...)
```

Checks whether all of the given arguments are zeros or positive integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

## isnonposint (...)

Checks whether all of the given arguments are zeros or negative integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

## isnumber (...)

Checks whether the given arguments are all of type number and returns true or false.

```
isnumeric (...)
```

Checks whether the given arguments are all of type number or of type complex and returns true or false.

```
ispair (...)
```

Checks whether the given arguments are all type pair and returns true or false.

```
isposint (...)
```

Checks whether all of its arguments are positive integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnonposint.

```
ispositive (...)
```

Checks whether all of its arguments are positive numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnonposint, isposint, isnegative, isnonneg.

```
isreg (...)
```

Checks whether all of its arguments are of type register and returns true or false.

## isseq (...)

Checks whether all of its arguments are of type sequence and returns true or false.

```
isstring (...)
```

Checks whether all of its arguments are of type string and returns true or false.

```
isstructure (...)
```

Checks whether all of its arguments are of type table, set, sequence or pair and returns true or false.

```
istable (...)
```

Checks whether all of its arguments are of type table and returns true or false.

## left (obj)

With the pair obj, the operator returns its left operand. This is equals to obj [1].
See also: right.
load (f [, chunkname])
Loads a chunk using function f to get its pieces. Each call to f must return a string that concatenates with previous results. A return of null (or no value) signals the end of the chunk.

If there are no errors, returns the compiled chunk as a function; otherwise, returns null plus the error message. The environment of the returned function is the global environment.
chunkname is used as the chunk name for error messages and debug information.

```
loadfile ([filename])
```

Similar to load, but gets the chunk from file filename or from standard input, if no file name is given.
loadstring (s [, chunkname])
Similar to load, but gets the chunk from the given string s. To load and run a given string, use the idiom

```
assume(loadstring(s))(...)
```


## Examples:

```
> f := loadstring('a := exp(1)');
> f():
> a:
2.718281828459
> f := loadstring('local x := exp(1); return x')();
> f:
2.718281828459
> f := loadstring('return exp(1)')():
2.718281828459
```

See also: strings.dump.

```
map (f, obj [, \cdots.] [, true])
map (f, g)
```

In the first form, the map function maps a function f to all the values in table, set, sequence, register, string or pair obj. f must return only one value. The type of return is the same as of obj. If obj has metamethods or user-defined types, the return will also have them.

If obj is a string, f is applied on all of its characters from the left to right. The return is a sequence of function values.

If function f has only one argument, then only the function and the structure obj must be passed to map. If the function has more than one argument, then all arguments except the first are passed right after the name of the table or set.

## Examples:

```
> map( << x -> x^2 >>, [1, 2, 3] ):
[1, 4, 9]
> map( << (x, y) -> x > y >>, [-1, 0, 1], 0 ): # 0 for y
[false, false, true]
```

If the very last argument is the Boolean true, then the operation will be done in-place, modifying the original structure, but saving memory. After completion, the function returns the modified structure.

In the second form, the function creates the composition of two functions $£$ @ $g=$ $f(g(x))$ and returns it is a new function ( $£$ @ $g)(x)$. $f$ and $g$ may be univariate or multivariate and also return multiple results.

Example:

```
> # first take root, then negate
> h := map(<< x -> -x >>, << x -> sqrt x >>) # which is equivalent to:
> h := << x -> -x >> @ << x -> sqrt x >> # which results to:
> h(2):
-1.4142135623731
```

See also: @ operator, iterate, sequences.new, registers.new, pipeline, reduce, remove, select, subs, times, zip.

```
max (obj [, 'sorted'])
max (x, y)
```

In the first form, returns the maximum of all numeric values in table, set, sequence or register obj. If the option 'sorted' is passed than the function assumes that all values in obj are sorted in ascending order and returns the last entry. The function in general returns null if it receives an empty table or sequence.

In the second form, the function returns the largest of the two numbers x and y .
See also: min, math.max, stats.minmax.

```
min (obj [, 'sorted'])
min (x, y)
```

In the first form, returns the minimum of all numeric values in table, set, sequence or register obj. If the option 'sorted' is passed than the function assumes that all values in obj are sorted in ascending order and returns the first entry. The function in general returns null if it receives an empty table or sequence.

In the second form, the function returns the smallest of the two numbers x and y .

See also: max, math.min, stats.minmax.
move (obj1, start, stop, newidx [, obj2])
Copies elements from the table, sequence, register or userdata obj1 to table, sequence, register or userdata obj2, performing the equivalent to the following multiple assignment: obj2[newidx], $\cdots=$ obj1[start], $\cdots$, obj1[stop]. The default for obj2 is obj1, i.e. elements are shifted in the same structure. The destination range can overlap with the source range. obj1 and obj2 must be of the same type.

Returns the destination structure obj2.
Example: The following statement copies four elements in table a from position 3 up to and including 6 to a new table b, starting with index 1 :

```
> a := seq('a', 'b', 'c', 'd', 'e', 'f', 'g', 'h');
> b := move(a, 3, 6, 1, seq());
> b:
seq(c, d, e, f)
```

The next statement copies four elements in a to its beginning:

```
> move(a, 3, 6, 1);
> a:
seq(c, d, e, f, e, f, g, h)
```

The function is implemented in the Agena language and is included in the lib/library.agn file.

See also: purge, shift, swap, tables.move.

```
mulup (obj)
```

Multiplies all numeric values in table, sequence or register obj, using round-off error correction. The return is a number. If obj is empty or consists entirely of non-numbers, null will be returned. If the structure contains numbers and other objects, only the numbers are multiplied. In tables, numeric entries with non-numeric keys are processed, as well.

See also: sumup, calc.fprod.

```
next (obj [, index [, sentinel]])
```

Allows a programme to traverse all fields of a table or all items of a set, sequence or register obj. With strings, it iterates all its characters. Its first argument is a table, set, string or sequence and its second argument is an index in the structure.

With tables, sequences or registers, next returns the next index of the structure and its associated value. When called with null as its second argument, next returns an initial index and its associated value. When called with the last index, or with null in an empty structure, next returns null.

With sets, next returns the next item of the set twice. When called with null as its second argument, next returns the initial item twice. When called with the last index, or with null in an empty set, next returns null.

With strings, next returns the position of the respective character (a positive integer) and the character. When called with null as its second argument, next returns the first character. When called with the last index, next returns null.

If the second argument is absent, then it is interpreted as null. In particular, you can use next (t) to check whether a table or set is empty. However, it is recommended to use the filled operator for this purpose.

If the third optional argument sentinel is given, and if next during traversal encounters an element that equals this sentinel, the function just returns null, and you may start iterating the structure again from its beginning.

With tables, the order in which the indices are enumerated is not specified, even for numeric indices. The same applies to set items.

The behaviour of next is undefined if, during the traversal, you assign any value to a nonexistent field in the structure. With tables, you may however modify existing fields. In particular, you may clear existing table fields.

See also: factory.iterate, factory.cycle, skycrane.iterate.

```
ops (index, ...)
```

ops (s, ...)

In the first form, if index is a number, returns all arguments after argument number index. Otherwise, index must be the string '\#', and ops returns the total number of extra arguments it received. The function is useful for accessing multiple returns (e.g. ops( n, ? )).

In the second form, the index positions (integers) in sequence s specify the values to be returned after the first argument to ops.

Example:

```
> f := << () -> 10, 20, 30, 40 >>
> ops(2, f()):
20 30 40
```

If you want to obtain only the element at index, put the call to ops in brackets.

```
> (ops(2, f())):
20
>ops(seq(2, 4), f()):
20 40
```

See also: columns, ops, unpack, values.

```
optboolean (x, y [, idx [, procname]])
```

The function checks whether $x$ is a Boolean and in this case returns $x$. If $x$ is null, it returns the Boolean $y$, otherwise the function issues an error. If the third argument $i d x$, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.
optcomplex (x, y [, idx [, procname]])
The function checks whether $x$ is a number or complex number and in this case returns $x$. If $x$ is null it returns the number or complex number $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

```
optint (x, y [, idx [, procname]])
```

The function checks whether x is an integer and in this case returns x . If x is null it returns the integer $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

```
optnonnegative (x, y [, idx [, procname]])
```

The function checks whether x is a non-negative number and in this case returns x . If $x$ is null it returns the non-negative number $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

## See also: optpositive, optnumber.

optnonnegint (x, y [, procname])
The function checks whether x is a non-negative integer and in this case returns x . If $x$ is null it returns the non-negative integer $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

See also: optint, optposint.
optnumber (x, y [, idx [, procname]])
The function checks whether x is a number and in this case returns x . If x is null it returns the number $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If
the fourth argument procname is given, this name is printed as the function issuing the error.

See also: optpositive, optnonnegative.

```
optposint (x, y [, idx [, procname]])
```

The function checks whether x is a positive integer and in this case returns x . If x is null it returns the positive integer $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

See also: optint, optnonnegint.

```
optpositive (x, y [, idx [, procname]])
```

The function checks whether x is a positive number and in this case returns x . If x is null it returns the positive number $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

See also: optnonnegative, optnumber.
optstring (x, y [, idx [, procname]])
The function checks whether x is a string and in this case returns x . If x is null it returns the string $y$, otherwise the function issues an error. If the third argument idx, a number, is given, then the position idx will be returned in error messages. If the fourth argument procname is given, this name is printed as the function issuing the error.

```
pairs (obj)
```

Returns three values: the next function, the table obj, and null, so that the construction

```
for k, v in pairs(obj) do body od
```

will iterate over all key~value pairs or values of table obj.
See next for the caveats of modifying the table during its traversal; and also: ipairs, factory.iterate, skycrane.iterate.

```
pipeline (f [, ...], obj [, ...])
```

Maps one or more functions $f$, etc. on a table, set, sequence, register or userdata obj, avoiding multiple internal copies of the structure if possible.

If given a userdata obj, the function will change its values in-place, whereas with tables, sets, sequences and registers, the original structure obj will not be modified.

The return is a new structure, depending on the type of obj. If the function has more than one argument, then all arguments except the first are passed right after the name of object obj.

See also: map, @ operator.

```
prepend (x, obj)
```

Prepends an object $x$ to the beginning of structure obj, in-place. The function returns the modified structure.

The new object can always be found at index 1, all other elements have been shifted up one index into open space. With a table, its hash part is not modified.

With a register, the function automatically increases its size by one. If obj is a pair, returns x: obj.

The function is written in Agena and included in the lib/library.agn file.
See also: put, insert statement.

```
print (... [, options])
```

Receives any number of arguments, and prints their values to the console, using the tostring function to convert them to strings. print is not intended for formatted output, but only as a quick way to show a value, typically for debugging. For formatted output, use strings.format.

In Agena, print also prints the contents of tables and nested tables to stdout if no __tostring metamethods are assigned to them. The same applies to sets and sequences.

If the option 'delim': <string> is given as the last argument, then print separates multiple values with the given <string> delimiter, otherwise ' $\backslash \mathrm{t}$ ' is used. If the option 'nonewline': true is passed, then Agena does not print a final newline when finishing output. The 'enclose':<string> option encloses the values in a given substring. All other types will not be enclosed. All options can be combined.

If the kernel setting environ.kernel('longtable') is set to true, then each key~value pair is printed on a separate line, and Agena halts after environ.more number of lines for the user to press any key for further output. Press ' $q$ ', ' $Q$ ' or the

Escape key to quit. The default for environ.more is 40 lines, but you may change this value in the Agena session or in the Agena initialisation file.

You may change the way print formats objects by changing the respective environ.print* functions in the lib/library, agn file. See Appendix A5 for further details.

See also: printf, io.write, io.writeline, skycrane.scribe, skycrane.tee.

```
printf ([fh,] template, ...)
```

If the first argument fh is not given, prints the optional arguments under the control of the template string template to stdout, else it writes to the open file denoted by its file handle $f$. See strings.format for information on how to create the template string.

Example:

```
> printf('%-10s %3d %10.2f\n', 'Carbon', 6, 12.0107);
Carbon 6 12.01
> fh := io.open('file.txt', 'w');
> printf(fh, '%-10s %3d %10.2f\n', 'Carbon', 6, 12.0107);
> close(fh);
```

See also: print, io.write, io.writeline, skycrane.scribe, skycrane.tee.

```
protect (f, arg1, ...)
```

Calls function f with the given arguments in protected mode. This means that any error inside f is not propagated; instead, protect simply catches the error. Note that protect does not work with operators.

The function either returns all results from the call in case there have been no errors, or returns the error message as a string as the only return. In case of an error, the error message is set to the global variable lasterror, otherwise lasterror is set to null.
lasterror is useful for checking the results of a call to protect as in the following:

```
if protect(...) = lasterror then ... fi
```

See also: xpcall, try/catch statement.

```
purge (obj [, pos])
purge (obj, a, b)
```

In the first form, the function removes from table, sequence or register obj the element at position pos, shifting down other elements to close the space, if necessary. It returns the value of the removed element. The default value for pos is
n , where n is the length of the table, sequence or register, so that a call purge (obj) removes the last element of obj.

In the second form, removes all elements starting from index a to index b (inclusive), moving excess elements down to close the space; the function automatically performs a garbage collection after shifting. In the $2^{\text {nd }}$ form, nothing will be returned.

Use the delete element from structure statement if you want to remove any occurrence of the table value element from a table or sequence. You might also consider using a linked list, a data structure which supports much faster operations when inserting or deleting elements, see Ilist package in Chapter 10.7.

Note that with tables, the function only works if the table is an array, i.e. if it has positive integral and consecutive keys only. With registers, the top pointer is reduced by the number of elements removed.

See also: move, prepend, put, Ilist.purge, ulist.purge.

```
put (obj, [pos,] value)
```

Inserts element value at position pos in table, sequence or register obj, shifting up other elements to open space, if necessary. The default value for pos is $n+1$, where n is the current length of the structure, so that a call put (obj, value) inserts value at the end of obj.

Use the insert element into structure statement if you want to add an element at the current end of a structure, for it is much faster. You might also consider using a linked list, a data structure which supports much faster operations when inserting or deleting elements, see llist package in Chapter 10.7.

The function returns the modified structure.
See also: prepend, purge, Ilist.put, ulist.put.

## qsumup (obj)

Raises all numeric values in table, sequence or register obj to the power of 2 and sums up these powers, using a precision-saving method. The return is a number. If obj is empty or consists entirely of non-numbers, the operator returns fail. If the structure contains numbers and other objects, only the powers of the numbers are added. Numeric entries with non-numeric keys are processed, as well.

The operator uses a combination of fused multiply-add and Kahan-Babuška Summation. To improve accuracy, you may sort obj before.

See also: qmdev, sumup, sort, sorted.
rawequal (obj1, obj2)
Checks whether obj1 is equal to obj2, without invoking any metamethod. Returns a Boolean.
rawget (obj, index)
Gets the real value of obj[index], without invoking any metamethod, obj must be a table, set, sequence or pair; index may be any value.

See also: getentry, rawset.

```
rawset (obj, index, value)
```

rawset (obj, value)

In the first form, sets the real value of obj[index] to value, without invoking any metamethod. obj must be a table, set, register, sequence or pair, index any value different from null, and value any value. To delete a value from any structure, pass null for value.

In the second form, the function inserts value into the next free position in the given structure obj. obj can be a table, set, sequence or register.

This function returns obj.

See also: rawget.
read (filename)
Reads an object stored in the binary file denoted by file name filename and returns it. The function is written in Agena and included in the lib/library.agn file.

See also: save.
readlib (packagename [, packagename2, ...] [, true])
Loads and runs packages stored to agn text files (with filename packagename.agn) or binary C libraries (packagename.SO in UNIX, packagename.dll in Windows), or to both.

If true is given as the last argument, the function prints the search path(s), and also quits and prints some diagnostics if a corrupt $C$ library has been found.

The function first tries to find the libraries in the current working directory, and thereafter in the path in mainlibname. If it fails, it traverses all paths in libname until it finds them. If it finds a library and the current user has at least read permissions for it, it is initialised. On successful initialisation, the name of the package is entered into the package.readlibbed set.

Note that if a package consists both of a C DLL and an Agena text file, they should both be located in the very same folder as readlib does not search for them across multiple paths and may thus initialise a package only partially.

Make sure that on the operating system level the environment variable AGENAPATH has been set, that the individual paths are separated by semicolons and that they do not end in slashes. In UNIX, if AGENAPATH has not been set, readlib by default searches in /usr/agena/lib.

In OS/2 and Windows, the Agena installation programme automatically sets AGENAPATH. If it failed, or you want to modify its contents, you may manually set the variable like in the following examples, assuming that the Agena libraries are located in the $\mathrm{d}:$ \agena $\backslash$ lib folder and optionally in the $\mathrm{d}:$ : agena $\backslash$ mypackage folder.

```
SET AGENAPATH=d:/agena/lib Or
SET AGENAPATH=d:/agena/lib;d:/agena/mypackage
```

In UNIX, you may execute one of the following statements in your shell, assuming that the Agena libraries are located in the /home/usr/agena/lib folder and optionally in the /home/usr/agena/mypackage folder.

```
SET AGENAPATH=/home/usr/agena/lib Or
```

SET AGENAPATH=/home/usr/agena/lib;/home/usr/agena/mypackage
In DOS, you have to set AGENAPATH in the autoexec.bat file:

```
SET AGENAPATH=d:/agena/lib Or
SET AGENAPATH=d:/agena/lib;d:/agena/mypackage
```

Of course, packages may reside in other directories as well. Just enter further paths to libname as you need them.

The function returns true if all the packages have been successfully loaded and executed, or fail if an error occurred.

Hint: the import statement is an interface to readlib (and initialise), but does not require to put the package names into quotes. For example,

```
> readlib('stats');
```

is equivalent to

```
> import stats;
```

See also: run, initialise, import statement.

```
recurse (f, obj [, \cdots.][[, option])
```

Checks each element of the structure obj (a table, set, pair, sequence or register) by applying a function f on each of its elements. f can be a multivariate function and must return either true or false. The optional second and all further arguments of f may be passed as the third, etc. argument.

With tables, all the entries and keys are scanned.
With sequences and registers, only the entries (not the keys) are scanned.
The function performs a recursive descent if it detects tables, sets, pairs, registers or sequences in obj so that it can find elements in deeply nested structures.

If obj is a table and the option skiphash=true has been passed, then the function ignores all non-numeric keys and their corresponding values.

The function immediately returns true if the function call to any element in obj evaluates to true, and false otherwise. If obj is a number, boolean, complex number, string, null, procedure, thread, userdata or lightuserdata, recurse returns fail. It issues an error if obj is unassigned.

See also: descend, has, satisfy.

```
reduce (f, obj [, init [, ... [, option]]])
```

Applies a function f on each item of a structure or string obj and returns an accumulated result.
f must have two or more parameters, but at least parameters x , a , where x will represent the respective item in obj, and a the accumulator to be updated. If init is given, then the accumulator is initialised with it, otherwise the accumulator is set to zero at first.

After traversal of obj, the accumulator will be returned. The function is equivalent to:

```
reduce := proc(f, s, init, ?) is
    local accumulator := init or 0;
    for item in s do
            accumulator := f(item, accumulator, unpack(?))
    od;
    return accumulator
end;
```

For example, reduce ( $\langle<\mathrm{x}, \mathrm{a}->\mathrm{x}+\mathrm{a} \gg,[1,2,3,4]$ ) computes the sum of the numbers in a table, i.e. 10; and reduce (<< x, a $->$ a \& x \& '।' >>, '1234', ' ' ) appends a pipe to each character, i.e. returns '1|2|3|4|'.

You can pass further arguments to the given accumulator function by just passing them as the fourth and following argument(s) to reduce. Example to compute the arithmetic mean of all the numbers in table [10, 20, 30]:

```
> tbl := [10, 20, 30];
> f := << x, a, len -> a + x/len >>
> a := reduce(f, tbl, 0, size tbl):
20
```

for:

```
> a, len := 0, size tbl;
> for x in tbl do
    inc a, x/len
> od;
```

A counter can also be used: it can be accessed within the accumulator function by the name _c when passing the _c = true option - with _c starting from 1. The performance penalty, however, may be quite significant:

```
> tbl := seq(3, 3, 3);
> a := reduce(<< x, a -> a + x * 10^(_c - 1) >>, tbl, 0, _c=true):
333
```

may be up to four time slower than

```
> a := 0;
> for _c from 1 to size tbl do
> inc a, tbl[_c] * 10^(__c - 1)
> od;
```

See also: @ operator, map.

## RELEASE

A global variable that holds a string containing the language name, the current interpreter main version, the subversion, and the patch level. The format of this variable is: 'AGENA >> <version>.<subversion>.<patchlevel>'.

See also: global environment variable environ.release, environ.version.

```
remove (f, obj [, \cdots. [, newarray=true]] [, inplace=true])
```

Returns all values in table, set, sequence or register obj that do not satisfy a condition determined by function $f$, as a new table, set, sequence or register. The type of return is determined by the type of second argument, depending on the type of obj.

If the function has only one argument, then only the function and the table/set/register/sequence are passed to remove.

```
> remove(<< x -> x > 1 >>, [1, 2, 3]):
```

[1]

If the function has more than one argument, then all arguments except the first are passed right after the name of the table or set obj.

```
> remove(<< x, y -> x > y >>, [1, 2, 3], 1): # 1 for y
```

[1]

If present, the function also copies the metatable and user-defined type of obj to the new structure.

Please note that if obj is a table, the return might include holes. If you pass the newarray=true option as the last argument, however, the result will be returned in a table array with consecutive positive integral keys, not preserving the original keys of the respective values determined, and not having holes; for example:

```
> remove(<< x -> x < 2 >>, [1, 2, 3]):
[2 ~ 2, 3 ~ 3]
> remove(<< x -> x < 2 >>, [1, 2, 3], newarray = true):
[2, 3]
```

With a register, all values up to the current top pointer are evaluated, and the size of the returned register is equal to the number of the elements in the return.

If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original structure, but saving memory. After completion, the function returns the modified structure. (You can combine the newarray and inplace options).

See also: cleanse, countitems, map, select, selectremove, subs, unique, zip.

## restart

Restarts an Agena session. No argument is needed.
If a procedure has been assigned to the name environ.onexit, then this procedure is automatically run before re-initialising the interpreter. An example:

```
> environ.onexit := proc() is print('Tschüß !') end
> restart
Tschüß !
```

During start-up, Agena stores all initial values, e.g. assigned package tables, in a global variable called _origG. Tables are copied, too, so their contents cannot be
altered in a session.
When the Agena session is reset, all values in the Agena environment are unassigned including the environment variable _G. The seeds used by math.random/math.randomseed are reset, too.

The system variables _origG, libname, mainlibname environ.onexit, the current working directory are not reset. mainlibname and libname, however, are reset to their original values if you issued the statement environ.kernel(libnamereset = true) before.

Then all entries in _origG are re-read and assigned to the new environment.
After this, the library base file library.agn and thereafter the initialisation file agena.ini or .agenainit - if present - are read and executed. Finally, restart runs a garbage collection.

```
reverse (obj)
```

Reverses the order of all elements in a sequence or register obj in-place. With tables, it reverses the elements in the array part, only. The function returns the modified structure.

## See also: strings.reverse, stack.reversed.

```
right (obj)
```

With the pair obj, the operator returns its right operand. This is equals to obj [2]. See also: left.

```
run (filename)
```

Opens the named file and executes its contents as a chunk. When called without arguments, run executes the contents of the standard input (stdin). Returns all values returned by the chunk. In case of errors, run propagates the error to its caller (that is, run does not run in protected mode).

See also: readlib, with.

```
satisfy (f, x [, \cdots]] [, option])
satisfy (f, obj [, ...] [, option])
```

In the first form, with x a number, complex number, string, boolean, null or userdata, calls the function f which should return true or false. The result is the return of this call. You may also specify optional arguments to $£$.

With obj a structure (second form), checks each element in obj by calling function $f$ which also should return true or false. If at least one element in obj does not satisfy the condition checked by $f$, the result is false, and otherwise true.

The function performs a recursive descent if it detects tables, sets, pairs, registers or sequences in obj so that it can find elements in deeply nested structures. If obj is a table and the option skiphash=true has been passed, then the function ignores all non-numeric keys and their corresponding values.

See also: has, recurse, descend.

## save (obj, filename)

Saves an object obj of any type into a binary file denoted by file name filename.
save returns an error if an object that cannot be stored to a file has been passed: threads, userdata, for example. It also returns an error if the object to be written is self-referencing (e.g._G). If obj contains one and the same structure multiple times, e.g. n times, then save stores it n times.

The function locks the file when writing, avoiding file corruption if another application tries to gain access to it.

Note that save overwrites existing files without warning. Whereas numbers, strings, and Booleans are stored in a portable fashion so that the data can be read both on Big Endian (e.g SPARCs, PPCs) and Little Endian systems, procedures cannot.

The function is written in Agena and included in the lib/library.agn file.
See also: read, io.writefile.

```
select (f, obj [, \cdots. [, newarray=true] [, inplace=true]])
```

Returns all values in table, set, sequence or register obj that satisfy a condition determined by function f . The type of return is determined by the type of the second argument.

If f has only one argument, then only the function and the object are passed to select.

```
> select(<< x -> x > 1 >>, [1, 2, 3]):
[2, 3]
```

If the function has more than one argument, then all arguments except the first are passed right after the name of the object obj.

```
> select(<< x, y -> x > y >>, {1, 2, 3}, 1): # 1 for y
{3, 2}
```

If present, the function also copies the metatable and user-defined type of obj to the new structure.

Please note that if obj is a table, the return might include holes. If you pass the newarray=true option as the last argument, however, the result will be returned in a table array with consecutive positive integral keys, not preserving the original keys of the respective values determined, and not having holes. Thus,

```
> select(<< x -> x :: number >>, ['a', 10, 20, 30, 'z'], newarray=true);
```

returns

```
[10, 20, 30]
```

instead of
$[2 \sim 10,3 \sim 20,4 \sim 30]$
If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original structure, but saving memory. After completion, the function returns the modified structure. (You can combine the newarray and inplace options).

With a register, all values up to the current top pointer are evaluated, and the size of the returned register is equal to the number of the elements in the return.

See also: cleanse, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

```
selectremove (f, obj [, \cdots. [, newarray=true]])
```

Combines the functionality of select with the one of remove: The first result contains all the elements of a structure obj (a table, set, sequence or register) that satisfy a given condition, the second result contains the elements of a structure not satisfying the condition. This may speed up computations where you need both results, maybe for post-processing, by around 33 \%.

If obj is a table, the return might include holes. If you pass the newarray=true option as the last argument, however, the result will be returned in table arrays with consecutive positive integral keys, not preserving the original keys of the respective values determined, and not having holes. Examples,

```
> a := ['a', 10, 20, 30, 'z'];
> selectremove(<< x -> x :: number >>, a):
[2 ~ 10, 3 ~ 20, 4 ~ 30] [1 ~ a, 5 ~ z];
> selectremove(<< x -> x :: number >>, a, newarray=true):
[10, 20, 30] [a, z]
```

See also: remove, select.
setbit (x, pos, bit)
Sets or unsets a bit in an integer x at the given bit position pos.
Internally, x is first converted into its binary representation. Then bit is set to the pos-th position from the right of this binary representation of x. bit may be either true or false, or the numbers 0 or 1 . E.g. if x is $2=0 \mathrm{bOO10}$, pos is 1 , and bit is true, then the result is $3=0 \mathrm{bOO} 1$.
pos should be an integer in the range $\mid$ pos $\mid \in[1$.. 32].
See also: getbit, getbits, setbits, setnbits, numarray.setbit.

```
setbits (x, r)
```

Sets or unsets all 32 bits of an integer x with the bits given in register r . The register must contain a minimum of one, and a maximum of 32 values, either the Booleans true or false, or the integers 0 and 1 . If the register contains less than 32 elements, and has length $n$, the first $32-\mathrm{n}$ bits 'to the left' are not set. Example:

```
> setbits(8, reg(1, 0, 0)):
12
```

See also: getbit, getbits, setbit, setnbits, numarray.setbit.

## setmetatable (obj, metatable)

Sets the metatable for the given table, set, sequence, or pair obj. (You cannot change the metatable of other types from Agena, only from C.) If metatable is null, removes the metatable of the given table. If the original metatable has a '_metatable' field, raises an error.

This function returns obj.
See also: getmetatable.
setnbits (x, y [, pos [, nbits [, 'or']]])
Sets nbits bits in 32-bit integer y into position pos of 32-bit integer $x$, and returns the modified value of $x$. pos and nbits should be in [1,32]. If pos is not given, it is 1 by default (the right-most bit in x).

If nbits is not given, it is math.mostsigbit(y) by default.

By default, the bits in $x$ are overwritten by the bits in $y$. If the fifth argument ' or ' (the string) is given, the bits are Boolean-OR'ed.

See also: getbit, getbits, getnbits, setbit, setbits.

```
settype (obj [, \cdots.], str)
settype (obj [, \cdots]], null)
```

In the first form the function sets the type of one or more procedures, sequences, tables, sets, pairs, or userdata obj to the name denoted by string str. gettype and typeof will then return this string when called with obj.

In the second form, by passing the null constant, the user-defined type is deleted, and gettype thus will return null whereas typeof will return the basic type of obj.

If obj has no __tostring metamethod, then Agena's pretty printer outputs the object in the form str \& ' (' \& <elements> \& ')' instead of the standard 'seq(' \& <elements> \& ')' Or '<element>:<element>' string.

If given just two arguments, i.e. an object and a string or an object and null, the function returns the modified object. In all other cases, the function returns null.

See also: gettype.
shift (obj, a, b)
Moves an element in table, sequence or register obj from position old to new, with old, new integers, shifting all the other elements accordingly - which might also cause a rotation. The function returns nothing.

See also: move, purge, swap.

```
size (obj)
```

With tables, the operator returns the number of key~value pairs in table obj.
With sets, pairs, and sequences, the operator returns the number of items in obj.
With registers, the operator returns the number of elements up to the current top pointer, but not the total number of elements in the registers.

With strings, the operator returns the number of characters in string obj, i.e. the length of obj.

See also: environ.attrib, strings.strlen, strings.utf8size, tables.getsize.

```
sort (obj [l [, u]] [, f])
```

Sorts table, sequence or register elements in a given order, in-place, from obj [1] to obj $^{[u]}$, where by default 1 is 1 and $u$ is the length of the structure. If $f$ is given, then it must be a function that receives two structure elements, and returns true when
the first is less than the second (so that not $\mathrm{f}(\mathrm{obj}[\mathrm{i}+1]$, obj[i]) will be true after the sort). If f is not given, then the standard operator < (less than) is used instead.

The sort algorithm is not stable; that is, elements considered equal by the given order may have their relative positions changed by the sort. Also, the function cannot sort structures featuring values of different types (see skycrane.sorted for an alternative). The return is the sorted structure.

See also: sorted, stats.issorted, skycrane.sorted, stats.sorted.
Example:

```
> s := [1, 2, 3]
> sort(s, << x, y -> x > y >>):
[3, 2, 1]
> s := seq(1:'a', 1.1:'b', 1.2:'c');
> sort(s, << x, y -> left(x) > left(y) >>):
seq(1.2:c, 1.1:b, 1:a)
sorted (obj [l [, u]] [, f])
```

Sorts table, sequence or register elements in obj in a given order from obj[1] to obj [u] , but - unlike sort - not in-place, and non-destructively. By default, 1 is 1 and $u$ is the length of the structure. Depending on the type of obj, the return is a new table or sequence.

If f is given, then it must be a function that receives two structure elements to determine the sorting order. See sort for further information.

The function cannot sort structures featuring values of different types (see skycrane.sorted for an alternative).

See also: sort, skycrane.sorted, stats.issorted, stats.sorted.

```
subs (x:v [, \cdots.], obj [, true])
```

Substitutes all occurrences of the value x in the table, set, sequence or register obj with the value v . More than one substitution pair can be given. The substitutions are performed sequentially and by default simultaneously starting with the first pair. The type of return is determined by the type of obj.

```
> subs(1:3, 2:4, [1, 2, -1]):
[3, 4, -1]
```

If present, the function also copies the metatable and user-defined type of obj to the new structure.

If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original structure, but saving memory. After completion, the function returns the modified structure.

By default, subs is still replacing the elements in a structure with _all_ the replacements given, including intermediate substitutions. So if we have an expression like

```
> subs(1:2, 2:3, 3:4, [1, 2, 3])
```

we will get:

```
[4, 4, 4]
```

By passing the multipass=false option, the rest of the replacement list will be skipped as soon as a substitution has been done:

```
> subs(1:2, 2:3, 3:4, [1, 2, 3], multipass=false):
[2, 3, 4]
```

You can check numbers for approximate instead of strict equality by passing the new strict=false option.

See also: countitems, map, remove, select, zip.

## sumup (obj)

Sums up all numeric values in table, sequence or register obj. The return is a number. If obj is empty or consists entirely of non-numbers, the operator returns fail. If the structure contains numbers and other objects, only the numbers are added. Numeric entries with non-numeric keys are processed, as well. The operator uses Kahan-Babuška Summation. To improve accuracy, you may sort obj before.

See also: mulup, qsumup, calc.fsum, stats.cumsum, stats.sumdata, sort, sorted.

```
swap (obj, a, b)
```

Swaps the table array, sequence or register obj entries at index positions a and b, with $a, b$ integers. The function returns nothing.

See also: move, purge, shift.

## time ()

Returns UTC time in seconds elapsed since the epoch in seconds as a number. The fractional part of the return represents milliseconds. The epoch usually is January 01 , 1970, but this may vary between platforms.

## See also: os.clock, os.difftime, os.time, watch, skycrane.stopwatch.

```
times (f, x, n [, \cdots.])
times (f, x, infinity, eps [, ...])
```

In the first form, the function takes a start value x of any type, applies function f to it and repeatedly applies f to its previous result $\mathrm{n}-1$ times. n should be a positive integer. It returns the result of the last call to f . The second and further arguments of f must be put right after $n$.

If n is less than 1 , the function returns null.

Example:

```
> times(<< x -> 1 + recip x >>, 1, 33) -> 1.6180339887499 # Golden ratio
> f := << x -> times(<< n -> 0.5*(n + x/n) >>, 1, 20) >> # square root
```

You can bail out of the loop prematurely by including a Boolean condition in the function definition. As soon as the expression evaluates to false, the iteration will stop and the previous interim result will be returned, e.g.:

```
> times( << x -> x < 10 and x + 1 >>, 1, 33):
1 0
```

If times should bail out in the first iteration then false, i.e. the result of the function call, will be returned:

```
> times( << x -> x < 0 and x + 1 >>, 1, 33):
false
```

In the second form, takes a start value $x$ of any type, applies function f to it and repeatedly applies f to its previous result until the absolute difference of the last two function calls reaches or drops below the numeric threshold eps, a non-negative value.

If a function call evaluates to $\pm$ infinity or undefined, the operator also quits, returning infinity or undefined, respectively.

The third argument infinity just signals that the user wants to use this mode. If f is multivariate, all arguments but the first are passed right after eps.

Example: Solve the equation $7^{3}+2 x-5=0$ using Newton's method.

```
> import calc
> s := << x -> 7*x^3 + 2*x - 5 >>
> times(<< x -> x - s(x)/calc.eulerdiff(s, x) >>, 4, infinity, DoubleEps):
0.78792505251729
```

```
> s(ans):
```

0

See also: @ operator, map, calc.aitken.

```
top (obj)
```

With the table array, sequence or register obj, the operator returns the element with the largest index. If obj is empty, it returns null.

See also: bottom.

## toreg (obj)

If obj is a string, the function will split it into its characters and return them in a register with each character in obj as a register value, and in the same order as the characters in obj.

If obj is a table, the function puts all its values - but not its keys - into a register.
If obj is a set, the function puts all its items into a register. The same applies to sequences.

If obj contains structures, then only their references are copied. Map copy to structures if you want to create independent copies of them.

In all other cases, the function issues an error.
See also: toseq, toset, totable.
toseq (obj)
If obj is a string, the function will split it into its characters and return them in a sequence with each character in obj as a sequence value, and in the same order as the characters in obj.

If obj is a table, the function puts all its values - but not its keys - into a sequence.
If obj is a set, the function puts all its items into a sequence. The same applies to registers.

If obj contains structures, then only their references are copied. Map copy to structures if you want to create independent copies of them.

In all other cases, the function issues an error.
See also: toreg, toset, totable.

## toset (obj)

If obj is a string, the function will split it into its characters and returns them in a set. Note that there is no order in the resulting set.

If obj is a table, sequence or register, the function puts all its values - but not its keys - into a new set.

If obj contains structures, then only their references are copied. Map copy to structures if you want to create independent copies of them.

In all other cases, the function issues an error.
See also: toreg, toseq, totable.

```
totable (obj)
```

If obj is a string, the function splits it into its characters, and returns them in a table with each character in obj as a table value in the same order as the characters in obj.

If obj is a sequence, register, or set, the function converts it into a table.
If obj contains structures, then only their references are copied. Map copy to structures if you want to create independent copies of them.

In all other cases, the function issues an error.
See also: toreg, toseq, toset.

## type (obj)

This operator returns the basic type of its only argument obj, coded as a string. The possible results of this function are 'null' (the string, not the value null), 'number', 'string', 'boolean', 'table', 'set', 'sequence', 'register', 'pair', 'complex', 'procedure', 'thread','lightuserdata', and 'userdata'.

If obj is a table, set, sequence, pair, or procedure with a user-defined type, then type always returns the basic type, e.g. 'sequence ' or 'procedure'.

See also: :: and :- operators, checkłype, gettype, typeof.

```
typeof (obj)
```

This operator returns the user-defined type - if it exists - of its only argument obj, coded as a string.

A self-declared type can be defined for procedures, tables, pairs, sets, and sequences with the settype function. If there is no user-defined type for obj, then the basic type will be returned, i.e. ' null' (the string, not the value null), ' number',

```
'string', 'boolean', 'table', 'set', 'register', 'sequence', 'pair',
```

'complex', 'procedure', 'thread', and 'userdata'.

See also: :: and :- operators, type, gettype.

## unassigned (obj)

This Boolean operator checks whether an expression obj evaluates to null. If obj is a constant, i.e. a number, boolean including fail, or a string, the operator always returns false.

See also: assigned.
unique (obj)
With a table obj, the function removes all holes ('missing keys`) and removes multiple occurrences of the same value in the array part, if present. The hash part of a table is considered to be always unique by definition, so it just copies it to the result. The return is a new table with the original table unchanged.

With a sequence or register obj, the unique function removes multiple occurrences of the same value, if present. The return is a new sequence or register with the original structure unchanged.

See also: tables.entries.
unpack (obj, [, i [, j]])
Returns the elements from the given table, sequence or register obj. This function is equivalent to

```
return obj[i], obj[i+1], \cdots., obj[j]
```

except that the above code can be written only for a fixed number of elements. By default, $i$ is 1 and $j$ is the length of the object, as defined by the size operator.

Please note that if you put a call to unpack into an expression list, only the first return of unpack is propagated if the call to unpack is not at the final position of the expression list, for example:

```
> s := [unpack([1, 2, 3]), 4, 5]: # 2 and 3 are discarded
[1, 4, 5]
> s := [-1, 0, unpack([1, 2, 3])]: # 2 and 3 are included
[-1, 0, 1, 2, 3]
```

Consider copyadd in this situation. See also: identity, ops, values.
values (obj, $i_{1}\left[, i_{2}, \cdots\right]$ )
Returns the elements $i_{k}$ from the given table, sequence or register obj. This function is equivalent to - for example -

```
return [ i i ~ obj[i_1], i i ~ obj[i\mp@subsup{i}{2}{}], ... ] Or
return seq( obj[i_i], obj[i\mp@subsup{i}{2}{}], \cdots. )
```

The type of return is determined by the first argument obj.
See also: columns, ops, select, unpack.

## watch ([option])

The function implements a stop watch. With the first call, the function starts counting and returns 0 . The second call returns the elapsed time in seconds and milliseconds and restarts the clock. If any argument is given, then the clock is reset, but it does not start counting.

See also: time, os.time, skycrane.stopwatch.

```
whereis (obj, x)
```

Returns the indices for a given value x in table, sequence or register obj as a new table, sequence or register, respectively, dependent on the type of obj.

See also: tables.entries, tables.indices.
write ([fh,] $\mathrm{v}_{1}\left[, \mathrm{v}_{2}, \cdots\right]$ [, delim $=$ <str>])
This function prints one or more numbers, Booleans or strings $\mathrm{v}_{\mathrm{k}}$ to the file denoted by the handle fh , or to stdout (i.e. the console) if fh is not given.

By default, no character is inserted between neighbouring values. This may be changed by passing the option 'delim':<str> (e.g. 'delim':'|' or delim='|') as the last argument to the function with <str> being a string of any length. Remember that in the function call, a shortcut to 'delim': <str> is delim = <str>.

The function is an interface to io.write.
See also: printf, skycrane.scribe, skycrane.tee.

```
writeline ([fh,] v [ [, vi, \cdots.] [, delim = <str>])
```

This function prints one or more numbers, booleans or strings $\mathrm{v}_{\mathrm{k}}$ followed by a newline to the file denoted by the handle $f$, or to stdout (i.e. the console) if $f$ f is not given.

By default, no character is inserted between neighbouring values. This may be changed by passing the option 'delim':<str> (i.e. a pair, e.g. 'delim':'।') as the last argument to the function with <str> being a string of any length. Remember that in the function call, a shortcut to 'delim': <str> is delim = <str>.

The function is an interface to io. writeline.
See also: printf, skycrane.scribe, skycrane.tee.
xpcall (f, err [, arg1, ‥])
This function is similar to protect, except that you can set a new error handler.
xpcall calls function f in protected mode, using err as the error handler. Arguments to f are optional. Any error inside f is not propagated; instead, xpcall catches the error, calls the err function with the original error object, and returns a status code. Its first result is the status code (a Boolean), which is true if the call succeeds without errors. In this case, xpcall also returns all results from the call, after this first result. In case of any error, xpcall returns false plus the result from err.

See also: protect.

```
zip (f, obj1, obj2 [, \cdots.])
```

zip (op, obj1, obj2)

In the first form, the function zips together either two sequences, two registers, or two tables obj1, obj2 by applying the function f to each of its respective elements. Depending on the type of obj1, obj2, the result is a new sequence, register, or table $s$ where each element $s[k]$ is determined by $s[k]:=\mathrm{f}\left(\mathrm{obj}_{1}[\mathrm{k}]\right.$, obj2 $\left.2[\mathrm{k}]\right)$.
obj1 and obj2 must have the same number of elements. If you pass tables, they must have the same keys.

If f has more than two arguments, then its third to last argument must be given right after B .

In the second form, op depicts an arithmetic operator, represented as a string, that zips together the structure elements:

- '+': addition,
- '-' : subctraction,
- '*': multiplication,
- '/': division,
- ' <br> ' : integer division,
- '\%': modulus,
- '^': exponentiation,
- '**': integer exponentiation.

This method is twice as fast with sequences and registers, and $50 \%$ faster with tables.

If obj1 or obj2 have user-defined types or metatables, they are copied to the resulting structure, as well. If obj1 has a metatable, then this metatable is copied, else the metatable of obj2 is used if the latter exists. The same applies to user-defined types.

See also: map, remove, select, subs.

## Chapter Nine

## Strings

## 9 Strings

### 9.1 Basic String Functions

Summary of Functions:

## Search

atendof, has, in, notin, instr, strings.find, strings.glob, strings.match, strings.mfind.

## Insertion, Substitution, and Deletion

replace, strings.appendmissing, strings.chomp, strings.chop, strings.gsub, strings.include, strings.remove, strings.wrap, strings.wrapmissing.

## Extraction

split, strings.advance, strings.between, strings.charset, strings.fields, strings.gmatch, strings.gmatches, strings.gseparate, strings.separate, strings.splitfields, strings.strchr, strings.strrchr, strings.strstr.

## Queries

abs, empty, filled, strings.charmap, strings.compare, strings.contains, strings.diffs, strings.dleven, strings.fuzzy, strings.isaligned, strings.isalpha, strings.isalphanumeric, strings.isalphaspace, string.isalphaspec, strings.isascii, strings.isblank, strings.iscenumeric, strings.iscontrol, strings.isdia, strings.isending, strings.isfloat, strings.isgraph, strings.ishex, strings.islatin, strings.isisoalpha, strings.isisolower, strings.isisoprint, strings.isisospace, strings.isisoupper, strings.islatinnumeric, strings.isloweralpha, strings.islowerlatin, strings.ismagic, strings.isnumber, strings.isnumeric, strings.isnumberspace, strings.isprintable, strings.isspace, strings.isspec, strings.isstarting, strings.isupperalpha, strings.isupperlatin,strings.isutf8, strings.iswrapped, strings.shannon, strings.stremp, strings.strverscmp.

## Counting

size, strings.hits, strings.strlen, strings.utf8size, strings.words.

## Formatting

lower, trim, upper, strings.align, strings.capitalise, strings.format, strings.isolower, strings.isoupper, strings.ljustify, strings.Itrim, strings.Itrim, strings.rjustify, strings.trim, strings.tolower, strings.toupper, strings.uncapitalise.

Conversion
\&, join, tonumber, tostring, strings.a64, strings.diamap, strings.iterate, strings.pack, strings.packsize, strings.reverse, strings.tolatin, strings.toutf8, strings.transform, strings.unpack.

## Manipulation

@, map, strings.iterate, strings.repeat, strings.rotateleft, strings.rotateright, strings.tobytes, strings.tochars.

## Miscellaneous

strings.random.

A note in advance: All operators and strings package functions know how to handle many diacritics properly. Thus, the lower and upper operators know how to convert these diacritics, and various is* functions recognise diacritics as alphabetic characters.

Diacritics in this context are the letters:

| â | A | ä | Ä | à | À | á | Á | a | £ | æ | $\ldots$ | a |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ê | E | ë | è | E | é | É | Ë |  |  |  |  |  |
| İ | $\ddot{\text { İ }}$ | 1 | $\hat{\text { I }}$ | i | İ | í | İ | ý | Ý | Y |  |  |
| ô | ô | ö | Ö | ò | ò | $\varnothing$ | $\varnothing$ | ó | ó | ธ | O |  |
| û | Û | ù | Ù | ü | Ü | ú | Ú |  |  |  |  |  |
| ¢ | Ç | n | $\tilde{N}$ | б | Đ | b | E | B |  |  |  |  |

### 9.1.1 Operators and Functions

$s 1 \underset{\sim}{\&}$ s2
This binary operator concatenates two strings s1, s2 and returns a new string. s1 or s2 may also be a number or a Boolean; in this case the argument will be converted to a string and then concatenated with the other operand.

See also: join.
v \&:= s
The compound concatenation operator appends string s to the contents of the string variable v . It is equivalent to: $\mathrm{v}:=\mathrm{v} \& \mathrm{~s}$.

```
s1 atendof s2
```

This binary operator checks whether string s2 ends in a substring s1. If true, the position of the position of $s 1$ in s2 will be returned; otherwise null will be returned. The operator also returns null if the strings have the same length or at least one of them is the empty string.

See also: in, instr, strings.isstarting, strings.isending.
s1 in s2
This binary operator checks whether string s2 includes s1 and returns its position as a number, or null if s1 cannot be found. The operator also returns null if at least one of the strings is the empty string.

See also: atendof, instr, notin, strings.contains, strings.isstarting, strings.isending.

```
s1 notin s2
```

This binary operator checks whether string s2 does not include s1 and returns true or false.

See also: in operator.

```
s1 split s2
```

Splits the string s1 into words. The delimiter is given by string s2, which may consist of one or more characters. The return of the operator is a sequence. If s1= s2, or if s2 is the empty string, then an empty sequence will be returned.

See also: strings.fields, strings.iterate, strings.separate.

## abs (s)

With strings, the operator returns the numeric ASCll value of the given character s (a string of length 1).

## empty (s)

The operator checks whether the string s is empty. The return is true or false. See also: filled.

```
filled (s)
```

The operator checks whether the string s is non-empty. The return is true or false. See also: empty.
has (s, chars)
Checks whether at least one character in s matches one of the characters in chars, a string representing a set of individual characters.

See also: in operator, strings.contains.

```
instr (s, pattern [, init] [, plain] [, 'reverse'] [, 'borders'])
```

Looks for the first match of string pattern in the string s. If it finds a match, then instr returns the index of $s$ where this occurrence starts; otherwise, it returns null.

If pattern is a set of pattern strings, returns true if at least one of the patterns matches s; otherwise returns false.

If the option 'reverse' is given, then the search starts from the right end and always runs to its left beginning and the first occurrence of pattern with respect to the beginning of $s$ will be returned. In the reverse search, pattern matching is not supported.

An optional numerical argument init passed anywhere after the second argument specifies where to start the search; its default value is 1 and may be negative. In the latter case, the search is started from the । init|'s position from the right end of s.

The function by default supports pattern matching, almost similar to regular expressions, see Chapter 9.1.3. instr is $45 \%$ faster than strings.find. If the optional Boolean argument plain is set to the Boolean true, pattern matching is switched off and a much faster plain search is conducted instead (speed bonus around $40 \%$ ).

The optional argument 'borders' returns the start and the end position of a match in a pair. However, this mode is slow, use strings.find instead which is twice as fast.

See also: atendof, in, strings.isstarting, strings.isending, strings.find.
join (obj [, sep [, i [, j]]])
Concatenates all string values in the table, sequence or register obj in sequential order and returns a string: obj[i] \& sep \& obj[i+1] $\cdots$ \& sep \& obj[j]. The default value for sep is the empty string, the default for $i$ is 1 , and the default for $j$ is the length of the sequence. The function issues an error if obj contains non-strings.

See also: \& operator.

## lower (s)

The operator receives a string and returns a copy of this string with all uppercase letters ('A' to 'Z' plus the above mentioned diacritics) changed to lowercase ('a' to 'z' and the diacritics listed at the end of Chapter 9.1). The operator leaves all other characters unchanged. Example:

```
> lower('Elektronika MK-61'):
elektronika mk-61
```

See also: strings.isolower, strings.tolower, upper.

```
map (f, s [, \cdots.] [, true])
```

This function maps a function f to all characters of string s from the left to right. The return is a sequence of function values.

If function f has only one argument, then only the function and the string s must be passed to map. If the function has more than one argument, then all arguments except the first are passed right after argument s. If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original structure, but saving memory. After completion, the function returns the modified structure.

```
replace (s1, s2, s3)
replace (s1, obj)
replace (s1, pos, s2)
```

In the first form, the function replaces all occurrences of string s2 in string s1 by string s3.

In the second form, the function receives a string si and a table, sequence or register obj of one or more string pairs of the form s2:s3 and replaces all occurrences of s2 in string s1 with the corresponding string s3. Thus you can replace multiple patterns simultaneously with only one call to replace.

In the third form, the function inserts a new string s2 into the string s1 at the given position pos, substituting the respective character in s1 with the new string s2 which may consist of zero, one or more characters. The return is a new string. If s2 is the empty string, the character in s1 is deleted. The return is always a new string.

The function does not support pattern matching, use strings.gsub instead.
See also: utils.singlesubs.

## size (s)

With a string s, the operator returns its length, i.e. the number of characters in s.

```
tonumber (e [, base])
```

Tries to convert its argument to a number or complex value. If the argument is already a number, complex value, or a string convertible to a number or complex value, then tonumber returns this value; otherwise, it returns e if e is a string, and fail otherwise. The function recognises the strings 'undefined' and 'infinity' properly, i.e. it converts them to the corresponding numeric values undefined and infinity, respectively.

An optional argument specifies the base to interpret the numeral. The base may be any integer between 2 and 36, inclusive. In bases above 10, the letter ' $A$ ' (in either upper or lower case) represents 10, 'B' represents 11, and so forth, with 'Z' representing 35. In base 10 (the default), the number may have a decimal part, as well as an optional exponent part. In other bases, only unsigned integers are accepted. If an option is passed, 'undefined' and 'infinity' are not converted to numbers; and if e could not be converted, fail will be returned.

## tostring (e [, anyoption])

Receives an argument e of any type and converts it to a string in a reasonable format. For complete control of how numbers are converted, use strings.format.

If the metatable of e has $a$ '_tostring' field, then the tostring function calls the corresponding value with e as argument, and uses the result of the call as its result. With numbers, the number of digits in the resulting string is dependent on the kernel/digits setting. See environ.kernel for further information.

If e is a complex number, its real and imaginary parts are returned as two strings. If any option is given, the return is one string of the format $\pm$ "re+im*l" or $\pm$ "re-im*|", depending on the sign of the imaginary part of e.

See also: tostringx.

## tostringx (e)

Works like tostring but also formats structures, userdata and complex numbers the same way as the prettyprinter does, or in other words: it returns the argument as a string formatted the same way as the print function outputs it on screen. This is useful if you want to write structures or complex numbers to a file.
trim (s)
Returns a new string with all leading, trailing and excess embedded white spaces removed. trim is an operator. See also: strings.Itrim, strings.IItrim, strings.ıtrim.

## upper (s)

The operator receives a string and returns a copy of this string with all lowercase letters ('a' to 'z' plus the above mentioned diacritics) changed to uppercase ('A' to 'Z' and the diacritics listed at the end of Chapter 9.1). The operator leaves all other characters unchanged. Example:

```
> upper('Elektronika MK-61'):
ELEKTRONIKA MK-61
```

See also: lower, strings.capitalise, strings.isoupper, strings.toupper.

### 9.1.2 The strings Library

The strings library provides generic functions for string manipulation, such as finding and extracting substrings, and pattern matching. When indexing a string in Agena, the first character is at position 1 (not at 0 , as in C). Indices are allowed to be negative and are interpreted as indexing backwards, from the end of the string. Thus, the last character is at position -1 , and so on.

The strings library provides all its functions inside the table strings.

```
strings.a64 (x)
```

The function converts between 32-bit long integers and little-endian base-64 ASCII strings (of length 0 to 6 ).

If the argument x is a base-64 ASCll string, the result is a signed 32-bit integer; if the argument x is a number, the result is the base-64 ASCll string, which consists of the characters:
./0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZabcdefghijklmnopqrstuvwxyz

```
strings.advance (s, p [, option])
strings.advance (s, pos)
```

In the first form, the function moves to substring p in string s and returns p up to the end of $s$. If $p$ could not be found, the function returns null. The function supports pattern matching. If the optional third argument true is given, the function returns the rest of $s$ following but not including $p$. In this case, if $s$ ends with $p$, null will be returned.

In the second form, the substring starting at position pos (a positive integer) up to the end of $s$ will be returned. If pos is greater than the length of $s$, the result is null.

See also: strings.find.

```
strings.align (s [, n])
```

Inserts newlines into a string s after each $n$ character. By default $n$ is 79, so a newline is inserted at position 80, 160, and so forth. The return is a string. The function helps with correctly outputting formatted text at the console.

```
strings.appendmissing (s, t)
```

Appends suffix $t$ (a string) to $s$ (a string) if $t$ is not already at its end; otherwise returns $s$. If $s$ is the empty string, $t$ will be returned.

```
strings.between (s, p, q [, true])
```

Returns the substring in string s that is nested between the prefix string p and the suffix string q. p or q may reside within the string. If the Boolean value true is given as a fourth argument, the function tries to return the substring found as a number. If nothing could be found, the function returns null.

## See also: strings.chomp, strings.include.

```
strings.capitalise (s)
```

Converts the first character in string s to upper case - if possible - and returns the capitalised string. If $s$ is the empty string, it is simply returned. It also converts ligatures if the Western European character set is being used.

See also: upper, strings.uncapitalise.
strings.charmap ()
Queries the internal tables to classify characters. Returns a table of key~value pairs:

| Key | Sequence of | Used by/Comment |
| :--- | :--- | :--- |
| alpha | alphabetical letters | strings.alpha, strings.isalphanumeric, strings. <br> isalphaspace, strings.isalphaspec |
| ascii | table of all ASCll <br> characters | result may vary across platforms and <br> codepages |
| upper | upper-case letters | strings.isupperalpha |
| lower | lower-case letters | strings.isloweralpha |
| vowel | vowels | strings.isvowel |
| dia | diacritics | strings.isalpha, strings.isalphanumeric, <br> strings.isalphaspace, strings.isalphaspec, <br> strings.isdia |
| digits | digits 0 to 9 | strings.isalphanumeric |
| hex | hexadecimals | strings.ishex |
| punct | punctuations | strings.isspec, strings.isalphaspec |


| Key | Sequence of | Used by/Comment |
| :--- | :--- | :--- |
| control | control characters <br> such as $\mathrm{ln}, \backslash \mathrm{r}, \backslash \mathrm{b}$ | strings. iscontrol |
| blank | white space, tab | strings.isblank |
| printable | printable <br> characters | strings.isprintable |

## strings.charset (s)

Returns a set of all the unique characters included in a string.
See also: has, strings.contains.
strings.chomp (s, t [, ..] $)$
Removes pattern string $t$ from the end of string $s$ if it is there, and returns the shortened string s; otherwise returns s unchanged. If more than one pattern is given, each additional pattern will be removed from the previous result.

The function supports pattern matching. In this case you or may not terminate the pattern with one final '\$'.

Example:

```
> strings.chomp('agena language', '(%a+)', 'ena '):
ag
```

See also: strings.chop.

```
strings.chop (s)
strings.chop (s, f)
```

In the first form, removes the last character from string s and returns the shortened string. If $s$ is empty, it is simply returned.

In the second form, if a function f returning true or false is given, chop checks each character in the string from the right to the left for the given Boolean condition and returns the string from its beginning up to and including the character that no longer satisfies the condition.

## Example:

```
> strings.chop('path/file.name', << x -> x <> '/' >>):
path/
```

```
strings.compare (s1, s2)
```

When called with no option, returns the first position - an integer - where the two strings s1 and s2 differ, or 0 if both strings are equal.

## See also: strings.strcmp, strings.strverscmp.

```
strings.contains (s, t)
```

Checks whether all characters in string s are part of the characters in string $t$, and returns true or false.

See also: has, in operator, strings.charset.

```
strings.cut (s, d)
```

The function takes a string s to be split into two pieces, and a string a of one or more single-character delimiters, and returns two values: the first part of s up to but not including - the delimiter found, and the rest of s also without the delimiter.

If a string cannot be split apart, it will be returned as the first result and the second return is null.

See also: split, strings.separate.
strings.diffs (s, t [, n [, option]])
Counts the differences between the two strings $s$ and t : substitutions, transpositions, deletions, and insertions.

By default, both strings must contains at least $n=3$ characters. You may change this by passing any other positive number for $n$. The function returns fail if at least one of the strings consists of less characters.

If any fourth argument is given, the return is a sequence of strings describing the respective difference found, otherwise the returns is the number of the differences encountered.

The function is at least thrice as fast as strings.dleven, but may count differently in odd situations.

See also: strings.dleven, strings.fuzzy, skycrane.tolerance.

```
strings.dleven (s, t)
```

Returns the Damerau-Levenshtein distance between two strings s and $t$. It is a count of the minimum number of insertions, deletions, substitutions of a single character, or transpositions of two neighbouring characters to convert $s$ into $t$. The return is a number. If at least one of the strings is empty, undefined will be returned.

See also: strings.fuzzy, strings.diffs, skycrane.tolerance.

```
strings.diamap (s [, option])
```

The function corrects problems in the Solaris, Linux, OS/2, Windows, and DOS consoles running code page 850 with diacritics and ligatures read in from the keyboard or a text file by mapping them to code page 1252. It takes a strings s, applies the mapping, and returns a new string. All other characters are returned unchanged.

If any option is given, the function transforms a string from code page 1252 to 850 . Example:

```
> strings.diamap('AEIOU-Í_ã+\ddot{I}'):
AEIOUÄÖÜÆÅ\varnothing
```

Note that the function does not convert all existing special tokens.
Agena is shipped with substitution tables for code page 1252. If you want to use another code page, edit the _c2f and _f2c tables in the lib/library.agn file accordingly.

## See also: os.codepage.

```
strings.dump (f [, strip])
```

Returns a string containing a binary representation of the given function $f$, so that a later loadstring on this string returns a copy of the function. f must be an Agena function without upvalues, remember table or internal store table.

If strip is a true value, the binary representation may not include all debug information about the function, to save space.

The function can also be used to binarily serialise data by defining a function returning data, e.g.:

```
> f := proc() is return [1, 2, 3] end;
> s := strings.dump(f);
> loadstring(s)():
[1, 2, 3]
```


## See also: strings.tobytes.

```
strings.fields (s, in [, i i, \cdots]] [, delim] [, true])
strings.fields (s, o [, delim] [, true])
```

Extracts the given fields (columns) in string s. In the first form, the field positions $i_{1}, i_{2}$, etc. are non-zero integers. The field positions may be negative, denoting fields counted from the right end of $s$. In the second form, the field positions are given in the sequence o.

An optional string delim may be passed to denote the character or character sequence that separates the individual fields. The default for delim is the white space. If the Boolean value true is given as the last argument, the function tries to convert the fields into numbers.

The return is a sequence of the fields (strings).
See also: strings.iterate, strings.gseparate, split, especially if you want to retrieve all fields in a string.
strings.find (s, pattern [, init [, plain]])
Looks for the first match of string pattern in string s. If it finds a match, then find returns the indices of s where this occurrence starts and ends; otherwise, it returns null. The function does support pattern matching facilities (which you can turn off, see below). If pattern is a table, set, sequence or register of string patterns, then the function checks whether at least one of the patterns matches s and returns the respective result.

A third, optional numerical argument init specifies where to start the search; its default value is 1 and may be negative. A value of true as a fourth, optional argument plain turns off the pattern matching facilities (see Chapter 9.1.3), so the function does a plain ` find substring` operation, with no characters in pattern being considered `magic`. Note that if plain is given, then init must be given as well.

If the pattern has captures, then in a successful match the captured values are also returned, after the two indices.

See also: in, atendof, and instr, strings.mfind.

```
strings.format (formatstring, ...)
```

Returns a formatted version of its variable number of arguments following the description given in its first argument (which must be a string). The format string almost follows the same rules as the ISO C function sprintf. The only differences are that the conversion specifiers ${ }^{*}, I$ and $L$ are not supported and that there are thirteen extra specifiers: $a, A, b, B, h, H, m, n, N, p, P, q, Q, D$, and $F$.

For an overview of all available specifies and examples, see below.
In general a format has the following syntax, where values in square brackets are optional:
\%[flags][width][.precision]
'flags' may be one of the specifiers described below, optionally preceded by:

-     - (minus): left-justify the result,
-     + (plus): print plus sign in front of positive numbers

You can mix - and +.
'width' is the minimum length of the output in characters. 'precision' depicts the minimum number of decimal places to appear, with trailing zeros to be added if necessary.

The following specifiers do not comply to the C standard:
The a specifier formats a string in a form suitable to be safely read back by the Agena interpreter: All double quotes, newlines, embedded zeros, and backslashes in the string are correctly escaped when written, and without trailing zeros in the fractional part when the precision specified in the specifier is greater than the number of significant digits in the argument supplied. The same applies to $Q$ but with single quotes. The a and A specifiers work the same like the $q$ and $Q$ specifiers, respectively, but do not include trailing or leading double quotes. The B specifier prints a string in backquotes. The b specifier prints a Binary value.

For instance, the call

```
> strings.format('%q', 'a string with \"quotes\" and \n new line')
```

will produce the string:

```
"a string with \"quotes\" and \
new line"
```

The h and H specifiers print a floating-point number in a hexadecimal fractional notation with the exponent to base 2 represented in decimal digits. On DOS and OS/2, the h and H specifiers are not available, and in Windows 2000 they do not work.

The p specifier multiplies the given number by 100 and displays it in fixed float (' f ') format, followed by a percent sign. The m specifier prints a monetary amount with thousands separators and the decimal point defined by the current locale, the default is the format string ${ }^{1 \%}$. $2 f^{\prime}$.

The specifier P formats the pointer (returned by lua_topointer). That gives a unique string identifier for structures, userdata, threads, strings, and functions. For other values (numbers, null, booleans), this specifier results in a string representing the pointer NULL.

The n and N specifiers print a number using the decimal point separator of the locale of the operating system (which may differ from the locale in use by Agena), otherwise they work like the f and F specifiers.

The specifiers D and F prevent quarrels with numerical functions that may return non-numbers in case of errors: D formats an integer like the d specifier if the argument is a number, and the C double representation of undefined otherwise if the value is not a number. Likewise, F and N either format a float, or the C double companion piece of undefined (e.g. 1.\#QNANO in Windows) if the value is not a number.

The conversion specifiers $\mathrm{c}, \mathrm{D}, \mathrm{d}, \mathrm{E}, \mathrm{e}, \mathrm{f}, \mathrm{F}, \mathrm{g}, \mathrm{G}, \mathrm{h}, \mathrm{H}, \mathrm{i}, \mathrm{m}, \mathrm{n}, \mathrm{N}, \mathrm{o}, \mathrm{p}, \mathrm{u}, \mathrm{X}$, and x all expect a number as argument, whereas s expects a string, and $a, A, P, q, Q$ and expect anything.

This function does not accept string values containing embedded zeros.
Examples:

```
> strings.format('%+15.9f', 10k*Pi):
+31415.926535898
> strings.format('%15.9f', 3.5):
    3.500000000
> strings.format('%-15.9f', 3.5):
3.500000000
> strings.format('%015.9f', 3.5):
00003.500000000
> strings.format('%15.0f', 3.5):
    4
> strings.format('%15d', 3.5):
    3
> strings.format('%X', 2^16-1):
FFFF
> strings.format('%c', 97):
a
> strings.format('%s', 'agena >>'):
agena >>
> strings.format('%q', 'agena >>'):
"agena >>"
```

```
> strings.format('%d\n%2d\n%02d\n%2.5f\n%+2.5f\n+2.5f\n%s', 1, 1, 1,
    Pi, Pi, -Pi, 'New Horizons'):
1
01
3.14159
+3.14159
-3.14159
New Horizons
```

Summary:

| Specifier | Description | Example |
| :---: | :---: | :---: |
| \%d, \%i | writes as an integer | -1, 1 |
| \% | writes as an octal number | 12 |
| \%b | writes a binary number in the range [-1023, 1023] | -Ob1111111111 |
| \%u | writes as an unsigned integer, with a cast to C 's uint32 $\dagger$ | 10 |
| \%x, \%X | writes as unsigned hexadecimal number, with a cast to uint32_t. \%x uses lower-case, \%X upper-case | f, F |
| \%f | writes as a floating-point number in normal, fixed-point notation | 3.141593 |
| \%lf | writes as a floating-point number in normal, fixed-point notation with 16 fractional digits by default | 3.1415926535.. |
| \%ld | writes a long double in normal, fixed-point notation with 19 fractional digits by default, see long package in Chapter 11.15 |  |
| \%e, \%E | writes a floating-point number in exponential notation. \%e uses lower-case, \%E upper-case | $\begin{aligned} & 3.141593 \mathrm{e}+000 \\ & 3.141593 \mathrm{E}+000 \end{aligned}$ |
| \%g, \%G | writes a floating-point number in either normal or exponential notation, depending on its magnitude. \%g uses lower-case, \%G upper-case | $\begin{aligned} & \text { 1e-006 } \\ & 1 \mathrm{E}-006 \end{aligned}$ |
| \%h, \%H | writes a floating-point number in a hexadecimal fractional notation with the exponent to base 2 represented in decimal digits. \%h uses lower-case, \%H upper-case | $\begin{aligned} & \text { Ox1.921fb5p+1, } \\ & 0 X 1.921 \mathrm{FB} 5 \mathrm{P}+1 \end{aligned}$ |
| \%p | writes in percent | 314.159265\% |
| \%m | writes a monetary amount with thousands separators and the decimal point defined by the current locale | 31,415.93 |
| \%n, \%N | writes a number using the decimal point separator of the locale of the operating system | 31415,926536 |
| \%D | writes an integer if the value is a number, and "undefined" otherwise | 3 , undefined |
| \%F | writes a floating-point number if the value is a number, and "undefined" otherwise | 3.141593, undefined |


| Specifier | Description | Example |
| :--- | :--- | :--- |
| \%q, \%Q, <br> \%B | writes a string put in double (\%q), single (\%Q) or <br> backquotes (\%B) suitable to be safely read back <br> by the interpreter | "3.1415926535.." |
| \%a, \%A | like \%q but without surrounding quotes | $3.1415926535 .$. |
| \%c | writes the corresponding ASCll character | a |
| \%s are automatically | agena, <br> writes a string, numbers are <br> converted properly | \% |
| \%\% | writes percentage sign |  |

```
strings.fuzzy (s, t)
```

Compares two strings case-insensitively and returns an estimate of their similarity as both an absolute and relative score, the latter taking into account the length of the longer string.

One point is given for a matching character. Subsequent matches are given two extra points. A higher score indicates a higher similarity. With the second return, 1 depicts equality, and a lower value the degree of similarity.

The function is written in Agena and included in the lib/library.agn file.
See also: strings.dleven, strings.diffs, skycrane.tolerance.

```
strings.glob (s, pattern [, true])
```

Compares a string s with a string pattern, the latter optionally including the wildcards ? and *, where ? represents exactly one unknown character, and * represents zero or more unknown characters. Other pattern matching facilities are not supported.

The return is true if the pattern could be found, and false otherwise. If the optional third argument is true, then the strings are compared case-insensitively.

See also: strings.find.

```
strings.gmatch (s, pattern)
```

Returns an iterator function that, each time it is called, returns the next captures from pattern over string s. The function supports pattern matching facilities described in Chapter 9.1.3.

If pattern specifies no captures, then the whole match is produced in each call.
As an example, the following loop

```
> s := 'hello world from Lua'
```

```
> for w in strings.gmatch(s, '%a+') do
    print(w)
> od
```

will iterate over all the words from string s, printing one per line. The next example collects all pairs key~value from the given string into a table:

```
> create table t;
> s := 'from=world, to=Lua'
> for k, v in strings.gmatch(s, '(%w+)=(%w+)') do
t[k] := v
> od
```

See also: strings.match, strings.gmatches.

```
strings.gmatches (s, pattern)
```

Wrapper around strings.gmatch which returns all occurrences of a substring pattern in string sa in a new sequence.

The function is written in Agena and included in the lib/library.agn file.

```
strings.gseparate (s, pattern [, tonumber [, init]])
```

The function takes a string s to be split apart into its tokens one after another, and a delimiter string pattern, and returns an iterator function that each time it is called, returns one token. If the end of s has been reached, the function returns null. The function supports pattern matching. For an iterator without pattern matching, see strings.iterate.

If $s$ starts with the delimiter, an empty string will be returned.
If the Boolean value true is passed to tonumber, the function tries to return a number. If init, a positive integer is given, the function searches from the init'th character in s.

If called with any argument, the function returns the number of tokens returned but does not search for the next token.

See also: split, strings.fields, strings.iterate, strings.separate.

```
strings.gsub (s, pattern, repl [, n])
```

Returns a copy of $s$ in which all occurrences of the pattern have been replaced by a replacement string specified by repl, which may be a string, a table, or a function. gsub also returns, as its second value, the total number of substitutions made. See Chapter 9.1.3 for more information on patterns.

If repl is a string, then its value is used for replacement. The character \% works as an escape character: any sequence in repl of the form \%n, with $n$ between 1 and 9, stands for the value of the n-th captured substring (see below). The sequence $\% 0$ stands for the whole match. The sequence \%\% stands for a single \%.

If repl is a table, then the table is queried for every match, using the first capture as the key; if the pattern specifies no captures, then the whole match is used as the key.

If repl is a function, then this function is called every time a match occurs, with all captured substrings passed as arguments, in order; if the pattern specifies no captures, then the whole match is passed as a sole argument.

If the value returned by the table query or by the function call is a string or a number, then it is used as the replacement string; otherwise, if it is false or null, then there is no replacement (that is, the original match is kept in the string).

The optional last parameter $n$ limits the maximum number of substitutions to occur. For instance, when $n$ is 1 only the first occurrence of pattern is replaced.

Here are some examples:

```
x := strings.gsub('hello world', '(%w+)', '%1 %1')
--> x = 'hello hello world world'
x := strings.gsub('hello world', '%w+', '%0 %0', 1)
--> x = 'hello hello world'
x := strings.gsub('hello world from Lua', '(%w+) %s*(%w+)', '%2 %1')
--> x = 'world hello Lua from'
x := strings.gsub('home = $HOME, user = $USER', '%$(%w+)', os.getenv)
--> x = 'home = /home/roberto, user = roberto'
x := strings.gsub('4+5 = $return 4+5$', '%$(.-)%$', proc (s)
return loadstring(s)()
end)
--> x = '4+5 = 9'
local t := [name~'lua', version~'5.1']
x = strings.gsub('$name%-$version.tar.gz', '%$(%w+)', t)
--> x = 'lua-5.1.tar.gz'
```

See also: replace.
strings.hits (s, pattern [, true])
Returns the number of occurrences of substring pattern in string s.
If only two arguments are passed, pattern matching facilities (see Chapter 9.1.3) are supported. If the Boolean constant true is passed as a third argument, pattern matching is switched off for faster execution.

See also: strings.words.
strings.include (s, pos, p)
Inserts the string p into the string s at position pos.
If pos $\leq$ size $s$, the character at position pos is moved size p places to the right.
If pos $=$ size $s+1, p$ is just appended to $s$, equal to the Agena expression $s$ \& $p$.
The function returns the new string and issues an error, if the index pos is invalid. p may be the empty string, in this case, $p$ will be returned.

See also: strings.between, strings.remove.

```
strings.isstarting (s, pattern [, true])
```

Determines whether a string s is beginning with the substring pattern, i.e. whether pattern fits entirely to the beginning of the string s in case the length of pattern is less than that of $s$. The function returns true or false.

If only two arguments are passed, pattern matching facilities (see Chapter 9.1.3) are supported. If the Boolean constant true is passed as a third argument, pattern matching is switched off for faster execution.

If $s$ or pattern are empty strings or have the same length, the function returns false.
The function can be useful in linguistics if you want to check whether a word has a given prefix.

See also: strings.isending, atendof.
strings.isaligned (s)
Checks whether the string $s$ is aligned on the 4-byte word boundary and returns true or false.

```
strings.isalpha (s [, t])
```

Checks whether the string s consists entirely of alphabetic letters (including diacritics) and returns true or false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in s might match one of the characters in $t$.

See also: strings.isdia, strings.isisoalpha, strings.islatin, strings.ismagic.

```
strings.isalphanumeric (s [, t])
```

Checks whether the string s consists entirely of numbers or alphabetic letters (including diacritics) and returns true or false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in s might match one of the characters in $t$.

See also: strings.islatinnumeric.
strings.isalphaspace (s [, t])
Checks whether the string s consists entirely of alphabetic letters (including diacritics) and/or a white space and returns true or false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in s might match one of the characters in $t$.

```
strings.isalphaspec (s)
```

Checks whether the string s consists entirely of the Latin letters a to $Z, A$ to $Z$, or all characters that are not blanks or alphanumeric, and returns true or false.

See also: strings.isspec, strings.isalphaspace.

```
strings.isascii (s)
```

Checks whether the string s consists entirely of $C$ unsigned char 7-bit characters only that fits into the UK/US character. It is a direct port to the $C$ function `isascii', and returns true or false.

```
strings.isblank (s [, true])
```

Checks whether the string s consists entirely white spaces or tabulators ( $\backslash$ ) and returns true or false. If the option true is given, the function checks for tabs, linefeeds, carriage returns, white spaces, vertical tabs, and form feeds.

See also: strings.isisospace, strings.isspace.

```
strings.iscenumeric (s)
```

Checks whether the string s consists entirely of the digits 0 to 9 and optionally exactly one decimal comma at any position, and returns true or false.

See also: strings.isfloat, strings.isnumber, strings.isnumeric, os.setlocale.
strings.iscontrol (s)
Checks whether the string s consists entirely of control characters and returns true or false. Control characters are: '\0', bell, backspace, tab, linefeed, carriage return, and all other characters between ASCll code 0 and 31, plus the DEL key (ASCII code127). The function is the opposite to strings.isprintable.

See also: strings.isblank, strings.isprintable, strings.isspec.

```
strings.isdia (s)
```

Checks whether the string s consists entirely of diacritics (such as á, â. $\varnothing$, Ü) and ligatures (such as $B, \nVdash$ ) and returns true or false. The function works correctly with the ISO/IEC 8859-1 character set only.

See also: strings.isalpha.

```
strings.isending (s, pattern [, true])
```

Determines whether a string s is ending in the substring pattern, i.e. whether pattern fits entirely to the end of the string $s$ in case the length of pattern is less than that of $s$. The function returns true or false.

If only two arguments are passed, pattern matching facilities (see Chapter 9.1.3) are supported. If the Boolean constant true is passed as a third argument, pattern matching is switched off for faster execution.

If $s$ or pattern are empty strings or both are the same, the function returns false.
The function can be useful in linguistics if you want to check whether a word has a given inflectional ending.

See also: strings.isstarting, atendof.
strings.isfloat (s)
Checks whether the string s consists entirely of the digits 0 to 9 and exactly one decimal point (or the decimal-point separator at your locale) at any position, and returns true or false.

See also: strings.isnumber, strings.isnumeric, os.setlocale.

```
strings.ishex (s)
```

Checks whether the string s represents a hexadecimal number which consists of the digits 0 to 9 and or the letters 'a' to 'f' or 'A' to 'F', and returns true or false.

See also: strings.isnumber, utils.hexlify.
strings.isgraph (s)
Checks whether the string s consists of glyphs only. It is a direct port to the C function `isgraph ', and returns true or false.

```
strings.isisoalpha (s)
```

Checks whether the string s consists entirely of ISO 8859/1 Latin-1 alphabetic lower and upper-case characters (including diacritics) and returns true or false. The function only correctly recognises strings read from a file. Mostly, it cannot process ligatures input in a shell, e.g. the Windows NT or Mac console.

See also: strings.isalpha.
strings.isisolower (s)
Checks whether the string s consists entirely of ISO 8859/1 Latin-1 alphabetic lower-case characters (including diacritics) and returns true or false. The function only correctly recognises strings read from a file. Mostly, it cannot process ligatures input in a shell, e.g. the Windows NT or Mac console.

## See also: strings.isalpha, strings.isloweralpha.

```
strings.isisoprint (s)
```

Checks whether the string s consists entirely of printable ISO 8859/1 Latin-1 letters and returns true or false.

```
strings.isisospace (s)
```

Checks whether the string s consists entirely of ISO 8859/1 Latin-1 white spaces and returns true or false.

## See also: strings.isspace.

```
strings.isisoupper (s)
```

Checks whether the string s consists entirely of ISO 8859/1 Latin-1 alphabetic upper-case characters (including diacritics) and returns true or false. The function only correctly recognises strings read from a file. Mostly, it cannot process ligatures input in a shell, e.g. the Windows NT or Mac console.

See also: strings.isalpha, strings.isupperalpha.

```
strings.islatin (s [, t])
```

Checks whether the string s entirely consists of the characters 'a' to 'z', and A' to 'Z'. It returns true or false. If $s$ is the empty string, the result is always false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in $s$ might match one of the characters in $t$.

See also: strings.isalpha.
strings.islatinnumeric (s [, t])
Checks whether the string s consists entirely of numbers or Latin letters 'a' to 'z' and 'A' to 'Z', and returns true or false.

If the optional string t representing a character set is given, the function also checks whether any character in $s$ might match one of the characters in $t$.

See also: strings.isalphanumeric.
strings.isloweralpha (s [, t])
Checks whether the string s consists entirely of the characters a to $z$ and lower-case diacritics, and returns true or false. If $s$ is the empty string, the result is always false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in s might match one of the characters in $t$.

See also: strings.isisolower, strings.isupperalpha.
strings.islowerlatin (s [, t])
Checks whether the string s consists entirely of the characters 'a' to 'z', and returns true or false. If $s$ is the empty string, the result is always false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in $s$ might match one of the characters in $t$.

See also: strings.isupperlatin.
strings.ismagic (s)
Checks whether the string s contains one or more magic characters and returns true or false. In this function, magic characters are anything unlike the letters ' $A$ ' to 'Z', 'a' to 'z', and the diacritics listed at the top of this chapter.

See also: strings.isalpha.

```
strings.ismultibyte (s)
```

Detects whether the given string $s$ is in UTF-8 encoding and returns two booleans (true or false): The first Boolean indicates that s is compliant to the UTF-8 standard. Remember that a string in ASCll or ISO 8859 encoding is also a valid UTF-8 string.

The second Boolean indicates that s contains at least one multi-byte UTF-8 character, i.e. that at least one character is part of the UTF-8 but not of the ASCII or ISO 8859 standard.

If an integer is returned as a third argument, it will denote the position where the string did not meet UTF-8 criteria.

Please note that the function may not produce correct results with text input in a console. The function can only return correct results if the string to be checked has been read from a file.

See also: strings.isutf8, strings.isisoalpha.

## strings.isnumber (s)

Checks whether the string s consists entirely of the digits 0 to 9 and returns true or false.

See also: strings.isfloat, strings.ishex, strings.isnumeric.

```
strings.isnumberspace (s)
```

Checks whether the string s consists entirely of the digits 0 to 9 or white spaces and returns true or false.

```
strings.isnumeric (s)
```

Checks whether the string s consists entirely of the digits 0 to 9 or digits and optionally exactly one decimal point (or the decimal-point separator at your locale) at any position, and returns true or false.

See also: strings.iscenumeric, strings.isfloat, strings.isnumber, os.setlocale.

```
strings.isolower (s)
```

Receives an ISO 8859/1 Latin-1 string s and returns a copy of this string with all upper-case letters changed to lower-case. The operator leaves all other characters unchanged.

See also: lower, strings.isoupper.

```
strings.isoupper (s)
```

Receives an ISO 8859/1 Latin-1 string s and returns a copy of this string with all lower-case letters changed to upper-case. The operator leaves all other characters unchanged.

See also: lower, strings.isoupper.

## strings.isprintable (s)

Checks whether the string s consists entirely of characters that can be output at the console (characters with ASCII codes 32 to 255 except the backspace) and returns true or false. The function is the opposite to strings.iscontrol.
strings.isspace (s)
Checks whether the string s consists entirely white spaces and returns true or false.
See also: strings.isblank, strings.isisospace.
strings.isspec (s)
Checks whether the string s consists entirely of punctuation characters (any printing character that is not a white space or alphanumeric), including
white space i ? i ! " \# \$ @ § \% \& ' * / + - . , ; ( ) [ ] \{ \} | | \ ^ ~ $=$ < >
and returns true or false.
See also: strings.isalphaspec, strings.isspace, strings.ismagic.
strings.isupperalpha (s [, t])
Checks whether the string s consists entirely of the capital letters ' $A$ ' to 'Z' and upper-case diacritics, and returns true or false. If $s$ is the empty string, the result is always false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in $s$ might match one of the characters in $t$.

See also: strings.isisoupper, strings.isloweralpha.
strings.isupperlatin (s [, t])
Checks whether the string s consists entirely of the capital letters ' A ' to ' Z ', and returns true or false. If $s$ is the empty string, the result is always false.

If the optional string $t$ representing a character set is given, the function also checks whether any character in $s$ might match one of the characters in $t$.

See also: strings.islowerlatin.

```
strings.isutf8 (s)
```

Detects whether the given string contains at least one multibyte and return true or false.

See also: strings.ismultibyte, strings.isisoalpha.

```
strings.iswrapped (s, t)
```

Checks a string $s$ with a another string $t$ if $t$ is missing at the start and the end of $s$, and returns true or false.

See also: strings.wrap, strings.wrapmissing.

```
strings.iterate (s [, pos [, n]])
strings.iterate (s, O [, option])
strings.iterate (s, delim)
```

In the first form, returns an iterator function that, when called returns the next n characters in string str, starting at position pos. pos and $n$ are 1 by default.

In the second form, when pos is zero, returns an iterator function that from the left to right returns each four consecutive characters in string str as an unsigned 4-byte integer. The iterator returns Little Endian integers unless the third argument is set to true to return Big Endian integers.

In the third form, by passing a string del of one or more delimiters as the second argument, returns an iterator function that step-by-step returns a field surrounded by at least one of the delimiters. Pattern-matching is not supported, use strings.gseparate instead.

If there are no more characters to process, the factory returns null.
See also: split, strings.fields, strings.gseparate, strings.separate, strings.splitfields, strings.tobytes.

```
strings.ljustify (s, width [, filler])
```

Adds filling characters to the right end of string s, as necessary to return a new string of the given width. If $s$ is a number, it is automatically converted to a string before padding starts. The filling characters may be denoted by the third optional argument filler (number or string), otherwise filler is a white space by default. If the resulting string is longer than the given width, it is truncated to the first width characters.

See also: strings.rjustify.

```
strings.lrtrim (s [, c])
```

Returns a new string with all leading and trailing white spaces removed from s. If a single character is passed for c as an optional second argument, then all leading and trailing characters given by c are removed. If c is a multi-character string, then if existing it is removed once from the start and once from the end of s. The function supports pattern matching.

It does not remove spaces or the given character(s) within the `actual` part of the string.

See also: trim operator, strings.Itrim, strings.trim, strings.wrap.

```
strings.ltrim (s [, c])
```

Returns a new string with all leading white spaces removed from s. If a single character is passed for c as an optional second argument, then all leading characters given by c are removed. If c is a multi-character string, then if existing it is removed once from the start of $s$. The function supports pattern matching.

See also: trim operator, strings.Irtrim, strings.rtrim.

```
strings.match (s, pattern [, init])
```

Looks for the first match of pattern in the string s. If it finds one, then match returns the captures from the pattern; otherwise it returns null. If pattern specifies no captures, then the whole match will be returned. A third, optional numerical argument init specifies where to start the search; its default value is 1 and may be negative.

The function supports pattern matching facilities. For examples and help in case of problems, see Chapter 4.7.7.

See also: strings.gmatch, strings.matches, skycrane.xmlmatch.

```
strings.matches (s, pattern [, init])
```

Works like strings.match, but returns all matches in only one call.

## Example:

```
> strings.matches('St. Petersburg, Europe', '([äÖüßÄÖÜ%a]*)'):
St Petersburg Europe
strings.mfind (s, pattern [, init [, plain]])
```

Like strings.find, but looks for all the matches of pattern in the string s. If it finds at least one match, it returns a sequence with at least one pair indicating where the respective match starts and ends, otherwise, it returns null.

A third, optional numerical argument init specifies where to start the search; its default value is 1 and may be negative. A value of true as a fourth, optional argument plain turns off the pattern matching facilities (see Chapter 9.1.3), so the function does a plain `find substring` operation, with no characters in pattern being considered `magic`. Note that if plain is given, then init must be given as well.

Contrary to strings.find, if the pattern has captures, then in a successful match the captured values are not returned.

See also: in, atendof, and instr, strings.find, strings.matches.

```
strings.pack (fmt, v1, v2, ...)
```

Returns a binary string containing the values v1, v2, etc. serialized in binary form (packed) according to the format string fmt, see Chapter 9.1.4.

```
strings.packsize (fmt)
```

Returns the size of a string resulting from strings.pack with the given format. The format string cannot have the variable-length options 's' or 'z'. For format strings, see Chapter 9.1.4.
strings.random (length [, kind [, l [, u]]])
Creates a random string of the given fixed length. By default, i.e. kind is set to 'base64', a Base64 string consisting of the characters

ABCDEFGHIJKLMNOPQRSTUVWXYZabcdefghijklmnopqrstuvwxyz0123456789+/
will be returned. If the second argument kind is 'ascii', a random ASCll string consisting of characters in the range ASCII 32 to ASCII 126 will be returned. You can change the upper and lower bounds by explicitly passing the non-negative integers 1 and $u$.
strings.remove (s, pos [, len])
strings.remove (s, p [, n])
strings.remove (s, p [, ...])
The function removes a substring from a string. It supports pattern matching.
In the first form, starting from string position pos, the function removes len characters from string $s$. The return is a new string. If len is not given, it defaults to one character to be deleted.

It is not an error if len is greater than the actual length of s. In this case all characters starting at position pos are deleted.

In the second form, substring p is removed n times from string s . The default for n is infinity, i.e. all occurrences of $p$ are removed.

In the third form, one or more substrings $p, \ldots$ are removed from string $s$, in the order of the arguments.

See also: replace, strings.include.

```
strings.repeat (s, n [, delimiter])
```

Returns a string that is the concatenation of $n$ copies of the string s. An optional delimiter string may also be given.

```
strings.reverse (s)
```

Returns a string that is the string s reversed. See also: reverse, stack.reversed.

```
strings.rjustify (s, width [, filler])
```

Adds filling characters to the beginning of string s, as necessary to return a new string of the given width. If $s$ is a number, it is automatically converted to a string before padding begins. The filling characters may be denoted by the third optional argument filler (number or string), otherwise filler is a white space by default. If the resulting string is longer than the given width, it is truncated to the last width characters.

See also: strings.ljustify.

```
strings.rtrim (s [, c])
```

Returns a new string with all trailing white spaces removed from s. If a single character is passed for c as an optional second argument, then all trailing characters given by c are removed. If c is a multi-character string, then if existing it is removed once from the end of $s$. The function supports pattern matching.

See also: trim operator, strings.Itrim, strings.Itrim.

```
strings.rotateleft (s, n [, xorkey [, xorval]])
```

Rotates all the bits in the string s n bits to the left, with n in range $0 . .7$.
The n bits dropping off the beginning of the string will be appended to the resulting string, so that there is no information loss when calling strings.rotateright to decrypt it.

For optional arguments xorkey and xorval see strings.rotateright.

```
strings.rotateright (s, n [, xorkey [, xorval]])
```

Rotates all the bits in the string s n bits to the right, with n in range $0 . .7$.
The n bits dropping off the end of the string will be prepended to the resulting string, so that there is no information loss when calling strings.rotateleft to decrypt it.

You can optionally xor the string by passing the third argument xorkey, an integer in the range 0 .. 255. (Note that in case the string might be corrupted, the function issues an error.) By explicitly setting the optional fourth argument xorval to true, you can achieve further obfuscation of the string while xoring.
strings.separate (s, d [, any])
Splits a string s into its tokens. a is a string that specifies a set of delimiters that may surround the token to be extracted. Thus, the delimiter in front of a token may be different from the delimiter at its end. All the tokens or returned in a sequence in sequential order. If s only consists of characters that are part of $d$, or if $s$ or a are empty strings, the function returns fail.

```
> strings.separate('a word, another word.', ' .,'):
seq(a, word, another, word)
```

If any third argument is passed, then a) the function returns a sequence with one empty string if $s$ is the empty string instead of fail, and b) if none of the delimiters could be found in s, returns a sequence with $s$ in it instead of fail.

See also: split operator, strings.iterate, strings.gseparate, strings.splitfields.

```
strings.shannon (s)
```

Returns the normalised specific Shannon entropy, the specific Shannon entropy, and the total information entropy (in bits) for string s, in this order.

The function does not look for any patterns that might be available for compression, so its use is quite limited and gzip.deflate might be a better alternative.

```
strings.splitfields (s, wrapper, delim)
```

Splits a string s containing fields delimited by substring delim into its fields and returns them in a sequence. The function is suited to parse database or other dumps.

One or more fields may each be wrapped by substring wrapper - if the wrapper exist, the respective leading and trailing substring wrapper is removed from each individual field. Pass the empty string for wrapper if no wrappers are to be deleted.

See also: split operator, strings.fields, strings.iterate, strings.gseparate, strings.separate.

```
strings.strchr (s, i)
```

The function is an interface to the $C$ strchr function, searches s for a single character represented by its ASCII code i and returns a substring starting from the first match to the end of $s$. The second return is the position of the match, starting from 1 . It returns null and 0 if no match was found and issues an error if needle is non-positive.

See also: abs, strings.strrchr, strings.strstr.

```
strings.strrchr (s, i)
```

The function is an interface to the C strrchr function, searches s backwards from the end for a single character represented by its ASCll code i and returns a substring starting from the first match to the end of s. The second return is the position of the match, starting from 1. It returns null and 0 if no match was found and issues an error if needle is non-positive.

See also: abs, strings.strchr, strings.strstr.

```
strings.strcmp (s1, s2)
```

The function calls the $C$ function strcmp and returns its result, "a value that has the same sign as the difference between the first differing pair of characters" (GNU C Library manual).

## See also: strings.compare, strings.strverscmp.

```
strings.strlen (s)
```

Returns the length of string s: the first return is the result of the call to the internal C function strlen, and the second return is the internally stored length of s, returned by Agena's size operator.

The difference between strlen and size is that C's strlen only counts the number of characters up to and excluding the first embedded zero (i.e. character ' $\backslash 0$ '), whereas size returns the real length including embedded zeros, but without the terminating zero.

Example:

```
> s := 'abc' & char(0) & 'defgh';
> # 3 chars up to the first embedded zero, 9 chars at all
> strings.strlen(s):
3 9
```

```
strings.strstr (s1, s2)
```

The function is an interface to the $C$ strstr function, searches s1 for a substring s2 and returns a substring starting from the first match to the end of s1. The second return is the position of the match, starting from 1 . It returns null and 0 if no match was found. If s2 is an empty string, the function returns s1.

## See also: strings.strchr, strings.strrchr.

```
strings.strverscmp (s1, s2)
```

The function compares two version strings. It is a direct interface to the GNU C strverscmp function. The following is a summary of the GNU documentation:
"If you have files jan1, jan2, ..., jan9, jan10, ..., it feels wrong when an application orders them jan1, jan10, ..., jan2, ..., jan9, because the expected order is just: jan1, jan2, ..., jan9, jan10, ...

The function returns an integer less than, equal to, or greater than zero if s1 is found, respectively, to be earlier than, equal to, or later than s2.

Both input strings should be in plain ASCII."

## See also: strings.compare.

strings.tobytes (s [, option [, bigendian]])
Converts a string s into a sequence of its numeric ASCII codes. If the string is empty, an empty sequence will be returned. If option is true or the integer 4, the function returns word-aligned 4-byte unsigned integers instead of individual bytes. If bigendian is true, then with word-aligned 4-byte unsigned integers the result is in Big Endian notation, otherwise it is Little Endian.

Note that numerical codes are not necessarily portable across platforms.

## Example:

```
> s := strings.tobytes('agena', 4): # convert to 4-byte integers
seq(1852139361, 97)
> str := '';
> for i in s do # convert each 4-byte integer
> t := bytes.tobytes(i, 4) # to four single bytes and convert
    str &:= strings.tochars(t) # back to string
> od
> str:
agena
> # or just simply:
```

```
> strings.tochars(s, 4):
```

See also: strings.iterate, bytes.tobytes, strings.tochars, utils.hexlify.

```
strings.tochars (...)
strings.tochars (s [, nbytes [, little]])
```

In the first form, receives zero or more integers in the range $0 . .255$ and returns a string with length equal to the number of arguments, in which each character has the internal numerical code equal to its corresponding argument.

In the second form, converts all the integers in sequence s to a string. By default, s is assumed to contain integers in the range 0 .. 255. If nbytes is 4 , s should include unsigned 4-byte integers. If little is the Boolean true - the default - the integers are converted to Little Endian before assembling the string, otherwise pass false.

Note that numerical codes are not necessarily portable across platforms.
See also: strings.tobytes.

```
strings.tolatin (s)
```

Creates a dynamically allocated copy of string s, changing the encoding from UTF-8 to ISO-8859-15. Unknown code points are returned unchanged. The return is a string. ISO-8859-15 is ISO-8859-1 plus the Euro symbol.

See also: aconv package, strings.toutf8.

```
strings.tolower (s [, option])
```

Converts all uppercase letters in string s to lowercase. By default, only the characters ' $A$ ' to 'Z' are transformed. If you pass any option, then also the diacritics listed at the end of Chapter 9.1 are converted, too.

See also: lower, strings.toupper.

```
strings.toupper (s [, option])
```

Converts all lowercase letters in string s to uppercase. By default, only the characters 'a' to 'z' are transformed. If you pass any option, then also the diacritics listed at the end of Chapter 9.1 are converted, too.

See also: lower, strings.toupper.

```
strings.toutf8 (s)
```

Creates a dynamically allocated copy of string s, changing the encoding from ISO-8859-15 to UTF-8. The return is a string. ISO-8859-15 is ISO-8859-1 plus the Euro symbol.

See also: aconv package, strings.isutf8, strings.tolatin, strings.utf8size.
strings.transform ( $f$, s)
Applies a function f to the ASCll value of each character in string s and returns a new string. f must return an integer in the range [0, 255], otherwise an error will be issued.

Note that numerical codes are not necessarily portable across platforms.

```
strings.uncapitalise (s)
```

Converts the first character in string s to lower case - if possible - and returns the uncapitalised string. If $s$ is the empty string, it is simply returned. It also converts ligatures if the Western European character set is being used.

See also: lower, strings.capitalise.
strings.unpack (fmt, s [, pos]])
Returns the values packed in string s (see strings.pack) according to the format string fmt, see Chapter 9.1.4. An optional pos marks where to start reading in s (default is 1). After the read values, this function also returns the index of the first unread byte in s. If s - depending on the requested transformation - is too short, the function just returns null and zero.

```
strings.utf8size (s)
```

Determines the size of the string $s$ in UTF-8 encoding and returns a non-negative integer. The return is not the number of bytes used to represent a UTF-8 string, but the number of single- and multi-byte `UTF-8 characters`. Thus, for example, while size strings.toutf8('à') rełurns 2, strings.utf8size(strings.toutf8('à')) returns 1 .

Please note that the function may not produce correct results with text input in a console. The function can only return correct results if the string to be checked has been read from a file.

See also: size, strings.isutf8.
strings.words (s [, delim [, true]])
Counts the number of words in a string s. A word is any sequence of characters surrounded by white spaces or its left and/or right borders. The user can define any other delimiter by passing an optional character delim (of type string) as a second argument. If the third argument is true, then succeeding delimiters are ignored. The return is a number.

See also: strings.hits.

```
strings.wrap (s, t)
```

Wraps a string s with another strings $t$, returning the Agena equivalent of $t \& s \in t$.
See also: strings.iswrapped, strings.Irtrim, strings.wrapmissing.
strings.wrapmissing (s, t)
Wraps a string $s$ with string $t$ if $t$ is missing at the start and the end of $s$; otherwise simply returns $s$.

See also: strings.iswrapped, strings.wrap.

### 9.1.3 Patterns

## Character Class:

A character class is used to represent a set of characters. The following combinations are allowed in describing a character class:

- $\mathbf{x}$ : (where x is not one of the magic characters $\wedge$ () $)$. []*+-? represents the character x itself.
- .: (a dot) represents all characters.
- \%a: represents all letters.
- \%c: represents all control characters.
- \%d: represents all digits.
- \%ı: represents all lowercase letters.
- \%k: represents all upper and lower-case consonants, y and Y are not considered consonants.
- ஃp: represents all punctuation characters.
- \%s: represents all space characters, e.g. white spaces, newlines, tabulators, and carriage returns,
- ஃu: represents all uppercase letters.
- ஃv: represents all upper and lower-case vowels including the letters $y$ and $Y$.
- ஃw: represents all alphanumeric characters.
- \%x: represents all hexadecimal digits.
- $\%$ z: represents the character with representation 0 .
- \%<y>: (where $<y>$ is any non-alphanumeric character) represents the character y . This is the standard way to escape the magic characters. Any punctuation character (even the non magic) can be preceded by a ' $\%$ when used to represent itself in a pattern.
- [set]: represents the class which is the union of all characters in set. A range of characters may be specified by separating the end characters of the range with a '-'. All classes $\%$ described above may also be used as components in set. All other characters in set represent themselves. For example, [ $\% \mathrm{w}_{-}$] (or [_\%w]) represents all alphanumeric characters plus the underscore, $[0-7]$ represents the octal digits, and [0-7\% $1 \%-$ ] represents the octal digits plus the lowercase letters plus the ' - ' character.
- The interaction between ranges and classes is not defined. Therefore, patterns like [\%a-z] or [a-\%\%] have no meaning.
- [^set]: represents the complement of set, where set is interpreted as above.


For all classes represented by single letters (\%a, \%c, \%v etc.), the corresponding uppercase letter represents the complement of the class. For instance, \%s represents all non-space characters.

The definitions of letter, space, and other character groups depend on the current locale. In particular, the class [a-z] may not be equivalent to $\% 1$.

Pattern Item:
A pattern item may be

- a single character class, which matches any single character in the class;
- a single character class followed by ' $\star^{\prime}$, which matches 0 or more repetitions of characters in the class. These repetition items will always match the longest possible sequence;
- a single character class followed by ' + ', which matches 1 or more repetitions of characters in the class. These repetition items will always match the longest possible sequence;
- a single character class followed by '-', which also matches 0 or more repetitions of characters in the class. Unlike ' $*$ ', these repetition items will always match the shortest possible sequence;
- a single character class followed by '?', which matches 0 or 1 occurrence of a character in the class;
- on, for $n$ between 1 and 9 ; such item matches a substring equal to the $n$-th captured string (see below);
- \%bxy, where $x$ and $y$ are two distinct characters; such item matches strings that start with $x$, end in $y$, and where the $x$ and $y$ are balanced. This means that, if one reads the string from left to right, counting +1 for an $x$ and -1 for a $y$, the ending $y$ is the first $y$ where the count reaches 0 . For instance, the item \%b() matches expressions with balanced parentheses;
- off[set], a frontier pattern; such item matches an empty string at any position such that the next character belongs to set and the previous character does not belong to set. The set `set` is interpreted as previously described. The beginning and the end of the subject are handled as if they were the character ' $\ 0$ '.


## Pattern:

A pattern is a sequence of pattern items. $A^{\prime} \wedge^{\prime}$ at the beginning of a pattern anchors the match at the beginning of the subject string. A 's' at the end of a pattern anchors the match at the end of the subject string. At other positions, '^' and ' $\$$ ' have no special meaning and represent themselves.

## Captures:

A pattern may contain sub-patterns enclosed in parentheses; they describe captures. When a match succeeds, the substrings of the subject string that match captures are stored (captured) for future use. Captures are numbered according to their left parentheses. For instance, in the pattern ' $\left(a^{*}(.) \% \mathrm{w}\left(\% s^{*}\right)\right)^{\prime}$, the part of the string matching ${ }^{\prime} a^{*}() \%. w\left(\% s^{*}\right)^{\prime}$ is stored as the first capture (and therefore has number 1); the character matching '.' is captured with number 2, and the part matching 'os*' has number 3.

As a special case, the empty capture () captures the current string position (a number). For instance, if we apply the pattern '()aa()' on the string 'flaaap', there will be two captures: 3 and 5 .

A pattern cannot contain embedded zeros. Use \%z instead.

### 9.1.4 Format Strings for Pack and Unpack

The first argument to strings.pack, strings.packsize, and strings.unpack is a format string, which describes the layout of the structure being created or read.

A format string is a sequence of conversion options. The conversion options are as follows:

- <: sets Little Endian
- >: sets Big Endian
- $=$ : sets native Endian
- ! [ n ] : sets maximum alignment to n (default is native alignment)
- b: a signed byte (char)
- B: an unsigned byte (char)
- $\mathrm{h}:$ a signed short (native size)
- $\quad$ : an unsigned short (native size)
- 1 : a signed long (native size)
- L: an unsigned long (native size)
- j: a lua_Integer
- J: a lua_Unsigned
- $\quad$ : a size_† (native size)
- $\quad i[n]$ : a signed int with $n$ bytes (default is native size)
- $\quad \mathrm{I}[\mathrm{n}]$ : an unsigned int with n bytes (default is native size)
- $\mathbf{f}$ : a float (native size)
- d: a double (native size)
- n : an Agena number of C type double = lua_Number
- $\quad$ cn: a fixed-sized string with $n$ bytes
- z: a zero-terminated string
- $\mathbf{s}[\mathrm{n}]$ : a string preceded by its length coded as an unsigned integer with $n$ bytes (default is a size_t)
- x: one byte of padding
- Xop: an empty item that aligns according to option op (which is otherwise ignored)
- ' ': (a white space) ignored
(A "[n]" means an optional integral numeral.) Except for padding, spaces, and configurations (options "xX <=>!"), each option corresponds to an argument in strings.pack or a result in strings.unpack.

For options " $!_{n}$ ", " $\mathrm{s}_{\mathrm{n}}$ ", " $\mathrm{in}_{n}$ ", and " $l_{n}$ ", $n$ can be any integer between 1 and 16. All integral options check overflows; strings.pack checks whether the given value fits in
the given size; strings.unpack checks whether the read value fits in a Lua integer. For the unsigned options, Lua integers are treated as unsigned values too.

Any format string starts as if prefixed by "! $1=$ ", that is, with maximum alignment of 1 (no alignment) and native endianness.

Native endianness assumes that the whole system is either Big or Little Endian. The packing functions will not emulate correctly the behavior of mixed-Endian formats.

Alignment works as follows: For each option, the format gets extra padding until the data starts at an offset that is a multiple of the minimum between the option size and the maximum alignment; this minimum must be a power of 2 . Options " c " and "z" are not aligned; option "s" follows the alignment of its starting integer.

All padding is filled with zeros by strings.pack and ignored by strings.unpack.

## 9.2 memfile - Memory File for Strings

The memfile library implements a character buffer, i.e. a `memory file` userdata that stores a string of almost unlimited length, along with functions to administer it. It is useful if you have to iteratively concatenate a lot of strings, being 20 times faster than the \& operator.

Typical usage:

```
> m := memfile.charbuf() # create a memory file
> memfile.append(m, 'nasa', 'jpl') # put two strings into it
> f := memfile.iterate(m, 1, 2) # from position 1, return 2 chars per call
> f():
na
> f():
sa
> f():
jp
> f():
l
> f():
null
```

Let us declare a bit field of two bytes:

```
> b := memfile.bitfield(16)
```

and in these two bytes, set the even bits to 1 , i.e. twice to $0 b 10101010=170$ :

```
> for i to 16 do if even(i) then b[i] := 1 fi od
```

The contents of the field is:

```
> b:
bitfield(0b10101010, 0b10101010)
```

Get some bits, the first and the tenth:

```
> b[1]:
0
> b[10]:
1
```

Clear the bits in the first byte:

```
> for i to 8 do if even(i) then b[i] := 0 fi od
```

$>\mathrm{b}$ :
bitfield(0b00000000, 0b10101010)

The package provides the following metamethods:

| Metamethod | Functionality |
| :---: | :---: |
| '__index' | read operation, e.g. n[p] or n[p to q], with p, q indices, both counting from 1 ; with bit fields, reads a bit, not a byte |
| '__writeindex' | write operation, e.g. $\mathrm{n}[\mathrm{p}]:=$ value, with p the index, counting from 1; with bit fields, sets a bit, not a byte |
| '__size' | size operator, number of characters currently stored; with bit fields returns the number of bits in the field, not bytes |
| '_-in' | in operator |
| '__notin' | notin operator |
| '__eq' | = equality operator |
| '__empty' | empty operator |
| '__filled' | filled operator |
| '__tostring' | formatting for output at the console; with bit fields, returns binary representations |
| '__gc' | garbage collection |

The functions are:
memfile.append (memfile, v [, ..] [, delim=str])
Appends one or more numbers, strings, Booleans or null's v, etc. to the end of memfile. The function returns nothing.

You can specify the optional character delimiter option `delim \(=\) str` that separates each value to be added to the memory file, e.g. memfile.append ( m , 'a', 'b', 'c', delim = ';') actually adds the string 'a;b;c;'. You may later on drop the final delimiter by calling memfile.dump with the size of the delimiter.

See also: memfile.move, memfile.rewind.

```
memfile.attrib (memfile)
```

Returns the total capacity of a memfile and the current number of allocated bytes, in this order.

See also: memfile.getsize.
memfile.bitfield (n, [, ...])
Creates a bit field of at least n bits and optionally sets zeros or ones into this field. The return is a byte buffer with initially all positions set to zero.

If you pass optional ones or zeros, or the Booleans true or false, they are set from the right end to the left end of the new bit field, e.g. if we have

```
> b := memfile.bitfield(4, 1, 1, 1, 0)
```

we will store 0b0111 = 7 decimal into the field. If you need it the other way around, execute something like

```
> b := memfile.bitfield(4, unpack(reverse(reg(1, 1, 1, 0))))
```

The number of bits actually allocated is always a multiple of 8, i.e. the field is filled up to whole bytes. In the example above, instead of four bits we created a bit field of eight bits.

Since the memory file created is no different from the one created by memfile.charbuf, with the exception of the metatable, you can apply all the other memfile functions on it. The bit field metatable `bitfield` contains specialised functions to get, set, determine the size and print bit fields, which work on the bit and not byte level.

See also: memfile.attrib, memfile.bytebuf, memfile.charbuf, memfile.resize.

```
memfile.bytebuf (n, [,...])
```

Creates a memory file of fixed size $n$ bytes and fills it with zeros by default. It can also initialise the buffer with bytes (second to last argument).

Since the memory file created is no different from the one created by memfile.charbuf, you can apply all the other memfile functions on it.

See also: memfile.attrib, memfile.bitfield, memfile.charbuf, memfile.resize.

```
memfile.charbuf ([v [,...] [, delim=str]])
```

Creates a memory file and optionally puts one or more numbers, strings, Booleans or null's v into it. The function returns the memory file created.

You can specify the optional character delimiter option `delim \(=\) str` that separates each value to be added to the memory file, e.g. memfile.charbuf ('a', 'b', 'c', delim = ';') actually adds the string 'a;b;c;'. You may later on drop the final delimiter by calling memfile.dump with the size of the delimiter.

See also: memfile.attrib, memfile.bytebuf, memfile.resize.

```
memfile.clearbit (memfile, n)
memfile.clearbit (memfile, pos, n)
```

In the first form, unsets absolute bit position n in the memfile, i.e. sets it to $0 . n$ counts from 1. To set a bit, use memfile.setbit.

In the second form, in byte no. pos of the memfile, unsets the n-th bit, i.e. sets it to 0, where $\mathrm{n}>0$.

The return is the modified byte at byte position pos.
See also: memfile.getbit, memfile.setbit, memfile.setbyte, memfile.setchar, memfile.setfield, memfile.setitem.

```
memfile.dump (memfile [, n])
```

Without a second argument, returns the whole string stored in memfile and resets memfile completely to its original state, so that it can store a new string. With a byte buffer, the function refills it with zeros again after dumping the contents.

If a positive integer $n$ is passed as an optional argument, then the function just dumps $n$ bytes from the end (tail) of the memory file and returns them as a string, leaving the rest of the memfile untouched. If the memfile should be empty after this operation, it is reset, which is equal to calling the function without an optional argument.

See also: memfile.get, memfile.getbytes.

```
memfile.find (memfile, str [, pos])
memfile.find (memfile, byte [, pos])
```

With a character buffer, searches memfile for a substring str and returns its position, an integer, or null if the string has not been found. The optional argument pos indicates the position where to start the search, and is 1 by default.

With a byte buffer, searches for the given byte, a non-negative integer in the range 0 to 255.

See also: memfile.substring, in metamethod.

```
memfile.get (memfile [, n])
```

Without a second argument, returns the whole string stored in memfile.
If a positive integer $n$ is passed as an optional argument, then the function just returns $n$ characters from the end (tail) of the memory file.

The function contrary to memfile.dump does not remove any contents and also does not reset or re-size the memory file.

See also: memfile.dump, memfile.getbytes, memfile.substring.

```
memfile.getbit (memfile, n)
memfile.getbit (memfile, p [, n])
```

In the first form, returns the bit stored at absolute bit position $n$ in the memfile. $n$ counts from 1.

In the second form, from byte no. p in the memfile, returns the n -th bit, where p and $\mathrm{n}>0$.

The return is either 1 or 0.
See also: memfile.clearbit, memfile.getfield, memfile.setbit.

```
memfile.getbyte (memfile, pos [, option])
```

From memfile, returns the byte at position pos, with pos $<>0$. If pos is negative, the position is relative to the end of the string. The return is an integer in the range [0, 255].

If any option is given, then the function returns a string with the binary representation of the byte at pos, e.g. '0b10000000'.

See also: memfile.getbit, memfile.getbytes, memfile.getchar, memfile.getitem.

```
memfile.getbytes (memfile [, pos])
```

From memfile, starting from byte position pos in memfile, returns a register of all the bytes (integers in the range [0, 255]) stored in the memory file. pos is 1 by default, i.e. all bytes will be returned. If pos is negative, the position is relative to the end of the string.

See also: memfile.dump, memfile.getbit, memfile.getbyte, memfile.getchar, memfile.getitem, memfile.getsize, size metamethod.

```
memfile.getchar (memfile, pos)
```

From memfile, returns the character at position pos, with $p<>0$. If pos is negative, the position is relative to the end of the string. The return is a string of size 1: the character.

See also: memfile.getbyte, memfile.get, memfile.getitem, memfile.substring.
memfile.getfield (memfile, n)
Returns the bit stored at absolute bit position $n$ in memfile. $n$ counts from 1.

The return is either 1 or 0.

See also: memfile.setfield, memfile.clearbit, memfile.getbit, memfile.setbit.

```
memfile.getitem (memfile, p [, n])
```

From memfile, returns the substring starting at position $p$ and of length $n$, with non-zero p. If $p$ is negative, the position is relative to the end of the string. By default, $n$ is 1 .

See also: memfile.getbyte, memfile.getchar, memfile.getsize, memfile.iterate, memfile.setitem, memfile.substring.

```
memfile.getsize (memfile)
```

From memfile, returns the number of characters (bytes) stored in it.

See also: size metamethod, memfile.attrib.

```
memfile.iterate (memfile [, pos [, n]])
```

Returns an iterator function that when called, returns the next $n$ characters stored in memfile, starting at position pos. If there are no more characters, the factory returns null. By default pos and $n$ are 1.

See also: memfile.getitem, memfile.substring.

```
memfile.map (f, memfile [,\cdots]])
```

Maps a function f on each character in memfile, in-place. f must always return a number or a string.

```
memfile.move (memfile, pos)
```

Moves the end of the current memfile to the given position pos, inclusive, with pos a non-negative integer, or in other words: changes the size of the memfile without reallocating memory. If pos is 0 , the memfile is cleared. If pos is, for example 2 , then if you call memfile.append thereafter with a substring, it will be added starting at position 3, preserving the values at position 1 and 2 . The function returns nothing.

See also: memfile.append, memfile.resize, memfile.rewind.

```
memfile.read (fh, memfile [, bufsize])
```

Reads data from the file denoted by its filehandle fh into the given memfile userdata.

The file should have previously been opened with binio.open and should finally be closed with binio.close.

By default, the function reads in the entire file if bufsize is not given.
If a positive integer has been passed with bufsize, the function only reads in the given number of bytes per each call, returns the number of bytes actually read and increments the file position thereafter so that the next bytes in the file can be read with a new call to memfile.read.
(Passing the bufsize argument may also be necessary if your platform requires that an internal input buffer is aligned to a certain block size.)

If the end of the file has been reached, or there is nothing to read at all, null will be returned. In case of an error, it quits with the respective error.

Example:

```
> m := memfile.charbuf();
> print(size m); # should be zero
> fd := binio.open('memfile.bin');
> pos := 1;
> # the following loop is equivalent to the simple call
> # `memfile.read(fd, m)`:
> do
> pos := memfile.read(fd, m, 512) # read 512 bytes per each call
> until pos = null;
> binio.close(fd); # should now be non-zero
> print(size m);
```

See also: memfile.write.

```
memfile.resize (memfile, n [, flag])
```

Resizes the memfile to exactly $n$ places (bytes), with $n>0$. It can grow or shrink $a$ memory file and in the latter case preserves the remaining content. If the memory file is to be enlarged, the function optionally fills the new space with zeros if the third argument flag true is given, otherwise you may just pass false which is the default.

You may call bytes.optsize before to determine the optimal number of places (bytes) in the memory file to be word-aligned.

See also: memfile.attrib, memfile.bytebuf, memfile.charbuf, memfile.getitem, memfile.move, memfile.rewind.

```
memfile.reverse (memfile)
```

Reverses the data, i.e. bytes, in a memory file, in-place. The function returns nothing.

```
memfile.rewind (memfile)
```

Sets the current size of a memfile to zero, effectively clearing the buffer without re-allocating memory. The function returns nothing.

See also memfile.append, memfile.move.

```
memfile.setbit (memfile, n)
memfile.setbit (memfile, pos, n [, val])
```

In the first form, sets absolute bit position $n$ in the memfile to 1. n counts from 1. To clear a bit, use memfile.clearbit.

In the second form, in byte no. pos of the memfile, sets the n-th bit to val, where val is either a Boolean or 0 or 1 and $n>0$. If val is omitted, sets the bit to 1 .

The return is the modified byte at byte position pos.
See also: memfile.clearbit, memfile.getbit, memfile.setbyte, memfile.setchar, memfile.setfield, memfile.setitem.

```
memfile.setbyte (memfile, pos, i [, count])
```

Sets byte i of type (non-negative) integer into memfile at the existing position pos, with pos $<>0$.

If pos is negative, the position is relative to the end of the string. i should be an integer in the range $[0,255]$. The function returns nothing.

If a fourth argument count is given, then the function sets count bytes - starting from position pos - to the given byte. By default, count is 1. If pos has not been set before, the function fills all preceding positions with zeros, if they have not yet been already set to any byte.

See also: memfile.getbyte, memfile.getchar, memfile.setbit, memfile.setchar, memfile.setitem.
memfile.setchar (memfile, pos, c)
Sets character c of type string into memfile at the existing position pos, with pos $<>$ 0. If $c$ is longer than one character only the first character is written to the memory file.

If pos is negative, the position is relative to the end of the string. i should be an integer in the range $[0,255]$. The function returns nothing.

If a fourth argument count is given, then the function sets count places - starting from position pos - to the given character. By default, count is 1. If pos has not been set before, the function fills all preceding positions with white spaces, if they have not yet been already set.

See also: memfile.getbyte, memfile.getchar, memfile.setbit, memfile.setchar, memfile.setitem.

```
memfile.setfield (memfile, n, val)
```

Sets the $n$-th bit in a memory file to val, where val is either the Boolean true or false, or 0 or 1 . In $n$ is negative, then the $|n|$-th bit from the left side of the buffer is set or unset.

The return is the modified byte in which the bit resides.
See also: memfile.clearbit, memfile.getfield, memfile.setbit.

```
memfile.setitem (memfile, str, pos [, count])
memfile.setitem (memfile, byte, pos [, count])
```

In the first form, sets a substring str into memfile at position pos, with non-zero pos. If the substring is too long, the function issues an error. If pos is negative, the position is relative to the end of the string.

In the second form, does the same with the non-negative integer byte.
The function returns nothing.
See also: memfile.getitem, memfile.setbyte, memfile.setchar.

```
memfile.shift (memfile, n)
```

Rotates the contents of the buffer memfile $n$ bytes to the right if $n$ is positive, and $n$ bytes to the left if n is negative. The function returns nothing.

See also: memfile.move, memfile.substring.

```
memfile.substring (memfile, p [, q])
```

From memfile, returns the substring from position $p$ to position $q$, with non-zero $p$, q. If p or q are negative, the respective positions are relative to the end of the string. q is p by default.

See also: memfile.get, memfile.getitem.

```
memfile.write (fh, memfile [, pos [, nchars]])
```

Writes the string in a memfile userdata to the file denoted by its numeric file handle fh.

The file should be opened with binio.open and closed with binio.close after completion.

The start position pos is 1 by default but can be changed to any other valid position in the memfile.

The number of characters (not necessarily bytes) to be written can be changed by passing an optional fourth argument nchars, a positive number, and by default equals the total number of characters in memfile. (Passing the nchars argument may also be necessary if your platform requires that buffers must be aligned to a particular block size.)

The function returns the index of the next start position (an integer) for a further call to memfile.write to write further characters, where the return should be passed to the third pos argument.

If the end of the string in memfile has been reached, the function returns null and flushes all unwritten content to the file so that you do not have to call binio.sync manually.

No further information is stored to the file created.
Example on how to write a string of 8,000 characters piece-by-piece:

```
> m := memfile.charbuf();
> to 1000 do
> memfile.append(m, 'nasa/jpl')
> od;
> fd := binio.open('memfile.bin');
> pos := 1;
> # The following is equivalent to "memfile.write(fd, m)":
> do # write 1024 values per each call
> pos := memfile.write(fd, m, pos, 1024)
> until pos = null;
```

> binio.close(fd);
Use binio.sync if you want to make sure that any unwritten content is written to the file when calling memfile.write multiple times.

See also: memfile.read.

## 9.3 utf8 - UTF-8 Helpers

As a plus package, the utf8 package is not part of the standard distribution and must be activated with the import statement, i.e. import utf8.

This library provides basic support for UTF-8 encoding. It provides all its functions inside the table utf8. This library does not provide any support for Unicode other than the handling of the encoding. Any operation that needs the meaning of a character, such as character classification, is outside its scope.

Unless stated otherwise, all functions that expect a byte position as a parameter assume that the given position is either the start of a byte sequence or one plus the length of the subject string. As with many string functions, negative indices count from the end of the string.

Functions that create byte sequences accept all values up to Ox7FFFFFFF, as defined in the original UTF-8 specification; that implies byte sequences of up to six bytes.

Functions that interpret byte sequences only accept valid sequences (well formed and not overlong). By default, they only accept byte sequences that result in valid Unicode code points, rejecting values greater than 1OFFFF and surrogates. A boolean argument lax, when available, lifts these checks, so that all values up to Ox7FFFFFFF are accepted. (Not well formed and overlong sequences are still rejected.)

```
utf8.chars (...)
```

Receives zero or more integers, converts each one to its corresponding UTF-8 byte sequence and returns a string with the concatenation of all these sequences.
utf8.charpattern
The pattern (a string, not a function) "[\0-\x7F|xC2-1xF4][\x80-\xBF]*", which matches exactly one UTF-8 byte sequence, assuming that the subject is a valid UTF-8 string.
utf8.codes (s [, lax])
Returns values so that the construction

```
for p, c in utf8.codes(s) do body od
```

will iterate over all characters in string $s$, with p being the position (in bytes) and c the code point of each character. It raises an error if it meets any invalid byte sequence.
utf8. codepoint (s, [, i [, j [, lax]]])
Returns the codepoints (as integers) from all characters in s that start between byte position $i$ and $j$ (both included). The default for $i$ is 1 and for $j$ is $i$. It raises an error if it meets any invalid byte sequence.

```
utf8.len (s, [, i [, j [, lax]]])
```

Returns the number of UTF-8 characters in string s that start between positions i and j (both inclusive). The default for $i$ is 1 and for $j$ is -1 . If it finds any invalid byte sequence, returns a false value plus the position of the first invalid byte.
utf8.offset (s, n [, i])
Returns the position (in bytes) where the encoding of the $n$-th character of $s$ (counting from position i) starts. A negative n gets characters before position i. The default for $i$ is 1 when $n$ is non-negative and size $s+1$ otherwise, so that utf8. offset( $s,-n$ ) gets the offset of the $n$-th character from the end of the string. If the specified character is neither in the subject nor right after its end, the function returns null.

As a special case, when $n$ is 0 the function returns the start of the encoding of the character that contains the $i$-th byte of $s$.

This function assumes that s is a valid UTF-8 string.

## 9.4 aconv - Internationalization

As a plus package, the aconv package is not part of the standard distribution and must be activated with the import statement, i.e. import aconv.

The package is not available for Mac OS X.
The aconv library allows to convert strings from one code page (character set) to another. For a list of available code pages, see aconv.list. It is a port to the GNU iconv package, where iconv stands for 'internationalization conversion`.

Typical usage: First open a handle by passing the from code page and the to code page, in this example, we convert a text from Latin-1 to UTF-8:

```
> import aconv
> cd := aconv.open('latin1', 'utf-8');
> aconv.convert(cd, 'äöüß'):
-ä-ö-\ddot{u}+í
```

After all strings have been converted, the handle must be closed.

```
> aconv.close(fd);
```

Hint for UNIX \& MacOS X users: You must have the iconv package installed on your system in order to use this package.

The available functions are:

## aconv.open (from, to)

Opens a new conversion descriptor, from the from character set (a string) to the to character set (also a string). Concatenating "//TRANSLIT" to the first argument will enable character transliteration and concatenating "//IGNORE" to the first argument will cause iconv to ignore any invalid characters found in the input string.

This function returns a new converter or issues an error. For a list of available character sets, see aconv.list. from and to may be given in upper and lower case.
aconv.convert (cd, str)
Converts string str to the desired character set. cd depicts the converter descriptor. This method always returns the converted string on success, and null and an error code otherwise:

- aconv.ERROR_NO_MEMORY

Failed to allocate enough memory in the conversion process.

- aconv.ERROR INVALID

An invalid character was found in the input sequence.

- aconv.ERROR_INCOMPLETE

An incomplete character was found in the input sequence.

- aconv.ERROR_FINALIZED

Trying to use an already-finalized converter. This usually means that the user was tweaking the garbage collector private methods.

- aconv.ERROR_UNKNOWN

There was an unknown error.

## See also: strings.tolatin, strings.toutf8

aconv.close (cd [, ...])
Closes one or more converters cd and for each converter successfully closed returns true, or false otherwise.
aconv.list ()
Returns a table of all supported codepages.

## 9.5 hashes - Hashes

As a plus package, the hashes package is not part of the standard distribution and must be activated with the import statement, i.e. import hashes.

### 9.5.1 Introduction

The packages computes various hashes for variable-sized strings and for numbers. All the functions require a string or number as the first argument, and - with the exception of the hashes.md5 function - optionally the maximum number of slots in an assumed hash table as the second argument if you want the modulus of the hash value to be returned. Alternatively, you can tentatively apply hashes.fibmod32 to the resulting hash for more evenly distributed results.

For almost each of the functions listed below an algorithm in the Agena language roughly explaining its mode of operation has been given.

### 9.5.2 Usefulness

With a dictionary of 517,996 surnames, where each surname consists of 7.55 characters on average, the following table shows the performance of some string hashes, computed on an Intel i-5 $6500 \mathrm{CPU}, 3.2 \mathrm{GHz}$.

| Hash | Collision quotient | Collisions | Max. values <br> per hash | Running <br> time |
| :--- | ---: | ---: | ---: | :--- |
| adler32 | 1.000054 | 28 | 2 | 2.46 |
| asu | 1.022457 | $11^{\prime} 377$ | 5 | 2.33 |
| bkdr | 1.000234 | 121 | 2 | 2.37 |
| bp | 3.360010 | $363^{\prime} 831$ | 4656 | 2.2 |
| bsd | 12.675476 | $477^{\prime} 130$ | 447 | 2.55 |
| cksum | 1.000054 | 28 | 3 | 2.33 |
| crc16 | 7.910631 | $452^{\prime} 515$ | 23 | 3.20 |
| crc32 | 1.000064 | 33 | 2 | 2.27 |
| dek | 1.003477 | 1.795 | 4 | 2.30 |
| djb | 1.000788 | 408 | 2 | 2.35 |
| djb2 | 1.000122 | 63 | 2 | 2.66 |
| djb2rot | 1.000073 | 38 | 2 | 2.46 |
| elf | 1.022457 | $111^{\prime} 377$ | 5 | 2.41 |
| fletcher | 3.447653 | $367^{\prime} 750$ | 42 | 2.28 |
| fnv | 1.000070 | 36 | 2 | 2.24 |
| jen | 1.000058 | 30 | 2 | 2.39 |
| lua | 1.001793 | 927 | 3 | 2.22 |
| md5 | 1.000000 | 0 | 1 | 6.94 |
| murmur2 | 1.000044 | 23 | 2 | 2.30 |
| murmur3 | 1.000075 | 39 | 2 | 2.30 |
| murmur3128 | 1.000066 | 34 | 2 | 2.57 |
| oaat | 1.000098 | 51 | 2 | 2.17 |


| Hash | Collision quotient | Collisions | Max. values <br> per hash | Running <br> time |
| :--- | ---: | ---: | ---: | :--- |
| pjw | 1.022457 | $11^{\prime} 377$ | 5 | 2.16 |
| pl | 1.000056 | 29 | 2 | 2.71 |
| raw | 1.003783 | $1 ' 952$ | 3 | 2.27 |
| roaat | 1.000655 | 339 | 2 | 2.37 |
| rs | 1.000073 | 38 | 2 | 2.19 |
| sax | 1.000879 | 455 | 2 | 2.29 |
| sdbm | 1.000064 | 33 | 2 | 2.31 |
| sth | 1.009873 | $5 '^{\prime} 064$ | 5 | 2.25 |
| strval | 8.042167 | $453^{\prime} 586$ | 8712 | 2.29 |
| varlen | 1.000000 | 0 | 1 | 5.75 |

### 9.5.3 Summary of Operators and Functions

## Numeric Hashes and Checksums

\%, symmod, math.morton, math.modulus, math.nearmod, bytes.parity, hashes.damm, hashes.digitsum, hashes.droot, hashes.fibmod32, hashes.ftok, hashes.interweave, hashes.j32to32, hashes.jinteger, hashes.jnumber, hashes.luhn, hashes.mix, hashes.mix64, hashes.mix64to32, hashes.parity, hashes.reflect, hashes.varlen, hashes.verhoeff

## String Hashes

hashes.adler32, hashes.asu, hashes.bkdr, hashes.bp, hashes.bsd, hashes.cksum, hashes.crc8, hashes.crc16, hashes.crc32, hashes.dek, hashes.djb, hashes.djb2, hashes.djb2rot, hashes.elf, hashes.fletcher, hashes.fuv, hashes.jen, hashes.lua, hashes.md5, hashes.murmur2, hashes.murmur3, hashes.murmur3128, hashes.oaat, hashes.pjw, hashes.pl, hashes.raw, hashes.roaat, hashes.rs, hashes.sax, hashes.sdbm, hashes.sha512, hashes.sth, hashes.strval, hashes.sumupchars, hashes.sysv, hashes.varlen

### 9.5.4 Functions

hashes.adler32 (s [, n [, h] ])
Returns the Adler32 hash for string s. If $n$ is given and non-zero, the hash is taken modulo n before returning. h by default is 65521, but may be any other non-negative integer.
hashes.asu (s [, $\mathrm{n}[\mathrm{l}, \mathrm{h}] \mathrm{]})$
Returns a hash for string s as proposed by A. V. Aho, R. Sethi, J. D. Ullman in their book "Compilers: Principle, Techniques, and Tools", Addison-Wesley, 1988, p. 436.

If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The optional argument $h$ determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default.

The algorithm used is equivalent to:

```
asu := proc(s :: string, n, h) is
    local g;
    n := n or 0;
    h := h or 0;
    for i in s do
            h := (h <<< 4) &+ abs i;
            g := h && 0xf0000000;
            if g <> 0 then
                h := h ^^ (g >>> 24);
                h := h ^^ g
            fi
    od;
    return if n <> 0 then h % n else h fi
end;
```

See also: hashes.elf.
hashes.bkdr (s [, n [, seed]])
Computes a hash value published by Brian Kernighan and Dennis Ritchie, for string s. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The optional integer seed determines a salt is 131 by default; you may chose other primes if necessary. The return is a number. The algorithm used is equivalent to:

```
bkdr := proc(s :: string, n, h) is
    n := n or 0;
    seed := seed or 131; # 31, 131, 1313, 13131, 131313, etc.
    h := 0;
    for i in s do
        h := (h &* seed) &+ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.bp (s [, n [, h] ])
Computes a hash for string s; it may be useful to classify words with common endings since they have the same hash code. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default.

The return is a number. The algorithm used is equivalent to:

```
bp := proc(s :: string, n, h) is
    n := n or 0;
    h := h or 0;
    for i in s do
        h := h <<< 7 ^^ abs i;
    od;
return if n <> O then h % n else h fi
end;
```

See also: hashes.strval, math.ndigits, math.nthdigit.
hashes.bsd (s [, mode])
Returns the 8-bit or 16-bit BSD checksum for the given string s. The return is a non-negative integer. By default, the function computes the 16-bit checksum, a value between 0 and 65,535 if mode is not given or is true. If mode is set to false, the 8 -bit checksum is computed, a value between 0 and 255 .
hashes.cksum (s [, len])
Returns the same checksum as the UNIX cksum utility for the given string s. The return is a non-negative integer. By default, the full length of $s$ is evaluated, but you may compute the hash for the first len characters by passing a second argument (an integer).

The function can be used to validate the integrity of a file but may not always detect hacker manipulation.
hashes.collisions (s, f [, iters [, factor [, returnbag]]])
Takes a table or sequence $s$ of strings and one of the hash functions f and returns the mean number of collisions (a value of 1 is best), number of total slots (occupied or free), the time it took to run the procedure, and if returnbag is true, the hashing table (a bag). If iters, a positive integer, is not given, then the function determines the hash values only once, otherwise iters times. If factor, a positive integer or fraction, is not given, the number of slots of the virtual hash table is twice the number of elements in s.

The function is written in Agena (see lib/hashes.agn).
hashes.crc8 (s [, init])
Performs 8-bit reversed cyclic redundancy check for string s, starting with initial CRC value init, which is 0 by default. The return is a non-negative integer.

```
hashes.crc16 (s [, init])
```

Performs 16-bit reversed cyclic redundancy check for string s, starting with initial CRC value init, which is 0 by default. The return is a non-negative integer.
hashes.crc32 (s [, init])
Performs 32-bit reversed cyclic redundancy check for string s, starting with initial CRC value init, which is 0 by default. The return is a non-negative integer.
hashes.damm (x [, true])
If passed no option, computes the checksum of its argument x (an integer or string consisting of ciphers), and returns an integer in the range $0 . .9$ using the Damm algorithm. Contrary to the Luhn algorithm, it detects all single-digit errors and all adjacent transposition errors.

If passed the Boolean option true, the function checks whether x includes the correct checksum digit at its end.

If you pass an integer x and if $|\mathrm{x}|>$ math.lastcontint, then an error will be issued, for $x$ cannot be represented accurately on your system. Pass a string instead.

See also: hashess.luhn, hashes.verhoeff.
hashes.dek (s [, n [, h]])
Computes a hash value for string s proposed by Donald E. Knuth in The Art Of Computer Programming Volume 3, under the topic of sorting and search.

If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The optional argument $h$ determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The algorithm used roughly resembles:

```
dek := proc(s :: string, n, h) is
    n := n or 0;
    h := h or size s;
    for i in s do
        h := ((h <<< 5) ^^ (h >>> 27)) ^^ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.digitsum (x [, n])
Computes the digit sum of the integer x to the base n and returns an integer. n is 10 by default. If $x$ is negative, the result is negative, i.e. -hashes.digitsum(abs(x), $n$ ) will be returned. The function is written in Agena and included in the lib/hashes.agn file.
hashes.djb (s [, n [, lsh [, h] ]])
Computes the Daniel J. Bernstein hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 5381 by default. The return is a number. The algorithm used roughly resembles:

```
djb := proc(s :: string, n, sh) is
    local h;
    h := 5381;
    n := n or 0;
    sh := sh or 5;
    for i in s do
            h :=(h <<< sh) &+ h &+ abs i
    od;
    return if n <> O then h % n else h fi
end;
```

hashes.djb2 (s [, n [, f [, h]]])
Computes a modified Daniel J. Bernstein hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 5381 by default. The return is a number. The algorithm used roughly resembles:

```
djb2 := proc(s :: string, n, f) is
    local h;
    h := 5381;
    f := f or 33;
    n := n or 0;
    for i in s do
        h := (f &* h) ^^ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.djb2rot (s [, n [, sh [, f [, h]]]])
Like hashes.djb2, but using an additional left rotation-bit shift operation; good performance, few collisions. The algorithm used is equivalent to:

```
djb2rot := proc(s :: string, n, sh, f) is
    local h;
    h := 5381;
    f := f or 33;
    sh := sh or 17;
    n := n or 0;
    for i in s do
        h := h <<<< sh;
        h := (f &* h) ^^ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.droot (x [, b])
Returns the digital root and the additive persistence for the integer x and base b . By default b is 10 .

The digital root is the sum of its digits and the sum of the digits of this sum, and so forth, until the respective sum is less than $b$. The additive persistence is the number of summations it took to compute the root.
hashes.elf (s [, n [, h] ])
Similar to hashes.asu, but optimised for 32-bit CPUs, commonly used in UNIX systems. The code is equivalent to:

```
elf := proc(s :: string, n, h) is
    local x;
    n := n or 0;
    h := h or 0;
    for i in s do
        h :=(h <<< 4) &+ abs i;
        x := h && 0xf0000000;
            if x <> 0 then
                h := h ^^ (x >>> 24);
            fi;
            h := h && ~~(x)
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.fibmod32 (k, m [, true])
Returns an unsigend 32-bit integer hash value for the non-negative integer $k$ and the given number of slots $m$ - also a non-negative integer - that may be more evenly distributed than just computing k $\% \mathrm{~m}$, but not necessarily. The function uses Fibonacci hashing, and returns a value that is equivalent to:

```
fibmod := proc(k :: nonnegint, m :: nonnegint) is
    local p := k *(math.Phi - 1);
    return bytes.numto32(m * frac(p))
end;
```

The result is in the range $0 \ldots \mathrm{~m}-1$ if m is odd; if m is even, the result is always in the range $1 . . \mathrm{m}-1$, unless $\mathrm{k}=0$ or $\mathrm{m}=0$ where the function returns 0 .

Note that with $a<b$, fibmod32( $a, m$ ) is not necessarily less than fibmod32( $b, m$ ).
If you pass the optional third argument true, then the results are always the same across different platforms - due to performance reasons, the default is false.

See also: \%, math.modulus.
hashes.fletcher (s, [mode [, len]])
If mode is not given or is true, returns the position-dependent 16 -bit checksum of a string s according to Fletcher's algorithm using an internal 32-bit accumulator, and returns an integer. The 360th and all succeeding characters are ignored.

If mode is false, returns the position-dependent 8-bit checksum using an internal 16-bit accumulator, and returns an integer in the range [257, 65535]. The 21 st and all succeeding characters are ignored.

If the option len is given, only the first len characters are processed.
hashes.fnv (s [, n])
Computes the Fowler-Noll-Vo hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The return is a number. The algorithm used is equivalent to:

```
fnv := proc(s :: string, n) is
    local h;
    h := 2166136261;
    n := n or 0;
    for i in s do
        h := (h &* 16777619) ^^ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.ftok (inode, device [, id, [, n]])
Computes the System V IPC (Inter Process Communications) key, inode, device and optional id are all 4-byte signed integers, with id defaulting to 0 . The return is an integer equivalent to, in signed bits mode:

$$
\text { (inode \&\& Oxfff) || ((device \&\& Oxff) <<< 16) || ((id \&\& Oxffu) } \lll 24 \text { ) }
$$

If n is given and non-zero, the hash is taken modulo n before returning.
See also: os.ftok.
hashes.interweave (x [, option [, mask [, sh [, n]]]])
Splits a number x into its higher and lower unsigned 4-byte words hx and Ix and applies one of the following binary operations on them: ' or' (the default), 'and', 'xor'.

By passing a non-negative mask as the optional third argument, the mask is applied to the intermediate result, the default is OxFFFFFFFF.

If a fourth positive sh integer is given, the intermediate result is right-shifted sh bits; if sh is a negative integer, it is left-shifted sh bits. If sh is 0 (the default), there is no shift.

If a fifth argument $n$ is given, a positive integer, the intermediate result is taken modulus $n$. The default is 1 .

Thus, with $\mathrm{hx}, \mathrm{lx}:=$ bytes.numwords $(\mathrm{x})$ :

- option = 'or': (((hx |||x) \&\&mask) $\ggg$ sh) \% $n$, if sh $>0$,
- option = 'and': (((hx \&\&|x) \&\& mask) $\ggg$ sh) $\% n$, if sh $>0$,
- option = 'xor': (((hx ^^|x) \&\& mask) $\ggg$ sh) $\% n$, if $s h>0$,
and
- option = 'or': (((hx |||x) \&\&mask) $\lll \mid$ sh |) \% n, if sh $<0$,
- option = 'and': (((hx \&\&|x) \&\& mask) $\lll \mid$ sh|) \% n, if sh $<0$,
- option = 'xor' $:(((h x \wedge \wedge \mid x) \& \&$ mask $) \lll \mid$ sh|) $\% n$, if sh $<0$.


## hashes.j32to32 (x [, n])

Hashes an unsigned 4-byte integer $x$ (i.e. in the range $0 . .2^{32}-1$ ) to yet another integer in the same range, Julia-style.

If a second argument n is given, a positive integer, the intermediate result is taken modulus $n$. The default for $n$ is 1 .

See also: hashes.jinteger.
hashes.jen (s [, n])
Computes the Bob Jenkins' hash (96 bit Mix Function) for string s. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The return is a number. Please see the C hashes.c source file for its implementation.
hashes.jinteger (x [, h])
Value-based hashing of an unsigned 4-byte integer x , with seed h which by default is $4,294,967,295=2^{32}-1$, ported from the Julia language.

See also: hashes.jnumber, hashes.j32to32.
hashes.jnumber (x [, n [, option]])
Maps a number x to one or two unsigned 4 byte integers, Julia-style. If n, a positive integer, is given, the computed hashes are taken modulo n. By default, only one unsigned 4-byte integer will be returned. If you pass true for option then the function will split $x$ into its higher and lower unsigned 4-byte words and returns
unsigned 4-byte integer hashes for each of them. In this case, the second return is equal to the result of hashes.jnumber when called without this option.

See also: bytes.numwords, hashes.jinteger.
hashes.lua (s [, n])
Returns the hash, an integer, Lua/Agena internally computes for string s. If $n, a$ positive integer, is given, the computed hash is taken modulo n . It is an adaption of the Shift-Add-XOR hash. This variant chooses the length of the string as its seed, not a fixed value, and scans from the right to the left. See also: hashes.sax.
hashes.luhn (x [, true])
If passed no option, computes the checksum of its argument $x$ (an integer or string consisting of ciphers), and returns an integer in the range $0 . .9$ using the Luhn formula, which is used to validate credit card numbers, IMEls or some social security numbers.

If passed the Boolean option true, the function checks whether x includes the correct checksum digit at its end.

If you pass an integer $x$ and if $|x|>$ math.lastcontint, then an error will be issued, for $x$ cannot be represented accurately on your system. Pass a string instead.

The Luhn formula does not recognise the transposition 09 vs .90 , nor does it detect twin 22 vs. 55,33 vs. 66, and 44 vs. 77.

See also: hashess.damm, hashes.verhoeff.
hashes.md5 (s [, anyoption])
Computes the MD5 hash for strings $s$. The return is a string of 32 characters that represent 16 pairs of hexagesimal numbers where the alphabetical letter is in upper-case.

If any option is given, the MD5 hash for file s will be returned.
See also: hashes.varlen.
hashes.mix ( $a, b, c$ )
The function mixes three non-negative integers $a, b, c$ assumed to be 32-bit and returns an integer.

```
hashes.mix64 (x [, n])
Computes the 64-bit mix for number x. If n, a positive integer, is given, the
computed hash is taken modulo n. The return is a number. See also:
hashes.mix64to32.
```

hashes.mix64to32 (x [, n])
Computes the 64-bit mix for number $x$. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The return is a number. See also: hashes.mix64.

```
hashes.murmur2 (s [, n])
```

Returns MurmurHash2 for string s. If n, a positive integer, is given, the computed hash is taken modulo $n$. Note that the function returns different values on littleendian and Big Endian machines.

See also: hashes.murmur3, hashes.murmur3128.
hashes.murmur3 (s [, n])
Computes MurmurHash3 using 32-bit unsigned integers internally, for the given string s and returns an integer. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. Note that the function returns different values on little-endian and big-endian machines.

See also: hashes.murmur2, hashes.murmur3128.
hashes.murmur3128 (s [, n [, seed]])
Computes MurmurHash3 using 128-bit unsigned integers internally, for the given string $s$ and returns four unsigned 32 -bit integers. If $n$, a positive integer, is given, the computed hash is taken modulo n . seed, if not given, is $0 \times 9747 \mathrm{~b} 28 \mathrm{c}$ by default. Note that the function returns different values on little-endian and big-endian machines. (In OS/2 and Raspberry Pi the function always returns an error.)

## See also: hashes.murmur2, hashes.murmur3128.

## hashes.oaat (s [, n [, h]])

Computes the One-at-a-Time hash for string s. If given, n must be a positive integer. The optional argument $h$ determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The return, which may vary across platforms, is a number. The algorithm used is equivalent to:

```
hashmask := << n -> (1 <<< n) - 1 >>
```

```
oaat := proc(s :: string, n) is
    local h := 0;
    n := n or 0;
    for i in s do
        inc h, abs i;
        inc h, h <<< 10;
        h := h ^^ (h >>> 6)
    od;
    inc h, h <<< 3;
    h := h ^^ (h >>> 11);
    inc h, h <<< 15;
    return if n <> 0 then h && hashmask(n) else h fi
end;
```

See also: hashes.roaat.

## hashes.parity (x)

Returns a byte with even parity for the non-negative integer $x$, and returns an integer in the range [0, 255]. See also: bytes.parity32.

## hashes.pjw (s [, n [, h] ])

Computes the P. J. Weinberger Hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default.

The return is a number.
hashes.pl (s [, n [, f [, h] ]])
Computes Paul Larson's hash of Microsoft Research for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The return is a number. The algorithm is equivalent to:

```
pl := proc(s :: string, n, f, h) is
    local h := 0;
    f := f or 101;
    n := n or 0;
    h := h or 0;
    for i in s do
        h :=(h &* f) &+ abs i
    od;
    return if n <> 0 then h % n else h fi
end;
```

With initial $\mathrm{h}=5381$ and $\mathrm{f}=33$, emulates the GNU hash.
hashes.raw (s [, n [, h] ])
Computes a self-invented hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial
value of the resulting hash code before the string is evaluated, and is 0 by default. The return is a number. The algorithm used is equivalent to:

```
raw := proc(s :: string, n, h) is
    n := n or 0;
    h := h or 0;
    for i in s do
        h := 38 &* (h <<< 1) &+ abs i &- 63
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.reflect ( x [, n$]$ )
Reorders the bits of the $n$-bit integer x by reflecting them about the middle position. By default, $n$ is 32 , but may be any other integer in $[1,32]$. The return is an integer.
hashes.roat (s [, n [, h] ])
Like hashes.oaat, but uses bit rotation internally instead of simple bit shifts. The result may vary across platforms.
hashes.rs (s [, n [, h] ])
Computes a hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The return is a number. The algorithm used is equivalent to:

```
rs := proc(s :: string, n, h) is
    local a, b := 63689, 378551;
    n := n or 0;
    h := h or 0;
    for i in s do
        h := h &* a &+ abs i;
        a}:=\textrm{a}&* 
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.sax (s [, n [, h]])
Computes the Shift-Add-XOR hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 5381 by default. The return is a number. The algorithm used is equivalent to:

```
sax := proc(s :: string, n) is
    local h := 5381;
    n := n or 0;
    for i in s do
        h := h ^^ ((h <<< 5) + (h >>> 2) + abs i)
    od;
    return if n <> 0 then h % n else h fi
end;
```


## hashes.sdbm (s [, n [, h]])

Computes the ndbm database library hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo $n$. The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The return is a number. The algorithm uses a public-domain implementation. The algorithm used is equivalent to:

```
sdbm := proc(s :: string, n) is
    local h := 0;
    n := n or 0;
    for i in s do
            h := abs i &+ (h <<< 6) &+ (h <<< 16) &- h
    od;
    return if n <> 0 then h % n else h fi
end;
```

hashes.sha512 (s [, salt [, rounds]])
Calculates a SHA512 cryptographic hash for string s, optionally using a salt of type string, and the optional number of rounds to be taken. salt by default is the empty string and rounds is 5000 .

The first return is the hash itself, and the second return includes the control parameters salt and rounds plus the first result. Thus, the second return is the same as the output of the mkpasswd UNIX command.

In case of errors, the function returns fail.
The function is very slow.
hashes.sth (s [, n [, h] ])
Computes the s-th hash for string s. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional argument h determines the initial value of the resulting hash code before the string is evaluated, and is 0 by default. The return is a number. The algorithm has been published at StackOverflow. The algorithm is equivalent to:

```
sth := proc(s :: string, n) is
    local h := 0;
    n := n or 0;
    for i in s do
        h := (h <<< 6) ^^ (h >>> 26) ^^ abs i
    od;
    return if n <> 0 then h % n else h fi
end
```

```
hashes.strval (s [, sh [, h]])
```

Computes a hash with many collisions, useful to classify words with common endings since they have the same hash code. s denotes the string to be hashed, sh the left-shift, which is -8 by default; and $h$ the initial hash value before computation starts, 0 by default. The algorithm used is equivalent to:

```
strval := proc(s :: string, sh, h) is
    sh := n or 8;
    h := h or 0;
    for i in s do
        h := h <<< sh;
        h := h &+ abs i
    od;
    return h
end;
```

See also: hashes.bp, math.ndigits, math.nthdigit.
hashes.sumupchars (s [, f [, g]])
Sums up all the ASCll values in string s and returns the result as a positive integer. The sum is expressed as an unsigned 32-bit integer, so keep overflows in mind.

Instead of just adding the plain ASCll values, you might optionally apply function $f$ to the first character in $s$, and function $g$ to the second character in $s$, then $f$ again on the third character, $g$ on the fourth character, and so forth. Example:

```
> import bytes;
> sum := hashes.sumupchars("agena",
> << x ->(x && 0xff) <<< 8 >>,
> << x -> x && 0xff >>):
> ~~(sum + (sum >>> 16)):
```

Note that the Internet checksum, even if strictly implemented according to RFC 1071, has by far more collisions than the other hash functions available in this package.
hashes.sysv (s [, n [, f [, h] ]])
For string s, computes the System V hash to access libraries via dynamic symbol tables on UNIX. If $n$, a positive integer, is given, the computed hash is taken modulo n . The optional positive integer f is the factor to multiply intermediate results, see algorithm below, and is 16 by default. The optional argument seed h determines the salt and is 0 by default; you may chose other primes if necessary.

The return is a number.
The algorithm used is equivalent to:

```
sysv := proc(s :: string, n, f, h) is
    n := n or 0;
    f := f or 16;
    h := h or 0;
    for i in s do
        h := f &* h &+ abs i;
        h := h ^^ ((h >>> 24) && 0xf0)
    od;
    h := h && Oxfffffff;
    return if }n<>0\mathrm{ then h % n else h fi
end;
```

For GNU hash, see hashes.pl.
hashes.varlen ( x , salt [, n$]$ )
Computes a variable-length integer hash for string or number $x$ and string salt. If the optional positive integer $n$ is given, the computed hash is taken modulo $n$. Depending on the given keyword, the number of collisions might be zero, so this function is an alternative to hashes.md5.
hashes.verhoeff (x [, true])
If passed no option, computes the checksum of its argument x (an integer or string consisting of ciphers), and returns an integer in the range $0 . .9$ using the Verhoeff algorithm. Contrary to the Luhn algorithm, it detects all single-digit errors, and all accidental transposition involving two adjacent ciphers.

If passed the Boolean option true, the function checks whether x includes the correct checksum digit at its end.

If you pass an integer x and if $|\mathrm{x}|>$ math.lastcontint, then an error will be issued, for $x$ cannot be represented accurately on your system. Pass a string instead. The function also returns an error, if a non-digit is included in string x .

See also: hashes.damm, hashes.luhn.

## 9.6 bloom - Bloom Filter

As a plus package, the bloom package is not part of the standard distribution and must be activated with the import statement, i.e. import bloom.

### 9.6.1 Introduction

This package implements the Bloom filter, a dictionary containing bit signatures of its individual strings (words).

A Bloom filter is a memory-efficient mean to check whether a string probably is part of a dictionary or whether it is definitely not part of the dictionary, with acceptable query times. It consumes less memory than the original dictionary of strings and can be used to prevent unnecessary access to the file system on which the actual dictionary resides, for example in dBASE III+ , binary or text files.

With respect to this package, a dictionary does not depict an Agena table dictionary, but just a list of strings, e.g.: "Akatsuki", "Chandrayaan", "Chang'e", "Mars Express", "Venera", "Voyager".

Depending on the size of the Bloom filter, the hash string function used, and the number of internal iterations - i.e. number of `salts` - when inserting or reading values, around $80 \%$ of memory can be saved with only around $5 \%$ of the words to be actually looked up in the original dictionary. Bloom filter lookup takes around a third more running time than searching Agena built-in data structures.

Technically, the hash value of a string - see hashes package for a variety of string hash functions - is converted into a bit signature that is stored to slots in the Bloom filter. Internally, the Bloom filter implemented here uses four unsigned bytes for each slot (C type uint32_t). The string hash function should produce the least number of collisions.

You cannot delete values from a Bloom filter. Also, you cannot change the number of slots of the bloom filter or the number of salts.

You may use the package as follows:

1. Determine the number of entries $s$ in your original dictionary $d$.
2. Create a Bloom filter b with $\mathrm{s} \backslash 4$ slots and 4 salts:
```
b := bloom(s \ 4, 4);
```

3. Insert all entries str of your dictionary into Bloom filter b using a string hash function, e.g.:
```
for str in d do
    bloom.include(b, hashes.sdbm(str))
od;
```

4. Query the Bloom filter for any entry, using the same hash function:
```
result := hashes.find(b, hashes.sdbm('Zond'));
if result = false then
    print('entry really not included')
else
    print('entry probably included, search original dictionary.')
fi;
```

5. Query a Bloom filter slot, with an index counting from 1:
```
b[1]:
```

of just output all slots with bloom.tosea.
6. Check the state of the bloom filter b:

```
bloom.attrib(b):
```


### 9.6.2 Functions

## bloom.attrib (b)

Returns various information on the Bloom filter:

- key 'size': number of internal slots of the bloom filter, the first argument to bloom.new.
- key 'salts': number of internal hash functions (salts) applied to a word when computing the signature, the second argument to bloom.new.
- key 'wordsincluded': number of words included into the filter. If the signature of a word is already included, it is not counted.
- key 'collisions': number of collisions detected when trying to include a word into the filter, for its internal signature is already present. If a word has already been included in the filter, its collision is being counted nevertheless.
- key 'bytes': size of the whole Bloom filter userdata in bytes.
bloom.get (b, i)
With a bloom filter $b$, returns the value stored at $b[i$ ], where $i$, the index, is an integer counting from 1.

See also: bloom.toseq.

```
bloom.find (b, hash)
```

Checks whether a string converted to the hash value is part of a dictionary of strings represented by Bloom filter userdata b . The function returns true or false, where false means that the string is definitely not included in the original dictionary, and true means it is probably part of the original dictionary.

Example: bloom.find(b, hashes.pl('Soyuz')).
See also: bloom.include.

```
bloom.include (b, hash)
```

Inserts the hash value (an integer) of a string into the Bloom filter b, a userdata. By default, the function returns nothing.

If a hash value has already been inserted, nothing happens.
If the optional third argument is true, internal information will be returned: the last internal subhash - an integer - computed before inserting the signature of the string into the Bloom filter, and a table with the keys representing the slot indices of the Bloom filter modified (an integer starting from 1) and the respective bit position set to 1 (counting from 0 , from the right of the bit field).

Example: bloom.include(b, hashes.pl('Soyuz')).
See also: bloom.find.

```
bloom.new (n, salts)
```

Creates a Bloom filter, of type userdata, consisting of $n$ slots. The number of salts internally applied when inserting or searching the hash value of a string is given by salts, a positive integer in the range [1,65]. If salts is 1 , then no salt is applied, otherwise (salts - 1) salts are applied.

With a large list of surnames, for example, n should be at least a fourth of the number of words contained in the dictionary, and salts should be 4.

See also: bloom.attrib, bloom.toseq.
bloom.toseq (b)
Receives a Bloom filter b and converts its internal slots into a sequence of integers, the return.

See also: bloom.get.

Chapter Ten

## Structures

## 10 Structures

### 10.1 Tables

Summary of Functions:
Queries
countitems, empty, filled, in, notin, size, tables.getsize, tables.maxn, type, typeof.

## Retrieving Values

getentry, unique, unpack, values, tables.array, tables.borders, tables.entries, tables.hash, tables.indices, tables.parts.

## Operations

copy, copyadd, map, move, purge, put, qsumup, remove, sumup, select, selectremove, shift, sort, sorted, subs, swap, zip, tables.include, tables.move, tables.reshuffle.

Relational Operators
$=,==, \sim=,\langle \rangle, \sim<\rangle$.
Cantor Operations
intersect, minus, subset, union, xsubset.

## Miscellaneous

tables.dimension, tables.allocate, tables.newtable.

### 10.1.1 Operators and Functions

Most of the following functions have been built into the kernel as unary operators, with the exception of map and zip.

## copy ( t )

The function copies the entire contents of a table t into a new table. See Chapter 8 for more information.

```
copyadd (t [, ...])
```

See Chapter 8.

```
countitems (item, t)
countitems (f, t [, ...])
```

In the first form, counts the number of occurrences of an item in the table $t$.
In the second form, by passing a function f with a Boolean relation as the first argument, all elements in the structure t that satisfy the given relation are counted. If the function has more than one argument, then all arguments except the first are passed right after the name of table $t$.

The return is a number. The function may invoke metamethods.
See also: select.

## empty ( $t$ )

Checks whether table $t$ does not contain any element. The return is true or false. The operator works with dictionaries, as well. See also: filled.

## filled (t)

Checks whether table t contains at least one element. The return is true or false. The operator works with dictionaries, as well. See also: empty.
getentry ( t [, $\mathrm{k}_{1}, \cdots, \mathrm{k}_{\mathrm{n}}$ ])
Returns the entry $t\left[k_{1}, \cdots, k_{n}\right]$ from the table $t$ without issuing an error if one of the given indices $k_{i}$ (second to last argument) does not exist. See also rawget.
join (t [, sep [, i [, j]]])
Concatenates all string values in the table $t$ in sequential order and returns a string: $t[i] \& \operatorname{sep} \& t[i+1] \cdots$ \& sep \& $t[j]$. The default value for sep is the empty string, the default for $i$ is 1 , and the default for $j$ is the length of the table. The function issues an error if $t$ contains non-strings.

Use the tostring function if you want to concatenate other values than strings, e.g.:

```
> join(map(tostring, [1, 2, 3])):
123
```

```
map (f, t [, \cdots.] [, true])
```

Maps the function f on all elements of a table t . See map in Chapter 8 for more information.

See also: countitems, remove, select, selectremove, subs, and zip.

```
move (t1, start, stop, newidx [, t2])
```

Copies elements from table t1 to table t2, performing the equivalent to the following multiple assignment: $t 2$ [newidx], $\cdots=t 1$ [start], $\cdots, t 1$ [stop]. The default for t2 is t1, i.e. elements are shiffed in the same table. The destination range can overlap with the source range.

Returns the destination table t2.
See also: purge, put.

```
purge (t [, pos])
purge (t, a, b)
```

Removes from table $t$ the element at position pos, shifting down other elements to close the space, if necessary. Returns the value of the removed element. The default value for pos is $n$, where $n$ is the length of the table, so that a call purge ( $t$ ) removes the last element of $t$.

In the second form, removes all elements starting from index a to index b (inclusive), moving excess elements down to close the space; the function automatically performs a garbage collection after shifting. In the $2^{\text {nd }}$ form, nothing will be returned.

Use the delete element from table statement if you want to remove any occurrence of the table value element from a table.

Note that the function only works if the table is an array, i.e. if it has positive integral and consecutive keys only.

See also: move, put, shift, swap.

```
put (t, [pos,] value)
```

Inserts element value at position pos in table $t$, shifting up other elements to open space, if necessary. The default value for pos is $n+1$, where $n$ is the current table size, so that a call put ( $t$, value) inserts value at the end of $t$.

Use the insert element into structure statement if you want to add an element at the current end of a table, for it is much faster.

The function returns the modified structure.
See also: move, prepend, purge.
qsumup ( $t$ )
Raises all numeric values in table t to the power of 2 and sums up these powers. See qsumup in Chapter 8 for more information. See also: sumup.

```
remove (f, t [, \cdots. [, newarray=true] [, inplace=true]])
```

Returns all values in table $t$ that do not satisfy a condition determined by function f. See remove in Chapter 8 for more information. See also: map, select, selectremove, subs, zip.

```
sumup (t)
```

Sums up all numeric values in table $t$. See sumup in Chapter 8 for more information. See also: qsumup.

```
select (f, t [, \cdots. [, newarray=true] [, inplace=true]])
```

Returns all values in table $t$ that satisfy a condition determined by function f . See select in Chapter 8 for more information. See also: map, remove, selectremove, subs, zip.

```
selectremove (f, t [, ... [, newarray=true]])
```

Returns all values in table $t$ that satisfy and do not satisfy a condition determined by function $f$, in two tables. See selectremove in Chapter 8 for more information.

See also: map, remove, select, subs, zip.

```
size (t)
```

Returns the number of actual entries in the array and hash parts of table $t$. The operator returns a number and conducts a linear traversal.

See also: environ.attrib, tables.getsize.

```
shift (t, a, b)
```

Moves an element in the table array $t$ from position old to new, with old, new integers, shifting all the other elements accordingly - which might also cause a rotation. The function returns nothing.

See also: move, purge, swap.

```
sort (t [, comp])
```

Sorts table t in a given order, and in-place. See sort in Chapter 8 for more information.

See also: sorted, skycrane.sorted, stats.issorted, stats.sorted.

```
sorted (t [, comp])
```

Sorts table elements in t in a given order, but - unlike sort - not in-place, and non-destructively. See sorted in Chapter 8 for more information.

See also: sort, skycrane.sorted, stats.issorted, stats.sorted.

```
subs (x:v [, \cdots.], t [, true])
```

Substitutes all occurrences of value x in table t with value v . See subs in Chapter 8 for more information.

See also: map, remove, select, zip.

```
swap (t, a, b)
```

Swaps the table array $t$ entries at index positions a and $b$, with $a, b$ integers. The function returns nothing.

See also: move, purge.
unique ( $t$ )
The function removes all holes ('missing keys') in the array part of table $t$ and removes multiple occurrences of the same value, if present. See unique in Chapter 8 for more information.

```
values (t, it [, in, \cdots]])
```

Returns the elements from the given table $t$ in a new table. This function is equivalent to

```
return [ i i ~ t[i\mp@subsup{i}{1}{}], i}\mp@subsup{i}{2}{~}~t[\mp@subsup{i}{2}{}],\cdots.. 
```

See also: ops, select, unpack.

```
zip (f, t1, t2)
```

This function zips together two tables t1, t2 by applying the function $f$ to each of its respective elements. See Chapter 8 for more information.

See also: map, remove, select, subs.

The following functions have been built into the kernel as binary operators.

Please note that the operators returning a Boolean work in the Cantor way, i.e. $\{1$, $1\}=\{1\} \rightarrow$ true, $\{1,2\}$ xsubset $\{1,1,2,2,3,3\} \rightarrow$ true.

```
t1 \equiv t2
```

This equality check of two tables t1, t2 first tests whether t1 and t2 point to the same table reference in memory. If so, it returns true and quits.

If not, the operator then checks whether t1 and t2 contain the same values without regard to their keys, and returns true or false. In this case, the search is quadratic.

## See also: environ.isequal.

```
t1 == t2
```

This strict equality check of two tables t1, t2 first tests whether t1 and t2 point to the same table reference in memory. If so, it returns true and quits.

If not, the operator then checks whether t1 and t2 contain the same number of elements and whether all key~value pairs in the tables are the same. In this case, the search is linear.

See also: environ.isequal.

```
t1 ~= t2
```

This approximate equality check of two tables t1, t2 first tests whether t1 and t2 point to the same table reference in memory. If so, it returns true and quits.

If not, the operator then checks whether t1 and t2 contain the same number of elements and whether all key~value pairs in the tables are approximately equal (please see approx for further details). In this case, the search is linear.

```
t1 <> t2
```

This inequality check of two tables t1, t2 first tests whether t1 and t2 do not point to the same table reference in memory. If so , it returns true and quits.

If not, the operator then checks whether t 1 and t 2 do not contain the same values, and returns true or false. In this case, the search is quadratic.
t1 ~<> t2
Approximate inequality check, the negation of the $\sim=$ operator.
$c$ in $t$
Checks whether the table $t$ contains the value $c$ and returns true or false. The search is linear.

See also: notin operator, binsearch for binary search.

```
c notin t
```

Checks whether table t does not contain the value cand returns true or false. The search is linear.

See also: in operator.

## t1 intersect t2

Searches all values in t1 that are also values in t2 and returns them in a new table. The search is quadratic, so you may use bintersect instead if you want to compare large tables since bintersect performs a binary search. The key $\sim$ value pairs in the hash part of a table are treated as being unique. If $t 1$ has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from t2.

## t1 minus t2

Searches all values in table ti that are not values in table $t 2$ and returns them as a new table. The search is quadratic, so you may use bminus instead if you want to compare large tables since bminus performs a binary search. The key ~ value pairs in the hash part of a table are treated as being unique. If $t 1$ has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from t2.

## t1 subset t2

Checks whether all values in table t1 are included in table t2 and returns true or false. The operator also returns true if $\mathrm{t} 1=\mathrm{t} 2$. The search is quadratic.

```
t1 union t2
```

Concatenates two tables t1 and t2 simply by copying all its elements - even if they occur multiple times - to a new table. The key ~ value pairs in the hash part of a table are treated as being unique. If ti has a metatable and/or a user-defined
type, then they will be copied to the result; otherwise the function will try to copy them from $t 2$.

## t1 xsubset t2

Checks whether all values in table t1 are included in table t2 and whether t2 contains at least one further element, so that the result is always false if $\mathrm{t} 1=\mathrm{t} 2$. The search is quadratic.

See also: bintersect, bisequal, bminus, purge, put in Chapter 8 Basic Functions.

## f @ t

The operator maps a function f to all the values in table t and returns a table as the result. f must be a univariate function and return only one value. If $t$ has metamethods or user-defined types, the return will also have them.

Examples:

```
> << x -> x^2 >> @ [1, 2, 3]:
[1, 4, 9]
> << x -> x > 0 >> @ [1, 2, 3]:
[true, true, true]
```

See also: \$ and \$\$ operators.

## f ${ }^{\text {s }} \mathrm{t}$

Returns all values in table $t$ that satisfy a condition determined by function f . f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored. The return might include holes.

```
> << x -> x > 1 >> $ [1, 2, 3]:
[2, 3]
```

If present, the function also copies the metatable and user-defined type of $t$ to the new table.

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

## f

Checks whether at least one element in table $t$ satisfies the condition defined by function f and returns true or false. f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x < 1 >> $$ [1, 2, 3]:
false
```

The return might include holes.
See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

### 10.1.2 tables Library

This library provides generic functions for table manipulation. It provides all its functions inside the table tables.

Most functions in the table library assume that the table represents an array or a list. For these functions, when we talk about the 'length' of a table we mean the result of the length operator.
tables.allocate ( $t$, key $y_{1}$, value ${ }_{1}$ [, key ${ }_{2}$, value ${ }_{2}, \cdots, k_{n}, v_{n}$ value ${ }_{n}$ )
Sets the specified keys and values to table $t$, i.e. $\dagger_{\left[k e y_{k}\right]}:=$ value $_{k}$. Note that if $a$ key is given multiple times, then only the first occurrence of the key in the argument sequence is processed. The function returns nothing.

See also: tables.include.

```
tables.array (t)
```

Returns the array part of table t in a new table, with all key~value pairs preserved.
See also: tables.hash, tables.parts.

```
tables.borders (t [, option])
```

By default, returns the smallest and largest assigned integral index - in this order - in the array part of a table $t$.

If any option is given, then the function determines the smallest and largest assigned integral index in both the array and hash part of table $t$. Note that this is slower since the entire hash part has to be searched linearly.

If zeros are returned, the array or the array and hash part of the table is empty.
See also: environ.attrib, tables.getsize, tables.indices, tables.maxn.

```
tables.dimension (a:b [, c:d, ...] [, default])
tables.dimension (a:b [, c:d, ...] [, init = default])
```

In the first form, creates a table of any dimension with arbitrary index ranges a:b etc. with $a, b$, etc. integers, and an optional default for all its entries. default must not be a pair.

In the second form the initialiser may be given as the option "init = default", which allows to also use pairs as a default.

If the initialiser is a structure, i.e. table, set, sequence or register, then individual copies of the initialiser are created to avoid referencing to the same structure.

See also: tables.newtable, create table/dict statements.

```
tables.entries (t)
```

Returns all entries of table $t$ (not its keys) in a new table array. Its second result, a Boolean, indicates whether a value has been found in the hash part of $t$.

See also: tables.indices, unique, whereis.

```
tables.getsize (t [, option])
```

Returns a guess on the number of elements in a table $t$. If any option is given, the function additionally returns a Boolean indicator on whether a table contains an allocated hash part, and a Boolean indicator on whether null has been assigned to a table. The latter return is not foolproof, especially if a table value has been deleted with a raw assignment, e.g. $\dagger[2]:=$ null;

The function is useful to determine the size of a table much more quickly than the size operator does, using a logarithmic instead of linear method, but may return incorrect results if the array part of a table has holes. It also does not count the number of elements in the hash part of a table.

See also: size, tables.getsizes.

```
tables.getsizes (t [, option])
```

If any option is given, returns the actual number of elements currently stored in the array and hash part. If no option is given, then an estimate of the number of elements in the array part will be returned, and 0 for the hash part as this cannot be estimated.

Returns two integers: the first for the array part, the second for the hash part.
See also: size, tables.getsize.

```
tables.hash (t)
```

Returns the hash part of table t in a new table with all key~value pairs preserved.
See also: tables.array, tables.parts.

```
tables.include (t, key, value [, ...])
```

Inserts values into a subtable of table $t$. If $t[k e y]$ already represents a table, value is added to the end of its array part. If $t[k e y]$ is unassigned, then it creates a new subtable and inserts value into it, which is equivalent to the pseudo code:

```
for i from 3 to nargs do
    if assigned t[key] then
        insert <argumenti> into t[key]
    else
        t[key] := [<argument i>]
    end
fi
```

The function returns nothing.
See also: copyadd, bags.include, tables.allocate.

```
tables.indices (t [, option])
```

Returns all keys of table t in an unsorted new table.
If you pass any optional argument, the function will return the integral indices of a table only. In this case, the second result, a Boolean, indicates whether at least one integral key has been found in the hash part, so you might sort the table if needed. This mode is $40 \%$ faster than the standard mode of the function.

See also: tables.borders, tables.entries, whereis.

## tables.maxn ( $t$ )

Returns the largest positive numerical index of the given table $t$, or zero if the table has no positive numerical indices. (To do its job this function does a linear traversal of the whole table.) See also tables.borders, which is faster with arrays.

```
tables.move (t1, start, stop, newidx [, t2])
```

Copies elements from the table t1 to the table t2, performing the equivalent to the following multiple assignment: t 2 [newidx], $\cdots=\mathrm{t} 1$ [start], $\cdots, \mathrm{t}$ [stop]. The default for t2 is t1, i.e. elements are shifted in the same table. The destination range can overlap with the source range.

Returns the destination table t 2 .

Example: The following statement copies four elements in table a from position 3 up to and including 6 to a new table $b$, starting with index 1 :

```
> a := ['a', 'b', 'c', 'd', 'e', 'f', 'g', 'h'];
> b := tables.move(a, 3, 6, 1, []);
> b:
[c, d, e, f]
```

The next statement copies four elements in a to its beginning:

```
> tables.move(a, 3, 6, 1);
> a:
[c, d, e, f, e, f, g, h]
```

See also: move, purge, shift, swap.

```
tables.new ([bool, ] a, b [, k])
tables.new ([bool, ] f, a, b [, k [, \cdots.]])
tables.new (n, init = default)
```

In the first form, if no Boolean bool is given as the very first argument, the function creates a table array [a, $a+k, \cdots, b-k, b]$, with $a, b$, and $k$ (the step size) being numbers. The step size is 1 if $k$ - a number - is not given. If any Boolean bool is given as the very first argument, the function generates a linearly spaced table array of $k$ numbers in the interval $[a, b]$.

In the second form, if no Boolean bool is given as the very first argument, the function returns a table array $[1 \sim f(a), 2 \sim f(a+k), \cdots,((b-a) * 1 / k+1) \sim f(b)]$, with $f a$ function, $a$ and $b$ numbers. Thus, the function f is applied to all numbers between and including a and b . If f requires two or more arguments, the second, third, etc. argument must be passed after $k$. If any Boolean bool is given as the very first argument, the function generates a linearly spaced table array of $k$ numbers in the interval $[a, b]$ with $f$ applied to all its members.

The function uses the Kahan-Babuška summation algorithm to prevent round-off errors in case the step size is non-integral.

In the third form, creates a table array of $n$ slots, pre-filled with default which may be of any type.

Examples:

```
> tables.new(<< x, y -> x:x^2 + y >>, 1, 5, 1, 10):
[1:11, 2:14, 3:19, 4:26, 5:35]
> p := [0.1, 0.2, 0.1, 0.3, 1]
```

```
> tables.new( << x -> x:p[x] >>, 1, size p):
[1:0.1, 2:0.2, 3:0.1, 4:0.3, 5:1]
> tables.new(true, -4, 4, 6):
[-4, -2.4, -0.8, 0.8, 2.4, 4]
> tables.new(8, init = 0):
[0, 0, 0, 0, 0, 0, 0, 0]
```

tables.new also accepts functions that may return null. Example:

```
> tables.new(<< x -> if x % 3 = 0 then x else null fi >>, 0, 10):
[1 ~ 0, 4 ~ 3, 7 ~ 6, 10 ~ 9]
```

See also: map, registers.new, sequences.new.
tables.newtable ( $\mathrm{a}, \mathrm{b}$ )
Returns a table with a pre-allocated array slots and b pre-allocated hash slots. a and b should be non-negative integers. If a or b is negative, zero slots will be pre-allocated with no error being issued.

The function is useful only if you have to pass a table initialiser as a function argument, otherwise it is recommended to use the create table statement.

See also: tables.dimension, create table/dict statements.

```
tables.parts (t)
```

Returns both the array and the hash part of table $t$ in two tables, with all key~value pairs preserved.

See also: tables.array, tables.hash.

```
tables.reshuffle (t)
```

The function moves all values in the hash part of table $t$ to the end of its array part, thus emptying the hash part. The function works in-place, thus destructively, and returns no result.

See also: sort, sorted.

### 10.2 Sets

Summary of Functions:
Queries
\$\$, empty, filled, in, notin, size, type, typeof.
Retrieving Values
unpack.
Operations
@, \$\$, copy, map, remove, select, selectremove.
Relational Operators
$=,==, \sim=,<>$.
Cantor Operations
intersect, minus, subset, union, xsubset.
Miscellaneous
cleanse, sets.newset, sets.resize.
cleanse (s)
Empties set s and returns the emptied structure. The memory previously occupied can be reused by the interpreter.
copy (s)
The function copies the entire contents of a set s into a new set. See Chapter 8 for more information.
empty (s)
The operator checks whether a set s does not contain any element. The return is true or false.

See also: filled.

## filled (s)

The operator checks whether a set s contains at least one element. The return is true or false.

See also: empty.
$\operatorname{map}\left(f, s[, \cdots]\left[, t_{r u e}\right)\right.$
Maps the function f on all elements of a set s. See map in Chapter 8 for more information.

See also: countitems, remove, select, selectremove, subs, and zip.
remove (f, s [, ‥] [, true])
Returns all values in set s that do not satisfy a condition determined by function f . See remove in Chapter 8 for more information.

See also: map, select, selectremove, subs, zip.
select (f, s [, $\cdot$ ] [, true])
Returns all values in set s that satisfy a condition determined by function f . See select in Chapter 8 for more information.

See also: map, remove, selectremove, subs, zip.
selectremove (f, s [, ••])
Returns all values in set s that satisfy and do not satisfy a condition determined by function $£$, in two sets. See selectremove in Chapter 8 for more information.

See also: map, remove, select, subs, zip.
size (s)
Returns the number of items in a set $s$.

## typeof (s)

Returns the user-defined type assigned to set s.

The following functions have been built into the kernel as binary operators.
Please note that the operators returning a Boolean work in a Cantor way, i.e. $\{1,1\}$ $=\{1\} \rightarrow$ true, $\{1,2\}$ xsubset $\{1,1,2,2,3,3\} \rightarrow$ true.

```
s1 三 s2
```

This equality check of two sets s1, s2 first tests whether s1 and s2 point to the same set reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 contain the same items, and returns true or false. In this case, the search is linear.

```
s1 \equiv= s2
```

With sets, the == operator acts exactly as the = operator.

```
s1 ~= s2
```

With sets, the $\sim=$ operator compares each element in s1 and s2 for approximate equality. See approx for further details. The return is either true or false.
s1 <> s2
This inequality check of two sets s1, s2 first tests whether s1 and s2 do not point to the same set reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 do not contain the same items, and returns true or false. In this case, the search is linear.
$c$ in $s$
Checks whether the set s contains the item c and returns true or false. The search is constant.

```
c notin s
```

Checks whether the set s does not contain the item c and returns true or false. The search is constant.

## s1 intersect s2

Searches all items in set s1 that are also items in set s2 and returns them in a set. The search is linear. If t 1 has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from $t 2$.

```
s1 minus s2
```

Searches all items in set s1 that are not items in set s2 and returns them as a set. The search is linear. If si has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from s2.

```
s1 subset s2
```

Checks whether all items in set s1 are included in set s2 and returns true or false. The operator also returns true if $s 1=s 2$. The search is linear.
s1 union s2
Concatenates two sets s1 and s2 simply by copying all its items to a new set. If s1 has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from s2.
s1 xsubset s2
Checks whether all items in set s1 are included in set s2 and whether s2 contains at least one further item, so that the result is always false if $s 1=s 2$. The search is linear.

## f @ s

The operator maps a function f to all the values in set s and returns a set as the result. f must be a univariate function and return only one value. If s has metamethods or user-defined types, the return will also have them.

Examples:

```
> << x -> x^2 >> @ {1, 2, 3}:
{1, 4, 9}
> << X -> X > 1 >> @ {1, 2, 3}:
{false, true}
```

See also: \$, \$\$, countitems, remove, select, selectremove, subs, and zip.

## f $\mathbf{s} \mathbf{s}$

Returns all values in set s that satisfy a condition determined by function f . f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x > 1 >> $ {1, 2, 3}:
{2, 3}
```

If present, the function also copies the metatable and user-defined type of $s$ to the new set.

See also: @, \$\$, map, remove, selectremove, subs, zip.

## f $\mathbf{\$} \mathbf{\$} \mathbf{s}$

Checks whether at least one element in set s satisfies the condition defined by function f and returns true or false. f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x < 1 >> $$ {1, 2, 3}:
false
```

sets.newset ( n )
Returns a set with $n$ pre-allocated slots. $n$ should be a non-negative integer.
The function is useful only if you have to pass a set initialiser as a function argument, otherwise it is recommended to use the create set statement.
sets.resize (s [, newsize [, true]])
Resizes set s to store at least newsize elements. If the last argument is true the number of pre-allocated slots will be adjusted to an optimum of the smallest power of 2 greater than or equal to $n$.

If only $s$ is given, the number of pre-allocated slots will be changed to the smallest power of 2 greater than or equal the current size, usually freeing formerly occupied space.

If newsize < size s or the number of pre-allocated slots would not change, the function does nothing and returns without modifying the set.

The function returns the number of allocated elements and the number of pre-allocated slots.

See also: math.nextpower, size, environ.attrib maxsize and size values.

### 10.3 Sequences

Summary of Functions:

## Queries

countitems, empty, filled, in, notin, size, typeof.
Retrieving Values
getentry, unique, unpack, values.
Operations
@, copy, copyadd, join, map, move, mulup, purge, qsumup, remove, reverse, select, selectremove, sumup, shift, sort, sorted, subs, swap, zip.

Relational Operators

$$
=,==, \sim=,<>.
$$

Cantor Operations
intersect, minus, subset, union, xsubset.

With the exception of getentry, map and zip, the following functions have been built into the kernel as unary operators.

### 10.3.1 Operators

## copy (s)

The function copies the entire contents of a sequence s into a new sequence. See Chapter 8 for more information.
copyadd (s [, ...])
See Chapter 8.
countitems (item, s)
countitems (f, s [, •.]
Counts the number of occurrences of an item in the sequence s. For further information, see Chapter 8.

## empty (s)

The operator checks whether the sequence s does not contain any element. The return is true or false. See also: filled.

## filled (s)

The operator checks whether the sequence s contains at least one element. The return is true or false. See also: empty.

```
getentry (s [, ki, \cdots, k
```

Returns the entry $s\left[k_{1}, \cdots, k_{n}\right]$ from the sequence $s$ without issuing an error if one of the given indices $k_{i}$ (second to last argument) does not exist.

```
join (s [, sep [, i [, j]]])
```

Concatenates all string values in sequence s in sequential order and returns a string: s[i] \& sep \& s[i+1] $\cdots$ \& sep \& s[j]. The default value for sep is the empty string, the default for $i$ is 1 , and the default for $j$ is the length of the sequence. The function issues an error if s contains non-strings.

Use the tostring function if you want to concatenate other values than strings, e.g.:

```
> join(map(tostring, seq(1, 2, 3))):
123
map (f, s [, \cdots.] [, true])
```

Maps the function f on all elements of a sequence s. See map in Chapter 8 for more information. See also: remove, select, subs, zip.
move (s1, start, stop, newidx [, s2])
Copies elements from sequence s1 to sequence s2, performing the equivalent to the following multiple assignment: s2[newidx], $\cdots=s 1$ [start], $\cdots$, s1[stop]. The default for s2 is s1, i.e. elements are shifted in the same sequence. The destination range can overlap with the source range.

Returns the destination sequence s2.
See also: purge, put.

## mulup (s)

Multiplies all numeric values in sequence s. See mulup in Chapter 8 for more information. See also: sumup.

```
purge (s [, pos])
purge (s, a, b)
```

In the first form, the function removes from sequence s the element at position pos, shifting down other elements to close the space, if necessary. Returns the value of the removed element, or nothing if pos is invalid. The default value for pos is $n$, where n is the length of the sequence, so that a call purge(s) removes the last element of $s$.

In the second form, it removes all elements starting from index a to index b (inclusive), moving excess elements down to close the space; the function automatically performs a garbage collection after shifting. In the $2^{\text {nd }}$ form, nothing will be returned.

See also: move, put.

## qsumup (s)

Raises all numeric values in sequence s to the power of 2 and sums up these powers. See qsumup in Chapter 8 for more information. See also: sumup.

```
remove (f, s [, \cdots.] [, true])
```

Returns all values in sequence s that do not satisfy a condition determined by function f. See remove in Chapter 8 for more information. See also: map, select, subs, zip.

## reverse (s)

Reverses the order of all elements in a sequence s in-place. The function returns the modified structure.

See also: strings.reverse, stack.reversed.
select (f, s [, …] [, true])
Returns all values in sequence s that satisfy a condition determined by function f . See select in Chapter 8 for more information. See also: map, remove, subs, zip.
selectremove (f, s [, ...])
Returns all values in sequence s that satisfy and do not satisfy a condition determined by function $f$, in two sequences. See selectremove in Chapter 8 for more information. See also: map, remove, select, subs, zip.

```
shift (s, a, b)
```

Moves an element in sequence s from position old to new, with old, new integers, shifting all the other elements accordingly - which might also cause a rotation. The function returns nothing.

See also: move, purge, swap.
size (s)
Returns the number of items in a sequence s.

```
sort (s [, comp])
```

Sorts sequence s in a given order, and in-place. See sort in Chapter 8 for more information. See also: sorted, skycrane.sorted, stats.issorted, stats.sorted.

```
sorted (s [, comp])
```

Sorts sequence elements in s in a given order, but - unlike sort - not in-place, and non-destructively. See sorted in Chapter 8 for more information. See also: sort, skycrane.sorted, stats.issorted, stats.sorted.

```
subs (x:v [, ...], s [, true])
```

Substitutes all occurrences of the value x in sequence s with the value v . See subs in Chapter 8 for more information. See also: map, remove, select, zip.

```
sumup (s)
```

Sums up all numeric values in sequence s. See sumup in Chapter 8 for more information. See also: qsumup.

```
swap (s, a, b)
```

In sequence s, swaps the entries at index positions a and $b$, with $a, b$ integers. The function returns nothing.

See also: move, purge, shift.

```
typeof (s)
```

Returns the user-defined type assigned to sequence s.

## unique (s)

With a sequence s, the function removes multiple occurrences of the same item, if present in s. See unique in Chapter 8 for more information.
values (s, $i_{1}\left[, i_{2}, \cdots\right]$ )
Returns the elements from the given sequence $s$ in a new sequence. This function is equivalent to

```
return seq( s[i_i_, s[i\mp@subsup{i}{2}{}], \cdots. )
```

See also: ops, select, unpack.

```
zip (f, s1, s2)
```

This function zips together two sequences s1, s2 by applying the function f to each of its respective elements. See Chapter 8 for more information. See also: map, remove, select, subs.

See also: bintersect, bisequal, bminus, purge, put in Chapter 8 Basic Functions.

Following are the binary operators.
Please note that the operators returning a Boolean work in a Cantor way, i.e. seq ( 1 , 1) $=\operatorname{seq}(1) \rightarrow$ true, seq(1, 2) xsubset seq(1, 1, 2, 2, 3, 3) $\rightarrow$ true.

```
s1 \equiv s2
```

This equality check of two sequences s1, s2 first tests whether s1 and s2 point to the same sequence reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 contain the same values without regard to their keys, and returns true or false. In this case, the search is quadratic.

```
s1 == s2
```

This strict equality check of two sequences s1, s2 first tests whether s1 and s2 point to the same sequence reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 contain the same number of elements and whether all entries in the sequences are the same and are in the same order, and returns true or false. In this case, the search is linear.

```
s1 ~= s2
```

This approximate equality check of two sequences s1, s2 first tests whether s1 and s2 point to the same sequence reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 contain the same number of elements and whether all entries in the sequences are approximately equal and are in the same order, and returns true or false. In this case, the search is linear. See approx for further information on the approximation check.
s1 <> s2
This inequality check of two sequences s1, s2 first tests whether s1 and s2 do not point to the same sequence reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 do not contain the same values, and returns true or false. In this case, the search is quadratic.

## $c$ in $s$

Checks whether the sequence s contains the value c and returns true or false. The search is linear. See also binsearch for binary search.

```
c notin s
```

Checks whether the sequence s does not contain the value c and returns true or false. The search is linear.

See also: in operator.

```
s1 intersect s2
```

Searches all values in sequence s1 that are also values in sequence s2 and returns them in a sequence. The search is quadratic. If si has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from s2.

```
s1 minus s2
```

Searches all values in sequence s1 that are not values in sequence s2 and returns them as a sequence. The search is quadratic. If si has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from s2.

```
s1 subset s2
```

Checks whether all values in sequence s1 are included in sequence s2 and returns true or false. The operator also returns true if $s 1=s 2$. The search is quadratic.

```
s1 union s2
```

Concatenates two sequences s1 and s2 simply by copying all its elements - even if they occur multiple times - to a new sequence. If si has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from s2.

## s1 xsubset s2

Checks whether all values in sequence s1 are included in sequence s2 and whether s2 contains at least one further element, so that the result is always false if $s 1=s 2$. The search is quadratic.

## f @ s

The operator maps a function f to all the values in sequence s and returns $a$ sequence as the result. f must be a univariate function and return only one value. If s has metamethods or user-defined types, the return will also have them.

Examples:

```
> << x -> x^2 >> @ seq(1, 2, 3):
seq(1, 4, 9)
> << x -> x > 0 >> @ seq(1, 2, 3):
seq(true, true, true)
```

See also: \$ and \$\$ operators.

## f $\$$

Returns all values in sequence s that satisfy a condition determined by function $£$. f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << X -> X > 1 >> $ seq(1, 2, 3):
seq(2, 3)
```

If present, the function also copies the metatable and user-defined type of obj to the new sequence.

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

## f

Checks whether at least one element in sequence s satisfies the condition defined by function f and returns true or false. f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x < 1 >> $$ seq(1, 2, 3):
false
```

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

The following functions in the base library also support sequences:

| Function | Meaning |
| :--- | :--- |
| bintersect | Same as the intersect operator but much faster with very <br> large sequences. |
| bisequal | Same as the = operator but much faster with very large <br> sequences. |
| bminus | Same as the minus operator but much faster with very large <br> sequences. |
| duplicates | Returns all the values that are stored more than once in the <br> given sequence. |

### 10.3.2 sequences Library

This library provides generic functions for sequence manipulation. It provides all its functions inside the table sequences.

```
sequences.dimension (a:b [, c:d, \cdots] [, default])
sequences.dimension (a:b [, c:d, ...] [, init = default])
```

In the first form, creates a sequence of any dimension with index ranges a:b etc. with $a, b$, etc. integers, and an optional default for all its entries. default must not be a pair. The left-hand side values $a, c, \ldots$ of the dimensions must always be 1 .

In the second form the initialiser may be given as the option "init = default", which allows to also use pairs as a default.

If the initialiser is a structure, i.e. table, set, pair, sequence or register, then individual copies of the initialiser are created to avoid referencing to the same structure.

See also: sequences.newtable, create sequence statements.

```
sequences.new ([bool, ] a, b [, k])
sequences.new ([bool, ] f, a, b [, k [, \cdots.]]])
sequences.new (n, init = default)
```

In the first form, if no Boolean bool is given as the very first argument, the function creates a sequence seq( $a, a+k, \cdots, b-k, b)$, with $a, b$, and $k$ (the step size) being numbers. The step size is 1 if $k$ - a number - is not given. If any Boolean bool is given as the very first argument, the function generates a linearly spaced sequence of $k$ numbers in the interval $[a, b]$.

In the second form, if no Boolean bool is given as the very first argument, the function returns a sequence seq( $1 \sim f(a), 2 \sim f(a+k), \cdots,((b-a) * 1 / k+1) \sim f(b))$, with $f$ a function, a and b numbers. Thus, the function f is applied to all numbers between and including a and $b$. If $f$ requires two or more arguments, the second, third, etc. argument must be passed after $k$. If any Boolean bool is given as the very first
argument, the function generates a linearly spaced sequence of $k$ numbers in the interval $[a, b]$ with $f$ applied to all its members.

The function uses the Kahan-Babuška summation algorithm to prevent round-off errors in case the step size is non-integral.

In the third form, creates a sequence of $n$ slots, pre-filled with default which may be of any type.

Examples:

```
> sequences.new(<< x, y -> x:x^2 + y >>, 1, 5, 1, 10):
seq(1:11, 2:14, 3:19, 4:26, 5:35)
> p := seq(0.1, 0.2, 0.1, 0.3, 1)
> sequences.new( << x -> x:p[x] >>, 1, size p):
seq(1:0.1, 2:0.2, 3:0.1, 4:0.3, 5:1)
> sequences.new(true, -4, 4, 6):
seq(-4, -2.4, -0.8, 0.8, 2.4, 4)
> sequences.new(8, init = 0):
seq(0, 0, 0, 0, 0, 0, 0, 0)
```

sequences.new also accepts functions that may return null. In this case, an element is not added to the resulting structure. Example:

```
> sequences.new(<< x -> if x % 3 = 0 then x else null fi >>, 0, 10):
seq(0, 3, 6, 9)
```

See also: map, tables.new, registers.new.

## sequences.newseq ( n )

Returns a sequence with $n$ pre-allocated slots. $n$ should be a non-negative integer.
The function is useful only if you have to pass a sequence initialiser as a function argument, otherwise it is recommended to use the create sequence statement.

See also: sequences.dimension.

## sequences.resize (s [, newsize [, true]])

Resizes sequence s to the given number of pre-allocated slots. If you actually shrink a sequence, then it discards any surplus elements.

The function returns the number of allocated elements and the number of pre-allocated slots, which may be vacant.

If newsize is 0 or newsize is less than the current size, then the function also purges all surplus values in the sequence.

If the optional third argument is true and newsize is non-zero, then the function sets the optimum number of pre-allocated slots to the smallest power of 2 greater than or equal to newsize.

If you pass just s without any further arguments, the function automatically allocates to the optimum number of slots without dropping any values.

Note that Agena automatically enlarges and shrinks a sequence if necessary when adding new or purging existing values, see environ.kernel/seqautoshrink.

See also: math.nextpower, size, environ.attrib maxsize and size values.

### 10.4 Registers

Summary of Functions:

## Queries

countitems, filled, in, size.
Retrieving Values
getentry, unique, unpack, values.
Operations
copy, copyadd, join, map, move, mulup, purge, remove, replace, sumup, select, selectremove, shift, sort, sorted, subs, swap, zip.

Relational Operators

$$
=,==, \sim=,<>.
$$

Cantor Operations
intersect, minus, subset, union, xsubset.

With the exception of getentry, map and zip, the following functions have been built into the kernel as unary operators:

### 10.4.1 Operators

## copy (r)

The function deep-copies the entire contents of a register $r$ into a new register. See Chapter 8 for more information.
copyadd (r [, …])
See Chapter 8.
countitems (item, r)
countitems (f, r [, ...])
Counts the number of occurrences of an item in the register r. For further information, see Chapter 8.

```
duplicates (r [, option])
```

Returns all the values that are stored more than once to the given register $r$, and returns them in a new register. Each duplicate will be returned only once.

If option is not given, the structure is sorted before evaluation since this is needed to determine all duplicates. The original structure is left untouched, however.

The total size of the new register is equal to the number of the elements in the result.
If a value of any type is given for option, the function assumes that the register has been already sorted. Otherwise it is suggested to use skycrane.sorted before the call to duplicates if the register contains values of different types, to prevent errors.

The function is written in Agena and included in the lib/library.agn file.
empty ( $r$ )
The operator checks whether the register $r$ does not contain any element. The return is true or false. See also: filled.

## filled (r)

The operator checks whether the register $r$ contains at least one element. The return is true or false. See also: empty.
getentry ( $\mathrm{r}\left[, \mathrm{k}_{1}, \cdots, \mathrm{k}_{\mathrm{n}}\right.$ ])
Returns the entry $r\left[k_{1}, \cdots, k_{n}\right]$ from the register $r$ without issuing an error if one of the given indices $k_{i}$ (second to last argument) does not exist.

```
join (r [, sep [, i [, j]]])
```

Concatenates all string values in register $r$ in sequential order and returns a string: $r[i] \& \operatorname{sep} \& r_{[i+1]} \cdots$ \& sep $\& r_{[j]}$. The default value for sep is the empty string, the default for $i$ is 1 , and the default for $j$ is the top of the register. The function issues an error if s contains non-strings.
$\operatorname{map}(f, r[, \cdots])$
Maps the function $£$ on all elements of a register r. See map in Chapter 8 for more information.

See also: has, remove, select, subs, zip.

```
move (r1, start, stop, newidx [, r2])
```

Copies elements from register $r 1$ to register $r 2$, performing the equivalent to the following multiple assignment: $r_{2}\left[\right.$ newidx],$\cdots=r_{1}$ [start], $\cdots, r_{1}$ [stop]. The default for $r 2$ is r1, i.e. elements are shifted in the same register. The destination range can overlap with the source range.

Returns the destination register $r 2$.
See also: purge, put, swap.
mulup ( r )
Multiplies all numeric values in register r. See mulup in Chapter 8 for more information. See also: sumup.

```
purge (r [, pos])
purge (r, a, b)
```

In the first form, the function removes from register $r$ the element at position pos, shifting down other elements to close the space, if necessary. Returns the value of the removed element, or nothing if pos is invalid. The default value for pos is $n$, where n is the length of the register, so that a call purge(r) removes the last element of $r$.

In the second form, removes all elements starting from index a to index b (inclusive), moving excess elements down to close the space; the function automatically performs a garbage collection after shifting. In the $2^{\text {nd }}$ form, nothing will be returned.

Note that the function also reduces the top pointer of $r$ by the number of elements removed.

See also: move, put, shift, swap.

## qsumup ( $r$ )

Raises all numeric values in register $r$ to the power of 2 and sums up these powers. See qsumup in Chapter 8 for more information. See also: sumup.

```
remove (f, r [, \cdots.] [, true])
```

Returns all values in register $r$ that do not satisfy a condition determined by function f. The total size of the new register is equal to the number of the elements in the result. See remove in Chapter 8 for more information. See also: map, select, subs, zip.

```
select (f, r [, \cdots.] [, true])
```

Returns all values in register $r$ that satisfy a condition determined by function $f$. The total size of the new register is equal to the number of the elements in the result. See select in Chapter 8 for more information. See also: map, remove, subs, zip.
selectremove (f, r [, ••])
Returns all values in register $r$ that satisfy and do not satisfy a condition determined by function $f$, in two new registers. The total size of the new registers is equal to the number of the elements in the respective results. See selectremove in Chapter 8 for more information.

See also: map, remove, select, subs, zip.
shift ( $\mathrm{r}, \mathrm{a}, \mathrm{b}$ )
Moves an element in register $r$ from position old to new, with old, new integers, shifting all the other elements accordingly - which might also cause a rotation. The function returns nothing.

See also: move, purge, swap.
size (r)
Returns the total number of items assignable in register $r$.

```
sort (r [, comp])
```

Sorts register $r$ in a given order, and in-place. All the values in the register up to the position pointed to by the size operator must be of the same type and non-null. See sort in Chapter 8 for more information. See also: sorted.

```
sorted (r [, comp])
```

Sorts register elements in $r$ in a given order, but - unlike sort - not in-place, and non-destructively. All the values in the register up to the position pointed to by the size operator must be of the same type and non-null. See sorted in Chapter 8 for more information.

See also: sort.

```
subs (x:v [, \cdots.], r)
```

Substitutes all occurrences of the value x in register r with the value v . See subs in Chapter 8 for more information.

See also: map, remove, select, zip.

## sumup ( $r$ )

Sums up all numeric values in register r. See sumup in Chapter 8 for more information. See also: qsumup.

```
swap (r, a, b)
```

In registers $r$, swaps the entries at index positions a and $b$, with $a, b$ integers. The function returns nothing.

See also: move, purge.

```
unique (r)
```

With a register $r$, the unique function removes multiple occurrences of the same item, if present in $r$, and returns a new register. The total size of the new register is equal to the number of the elements in the result. See unique in Chapter 8 for more information.

```
values (r, in [, in, \cdots]])
```

Returns the elements from the given register $r$ in a new register. This function is equivalent to

```
return reg( r[i_1], r[i\mp@subsup{i}{2}{}], \cdots. )
```

The total size of the new register is equal to the number of the elements in the result. See also: ops, select, unpack.

```
zip (f, r1, r2)
```

This function zips together two registers $r 1, r 2$ by applying the function $f$ to each of its respective elements. See Chapter 8 for more information. See also: map, remove, select, subs.

The following functions have been built into the kernel as binary operators.
Please note that the operators returning a Boolean work in a Cantor way, i.e. reg (1, 1) $=\operatorname{reg}(1) \rightarrow$ true, $r e g(1,2)$ xsubset $\operatorname{reg}(1,1,2,2,3,3) \rightarrow$ true.
$r 1 \equiv r 2$
This equality check of two registers r1, r2 first tests whether r1 and r2 point to the same register reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 contain the same values without regard to their keys, and returns true or false. In this case, the search is quadratic.
r1 三= r2
This strict equality check of two registers r1, r2 first tests whether r1 and r2 point to the same register reference in memory. If so, it returns true and quits.

If not, the operator then checks whether r1 and r2 contain the same number of elements and whether all entries in the registers are the same and are in the same order, and returns true or false. In this case, the search is linear.
r1 ~= r2
This approximate equality check of two registers $r 1, r 2$ first tests whether $r 1$ and $r 2$ point to the same register reference in memory. If so, it returns true and quits.

If not, the operator then checks whether r1 and r2 contain the same number of elements and whether all entries in the registers are approximately equal and are in the same order, and returns true or false. In this case, the search is linear. See approx for further information on the approximation check.

```
r1 <> r2
```

This inequality check of two registers s1, s2 first tests whether s1 and s2 do not point to the same register reference in memory. If so, it returns true and quits.

If not, the operator then checks whether s1 and s2 do not contain the same values, and returns true or false. In this case, the search is quadratic.
$c$ in $r$
Checks whether the register s contains the value c and returns true or false. The search is linear. See also binsearch for binary search.

## r1 intersect r2

Searches all values in register $r 1$ that are also values in register $r 2$ and returns them in a new register. The search is quadratic. The total size of the new register is equal to the number of the elements in the result. If r1 has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from $r 2$.

```
r1 minus r2
```

Searches all values in register $r 1$ that are not values in register $s r 2$ and returns them as a new register. The search is quadratic. The total size of the new register is equal to the number of the elements in the result. If ri has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from r 2 .
r1 subset r2
Checks whether all values in register $r 1$ are included in register $r 2$ and returns true or false. The operator also returns true if $r 1=r 2$. The search is quadratic. The total size of the new register is equal to the number of the elements in the result.

```
r1 union r2
```

Concatenates two registers r1 and $r 2$ simply by copying all its elements - even if they occur multiple times - to a new register. The total size of the new register is equal to the number of the elements in the result. If $r 1$ has a metatable and/or a user-defined type, then they will be copied to the result; otherwise the function will try to copy them from r 2 .

## r1 xsubset r2

Checks whether all values in register $r 1$ are included in register $r 2$ and whether $r 2$ contains at least one further element, so that the result is always false if $r 1=r 2$. The search is quadratic. The total size of the new register is equal to the number of the elements in the result.

```
f @ r
```

In the first form, the operator maps a function f to all the values in register r . f should be a univariate function and return only one value. The return is a register. If $r$ has metamethods or user-defined types, the return will also have them.

Examples:

```
> << x -> x^2 >> @ reg(1, 2, 3):
reg(1, 4, 9)
> << x -> x > 1 >> @ reg(1, 2, 3):
reg(false, true, true)
```

See also: @ and \$\$ operators, map, reduce, remove, select, subs, times, zip.

## f

Returns all values in register $r$ that satisfy a condition determined by function $£$. $£$ should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x > 1 >> $ reg(1, 2, 3):
[2, 3]
```

If present, the function also copies the metatable and user-defined type of $r$ to the new register.

All values up to the current top pointer are evaluated, and the size of the returned register is equal to the number of the elements in the return.

See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

```
f \(\mathbf{\$ \$} \mathbf{r}\)
```

Checks whether at least one element in register $r$ satisfies the condition defined by function f and returns true or false. f should be a univariate function and return at least one value. In the multivariate case, all results but the first are ignored.

```
> << x -> x < 1 >> $$ reg(1, 2, 3):
false
```

All values up to the current top pointer are evaluated.
See also: @ operator, countitems, descend, map, remove, selectremove, subs, unique, values, zip.

The following functions in the base library also support registers:

### 10.4.2 registers Library

This library provides generic functions for register manipulation. It provides all its functions inside the table registers.

```
registers.dimension (a:b [, c:d, ...] [, default])
registers.dimension (a:b [, c:d, ...] [, init = default])
```

In the first form, creates a register of any dimension with index ranges a:b etc. with a, b, etc. integers, and an optional default for all its entries. default must not be a pair. The left-hand side values $a, c, \ldots$ of the dimensions must always be 1 .

In the second form the initialiser may be given as the option "init = default", which allows to also use pairs as a default.

If the initialiser is a structure, i.e. table, set, pair, sequence or register, then individual copies of the initialiser are created to avoid referencing to the same structure.

See also: registers.newtable, create register statements.

## registers.extend ( $r, n$ )

Extends the given register $r$ to - and not by - the given number of elements. All the elements already residing in $r$ are kept. If $n$ is less or equal to the current top (see
size), the structure is left unchanged and false will be returned - otherwise returns true.

See also: registers.reduce.

```
registers.new ([bool, ] a, b [, k])
registers.new ([bool, ] f, a, b [, k [, ...]])
registers.new (n, init = default)
```

In the first form, if no Boolean bool is given as the very first argument, the function creates a register reg(a, $a+k, \cdots, b-k, b)$, with $a, b$, and $k$ (the step size) being numbers. The step size is 1 if $k$ - a number - is not given. If any Boolean bool is given as the very first argument, the function generates a linearly spaced register of $k$ numbers in the interval $[a, b]$.

In the second form, if no Boolean bool is given as the very first argument, the function returns a register reg(1~f(a), 2~f(a+k), $\cdots,((b-a) * 1 / k+1) \sim f(b))$, with $f a$ function, a and b numbers. Thus, the function f is applied to all numbers between and including a and b. If $f$ requires two or more arguments, the second, third, etc. argument must be passed after $k$. If any Boolean bool is given as the very first argument, the function generates a linearly spaced register of $k$ numbers in the interval $[a, b]$ with $f$ applied to all its members.

The function uses the Kahan-Babuška summation algorithm to prevent round-off errors in case the step size is non-integral.

In the third form, creates a register of $n$ slots, pre-filled with default which may be of any type.

## Examples:

```
> registers.new(<< x, y -> x:x^2 + y >>, 1, 5, 1, 10):
reg(1:11, 2:14, 3:19, 4:26, 5:35)
> p := reg(0.1, 0.2, 0.1, 0.3, 1)
> registers.new( << x -> x:p[x] >>, 1, size p):
reg(1:0.1, 2:0.2, 3:0.1, 4:0.3, 5:1)
> registers.new(true, -4, 4, 6):
reg(-4, -2.4, -0.8, 0.8, 2.4, 4)
> registers.new(8, init = 0):
reg(0, 0, 0, 0, 0, 0, 0, 0)
```

registers.new also accepts functions that may return null. Example:

```
> registers.new(<< x -> if x % 3 = 0 then x else null fi >>, 0, 10):
reg(0, null, null, 3, null, null, 6, null, null, 9, null)
```


## See also: map, tables.new, sequences.new.

registers.newreg ( n )
Returns a register with n pre-allocated slots. n should be a non-negative integer.
The function is useful only if you have to pass a register initialiser as a function argument, otherwise it is recommended to use the create register statement.

See also: registers.dimension.
registers.reduce ( $r, n$ )
Reduces register r to - and not by - to the first n given number of elements. All the elements residing above are removed. If the current top pointer is greater than $n$, it is reset to $n$.

See also: registers.extend.
registers.settop ( $r, n$ )
Sets the current position of the pointer to the top of register $r$ to the given position $n$, a non-negative integer. Values above this position cannot be altered by any functions and operators. It returns true on success, and false otherwise. If the return is false, the current position of the top pointer has not been changed.

See also: size.

### 10.5 Pairs

Summary of Functions:

## Queries

in, notin, left, right, size, type, typeof.
Operations
copy, map.
Relational Operators

$$
=,==, \sim=,<>.
$$

The following functionality has been built into the kernel as unary operators:
copy (p)
The function deep-copies the entire contents of a pair p into a new pair.
$\operatorname{map}(f, p[, \cdots])$
Maps the function f on both elements of a pair p and returns a new pair. See map in Chapter 8 for more information.
size ( p )
Returns the number of items in a pair p, i.e. always returns 2.
type ( $p$ )
Returns the type of a pair p, i.e. the string 'pair'.
typeof (p)
Returns either the user-defined type of the pair p, or the basic type 'pair'.

The following functionality has been built into the kernel as binary operators.

```
p1 \equiv p2
```

This equality check of two pairs p1, p2 first tests whether p 1 and p 2 point to the same pair reference in memory. If so, it returns true and quits.

If not, the operator then checks whether the left-hand side of pi and the left-hand side of p2 are equal, and the same with both right-hand sides, and returns true or false.

```
p1 \equivE p2
```

With pairs, the $==$ operator acts exactly as the $=$ operator.

```
p1 ~= p2
```

With pairs, the $\sim=$ operator compares the left-hand side of p 1 and the left-hand side of p 2 for approximate equality, and the same with both right-hand sides. The return is either true or false. See approx for further details.

```
p1 <> p2
```

This inequality check of two pairs p1, p2 first tests whether p1 and p2 do not point to the same set reference in memory. If so, it returns true and quits.

If not, the operator then checks whether p1 and p2 do not contain the same items, and returns true or false.

## $c$ in $p$

Checks whether the number c fits into the closed interval with borders denoted by the numeric elements of pair $p$, and returns true or false.

```
c notin p
```

Checks whether the number c does not fit into the closed interval with borders denoted by the numeric elements of pair $p$, and returns true or false.

## 10.6 numarray - Numeric C Arrays

As a plus package, the numarray package is not part of the standard distribution and must be activated with the import statement, i.e. import numarray.

### 10.6.1 Introduction

The numarray package implements arrays of the C data types of either double, unsigned char, unsigned 2-byte and signed or unsigned 4-byte integers. The unsigned char type also supports bit fields.

The arrays implemented by this package are called numarrays for short.
Since numbers stored to numarrays consume less space, numarrays may be useful if a large amount of numbers have to be processed, but the amount of random-access memory of your system is limited.

While any element in a sequence, for example, occupies 24 bytes of memory, a number in a numeric stack takes only eight bytes, and a character in a character stack only one byte.

Also, numarrays are useful to store binary data. Operations on numarrays, however, are usually slower than those on Agena's native structures: tables, pairs, sequences or registers - so you will trade speed for memory.

Internally, numarrays are userdata structures that also support various metamethods.

You can create numarrays, assign and read numbers, resize arrays, store them to binary files, and read from files.

Functions to convert arrays to Agena's native structures, and vice versa, are provided, as well.

To create an array of unsigned chars, use numarray.uchar, of signed 64-bit doubles use numarray.double, of 16-bit unsigned integers use numarray.ushort, of 32-bit unsigned integers use numarray.uint32 and of 32-bit signed integers use numarray.int32. The number of entries to be stored must be given when calling these three procedures. When creating arrays, all slots are automatically filled with zeros. Array indices count from 1, not 0 . You can pass negative indices to access values from the end of an array.

Agena's standard indexing functions save and read numbers. So, for example, a[1] $:=-1$ stores the number -1 to index 1 of the array $a$. $a[1]$ reads the value stored at index 1 of the array a. Alternatively, numarray.setitem and numarray.getitem save and read numbers, respectively. Furthermore, numarray.include (bulk-assigns) numbers.

Arrays can be shrunk or extended with the numarray.resize function.

Arrays can be converted to sequences and registers with numarray.toseq and numarray.toreg. numarray.toarray creates arrays from tables, sequences and registers.

Functions numarray.setbit, numarray.getbit, numarray.iterate support bit fields with unsigned char arrays.
numarray.whereis searches for numbers, and numarray.iterate can sequentially traverse arrays.
numarray.write writes the contents of any array to a binary file. numarray.readuchars reads a complete file of unsigned chars, numarray.readushorts of unsigned 2-byte integers, numarray.readdoubles of doubles, numarray.readlongdoubles of longdoubles (see long package) and numarray.readintegers of signed integers with only one call. To open and close these files, use binio.open and binio.close. Most other binio function, such as binio.sync, binio.rewind, and binio.filepos, is supported, as well, with the exception of the binio.read* procedures. The low-level numarray.read function is used by the above mentioned numarray.read* functions.

The following metamethods exist: standard read and write indexing (see above), in and notin operators, strict and approximate equality $(=,==,<>, \sim=, \sim<>$ operators), size, zero, nonzero and `tostring`. To easily add further metamethods, have a look at the end of the lib/numarray.agn source file.

The arrays can store status information or other data in a special registry table that is available at pseudo-index position 0 . You can use the index metamethod or numarray.getitem to read from or write data into this table, e.g. n[0] or numarray.getitem(n, 0).

### 10.6.2 Functions

numarray. convert (f, a [, ..] )
Same as numarray.map, but processes in-place: Maps a function $f$ on each element in the numarray a and changes the entries accordingly, i.e. the array elements will be transformed from $a[1]$ to $f(a[1])$, etc. $f$ must always return $a$ number.

```
numarray.cycle (a [, i [, p, [, true]]])
```

Like numarry.iterate, but cycles through the numarray a, restarting from the i-th element which is 1 by default. For arguments $p$ and true, see numarray.iterate.
numarray. double ( $n$ )
Creates a numarray of (signed) doubles (C double) with the given number of entries $n$, with $n$ an integer, and with each slot set to the number 0 .

Initially, the number of elements can be zero or more, use numarray.resize to extend the array before assigning values.

## See also: numarray.int32, numarray.longdouble, numarray.uint32, numarray.uchar, numarray.ushort.

numarray.getitem (a, i [, n])
With a any numarray, returns the value stored at a[i], where $i$, the index, is an integer counting from 1. The function is provided to avoid the index metamethod overhead.

If $n$ is given, then besides a[i], the values a[i+1] ... a[i + $n-1]$ are also returned as additional results. The default for n is 1 .

See also: numarray.iterate, numarray.setitem, numarray.replicate, numarray.subarray.

```
numarray.getbit (a, i)
```

Returns the bit at index position i of uchar array a. i starts from 1, the rightmost bit, not zero.

The return is either 0 or 1 .
See also: getbit, numarray.setbit, numarray.iterate.

```
numarray.getsize (a)
```

Returns the number of slots used by the numarray.

```
numarray.include (a, pos, b)
numarray.include (a, i, x)
```

In the first form, copies all values in the numarray b into the numarray $a$, starting at index pos (a number) of a. The function returns nothing. Both numarrays must by of the same type: either be uchar, integer, or double arrays. See also numarray.setitem.

In the second form, inserts a new number x into an array. First, the array is enlarged by one slot, all values starting at position i (thus including the value already stored at a [ i ]) are pushed to open space and finally the number x is assigned to $\mathrm{a}[\mathrm{i}]$.

The function returns nothing.
numarray.int32 ( n )
Creates a numarray of signed 4-byte integers ( C int32_t) with the given number of entries $n$, with $n$ an integer, and with each slot set to the number 0 . Initially, the number of elements can be zero or more.

See also: numarray.double, numarray.resize, numarray.uchar, numarray.uint32, numarray.ushort.
numarray.iterate (a [, i [, p, [, true]]])
Returns an iterator function that when called returns the next value in the numarray userdata structure $a$, or null if there are no further entries in the structure.

If an index $i$ is passed, the first call to the iterator function returns the $i$-th element in the numarray list and with subsequent calls, the respective elements after index i.

You may also pass a positive integer step p to the iterator function: If given, then in subsequent calls the p-th element after the respective current one will be returned, equivalent to giving an optional step size in numeric for loops.

Bit Fields can be iterated one after the other by passing the fourth argument, the Boolean value true. (You may set $i$ and $p$ to 1 each to traverse all bits.)

Example 1: C doubles

```
> import numarray
> a := numarray.double(3)
> for i to 3 do a[i] := i * Pi od
> f := numarray.iterate(a, 2): # return all values starting with index 2
procedure(01CDC200)
> f():
6.2831853071796
> f():
9.4247779607694
> f(): # no more values in a
null
```

Example 2: Bit Fields

```
> import numarray as n
> a := n.uchar(1)
> for i to 8 do n.setbit(a, i, 1) od
> n.get(a, 1):
255
```

```
> f := numarray.iterate(a, 1, 1, true) # iterate each bit, from the right
> f():
1
(etc.)
```

See also: numarray.cycle.

```
numarray.longdouble (n)
```

Creates a numarray of (signed) longdoubles (C long double) with the given number of entries $n$, with $n$ an integer, and with each slot set to the number 0 . Check the long package for further information.

Initially, the number of elements can be zero or more, use numarray.resize to extend the array before assigning values.

See also: numarray.int32, numarray.double, numarray.uint32, numarray.uchar, numarray.ushort.

```
numarray.map (f, a [,\cdots] [, true])
```

Maps a function f on each element in the numarray a and returns a new numarray with the mapped results, i.e. the new array includes the values $£(a[1]), f(a[2])$, etc. $f$ must always return a number.

If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original array, but saving memory. After completion, the function returns the modified array.

See also: numarray.convert, numarray.subs.
numarray.purge (a, i [, bool])
Removes the value stored at a[i], shifting down other elements to close the space, and by default reduces the size of the array by one slot. If the array already is of size 0 , an error will be returned. The function returns the value deleted.

If bool is false, the size of the array is not reduced. Instead, the last entry of the array is set to 0 . Use numarray.resize if you want to finally shrink the array to its new smaller size. Passing the false option may be useful to avoid memory re-allocation overhead when deleting a lot of values at one time.

See also: numarray.include, numarray.setitem.

Reads data from the file denoted by its filehandle fh and returns a numarray userdata structure of unsigned C chars.

The file must be opened before with binio.open and must finally be closed with binio.close.

In general, the function reads in a limited amount of bytes per call. If only fh is passed, the number of bytes read is determined by the environ.kernel('buffersize') setting, usually 512 bytes.

You can pass the second argument bufsize, a positive integer, to read less or more bytes. Passing the bufsize argument may also be necessary if your platform requires that an internal input buffer is aligned to a certain block size.

The function increments the file position thereafter so that the next bytes in the file can be read with a new call to numarray.read.

If the end of the file has been reached, or there is nothing to read at all, null will be returned.

In case of an error, it quits with the respective error. Use one of the following functions to read an entire file with only one call: numarray.readdoubles, numarray.readintegers, numarray.readuchars.
numarray.readdoubles (fh [, bufsize])
Reads all the numeric data from the file denoted by its filehandle $f$ f and returns a numarray of C doubles.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function however reads in the entire file with only one call, too.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).
numarray.readintegers (fh [, bufsize])
Reads all the numeric data from the file denoted by its filehandle fh and returns a numarray of C (signed) int32_t's.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function however reads in the entire file with only one call, too.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).

```
numarray.readlongdoubles (fh [, bufsize])
```

Reads all the numeric data from the file denoted by its filehandle fh and returns a numarray of C long doubles, see long package.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function reads in the entire file with only one call, too.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).

```
numarray.readuchars (fh [, bufsize])
```

Reads all the numeric data from the file denoted by its filehandle fh and returns a numarray of $C$ unsigned chars.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function however reads in the entire file with only one call, as well.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).

```
numarray.readuint32 (fh [, bufsize])
```

Reads all the numeric data from the file denoted by its filehandle $f$ f and returns a numarray of $C$ unsigned uint32_t's.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function however reads in the entire file with only one call, too.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).
numarray.readushorts (fh [, bufsize])
Reads all the numeric data from the file denoted by its filehandle $f$ h and returns a numarray of 16 -bit $C$ unsigned integers.

By default, the function internally uses an input buffer of environ.kernel('buffersize') bytes, but you may choose another setting by passing the bufsize option. When passing an alternative buffer size, the function however reads in the entire file with only one call, too.

The file must be opened before with binio.open and finally be closed with binio.close.

The function is written in Agena (see lib/numarray.agn).
numarray.remove (f, a [, …] [, true])
Returns all values in numeric array a that do not satisfy a condition determined by function f and returns a new array, or null if the condition has not been satisfied at all.

If f has only one argument, then only the function and the array are passed.
> numarray.remove(<< x -> x > 1 >>, a);

If the function has more than one argument, then all arguments except the first are passed right after the name of a.
> numarray.remove(<< x, y -> x > y >>, a, 1): \# 1 for y
If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original array if the given condition has been satisfied at least once, but saving memory. After completion, the function returns the modified array. If the result is null, then the array has not been changed.

See also: numarray.map, numarray.satisfy, numarray.select, numarray.subs.
numarray.replicate (a)
Copies the entire contents of numarray a into a new array and returns it.
See also: numarray.getitem, numarray.subarray.
numarray.resize ( $\mathrm{a}, \mathrm{n}$ )
The function re-sizes a numarray userdata structure a to the given number of entries n. Thus you can extend or shrink a numarray. When extending, the function fills the
new array slots with zeros, while existing values are preserved. An array can be reduced to zero entries, as well.

The function returns the new size, an integer.

```
numarray.satisfy (f, a [,\cdots])
```

With any numarray a, checks each element by calling function f which should return true or false. If at least one element in a does not satisfy the condition checked by f , the result is false, and true otherwise.
numarray.select (f, a [, …] [, true])
Returns all values in numeric array a that satisfy a condition determined by function f and returns a new array, or null if the condition has not been satisfied at all.

If f has only one argument, then only the function and the array are passed.

```
> numarray.select(<< x -> x > 1 >>, a);
```

If the function has more than one argument, then all arguments except the first are passed right after the name of a.

```
> numarray.select(<< x, y -> x > Y >>, a, 1): # 1 for y
```

If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original array if the given condition has been satisfied at least once, but saving memory. After completion, the function returns the modified array. If the result is null, then the array has not been changed.

See also: numarray.map, numarray.remove, numarray.satisfy, numarray.subs.

```
numarray.setbit (a, i, n)
```

Sets bit $n$ at index position i of unsigned char array a. n must be either 0 or 1. i starts from 1 , the rightmost bit, not from position zero. The function returns nothing.

See also: setbit, numarray.getbit, numarray.iterate.
numarray.setitem (a, i, v)
With a any numarray, sets number $v$ to a[i], where $i$, the index, is an integer counting from 1. The function is provided to avoid the __index metamethod overhead.

See also: numarray.include, numarray.purge.
numarray. sort (a)
Sorts a numarray a in ascending order, in-place. The function returns nothing.

## numarray.sorted (a)

Sorts a numarray a in ascending order, non-destructively, and returns a new array.
numarray.subarray (a, i, j)
With a any numarray, returns the subarray a[i to $j]$, where $i$, $j$, the indices, are integers counting from 1. The function is provided to avoid the index metamethod overhead.

See also: numarray.getitem.
numarray.subs (x:v [, ...], a [, true])
Substitutes all occurrences of the value x in the numarray a with the value v . More than one substitution pair can be given. The substitutions are performed sequentially and simultaneously starting with the first pair.

```
> numarray.subs(1:3, 2:4, [1, 2, -1]):
[3, 4, -1]
```

If the last argument is the option inplace=true, or the Boolean true, then the operation will be done in-place, modifying the original array, but saving memory. After completion, the function returns the modified array.

You can check numbers for approximate instead of strict equality by passing the new strict=false option.

See also: numarray.map, numarray.remove, numarray.select.

```
numarray.toarray (o [ , option])
```

Writes all data in the table array, sequence or register o into a numarray and returns it. By default, a double array will be returned (option 'double'); if the second argument option is the string 'uchar', an unsigned char array is created; if it is the string 'integer ', an integer array will be returned.

If a value in o is not a number, zero is written to the array.

```
numarray.toreg (a)
```

Receives numarray a and converts it into a register of numbers, the return.

```
numarray.toseq (a)
```

Receives numarray a and converts it into a sequence of numbers, the return.

```
numarray.uchar (n)
```

Creates a numarray of unsigned 1-byte characters (C unsigned char) with the given number of entries $n$, with $n$ an integer, and with each slot set to the number 0 . Initially, the number of elements can be zero or more.

See also: numarray.double, numarray.int32, numarray.uint32, numarray.ushort, numarray.resize.

```
numarray.uint32 (n)
```

Creates a numarray of unsigned 4-byte integers ( C uint32_t) with the given number of entries $n$, with $n$ an integer, and with each slot set to the number 0 . Initially, the number of elements can be zero or more.

See also: numarray.double, numarray.resize, numarray.uchar, numarray.int32, numarray.readuint32, numarray.uint32, numarray.ushort.

```
numarray.used (a)
```

Returns the estimated number of bytes consumed by the given array a.

```
numarray.ushort (n)
```

Creates a numarray of unsigned 2-byte integers ( C int16_t) with the given number of entries n, with n an integer, and with each slot set to the number 0. Initially, the number of elements can be zero or more.

```
See also: numarray.double, numarray.int32, numarray.resize, numarray.uchar, numarray.uint32.
```

numarray.whereis (a, what [, pos [, eps]])
Returns the index for a given value what in the numarray a. By default, the search starts at the beginning of the array, but you may pass any valid position pos (a positive integer) to determine where to start the search. The return is the index position, a positive number, or null if what could not be found in a.

By default, the function checks for exact equality to detect the existence of a value. By passing the fourth argument eps, a non-negative number, the function also compares the values approximately with the given maximum deviation eps. See approx for more details.

The '__in' metamethod internally uses this function to check for the existence of values.
numarray.write (fh, a [, pos, nvalues]])
Writes unsigned chars, doubles, long doubles or integers stored in a numarray a to the file denoted by its numeric file handle fh . The file must be opened with binio.open and closed with binio.close.

The start position pos is 1 by default but can be changed to any other valid position in the numarray.

The number of values (not bytes !) nvalues to be written can be changed by passing an optional fourth argument, a positive number, and by default equals the total number of entries in a, so the function can be called only once to write the entire array. Passing the nvalues argument may also be necessary if your platform requires internal buffers to be aligned to a particular block size. Depending on the type of data stored in a , the function automatically computes the number of bytes to be written.

The function returns the index of the next start position (an integer) for a further call, to write the next bunch of data in a, or null, if the end of the array has been reached. When the function returns null, then it also automatically flushes all unwritten content to the file so that you do not have to call binio.sync manually if you want to read the file subsequently.

No further information is stored to the file created, so you always must know the type of data you want to read in later.

Example on how to write an entire array of 4,096 integers piece-by-piece:

```
> a := numarray.int32(4 * 1024);
> fd := binio.open('integer.bin');
> pos := 1;
> do # write 1024 values per each call
> pos := numarray.write(fd, a, pos, 1024)
> until pos = null;
> binio.close(fd);
```

Use binio.sync if you want to make sure that any unwritten content is physically written to the file when calling numarray. write multiple times on one array.

If you want to add data to the end of a file later on, pass the 'a' option to binio.open.

### 10.6.3 Metamethods

| Metamethod | Functionality |
| :---: | :---: |
| '__index' | read operation, e.g. n[p] or n[p to q], with p, q any valid indices |
| '__writeindex' | write operation, e.g. n[p] : = value, with p any valid index |
| '__size' | size operator, number of elements in a numarray |
| '__in' | in operator |
| '__notin' | notin operator |
| '__empty' | empty operator |
| '__filled' | filled operator |
| '__tostring' | formatting for output at the console |
| '__aeq' | approximate equality $\sim=$ operator |
| '__eq' | equality operator $=$ |
| '__eeq' | strict equality operator = = |
| '__zero' | zero operator |
| '__nonzero' | nonzero operator |
| '__gc' | garbage collection |

## 10.7 list - Linked Lists

As a plus package, the llist package is not part of the standard distribution and must be activated with the import statement, e.g. import llist.

### 10.7.1 Introduction and an Example

Tables and sequences are quite slow if you have to insert or delete a lot of elements during an operation, for with each insertion or deletion, objects have to be shifted upward or downward physically.

To avoid these costly operations, data can also be represented in containers, or `nodes`, where "[e]ach node contains two fields: a "data" field to store whatever element [...], and a "next" field which is a pointer used to link one node to the next node. ${ }^{1911}$ For example, if you would like to insert a new element at position $n$, the address of the 'next entry' of node $\mathrm{n}-1$ is changed to the address of the new node containing the element to be inserted, and the 'next entry' in the new node is assigned the address of the node containing the original value at position $n$.

This speeds up write operations by dimensions; read operations, however, are slower, for the linked list has to be traversed linearly. However, linked lists as implemented in this package are around fifteen times faster even when conducting a read operation with each write operation.

Metamethods exist to support printing, indexing, and indexed assignments; the size, in, notin, $=$, and $\sim=$ operators are also supported.

Linked lists can contain nulls, i.e. putting null into the data field of a node does not delete this node from the chain.

Linked list can store status information or other data in a special registry table that is available at pseudo-index position 0 . You can use the index metamethod or Ilist.getitem to read from or write data into this table. Examples:

```
> print(a[0]); # print contents of status table
> print(llist.getitem(a, 0)); # dito
> a[0].cursor := 16; # assign 16 to status table key 'cursor'
> a[0, 'cursor'] := 16; # dito
```

For an example of how to use linked lists, see Chapter 6.27.
Note that the linked list implemented in this package always knows about the position of the top and the bottom element - so read and write access to them is

[^0]always $O(1)$.

### 10.7.2 Functions

llist.append (l, obj [, ‥])
Appends one or more elements obj which may be of any type, to the singly-linked list 1 , in sequential order. There is no return.

See also: Ilist.prepend, Ilist.put.
llist. checkllist (1)
Checks whether its argument is a singly-linked list and issues an error otherwise. The function returns nothing.

## llist.dump (1)

Writes each element in the singly-linked list 1 to a sequence and then deletes it from the list. The linked list thereafter is completely empty and cannot be used any longer. It will be garbage collected later as soon as you delete the reference to it. The return is the sequence.

The function can be used in case available memory is insufficient.
See also: Ilist.toseq.
llist.getitem (1, idx [, n])
Returns the item at index idx of the singly-linked list 1 . If the index does not exist, the function returns null.

If idx is negative, the function returns the value stored at the -idx's position counting from end of the list.

If n is given, then besides $\mathrm{a}[\mathrm{idx}]$, the values $a[i d x+1] \ldots \mathrm{a}[i d x+n-1]$ are also returned as additional results. The default is 1 .

See also: Ilist.setitem.
llist.iterate (l [, n [, p]])
Returns an iterator function that when called returns the next value in the singly-linked list 1 , which might also be null if one or more nulls are included in the linked list, or null if there are no more entries in the list. Also returns null if the linked list is empty.

If an index $n$ is passed, the first call to the iterator function returns the $n$-th element in the list and with subsequent calls, the respective elements after index $n$.

You may also pass a non-negative integer p to the iterator function: In this case, the next consecutive p elements in the list are skipped before determining and returning a value.

Example: Since the iterator can return null even if the end of the list has not yet been reached, we use a counter:

```
> L := llist.list(1); llist.append(L, null); llist.append(L, 2);
> f := llist.iterate(L);
> c := 0;
> while c++ < size L do
    print(f())
    od;
1
null
2
```

The function can also process ulists.
See also: ipairs.

## llist.list ([..•])

The function creates a new singly-linked list and optionally stores all of the given elements in it. The return is a userdata of user-type 'llist'.
llist.prepend (1, obj [, ‥])
Prepends an element obj, and optionally further elements, which may be of any type, to the singly-linked list 1 . There is no return.

## See also: Ilist.append, Ilist.put.

## llist.purge (l [, n])

The function removes the element at position $n$ from the linked list l. All the successors of the element to be deleted are `shifted` downwards. The function returns the value deleted, but issues an error if there is no element (i.e. node) at index n .

If $i d x$ is negative, the function deletes the value stored at the -idx's position counting from end of the list.

If $n$ is not given, then the last, i.e. top node is deleted; this is equal to llist.purge( 1 , size 1).

The function can also process ulists.
llist.put (l, $n$, obj)
The function inserts the given element obj into singly-linked list 1 at position $n$. The original element at position $n$ is not deleted - it and all of its successors are `shifted` to open space. The function returns nothing, and issues an error if the index is out-of-range.

If idx is negative, the function inserts the value at the -idx's position counting from end of the list.

The function can also process ulists.

## See also: Ilist.append, Ilist.prepend.

```
llist.replicate (l)
```

The function creates a copy of the singly-linked list 1 and returns a new linked list. However, if an element in 1 is a structure, it is not deep-copied.

```
llist.setitem (l, idx, obj)
```

Stores obj, which may be of of any type, to position idx of the singly-linked list 1 , overwriting the existing value. If size $1>$ idx +1 and the index does not yet exist, the function simply quits without an error. If idx $=$ size $1+1$, then the call is equivalent to llist.append. The function returns nothing.

If $i d x$ is negative, the function sets value to the -idx's position counting from the end of the list.

## See also: Ilist.getitem.

## llist.toseq (1)

The function creates a new sequence and copies all elements in the singly-linked list 1 into it, in sequential order. The return is the sequence. If there are no elements in 1 , an empty sequence will be returned. If the list includes nulls, they are ignored.

```
llist.totable (l)
```

The function creates a new table and copies all elements in the singly-linked list 1 into it, in sequential order. The return is the table. If there are no elements in 1 , an empty table will be returned. If the list includes nulls, the resulting table will contain holes.

### 10.7.3 Unrolled Singly-Linked Lists

The llist package also supports unrolled singly-linked lists. You will find the respective functions in the `package` table ulist. To use the functions, it suffices you have already invoked the llist package with import llist.

Unrolled singly-linked lists (ulists) internally consist of a singly-linked list storing sequences of the actual values in each of its nodes. Various administrative information - the current number of sequences (i.e. nodes), the current and the maximum number of values in each sequence - is stored in a `registry` table at pseudo-index 0 . However, this internal structure is hidden from the user, and you can use the same indices as you would do when calling llist functions to read or write values.

Insert and delete operations on ulists are twenty times faster when compared to singly-linked lists, with only a small increase of memory consumption. Similarly, simple read and write operations are 15 times faster.

Note that contrary to llists, ulists cannot store null. The ulist package provides the following metamethods:

| Functionality | ulist metamethod | ulist alternative |
| :--- | :--- | :--- |
| Pretty printer | print function, colon utility | ulist.tostring(L) |
| Reading values | $\mathrm{L}[\mathrm{k}]$ | ulist.getitem $(\mathrm{L}, \mathrm{K})$ |
| Saving values | $\mathrm{L}[\mathrm{k}]:=\mathrm{v}$, etc. | ulist.setitem(L, $\mathrm{K}, \mathrm{v})$ |
| Size | size operator | ulist.getsize(L) |
| Existence check | in operator | ulist.has(L, v) |
| Existence check | notin operator | ulist.hasnot $(\mathrm{L}, \mathrm{v})$ |
| Equality check | = operator | ulist.isequal(K, L) |

The following ulist functions work like the llist functions of the same name, with the exception of ulist.list:
ulist.append (ul, obj [, ...])
The function works like llist.append.
It is written in Agena and included in the lib/llist.agn file.

```
ulist.checkulist (ul)
```

Checks whether its argument is a ulist and issues an error otherwise. The function returns nothing.

See also: ulist.isulist.

```
ulist.dump (ul)
```

The function works like llist.dump.

```
ulist.getitem (ul, idx [n])
```

The function works like llist.getitem.
ulist.getllist (ul, node)
Returns the sequence stored at node (a positive integer) of the underlying llist. If the node does not exist, the function returns null.

```
ulist.getsize (ul)
```

Returns the number of items in a ulist.

```
ulist.has (ul, v)
```

Checks whether the ulist contains item v and returns true or false.

```
ulist.isulist (ul)
```

Checks whether its argument is a ulist and returns true or false.

See also: ulist.checkulist.
ulist.iterate (ul [, n [, p]])
The function works like Ilist.iterate.

It is written in Agena and included in the lib/llist.agn file.

See also: ipairs.
ulist.list (n [, fill])
The function creates a new unrolled singly-linked list and internally uses sequences with a maximum size of $n$ slots. The default for $n$ is 128 .

If the number fill is given, with $0<$ fill $<1$, each underlying sequence is filled to the given percentage before a new one is created. The default is 0.75 for 75 percent. Reasonable values for fill may range between 0.5 to 0.75 .
ulist.prepend (ul, obj [, ...])
The function works like llist.prepend.

It is written in Agena and included in the lib/llist.agn file.
ulist.purge (ul, n)
The function works like llist.purge, but also returns the element deleted.

It is written in Agena and included in the lib/llist.agn file.
ulist.put (ul, $n$, obj)
The function works like llist.put.

It is written in Agena and included in the lib/llist.agn file.

```
ulist.setitem (ul, idx, value)
```

The function works like llist.setitem.
ulist.sort (ul [, f])
The function works like sort and returns nothing.
ulist.swap (ul, i, j)
Swaps the positions of $u l[i]$ and $u l[j]$ in-place. The function returns nothing.
ulist.tostring (ul)
Converts the contents of a ulist to a formatted string that can be output at the prompt.

It is written in Agena and included in the lib/llist.agn file.

```
ulist.toseq (ul)
```

The function works like llist.totable but returns a sequence instead of a table.

See also: ulist.dump.
ulist.totable (ul)
The function works like llist.totable.

### 10.7.4 Doubly-Linked Lists

Finally, the llist package features doubly-linked lists. Read and write access to elements in doubly-linked lists is twice as fast as for singly-linked lists.

You find the respective functions in the package table dlist. It suffices you have already invoked the llist package with import llist.

The functions implemented for doubly-linked lists have the same name, work the same and have the same syntax as those for singly-linked lists, which are available in package table llist. Just replace the prefix `llist` with `dlist`.
dlist.append (l, obj [, ..] $)$
Appends one or more elements obj which may be of any type, to the doubly-linked list 1 , in sequential order. There is no return.

See also: dlist.prepend, dlist.put.

```
dlist.checkdlist (1)
```

Checks whether its argument is a doubly-linked list and issues an error otherwise. The function returns nothing.
dlist.dump (1)
Writes each element in the doubly-linked list 1 to a sequence and then deletes it from the list. The linked list thereafter is completely empty and cannot be used any longer. It will be garbage collected later as soon as you delete the reference to it. The return is the sequence.

The function can be used in case available memory is insufficient.
See also: dlist.toseq.
dlist.getitem (l, idx [, n])
Returns the item at index idx of the doubly-linked list 1 . If the index does not exist, the function returns null.

If $i d x$ is negative, the function returns the value stored at the -idx's position counting from end of the list.

If $n$ is given, then besides a[idx], the values a[idx + 1] ... a[idx $+n-1]$ are also returned as additional results. The default is 1 .

See also: dlist.setitem.
dlist.iterate (l [, n [, p]])
Returns an iterator function that when called returns the next value in the doubly-linked list 1 , which might also be null if one or more nulls are included in the linked list, or null if there are no more entries in the list. Also returns null if the linked list is empty.

If an index $n$ is passed, the first call to the iterator function returns the $n$-th element in the list and with subsequent calls, the respective elements after index $n$.
You may also pass a non-negative integer p to the iterator function: In this case, the next consecutive p elements in the list are skipped before determining and returning a value.

Example: Since the iterator can return null even if the end of the list has not yet been reached, we use a counter:

```
> L := dlist.list(1); dlist.append(L, null); dlist.append(L, 2);
> f := dlist.iterate(L);
> c := 0;
> while c++ < size L do
        print(f())
    od;
1
null
2
```

See also: ipairs.

## dlist.list ([..•])

The function creates a new doubly-linked list and optionally stores all of the given elements in it. The return is a userdata of user-type 'dlist'.
dlist.prepend (l, obj [, $\cdot \cdot]$ )
Prepends an element obj, and optionally further elements, which may be of any type, to the doubly-linked list 1 . There is no return.

## See also: dlist.append, dlist.put.

## dlist.purge (l [, n])

The function removes the element at position $n$ from the doubly-linked list 1. All the successors of the element to be deleted are `shifted` downwards. The function returns the value deleted, but issues an error if there is no element (i.e. node) at index n .

If idx is negative, the function deletes the value stored at the -idx's position counting from end of the list.

If n is not given, then the last, i.e. top node is deleted; this is equal to dlist.purge( 1 , size 1).
dlist.put (1, $n$, obj)
The function inserts the given element obj into doubly-linked list 1 at position n. The original element at position $n$ is not deleted - it and all of its successors are `shifted` to open space. The function returns nothing, and issues an error if the index is out-of-range.

If idx is negative, the function inserts the value at the -idx's position counting from end of the list.

See also: dlist.append, dlist.prepend.
dlist.replicate (l)
The function creates a copy of the doubly-linked list 1 and returns a new linked list. However, if an element in 1 is a structure, it is not deep-copied.
dlist.setitem (l, idx, obj)
Stores obj, which may be of of any type, to position idx of the doubly-linked list 1, overwriting the existing value. If size $1>i d x+1$ and the index does not yet exist, the function simply quits without an error. If idx $=$ size $1+1$, then the call is equivalent to dlist.append. The function returns nothing.

If idx is negative, the function sets value to the -idx's position counting from the end of the list.

See also: dlist.getitem.
dlist.toseq (l)
The function creates a new sequence and copies all elements in the doubly-linked list 1 into it, in sequential order. The return is the sequence. If there are no elements in 1 , an empty sequence will be returned. If the list includes nulls, they are ignored.

```
dlist.totable (l)
```

The function creates a new table and copies all elements in the doubly-linked list 1 into it, in sequential order. The return is the table. If there are no elements in 1, an empty table will be returned. If the list includes nulls, the resulting table will contain holes.

## 10.8 bags - Mulitsets

As a plus package, the bags package is not part of the standard distribution and must be activated with the import statement, e.g. import bags.

### 10.8.1 Introduction and Examples

A bag, also called a multiset, is a kind of Cantor set that also stores the number of occurrence of each unique element.

Consider a bulk of orders of books where each order is reported individually. You may only want to know how many times a book has been sold, instead of storing each individual order (and maybe all its data) to finally count them. You may want to save space and perform the count immediately as soon as the order has been committed.

The package uses tables of the user-defined type 'bag' to implement multisets.
A sequence of orders might look like this:

```
> import bags;
> orders := seq(
    'Programming in Lua', 'Moon Lander', 'Lost Moon',
    'Programming in Lua', 'Moon Lander', 'Lost Moon',
    'C von A bis Z');
> books := bags.bag(unpack(orders));
> books['Lost Moon']:
2
```

For a further order, just enter

```
> bags.include(books, 'Agena');
> books:
bag(Agena ~ 1, C von A bis Z ~ 1, Lost Moon ~ 2, Moon Lander ~ 2,
Programming in Lua ~ 2)
```

A customer has cancelled his previous orders:

```
> bags.remove(books, 'Agena'):
> books:
bag(C von A bis Z ~ 1, Lost Moon ~ 2, Moon Lander ~ 2, Programming in Lua ~
2)
```


### 10.8.2 Functions \& Metamethods

The package also provides the following metamethods:

| Metamethod | Functionality |
| :--- | :--- |
| '_-index' | read operation, e.g. $\mathrm{n}[\mathrm{p}]$, with p an index |
| '_-writeindex' | write operation, e.g. $\mathrm{n}[\mathrm{p}]:=$ value, with p the index |
| '_size' | size operator, number of characters currently stored |
| '_-in' | in operator |
| '_-notin' | notin operator |
| '_-empty' | empty operator |
| '_-filled' | filled operator |
| '_-union' | union operator |
| '_-intersect' | intersect operator |
| '_-minus' | minus operator |
| '_-tostring' | formatting for output at the console |
| '_-gc' | garbage collection |

The functions provided by the package are:

## bags.attrib (b)

Returns the number of occurrence of all unique elements in the bag b and also the accumulated number of all occurrences of these elements in it. For example, the multiset bag('Curiosity' ~ 2, 'Skycrane' ~ 1) results to 2, 3.

See also: bags.getsize.

## bags.bag ([...])

The function creates a new bag and optionally stores all of the given elements in it.
See also: sykcrane.bagtable.

## bags.bagtoset (b)

The function returns all of the unique elements in b as a set.

## bags.getsize (b)

Returns the number of occurrence of all unique elements in the bag b. without the overhead of calling bags.attrib. For example, the multiset bag('Curiosity' ~ 2, 'Skycrane' $\sim 1$ ) results to 2 .

See also: bags.attrib.
bags.include (b, obj [, ...])
The function inserts all of the given elements obj, etc. into bag b.
The function returns nothing.
See also: bags.minclude, tables.include.
bags.minclude (b, obj)
The function inserts all of the given elements in the sequence obj into bag b. The function should be used instead of bags.include if the number of elements to be inserted exceeds Agena's argument stack.

The function returns nothing.
See also: bags.include.
bags.remove (b, obj [, ...])
The function removes all of the given elements obj, etc. from bag b. If the number of counts of the removed element reaches 0 , the element will be deleted from the bag.

The function returns nothing.
There are metamethods for conducting some sort of arbitrary Cantor set operations on bags. Try out the binary operators union (for union), minus for difference set, intersect for intersection, in and notin for searching an object, plus support of the size, empty and filled operators.

If you would like to iterate a bag, you can use conventional for/in loops, for example, using the bag in the previous chapter:

```
> for i, j in books do print(i, j) od
Programming in Lua 2
C von A bis Z 1
Lost Moon 2
Moon Lander 2
```


## 10.9 bimaps - Bi-directional Maps

As a plus package, the bimaps package is not part of the standard distribution and must be activated with the import statement, i.e. import bimaps.

### 10.9.1 Introduction and Examples

The bimaps package implements a bi-directional map through tables. It is intended to hold items, i and j, that have a 1-to-1 relationship and allows to look up item j from table i and look up i from table j.

Examples:

```
> import bimaps
> l, r := bimaps.bimap()
> l.foo:= 1
> l.bar := 2
> l.spam := 'eggs'
> l:
[bar ~ 2, foo ~ 1, spam ~ eggs]
> r:
[1 ~ foo, 2 ~ bar, eggs ~ spam]
> l = r:
true
```


### 10.9.2 Functions and Metamethods

The functions are:

```
bimaps.bimap ([tbl])
```

Creates two tables representing a bi-directional map. You can initialise the bimap by passing an optional table tbi with pre-defined values.

```
bimaps.attrib (bm)
```

Returns administrative information for bimap bm, see environ.attrib for details.

```
bimaps.entries (bm)
```

Returns all entries in bimap bm, without invoking any metamethods.
See also: bimaps.indices.

## bimaps.indices (bm)

Returns all indices in bimap bm, without invoking any metamethods.
See also: bimaps.entries.
bimaps.rawget (bm [, k])
Returns the underlying table in bimap bm, without invoking any metamethods, if no index $k$ is given - or if $k$ is given, returns entry bm[k] without invoking any metamethods.

The package also provides the following metamethods:

| Metamethod | Functionality |
| :--- | :--- |
| '_-index' | read operation, e.g. $\mathrm{n}[\mathrm{p}]$, with p any valid table index |
| '_writeindex' | write operation, e.g. $\mathrm{n}[\mathrm{p}]:=$ value, with p any valid index |
| '_-size' | size operator, number of bi-directional pairs |
| '_-in' | in operator |
| '_-notin' | notin operator |
| '_-empty' | empty operator |
| '_filled ' | filled operator |
| '__tostring' | formatting for output at the console |

### 10.10 heaps - Priority Queues

As a plus package, the heaps package is not part of the standard distribution and must be activated with the import statement, i.e. import heaps.

### 10.10.1 Introduction and Examples

The package implements skew heaps, `emulated` binary heaps and AVL trees which for example can be used as priority queues. A skew heap is a mostly unbalanced binary tree, usually avoiding costly reshuffles with each insert, whereas binary heaps and AVL trees are usually balanced - with extra cost at insertion.

The exact amortized complexity $O(n)$ of all operations on a skew heap is known to be log(n, Phi), and the one for AVL and binary heaps is log(n, 2).

The package provides constructors (avl.new, skew.new, binary.new), metamethods (see table below), functions to insert new and replace existing values (avl.include, skew.include, binary.include), to remove the entry with the smallest index (avl.remove, skew.remove, binary.remove), and iterators (avl.iterate, skew.iterate, binary.iterate) that traverse the heaps in an ordered fashion depending on the sorting method chosen at heap creation, which by default is in ascending order of the indices.

Usage is:

```
> import heaps;
```

All the functions to work with skew heaps reside in the `skew `able, those for binary heaps are in table `binary`, and those for AVL trees in table `avl'.

The package operations on binary heaps and AVL trees are at least 25 times faster than on skew heaps.

```
> h := binary.new()
> binary.include(h, 2, 'world')
> binary.include(h, 1, 'hello')
> binary.include(h, 10, 'everybody')
> k1, v1 := binary.remove(h)
> k2, v2 := binary.remove(h)
> k3, v3 := binary.remove(h)
> print(v1, v2, v3)
hello world everybody
> binary.include(h, 2, "world"); binary.include(h, 1, "hello");
> binary.include(h, 10, "everybody");
> f := binary.iterate(h);
```

```
> f():
1 hello
> f():
2 world
> f():
10 everybody
```

The skew heap functions have the same syntax and work the same.

### 10.10.2 Metamethods

The package provides the following metamethods for all three heap types:

| Metamethod | Functionality |
| :--- | :--- |
| '_-index' | read operation, e.g. $\mathrm{n}[\mathrm{p}]$, with p any valid non-null index |
| '__writeindex' | skew heaps and AVL trees only: write operation, e.g. $\mathrm{n}[\mathrm{p}]:=$ <br> value, with p any valid non-null index |
| '__size' | size operator, number of key $\sim$ value pairs in the heap |
| '_-in' | in operator |
| '_notin' | notin operator |
| '_-empty' | empty operator |
| '__filled' | filled operator |

### 10.10.3 Binary Heap Functions

## binary.entries (h)

The function returns all entries in heap h in a new table. For the ordering, see binary.iterate.

See also: binary.indices.
binary.include (h, k, v)
Inserts a new key~value pair into heap $h$. The key $k$ and value v must be non-null. The function returns nothing.

See also: binary.remove.

## binary.indices (h)

The function returns all indices in heap h in a new table. For the ordering, see binary.iterate.

See also: binary.entries.

## binary.iterate (h)

The factory returns an iterator that with each call returns a key~value pair from heap $h$, in an ordered fashion.

The ordering is determined by the comparison function passed to binary.new, which by default is a `less than` comparison, so that the iterator returns the values in ascending order of its indices.

## binary.new ([comparison])

Creates an empty binary heap with the default comparison method for various operations the `less than` relation, i.e.

$$
\ll \mathrm{k} 1, \mathrm{k} 2->\mathrm{k} 1 \text { and type k1 }=\text { type k2 and k1 }<\mathrm{k} 2 \gg
$$

You might pass another comparison function to be used.

## binary.remove (h)

Removes the key~value pair with the smallest key and returns the key and the value removed. If the key does not exist, the function just returns null.

See also: binary.include.

```
binary.reorder (h)
```

The function deletes all obsolete datasets in binary heap h - to free memory.

### 10.10.4 AVL Tree Functions

The AVL tree functions are:

```
avl.attrib (h)
```

The function returns administrative information about an AVL tree: maximum height (key maxheight), number of key~value pairs currently included (key length) and the balance factor (key balancefactor).

```
avl.entries (h)
```

The function returns all entries in the AVL tree h in a new table, in ascending order of its respective indices.

See also: avl.indices.
avl.getmax (h)
The function returns the largest key along with its associated value from AVL tree h . The function does not remove the data from $h$.

See also: avl.getmin, getminmax, avl.getroot.

```
avl.getmin (h)
```

The function returns the smallest key along with its associated value from AVL tree $h$. The function does not remove the data from $h$.

See also: avl.getmax, avl.getminmax, avl.getroot.

```
avl.getminmax (h)
```

The function returns the smallest and largest key along with their associated values from AVL tree $h$. The function does not remove the data from $h$.

See also: avl.getmax, getminmax, avl.getroot.
avl.getroot (h)
The function returns the key along with its associated value from the root node of AVL tree $h$. The function does not remove the data from $h$.
avl.include (h, k, v)
Inserts a new key~value pair into AVL tree h. The key k must be non-null; if v is null then the function will call avs.remove( $h, k$ ). The function returns nothing.

See also: avl.remove.
avl.indices (h)
The function returns all indices in AVL tree h in ascending order and returns them in a new table.

See also: avl.entries.
avl.iterate (h)
The factory returns an iterator that with each call returns a key~value pair from AVL tree $h$, in ascending order of its indices.

```
avl.new ()
```

Creates an empty AVL tree.
avl.remove (h)
avl.remove (h, k)
In the first form, removes the key~value pair with the smallest key and returns the key and the value removed.

In the second form, deletes the given key~value pair from the tree.
If the key does not exist or the tree is empty, the function just returns null.
See also: avl.include.

### 10.10.5 Skew Heap Functions

The skew heap functions are:
skew.entries (h)
The function returns all entries in heap h in a new table. For the ordering, see skew.iterate.

See also: skew.indices.
skew.height (h, k)
Returns the height of a key $k$ in skew heap $h$, with 0 depicting that the key is in the root node.

```
skew.include (h, k, v)
```

Inserts a new key~value pair into the skew heap $h$. The key $k$ and value v must be non-null. The function returns nothing.

See also: skew.remove.

```
skew.indices (h)
```

The function returns all indices in heap h in a new table. For the ordering, see skew.iterate.

See also: skew.entries.

## skew.iterate (h)

The factory returns an iterator that with each call returns a key~value pair from heap $h$, in an ordered fashion.

The ordering is determined by the comparison function passed to skew.new, which by default is a `less than` comparison, so that the iterator returns the values in ascending order of its indices.

## skew.new ([comparison])

Creates an empty skew heap with the default comparison method for various operations the `less than` relation, i.e.

$$
\ll \mathrm{k} 1, \mathrm{k} 2->\mathrm{k} 1 \text { and type k1 }=\text { type k2 and k1 < k2 >> . }
$$

You might pass another comparison function to be used.

## skew.remove (h)

Removes the key~value pair with the smallest key from heap h and returns the key and the value removed. If the key does not exist, the function just returns null.

See also: skew.include.

## skew.reorder (h)

The function balances skew heap h internally by popping the node with the highest priority and then re-inserting it. This is just for maintenance, you do not have to run this function before executing any other package function.

### 10.11 bfield - Bit Fields

The package provides lean, low-level functions to work with memory-saving bit fields. The functions are generally faster than those implemented in the memfile package.

Typical usage:
Create a bit field of at least ten bits, which is internally rounded up to 16 bits, as 16 is a multiple of eight whereas ten is not:

```
> m := bfield.new(10);
```

The field is by default pre-filled with zeros. If you want to preset other values, like 255 to set all bits to 1 , enter:

```
> m := bfield.new(10, 0xff);
```

The actual size of the field is:

```
> size m:
16
```

Get some bits:

```
> m[1], m[9]:
1 1
```

Set some bits to zero:

```
> m[1] := 0; m[9] := 0;
> m[1], m[9]:
0 0
```

The package provides the following metamethods:

| Metamethod | Functionality |
| :--- | :--- |
| '__index' | read operation, e.g. $\mathrm{n}[\mathrm{p}]$, with p an index counting from 1; <br> reads a bit, not a byte |
| '__writeindex' | write operation, e.g. $\mathrm{n}[\mathrm{p}]:=$ value, with p the index, counting <br> from 1; sets a bit, not a byte |
| '__size' | size operator, number of bits in the field |
| '_zero' | zero operator, checks whether all field bits are set to zero |
| '__tostring' | formatting for output at the console; returns binary <br> representations |
| '__gc' | garbage collection |

The bit field functions are:
bfield.clearbit (bitfield, n)
Clears a bit, i.e. sets absolute bit position $n$ in the bitfield to $0 . n$ counts from 1.
The function returns nothing.

See also: bfield.flipbit, bfield.getbit, bfield.setbit, bfield.setbitto, bfield.setbyte.

```
bfield.flipbit (bitfield, n)
```

Flips the bit stored at absolute bit position $n$ in the bitfield: if the current bit is 1 , it is set to 0 , and vice versa. n counts from 1.

The return is the bit value after flipping, either 1 or 0.
See also: bfield.clearbit, bfield.setbit.
bfield.getbit (bitfield, n)
Returns the bit stored at absolute bit position $n$ in the bitfield. $n$ counts from 1.

The return is either 1 or 0.
See also: bfield.clearbit, bfield.setbit.
bfield.getbyte (bitfield, pos [, option])
From bitfield, returns the byte at position pos, with pos $>0$. The return is an integer in the range $[0,255]$.

See also: bfield.getbit, bfield.getbytes.
bfield.new (n, [, val])
Creates a bit field of at least n bits. If val is not given, then every byte in the field is set to zero. If val - a non-negative integer preferably in the range [0,255] - is given, then every byte in the field is filled with it.

The number of bits actually allocated is always a multiple of 8 , i.e. the field is filled up to whole bytes.

See also: bfield.resize.
bfield.resize (bitfield, $n$ [, val])
Resizes the bitfield to exactly $n$ bits, with $n>0$. It can grow or shrink a bit field and in the latter case preserves the remaining content. If the bit field is to be enlarged, the function fills the new space with zeros if the third argument val is not given, otherwise the added bytes are set to the non-negative integer val, which should be in the range $[0,255]$.

The size of the modified bit field is always a multiple of 8 .
See also: bfield.new.
bfield.setbit (bitfield, n)
Sets absolute bit position $n$ in the bitfield to 1. n counts from 1. To clear a bit, use bfield.clearbit.

The function returns nothing.
See also: bfield.clearbit, bfield.flipbit, bfield.getbit, bfield.setbyte.
bfield.setbitto (bitfield, $n$, val)
Sets absolute bit position $n$ in the bitfield to 1 the val, a non-negative integer preferably in the range [0, 255]. n counts from 1.

The function returns nothing.
See also: bfield.clearbit, bfield.getbit, bfield.setbyte.
bfield.setbyte (bitfield, pos, val)
Sets val, a non-negative integer preferably in the range [0,255] into bitfield at byte position pos, with pos $>0$.

The function returns nothing.
See also: bfield.getbyte, bfield.setbit.

Chapter Eleven
Numbers

## 11 Numbers

### 11.1 Mathematical Functions

The mathematical operators and functions explained in this chapter work on both real numbers as well as complex numbers, except if indicated otherwise.

For the sake of speed, basic arithmetic functions have been implemented as operators, whereas all other mathematical functions are implemented as Agena library functions (implemented either in C or Agena). While functions can be overwritten with self-defined versions, operators cannot be overwritten.

## Summary of Operators and Functions:

## Basic Arithmetic Operators

+, -, *, /, /*, \& + , \&-, \&*, \&/, \&
Relational Operators

$$
=,==,<,>,<=,>=,<>, \mid, \text { approx. }
$$

Integer Division
<br>, \%, drem, iqr, modf, symmod, math.cld, math.fld, math.modiv, math.modulus, math.nearmod.

Exponentiation
^, **, antilog2, antilog10, cube, exp, expx2, frexp, Idexp,
math.expminusone, math.exp2, math.exp10, math.iscube, math.issquare, square, squareadd.

Roots
cbrt, hypot, hypot2, hypot3, hypot4, invsqrt, proot, pytha, root, sqrt, math.isqrt, fastmath. hypotfast, fastmath. sqroot, fastmath.sqrfast.

Logarithms
ilog2, In, log, log2, log10, math.ceillog2, fastmath.Ibfast, math.Inplusone, math.xInplusone.

## Trigonometric Functions

cas, cos, cot, csc, sec, sin, tan, math.quadrant, math.sincos, fastmath.sincosfast, math.wrap.

## Inverse Trigonometric Functions

arccos, arccsc, arccot, arcsec, arcsin, arctan, arctan2, math.arccosh, math.arcsinh, math.arctansh.

## Hyperbolic Functions

cosh, coth, csch, sech, sinh, tanh.
Inverse Hyperbolic Functions
arccosh, arccsch, arccoth, arcsech, arcsinh, arctanh.
Sign
sign, signum, math.copysign, math.flipsign, math.mulsign, math.signbit.

## Miscellaneous

erf, erfc, erfcx, erfi, inverf, inverfc, fma, sinc, cosc, tanc, math.fib, math.fibinv, math.gcd, math.isfib, math.Icm, math.max, math.min, math.rectangular, math.relerror, math.triangular, muladd.

## Miscellaneous Complex Functions

 argument, bea, conjugate, cosxx, flip, polar.Gamma, etc.
beta, binomial, fact, gamma, Ingamma, math.fall, math.Infact, math.pochhammer.

## Bessel Functions

besselj, bessely.
Rounding Functions
ceil, entier, int, mdf, round, xdf, math.rint.

## Numbers

frac, frexp, ++, --, +++, ---, math.compose, math.decompose, math.eps, math.epsilon, math.exponent, math.fraction, math.frexp, math.mantissa, math.ndigits, math.nextafter, math.nextmultiple, math.nextpower, math.nthdigit, math.tohex, math.uexponent, math.ulp.

## Numeric Checks

even, finite, float, in, infinite, inrange, isint, isnegative, isnegint, isnonneg, isnonnegint, isnonposint, isnumber, isnumeric, isposint, ispositive, nan, odd, math.fpclassify, math.isinfinity, math.isminuszero, math.isnormal, math.isordered, math.ispow2, math.issubnormal.

## Range Reduction and Conversion

abs, ||, heaviside, math.branch, math.chop, math.clip, math.Inabs, math.norm, math.normalise, math.piecewise, math.ramp, math.rectangular, math.rempio2, math.unitise, math.unitstep, math.wrap.

## Random Numbers

math.random, math.randomseed.

## Bases and Conversion

math.convertbase, math.norm, math.tobinary, math.todecimal, math.tohex, math.toradians, math.tosgesim.

## Primes

math.congruentprime, math.isprime, math.nextprime, math.prevprime.

## Bitwise Operators, Bit and Byte Twiddling

\&\&, ~~, \|, ^ ^, $\lll<\ggg, \lll<, \ggg>$, implies, nand, nor, xnor, xor, getbit, getbits, getnbits, setbit, setbits, setnbits, math.inttofpb, bytes.numhigh, bytes.numlow, bytes.gethigh, bytes.getlow, bytes.numwords, math.fpbtoint, bytes.leadzeros, bytes.leastsigbit, bytes.mostsigbit, bytes.onebits, bytes.reverse, bytes.setdouble, bytes.sethigh, bytes.setnumhigh, bytes.setlow, bytes.setnumlow, bytes.setnumwords, bytes.tobytes.

## Boolean Operators

and, implies, nand, nor, not, or, xnor, xor

### 11.1.1 Operators and Functions

## $\mathbf{x} \pm \mathbf{y}$

The operator adds two numbers; returns a number. Complex numbers are supported.

See also: factory.count, math.accu, math.koadd, inc operator in Chapter 4.6.8.

## $\mathbf{x}=\mathbf{y}$

The operator subtracts two numbers; returns a number. Complex numbers are supported.

See also: math.fdim, dec operator in Chapter 4.6.8.

## x * $\mathbf{y}$

The operator multiplies two numbers; returns a number. Complex numbers and Booleans are supported. A Boolean operand represents 1 for true, and 0 for false or fail.

See also: mul operator in Chapter 4.6.8.

## $\mathbf{x} \operatorname{Ly}$

The operator divides two numbers; returns a number. Complex numbers are supported.

See also: recip,math.cld, math.fld, div operator in Chapter 4.6.8.

## $\mathbf{x}$ 】 y

The operator performs an integer division of two numbers, and returns a number. The integer division is defined as: $x \backslash y=\boldsymbol{\operatorname { s i g n }}(\mathrm{x}){ }^{*} \boldsymbol{\operatorname { s i g n }}(\mathrm{y}){ }^{*}$ entier $\left(\left|\frac{x}{y}\right|\right)$.

See also: \%, /, iqr, math.cld, math.fld, intdiv operator in Chapter 4.6.8.

## $\mathbf{x} \underline{\varepsilon}+\mathbf{y}$

The operator adds two signed or unsigned 32-bit numbers; returns a number. Complex numbers are supported, as well. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option.

See also: bytes.add32, factory.count, math.accu, math.koadd.

## $\mathbf{x} \underline{\varepsilon}-\mathbf{y}$

The operator subtracts two signed or unsigned 32-bit numbers; returns a number. Complex numbers are supported, as well. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option.

See also: bytes.sub32, math.fdim.

## $\mathbf{x} \underline{\varepsilon^{*}} \mathbf{y}$

The operator multiplies two signed or unsigned 32-bit numbers; returns a number. Complex numbers are supported. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option.

## See also: bytes.mul32.

## $\mathbf{x} \& / \mathrm{y}$

The operator divides two signed or unsigned 32-bit numbers; returns a number. Complex numbers are supported. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option. See also: bytes.div32.

## $x$ *\% $y$

The operator multiplies two numbers and divides the result by 100; returns a number, the percentage.

## $x$ /\% $\mathbf{y}$

The operator divides two numbers and multiplies the result by 100; returns a number, the ratio.

## $x$ ㅇ% y

The operator computes the percentage change from the number x to the number y and returns a number. It is equivalent to y $/ \% \mathrm{x}-100$.

## $x+\frac{8}{-}$

The operator adds the given percentage y to x .
$x$ 으 y
The operator subtracts the given percentage y from x .

## z roll r

The binary operator rotates a two-dimensional vector, represented by the complex number $z$, through the angel $r$ (given in radians) counterclockwise and returns the new complex number z*exp(|*r). To convert degrees to radians, multiply by Pi/180. If $z$ is just a number, it is internally converted to the complex number $z+0 *$.

See also: conjugate, flip.

## $\mathbf{x}$ 음 $y$

The modulus operator conducts the operation $\mathrm{x} \% \mathrm{y}=\mathrm{x}-\operatorname{entier}\left(\frac{\mathrm{x}}{\mathrm{y}}\right)^{\star} \mathrm{y}$. The return is always non-negative.

See also: <br>, drem, everyth, iqr, symmod, hashes.fibmod32, math.modinv, math.modulus, math.wrap, mod operator in Chapter 4.6.8.

## x symmod y

The symmetric modulus operator evaluates the remainder of a division $\mathrm{x} / \mathrm{y}$ (with $\mathrm{x}, \mathrm{y}$ two Agena numbers). The result has the same sign as the numerator $x$. Specifically, the return value is $x-q^{*} y$, where $q$ is the quotient $x / y$, rounded towards 0 to the next integer.

See also: $\backslash, \%$, drem, iqr, math.modinv, math.modulus, math.wrap.

## $\mathbf{x}$ ~ $\mathbf{y}$

The operator performs an exponentiation of real or complex $x$ with a rational power $y$. With numbers, if $x$ is negative and $y$ non-integral, it returns undefined.

See also: ^ operator, antilog2, antilog10, proot, root, square, squareadd.

## x ** y

The operator exponentiates the real or complex number $x$ with the integer power $y$. Depending on the platform and with small $y$, the operator is at least $50 \%$ faster than the ${ }^{\wedge}$ operator. If y is undefined or $\pm$ infinity, undefined will be returned.

See also: cube, square, squareadd.

## z squareadd c

For numeric or complex $z, c$, computes $z^{\wedge} 2+c$, preventing round-off errors.
See also: **, fma, square.

## $\perp \times \perp$

The operator computes the absolute value of the number or complex number $x$, i.e. $\operatorname{abs}(\mathrm{x})$. The return in both cases is a number.

See also: |-, abs, cabs, calc.eucliddist, math.Inabs, math.fdim.
$\mathbf{x}$ 」- $\mathbf{y}$
The operator computes the absolute difference of the two numbers $x$ and $y$, i.e. abs $(x-y)$. The return is a number.

See also: |-, abs, cabs, calc.eucliddist, math.fdim.

## $\mathbf{x}$ \& \& Y

Bitwise `and` operation on two numbers $x$ and $y$. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option. See also: environ.kernel in Chapter 14.2. See also: bytes.and32.

## $+++\mathbf{x}$

Returns the next representable number larger than $x$. If given a variable, the operator does not change its value. See also: ---, math. nextafter.

## --- $\times$

Returns the next representable number smaller than x. If given a variable, the operator does not change its value. See also: +++ , math.nextafter.
$\sim \sim \mathbf{x}$
Bitwise 32-bit complementary operation on the number x, i.e. bitwise NOT, flipping all the bits representing $x$. The operator returns signed results only, regardless of the environ.kernel/signedbits setting. See also: bytes.not32.

## $\mathbf{x}$ 山 y

Bitwise `or` operation on two numbers $x$ and $y$. By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option. See also: environ.kernel in Chapter 14.2.

See also: bytes.or32.

```
x ^^ y
```

Bitwise 32-bit `exclusive-or` operation on two numbers x and y . By default, the operator internally calculates with unsigned 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option. See also: environ.kernel in Chapter 14.2.

See also: bytes.xor32.

## $x \leq \ll 1$

Bitwise left-shift operation (multiplication by 2, i.e. $x \lll y=x^{*} 2 y$ ). By default, the operator internally calculates with signed 32 -bit integers. You can change this to signed integers by calling environ.kernel with the signedbits option. If $y>=$ environ.kernel('nbits'), returns 0 . Please note that the results may vary across platforms with overflows and that shift by negative y are undefined. Shift by zero is the identity shift.

See also: >>>, environ.kernel, bytes.shift32.

## $x$ 2>2 y

Bitwise right-shift operation (division by 2, i.e. $\mathrm{x} \ggg \mathrm{y}=\mathrm{x} / 2 \mathrm{y}$ ). The operator by default calculates with unsigned 32-bit integers internally. You can change this to signed integers by calling environ.kernel with the signedbits option. If y $>=$ environ.kernel('nbits'), returns 0 . Please note that the results may vary across platforms with overflows and that shift by negative y are undefined. However, if x is negative and y positive, an arithmetic right-shift is accomplished, thus preserving the sign of x . A shift by zero is the identity shift.

See also: <<<, environ.kernel, bytes.shift32.

## $\mathrm{x} \leq \lll 1 \mathrm{Y}$

Returns the number x rotated a given number of bits y to the left. Internally it uses unsigned 32-bit integers by default. You can change this to signed integers by calling environ.kernel with the signedbits option.

See also: \ggg > , environ.kernel, bytes.rotate32.

## $x$ >>>> $y$

Returns the number x rotated a given number of bits y to the right. Internally it uses unsigned 32-bit integers by default. You can change this to signed integers by calling environ.kernel with the signedbits option.

See also: <<<<, environ.kernel, bytes.rotate32

## $x$ in $y$

Checks whether the number x is part of the interval defined by the pair y consisting of two numbers. The operator returns true or false. For a much faster check, see inrange operator.

## $\mathbf{x} \perp \mathbf{y}$

The operator compares two finite numbers $x, y$, determines whether $x$ is less than $y$, $x$ is exactly equal to $y$, or $x$ is greater than $y$, and returns $-1,0$, or 1 respectively.

If at least one of the operators is infinite or undefined, the function returns undefined.

The operator is twice as fast as sign. See also: $\sim \mid$, signum.
To build a piece-wise function, for example the absolute function, you may enter:

```
> my_abs := proc(x) is
    case x | 0
                of -1 then return -x
    else
        return x
    esac
end;
```

$x \sim 1$ y
The operator compares two finite numbers $x$, $y$, determines whether $x$ is approximately equal to $y$, $x$ is less than $y$, or $x$ is greater than $y$, and returns $0,-1$, or 1 respectively. See also: | operator.

## abs (z)

If $z$ is a number, the abs operator returns the absolute value of $z$. With a complex number $z=x+I^{*} y$, it returns the distance between it and the origin as a number, i.e. $\sqrt{x^{2}+y^{2}}$.

See also: ||, |-, argument, cabs, math.Inabs, polar.
antilog2 (z)
The operator computes $2^{z}$, i.e. 2 raised to the power of the number or complex number $z$.

See also: ^ and ** operators, antilog10, log2.

```
antilog10 (z)
```

The operator computes $10^{\text {z }}$, i.e. 10 raised to the power of the number or complex number z.

See also: ^ and ** operators, antilog2, log10.

```
approx (x, y [, eps])
```

Compares the two numbers or complex values x and y and checks whether they are approximately equal. If eps is omitted, Eps is used.

The algorithm uses a combination of simple distance measurement (|x-y| eps) suited for values `near` 0 and a simplified relative approximation algorithm developed by Donald H. Knuth suited for larger values (|x-y| $\leq$ eps * max(|x|, $|\mathrm{y}|)$ ), that checks whether the relative error is bound to a given tolerance eps.

The function returns true if x and y are considered equal or false otherwise. If both a and b are infinity, the function returns true. The same applies to $a$ and $b$ being -infinity or undefined.

See also: math.eps, math.epsilon.

## $\arccos (x)$

Returns the inverse cosine operator ( $x$ in radians). Complex numbers are supported.

## arccosh (x)

Returns the inverse hyperbolic cosine of x (in radians). The function is implemented in Agena and included in the lib/library.agn file.

## $\operatorname{arccsc}(x)$

Returns the inverse cosecant of x (in radians). The function works on both numbers and complex values. The function is implemented in Agena and included in the lib/library.agn file.

```
arccsch (x)
```

Returns the inverse hyperbolic cosecant of x (in radians). The function works on both numbers and complex values. The function is implemented in Agena and included in the lib/library.agn file.

## $\operatorname{arccot}(x)$

Returns the inverse cotangent of $x$ (in radians). The function works on both numbers and complex values. The function is implemented in Agena and included in the lib/library.agn file.

```
arccoth (x)
```

Returns the inverse hyperbolic cotangent of x (in radians). The function works on both numbers and complex values.

## $\operatorname{arcsec}(x)$

Returns the inverse secant of x (in radians). The operator works on both numbers and complex values.

```
arcsech (x)
```

Returns the inverse hyperbolic secant of $x$ (in radians). The function works on both numbers and complex values. The function is implemented in Agena and included in the lib/library.agn file.

```
arcsin (x)
```

Computes the inverse sine operator (in radians). Complex numbers are supported.

```
arcsinh (x)
```

Returns the inverse hyperbolic sine of x (in radians). The function works on both numbers and complex values. See also: math.arcsinh.

## $\arctan (x)$

Computes the inverse tangent operator (in radians). Complex numbers are supported. See also: arctan2.

```
arctan2 (y, x)
```

Returns the arc tangent of $\mathrm{y} / \mathrm{x}$ (in radians), but uses the signs of both parameters to find the quadrant of the result. (It also handles correctly the case of y being zero.) x and y must be numbers or complex numbers. See also: arctan.

## $\operatorname{arctanh}(x)$

Returns the inverse hyperbolic tangent of x (in radians). The function works on both numbers and complex values. The function is implemented in Agena and included in the lib/library.agn file. See also: math.arctanh.

## argument ( $z$ )

Returns the argument (the phase angle) of the complex value $z$ in radians as a number. If $z$ is a number, the function returns 0 if $z \geq 0$, and $\pi$ otherwise.

See also: abs, cabs, polar.

## bea (z)

The operator takes the complex number $z=x!y$ and returns the complex number $\boldsymbol{\operatorname { s i n }}(\mathrm{x})^{*} \boldsymbol{\operatorname { s i n h }}(\mathrm{y})+I^{*} \boldsymbol{\operatorname { c o s }}(\mathrm{x})^{*} \boldsymbol{\operatorname { c o s h }}(\mathrm{y})$. This function may be mathematically useless, but it creates beautiful fractals. With numbers, it returns undefined.

See also: cosxx, flip.
beta ( $\mathrm{x}, \mathrm{y}$ )
Computes the Beta function. x and y are numbers or complex values. The return may be a number or complex value. The Beta function is defined as: Beta(x, y) = $\frac{\Gamma x * \Gamma \mathrm{y}}{\Gamma(\mathrm{x}+\mathrm{y})}$, with special treatment if x and y are integers.

## binomial (n, k)

Returns the binomial coefficient $\binom{n}{k}$ as a number. $n, k$ may also be negative integers, or floats of any sign.

## besselj ( $\mathrm{n}, \mathrm{x}$ )

Returns the Bessel function of the first kind. The order is n given as the first argument, the argument x as the second argument. The return is a number. The function works on both numbers and complex values.

## bessely ( $\mathrm{n}, \mathrm{x}$ )

Returns the Bessel function of the second kind. The order $n$ is given as the first argument, the argument x as the second argument. The return is a number. The function works on both numbers and complex values.

```
cabs (z [, option])
```

If $z$ is a number, the cabs function returns the absolute value of $z$ as a number (default) or abs(z) $+I^{*} 0$ if any option is given.

If $z$ is a complex number $z=x+\mid * y$, contrary to the abs operator, it returns the real and imaginary absolute value, i.e. $|x|+|*| y \mid$.

See also: ||, |-, abs, argument, polar.
cartesian ( $\mathrm{x}, \mathrm{y}$ )
Returns a complex number z in Cartesian notation a + I*b for magnitude/modulus x and argument/phase angle $\mathrm{y} . \mathrm{x}$ and y must be numbers. The result is equivalent to $\mathrm{Z}=\mathrm{x}$ * $\boldsymbol{\operatorname { c i s }}(\mathrm{y})$.

See also: cis, polar.
cas ( x )
Returns the `casine` of the number or complex number $x$ the efficient way, i.e. $\sin (x)+\cos (x)=\sqrt{2} \sin \left(x+\frac{\pi}{4}\right)$. It is written in Agena and included in the lib/library.agn file.

```
cbrt (x)
```

Returns the cubic root of the number or complex number $x$. With complex $x$, it is equal to $x^{\wedge}(1 / 3)$, but not to root( $x, 3$ ).

See also: ^ operator, root.

## ceil (x)

The function rounds upwards to the nearest integer larger than or equal to the number or complex number x. See the entier operator for a function that rounds downwards to the nearest integer. For the definition of ceil, see entier.

See also: entier, floor, int, round, math.rint.

```
cis (x)
```

Returns the complex exponential function $\exp \left(I^{*} x\right)=\cos (x)+I^{*} \sin (x)$ for any real or complex argument x . It is around $33 \%$ faster than the equivalent expression $\exp \left(I^{*} \mathrm{x}\right)$. Note the equality $\mathbf{a b s}(\mathrm{x}){ }^{*} \boldsymbol{\operatorname { c i s } ( \operatorname { a r g u m e n t } ( \mathrm { x } ) )}=\mathrm{x}$.

See also: polar.

```
conjugate (z)
```

The operator returns the conjugate $x-I^{*} y$ of the complex value $z=x+I^{*} y$. If $z$ is of type number, it is simply returned.

See also: flip.

## $\cos (x)$

The operator returns the cosine of x (in radians). Complex numbers are supported.
See also: math.cospi, math.sincos.

```
cosc (x)
```

The function returns the un-normalised cardinal cosine of $x$ (in radians), i.e. $\cos (x) / x$, with $\operatorname{cosc}(0)=$ undefined. Complex numbers are supported.

See also: math.rectangular, sinc, tanc.

## cosh (x)

The operator returns the hyperbolic cosine of x (in radians). Complex numbers are supported. See also: sinh, tanh, math.sinhcosh.
cosxx (z)
The operator takes the complex number $z=x!y$ and returns the complex number $\cos (x)^{\star} \cosh (y)+I^{*} \sin (x)^{*} \sinh (y)$, i.e. the imaginary part of the result had the wrong sign. It represents FRACTINT's buggy cos function till v16. This function may be mathematically useless, but it creates beautiful fractals. With the number z, it returns $\cos (z)$.

See also: cos, bea, flip.
$\cot (x)$
Returns the cotangent $-\tan \left(\frac{\pi}{2}+x\right)$ as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.

```
coth (x)
```

Returns the hyperbolic cotangent $\frac{1}{\tanh (x)}$ as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.
csc ( x )
Returns the cosecant $\frac{1}{\sin (x)}$ as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.

## csch (x)

Returns the hyperbolic cosecant as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.
cube (x)
The operator raises the number or complex number $x$ to the power of 3 . See also: **, ^, square operators.
drem ( $\mathrm{x}, \mathrm{y}$ )
Evaluates the remainder of an integer division $x / y$ (with $x, y$ two Agena numbers), but contrary to symmod, rounds the internal quotient $x / y$ to the nearest integer instead of towards zero. The function actually is a wrapper to C's remainder.

See also: <br>,\%, iqr, modf, symmod, math.modinv, math.modulus.
entier ( x )
The operator rounds the number x downwards to the nearest integer. For complex $x$, the return is:

$$
\begin{aligned}
& \text { re }=\text { real }(x)-\text { entier }(\text { real }(x)) \text { and } \operatorname{im}=\operatorname{imag}(x)-\text { entier (imag }(x)) \text {, } \\
& \text { then entier }(x)=\operatorname{int}(\text { real }(x))+I * \operatorname{int}(\operatorname{mag}(x))+X, \text { where }
\end{aligned}
$$

$$
X=\left\{\begin{array}{l}
0 \quad \text { if } a+b<1 \\
1 \text { if } a+b>1 \wedge a>b \\
1 \\
\text { if } a+b>1 \wedge a<b
\end{array}\right.
$$

Also: ceil( x ) $=$-entier( -x ). (With numbers, the function internally calls C's floor.)
See also: ceil, frac, int, mdf, round, math.rint.
erf (x)
Returns the error function of $x$. It is defined by $\operatorname{erf}(\mathrm{x})=\frac{2}{\sqrt{\pi}} \int_{\mathrm{t}=0}^{\mathrm{x}} \mathrm{e}^{-\dagger^{\wedge} 2}$. The function works on both numbers and complex values.

See also: erfc, erfcx, erfi, inverf.

## erfc (x)

Returns the complementary error function of $x$, a number or complex value. It is defined $b y \operatorname{erfc}(x)=1-\operatorname{erf}(x)$. The return is a number or complex value.

See also: erf, erfcx, erfi, inverfc.

```
erfcx (x)
```

Implements the Scaled Complementary Error Function $\operatorname{erfcx}(x)=\exp \left(x^{\wedge} 2\right)^{\star} \operatorname{erfc}(x)$, with $x$ a number or complex number and - depending on the type of $x$ - a numeric or complex result.

See also: erfc, erfcx, erfi, inverfc.

## erfi (z)

Computes the imaginary error function erfi( $(z)=-\mid * \operatorname{erf}\left(\mid{ }^{\star} z\right)$ for real or complex $z$. The type of return depends on the type of $z$.

See also: erf, erfc, erfcx, inverfc.

## even (x)

Checks whether the number x is even. The operator returns true if x is even, and false otherwise. With non-integral numbers, the operator returns false. With the complex value x , the operator returns fail. See also: odd.
$\exp (x)$
Exponential function; the operator returns the value $e^{x}$, with e Euler's number. Complex numbers are supported. See also: antilog2, antilog10, cis, expx2, math.expminusone, math.exp2, math.exp10.

## exp2 (x)

Returns $2^{\times}$with x any (complex) number. See also: ${ }^{\wedge}$ operator, $\exp$, exp 10.

```
exp10 (x)
```

Returns $10 \times$ with $x$ any (complex) number. See also: ^ operator, exp, exp2.
$\operatorname{expx2}(x[, s i g n])$
Computes either $e^{x^{\wedge} 2}$ if sign $\geq 0$, or $e^{-x^{\wedge} 2}$ if sign $<0$ while suppressing error amplification that would occur from the in-exactness of the exponential argument $x^{2}$. x may be a number or complex number, while sign must be a number. By default, sign is positive.

## fact ( n )

Returns the factorial of $n$, i.e. the product of the values from 1 to $n . n$ may be $a$ non-negative integer or a negative or positive rational number that is non-integral, otherwise the function returns undefined. The function is implemented in Agena and included in the lib/library.agn file. It features a defaults remember table (rotable) which you may extend by adding new defaults to your agena.ini file (see rtable. defaults and Appendix A6).

See also: math.fall, math.pochhammer.

```
finite (x)
```

Checks whether the number or complex number x is neither $\pm$ infinity nor undefined (C NaN). The operator returns true or false.

See also: even, float, infinite, nan, odd, math.isinfinity, math.isordered.

```
flip (z)
```

The operator takes the complex number $z$ and returns the new complex number imag(z)!real(z), i.e. the real and imaginary parts are swapped. With numbers, always returns 0 .

See also: bea, conjugate, cosxx.
floor (x)
The function rounds downwards to the nearest integer larger than or equal to the number or complex number x . It works like the entier operator.
float (x)
Checks whether the number x is a float, i.e. not an integer, and returns true or false.

With complex numbers, if returns true if the real part is integral and the imaginary part is zero, and false otherwise.

If $x$ is not a (complex) number, the operator returns fail. With $+/$-infinity and undefined, returns false.

See also: finite, integral, isint.
fma ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ )
Performs the fused multiply-add operation ( x * y ) + z , with the intermediate result not rounded to the destination type, to improve the precision of a calculation. $x, y$, and $z$ must be numbers or complex numbers. See also: squareadd and muladd operators.
frac (x)
Returns the fractional part of the number x, i.e. $\mathrm{x}-\boldsymbol{\operatorname { i n t }}(\mathrm{x})$, thus preserving the sign. With complex numbers $a+1 * b$, returns frac(a) + I*frac(b).

See also: entier, int, modf.

## frexp (x)

Returns the mantissa $m$ and the exponent $e$ of the number $x$ such that $x=m 2^{e}$. $e$ is an integer, and the value of $m$ is in the range $[0.5,1$ ) (or zero when $x$ is zero). The operation is bijective, i.e. $\operatorname{ldexp}(f r e x p(x))=x$. With complex $x$, returns $m$ and e both for the real and the imaginary part.

See also: frexp 10, ilog2, Idexp, math.exponent, math.frexp, math.mantissa.

```
frexp10 (x)
```

Returns the mantissa $m$ and the exponent e of the number $x$ such that $x=m 10^{\circ}$. $e$ is an integer, and the value of $m$ is in the range $[0,1)$. Since floats are represented with base 2, and not base 10, the operation is not bijective, i.e. $\operatorname{Idexp}(\operatorname{frexp}(\mathrm{x})) \neq \mathrm{x}$. With complex $x$, returns $m$ and $e$ both for the real and the imaginary part. See also: frexp.

## gamma (x)

The gamma function $\Gamma$ x. x may be a number or complex value.
See also: Ingamma.
heaviside (x [, z])
The Heaviside function. Returns 0 if $x<0$, 1 if $x>0$, and $z$ if $x=0$, where $z$ defaults to undefined. The function is implemented in Agena and included in the lib/library.agn file.

See also: calc.smoothstep, math.clip, math.ramp, math.rectangular, math.unitise, math.unitstep.
hypot (x, y)
Returns $\sqrt{x^{2}+y^{2}}$ with $x, y$ numbers, complex numbers or a mix of them. With $x, y$ numbers, it is the length of the hypotenuse of a right triangle with sides of length $x$ and $y$, or the distance of the point $(x, y)$ from the origin. The function is slower but more precise than using sqrt along with square, avoiding over- and underflows and treating subnormal numbers accordingly. The return is a number or complex number.

See also: hypot2, hypot3, hypot4, invhypot, pytha, root, sqrt, calc.eucliddist.

## hypot2 (x)

Returns the number or complex number $\sqrt{1+x^{2}}$, with x a number or complex number. The function is slower but more precise than using sqrt along with square, avoiding over- and underflows and treating subnormal numbers accordingly.

See also: hypot, hypot3, hypot4, root, sqrt.
hypot3 (x)
Returns the number $\sqrt{1-x^{2}}$, with x a number or complex number. The function is slower but more precise than using sqrt along with square, avoiding over- and underflows and treating subnormal numbers accordingly.

See also: hypot, hypot2, hypot4, root, sqrt.
hypot4 (x, y)
Returns the number $\sqrt{x^{2}-y^{2}}$, with $x, y$ numbers, complex numbers or a mix of them. The function is slower but more precise than using sqrt along with square, avoiding over- and underflows and treating subnormal numbers accordingly.

See also: hypot, hypot2, hypot3, root, sqrt.
ilog2 (x)
Extracts the exponent of the number or complex number x (i.e. the integer part of the base-2 logarithm of the positive number $x$ ) and returns it as the number entier $(\log 2(\mathrm{x}))$.

See also: frexp, ilog10, In, log, $\log 2, \log 10$, math.ceillog2, math.ispow2.
ilog10 (x)
Extracts the exponent of number x and returns it as the number entier $(\log 10(\mathrm{x}))$.
See also: ilog2, log10.
implies ( $\mathrm{x}, \mathrm{y}$ )
With two booleans, the function computes not $(\mathrm{x})$ or y , with numbers returns:

$$
(\sim \sim x) \| y .
$$

```
infinite (x)
```

Checks whether the number or complex number x is $\pm$ infinity. The operator returns true or false.

See also: even, float, finite, nan, odd, math.isinfinity, math.isordered.
inrange ( $\mathrm{x}, \mathrm{a}, \mathrm{b}$ )
The operator checks whether x is part of the closed interval $[\mathrm{a}, \mathrm{b}]$ and returns true or false. All arguments must be numbers.

See also: in operator.
int (x)
Rounds x to the nearest integer towards zero. The operator also supports complex numbers. To round a float to a given decimal place, use xdf. To get the fractional part of a number, call frac.

See also: \operator, ceil, entier, float, iqr, mdf, modf, round, math.rint, xdf.

```
integral (x)
```

Checks whether the number x is an integer, i.e. not a float, and returns true or false.
With complex numbers, if returns true if the real part is integral and the imaginary part is zero, and false otherwise.

If $x$ is not a (complex) number, the operator returns fail. With + -infinity and undefined, returns false.

See also: finite, float, isint, multiple.
inverf (x)
Computes the inverse error function erf $^{-1}(\mathrm{x})$, where x is a number.
See also: erf, inverfc.

## inverfc (x)

Computes the inverse complimentary error function $\operatorname{erfc}^{-1}(\mathrm{x})$, where x is a number.
See also: erfc, inverfc.

```
invhypot (x, y)
```

Computes $1 / \sqrt{x^{2}+y^{2}}=1 / \operatorname{hypot}(x, y)$, is $35 \%$ faster than the naive $1 /$ hypot approach and is protected against underflow and overflow.

See also: hypot.

```
invsqrt (x)
```

Returns the inverse square root of numeric or complex $x$, i.e. $1 / s q r t(x)$.

See also: sqrt.

```
iqr (x, y)
```

Computes both the integer quotient and the integer remainder - rounded toward zero - of the number x divided by the number y and returns them. If x or y are not integers, the function returns undefined twice. The function is equivalent to the Agena representation:

```
iqr := proc(x :: number, y :: number) is
    if float(x) or float(y) then
        return undefined, undefined
    else
        return x \ y, x symmod y
    fi
end;
```

See also: \ and \% operators, drem, modf, math.cld, math.fld, math.modinv, math.modulus, symmod.

```
iscomplex (...)
```

Checks whether the given arguments are all of type complex and returns true or false.

## isint (...)

Checks whether all of the given arguments are integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: float, integral.

## isnegative (...)

Checks whether all of its arguments are negative numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnegint, isnegative, isnonneg, ispositive.

```
isnegint (...)
```

Checks whether all of the given arguments are negative integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnonnegint, isposint, isnegative, ispositive.

```
isnonneg (...)
```

Checks whether all of its arguments are zero or positive numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnegint, isposint, isnegative, ispositive.

```
isnonnegint (...)
```

Checks whether all of the given arguments are zeros or positive integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

```
isnonposint (...)
```

Checks whether all of the given arguments are zeros or negative integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

```
isnumber (...)
```

Checks whether the given arguments are all of type number and returns true or false.

```
isnumeric (...)
```

Checks whether the given arguments are all of type number or of type complex and returns true or false.

See also: numeric.
isposint (...)
Checks whether all of its arguments are positive integers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isnonposint.

```
ispositive (...)
```

Checks whether all of its arguments are positive numbers and returns true or false. If at least one of its arguments is not a number, the function returns fail.

See also: isposint, isnegative, isnonneg.
ldexp (m, e)
Returns $m 2^{\mathrm{e}}$ (e should be an integer, and m must be a number).
See also: frexp.
$\ln (x)$
Natural logarithm of $x$ with the base $e^{1}$. If $x$ is non-positive, the operator returns undefined. Complex numbers are supported.

See also: exp, log, log2, log10.

## lngamma (x)

Computes $\ln \Gamma \mathrm{x}$. If x is a non-positive number, the operator returns undefined. Complex numbers are supported.

See also: gamma, calc.Psi.
$\log (x, b)$
The operator returns the logarithm of the number or complex number x to the base b , with b a number or a complex number.

See also: In, log2, log10.

## $\log 2(x)$

Returns the base-2 logarithm of the number or complex number x .
See also: antilog2, ilog2, In, log, log10, math.ceillog2.
$\log 10(x)$
Returns the base-10 logarithm of the number or complex number x.
See also: antilog2, ilog10, In, log, log2.

```
mdf (x [, n])
```

Rounds up the number $x$ at its $n$-th decimal place and returns a number. If $x$ is positive, rounds towards $+\infty$; if x is negative, rounds towards $-\infty$. The default of n is 2. With complex $x$, rounds both the real and imaginary parts.

See also: entier, int, round, xdf.

## modf (x)

Returns two numbers, the integral part of the number x and its fractional part. The integral part is rounded towards zero. Both the integral and fractional part of the return have the same sign as $x$. The sum of the two values returned equals x . The function actually is a wrapper to C's modf. With complex $x$, returns the integral and fractional parts for both its real and the imaginary part.

See also: <br>, \%, frac, entier, int, symmod, mod assignment statement.

```
muladd (x, y, z)
```

The operator computes $x^{*} y+z$ with extended internal precision, with $x, y, z$ all numbers. See also: fma.

```
multiple (x, y [, option])
```

Checks whether numeric or complex x is a multiple of numeric $y$, i.e. whether $\mathrm{x} / \mathrm{y}$ evaluates to an integral, and returns true or false.

Also returns true with $\mathrm{x}=0$ and any non-zero y .
If y is zero, undefined or +/-infinity, the function returns fail.
With complex $x$, returns true if both real $(x) / y$ and $\operatorname{imag}(x) / y$ evaluate to the same integral, or if real $(\mathrm{x}) / \mathrm{y}$ evaluates to an integral and imag(x) is zero.

By passing the optional third argument true, a tolerant check is done, with subnormal x or y first converted to zero, and a subsequent approximate equality check to the nearest integer of $x / y$. The tolerance value internally used is the value of DoubleEps at the time of the function call.

In most cases, it may suffice to just call integral( $x / y$ ), which is twice as fast as this function.
nan (x)
Checks whether the number or complex number x evaluates to undefined (NaN). The operator returns true or false.

See also: finite, float, math.isordered.
$\mathbf{x}$ nand $y$
The operator returns the bitwise complement Boolean `and`, a signed integer: $\sim \sim(x \& \& y)$.

See also: bytes.nand32.

## $x$ nor $y$

The operator returns the bitwise complement Boolean `or` , a signed integer:
$\sim \sim(x|\mid y)$.
See also: bytes.nor32.
nonzero (x)
Checks whether the number or complex number $x$ is neither 0 nor $0+0 *$, respectively. The operator returns true or false.

See also: zero.
odd (x)
Checks whether the number x is odd. The operator returns true if x is odd, and false otherwise. With non-integral numbers, the operator returns false. With the complex value $x$, the operator returns fail.

See also: even.

```
polar (z)
```

Transforms the complex number $z$ in Cartesian notation or the number $z$ to polar form and returns two numbers: the magnitude (modulus) and the argument (phase angle), in this order. If $z$ is a number and is zero, or if $z$ is complex and its real and imaginary parts equal zero, the function returns zero twice.

See also: abs, argument, cabs, cis.
proot ( $\mathbf{x}, \mathrm{n}$ )
Returns the principal $n$-th root of the number or complex value $x$. $n$ must be a positive integer. The principal $n$-th root in the complex domain is the first root found starting from the positive real axis going counter-clockwise.

See also: cbrt, hypot, hypot2, hypot3, hypot4, root, sqrt.

```
pytha (a, b)
```

Computes the Pythagorean equation $c^{2}=a^{2}+b^{2}$, without undue underflow or overflow and treating subnormal numbers accordingly, for numbers $a, b$.

See also: hypot, squareadd.

## qmdev (o)

The operator computes the sum of the squared deviations of each observation $o_{i}$ in the sequence, register, or table $\circ$, from its arithmetic mean $\mu$, i.e.

$$
\sum_{i=1}^{n}\left(o_{i}-\mu\right)^{2}
$$

The return should be divided either by the number of elements n in the distribution $\circ$ to calculate its population variance, or by $\mathrm{n}-1$ to compute its sample variance.

The Knuth-Welford algorithm used by the operator tries to prevent round-off errors as much as possible.

See also: stats.sd, stats.var.

```
recip (x)
```

Returns the inverse $1 / x$ of a number or complex number $x$.
See also: /, fastmath.reciprocal.

```
root (x [, n])
```

Returns the non-principal $n$-th root of the number or complex value x. n must be an integer and is 2 by default. Note, that since the function computes the non-principal root, with complex $x, \operatorname{root}(x, n) \neq x^{\wedge}(1 / n)$. In the complex domain, the function returns the $n$-th root of $x$ whose argument is nearest to the argument of $x$. See also: argument, cbrt, hypot, hypot2, hypot3, hypot4, proot, sqrt.

```
round (x [, d])
```

Rounds the number x to its d -th digit, using the round-half-up method. The return is a number. If $d$ is omitted, the number is rounded to the nearest integer. If d is positive, the function rounds to the d-th fractional digit. If a is negative, it rounds to the $\alpha$-th integral digit. round treats positive and negative values symmetrically, and is therefore free of sign bias. With complex numbers $x=a+l^{*} b$ returns round(real(a), d) + I*round(imag(a), d).

The following Agena code explains the algorithm used:

```
round := proc(x, d) is
    d := d or 0; # assign zero if d is null
    return int((10^d)*x + sign(x)*0.5) * (10^(-d))
end;
```

See also: ceil, entier, int, mdf, xdf, math.rint.

```
scalbn (x, n)
```

Just an alias for Idexp.
$\sec (x)$
Returns the secant $\frac{1}{\cos (x)}$ as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.
sech ( x )
Returns the hyperbolic secant as a number (in radians). The function is implemented in Agena and included in the lib/library.agn file. The function works on both numbers and complex values.
sign (x)
Determines the sign of the number or complex value x . The result of the operator is determined as follows:

- 1, if real $(x)>0$ or real $(x)=0$ and $\operatorname{imag}(x)>0$
- -1 , if real( x$)<0$ or real( x$)=0$ and $\operatorname{imag}(\mathrm{x})<0$
- O otherwise, even for -0.

If $x$ is undefined, sign returns undefined.
See also: math.copysign, math.flipsign, math.mulsign, signum, | operator.

## signum (x)

Determines the sign of the number or complex value x . If x is a number, the result of the operator is determined as follows:

- 1 , if $x \geq 0$
- -1 otherwise.

With complex $x$, the operator returns $x /|x|$.
If x is undefined, signum returns undefined.

See also: math.copysign, math.mulsign, sign, | operator.

```
sin (x)
```

The operator returns the sine of x (in radians). Complex numbers are supported.

See also: math.sincos, math.sinpi.
sinc ( x )
The operator returns the un-normalised cardinal sine of $x$ (in radians), i.e. $\sin (x) / x$, with $\operatorname{sinc}(0)=1$. Complex numbers are supported.

See also: cosc, math.rectangular, tanc.
$\sinh (x)$
The operator returns the hyperbolic sine of x (in radians). Complex numbers are supported. See also: cosh, tanh, math.sinhcosh.
sqrt ( x )
Returns the square root of $x$.

If $x$ is a number and negative, the operator returns undefined.
With complex numbers, the operator returns the complex square root, in the range of the right halfplane including the imaginary axis.

See also: cbrt, hypot, hypot2, hypot3, invsqrt, proot, root, fastmath.sqroot, fastmath.sqrffast.

```
square (x)
```

The operator squares the number or complex number $x$ and returns $x * * 2$.
See also: **, ^, cube operators, math.issquare, squareadd.

```
tan (x)
```

The operator returns the tangent of x (in radians). Complex numbers are supported. See also: math.tanpi.

## tanc (x)

The operator returns the un-normalised cardinal tangent of $x$ (in radians), i.e. $\tan (x) / x$, with $\operatorname{tanc}(0)=1$. Complex numbers are supported.

See also: cosc, math.rectangular, sinc.

## $\tanh (x)$

The operator returns the hyperbolic tangent of x (in radians). Complex numbers are supported.

See also: cosh, sinh.
xdf (x [, n])
Rounds down the number x at its n -th decimal place towards zero and returns a number. This is equivalent to truncating a float at its $n$-th decimal place. The default of $n$ is 2 .

With complex x , rounds both the real and imaginary parts.
See also: entier, int, round, mdf.

## $x$ xnor $y$

With numbers, the operator returns the bitwise complement Boolean `xor`, a signed integer: $\sim \sim(x$ ^ ^ y). With Booleans, returns not(x xor y), sometimes also called `if-and-only-if` (iff). See also: bytes.xnor32.

## $x$ xor $y$

With Booleans, returns x < > y. With non-booleans: returns the first operand if the second operand evaluates to null, otherwise the second operand will be returned.

See also: ^ ^, bytes.xor32.
zero (x)
Checks whether the number or complex number x is 0 or $0+0 *$ l, respectively. The operator returns true or false.

See also: nonzero.

### 11.1.2 math Library

This library is an interface to the standard $C$ math library. It provides all miscellaneous functions inside the table math.
math.accu ([init [, method]])
Returns a factory that gets a number with each call, adds it to an internal accumulator, and returns the accumulated sum. If the factory is called with no argument, the current accumulated sum will be returned.

The function can be used if high accuracy numeric addition is needed. The initial value of the accumulator is 0 . If init, a number, is given, the accumulator is set to init instead.

The function automatically takes care of storing and processing internal correction values - so the user does not have to worry about this.

By default, Neumaier summations is used. By passing a method (of type string), you may use an alternative algorithm to add numbers:

| method | algorithm |
| :--- | :--- |
| 'babuska' | Kahan-Babuška summation, highest accuracy but slowest |
| 'kahan' | classic Kahan summation, lowest accuracy but fastest |
| 'kbn' | Kahan-Babuška-Neumaier compensated summation, used in the <br> Julia programming language |
| 'neumaier' | Neumaier summation, good accuracy and performance (default) |
| 'ozawa' | Kahan-Ozawa summation |
| 'raw' | no auto-correction |

See also: factory.count, math.koadd.
math.arccosh (x)
Returns the inverse hyperbolic cosine of the number x and returns a number. It works in the real domain only, and is a simple port of the acosh $C$ function.

See also: arccosh.
math.arcsinh (x)
Returns the inverse hyperbolic sine of the number $x$ and returns a number. It works in the real domain only, and is a simple port of the asinh $C$ function.

See also: arcsinh.

## math.arctanh (x)

Returns the inverse hyperbolic tangent of the number $x$ and returns a number. It works in the real domain only, and is a simple port of the atanh C function.

See also: arctanh.
math.branch (x [, d [, subs]])
Returns its argument x - a number - if x is non-negative, otherwise returns 0 . By passing any non-negative optional number a (the 'direction'), the return is the same.

By passing any non-positive optional number d , returns x if it is negative, otherwise returns 0 .

If x should be undefined, you can return any other number by passing the optional argument subs, which is undefined by default.

See also: math.clip, math.wrap, end of Chapter 11.1.2 for a comparison chart.

```
math.ceillog2 (x)
```

Returns the smallest exponent to 2 equals or greater than $x$, i.e. $\operatorname{ilog} 2(x-1)+1$, where x is a positive integer. If $\mathrm{x}=1$, the result is 0 ; if $\mathrm{x}<1$, undefined will be returned.

See also: ilog2, math.ceilpow2.

```
math.ceilpow2 (x)
```

Finds the smallest power of 2 greater than or equal to $x$, where x is a non-negative integer. If $x=0$, the result is 1 ; if $x<0$, undefined will be returned. Examples: math.ceilpow2(3) $\Rightarrow 4=2^{2}$, and math.ceilpow2(8) $\Rightarrow 8=2^{3}$.

The function returns fail if $\mathrm{x} \geq 2^{31}$.
See also: ilog2, math.ceillog2, math.floorpow2, math.ispow2.
math.chop (x [, eps [, method [, n]]]])
Shrinks a number or complex number x more or less near zero to exactly zero, using one of many methods, passed as an integer. The default for eps is Eps. The standard method is 0 for hard shrinking. n is used in the SmoothGarrote method.
$\left.\left.\begin{array}{|c|l|c|l|}\hline \text { method } & \text { Comment } & \text { Value } & \text { Domain } \\ \hline 0 & \text { "Hard", performs hard shrinking } & 0 & |x| \leq e p s \\ x & 0 & |x|>e p s\end{array} \right\rvert\, \begin{array}{l}|x| \leq e p s \\ |x|>e p s\end{array}\right]$

Method 2 has not been implemented. The function is a port of Mathematica's Chop function.

See also: math.clip, math.unitise, math.zeroin.
math.cld (x, y)
Returns the largest integer less than or equal to the real quotient $\frac{x}{y}$ of the numbers $x$ and $y$.

See also: \operator, math.fld.

```
math.clip (x [, a [, b [, f]]])
math.clip (x, a)
```

In the first form, returns x clipped to be between a and b . The return is x if $\mathrm{a} \leq \mathrm{x} \leq \mathrm{b}$, a if $\mathrm{x}<\mathrm{a}$, and b if $\mathrm{x}>\mathrm{b}$. By default $\mathrm{a}=-1, \mathrm{~b}=+1$. If function f is given which should return one numeric result, then if $x$ is not in $[a, b]$, the result of $f(x)$ will be returned.

In the second form, returns $x$ clipped to be between $-a$ and $+a_{1}-a$ if $x<a$ and $+a$ if $x>+a$.

See also: calc.sigmoid, heaviside, math.branch, math.chop, math.rectangular, math.unitise, math.wrap, end of Chapter 11.1.2 for a comparison chart.

```
math.compose (coeffs [, b])
```

Takes a table, sequence or register of coefficients coeffs and a base b and returns the composed number. In coeffs, the highest-order digit as the first element and the lowest-order digit as the last element. By default, the base is 10. The function does not take care of potential overflows. It is the complement to math.decompose.
math.congruentprime (n [, a [, b] ])
Determines whether integer $n$ is a prime number congruent to a modulo $b$ - or in other words: a prime of the form $b n+a$, and returns it; otherwise for $n$, returns the next prime number congruent to a modulo b . By default, a is 3 and b is 4 .

The function is implemented in Agena and included in the lib/library.agn file.
See also: math.nextprime.

## math. convertbase (s, a, b)

Converts a number s or a number represented as a string s from base a to base b. a and b must be integers in the range 1 to 36 . The number in s must be an integer of any sign. Floats are not allowed. The return is a string. The function is implemented in Agena and included in the lib/library.agn file.

See also: math.decompose, math.ndigits.

```
math.copysign (x, y)
```

Returns a number with the magnitude of $x$ and the sign of $y$, i.e. $\operatorname{abs}(x)$ * $\operatorname{sign}(y)$. If $y$ is 0 , then its sign is considered to be 1 . It is a plain binding to $\mathrm{C}^{\prime}$ copysign function and does not post-process its result.

See also: math.flipsign, math.mulsign, math.signbit, sign, signum.

```
math.cospi (x)
```

Returns $\cos \left(\pi^{*} x\right)$ for number $x$ with better precision than calling the respective standard operator.

See also: cos, math.sincos, math.sincospi, math.sinpi, math.tanpi.

```
math.dd (x)
```

Converts a number x representing a sexagesimal number in Tl-30 DMS format into its decimal representation, and returns a number. For example: 10.3045 representing $10^{\circ} 30^{\prime} 45$ returns 10.5125 .

The function is implemented in Agena and included in the lib/library.agn file.
See also: math.dms, math.splitdms, math.todecimal, math.tosgesim.
math.decompose (x [, b])
Splits an integer x to the base b into its digits and returns them in a sequence, with the highest-order digit as the first element and the lowest-order digit as the last
element. Any sign of x is ignored. By default, the base is 10, but you may choose any other positive base.

## Example:

```
> b := 256;
> math.decompose(15 * b^2 + 7 * b + 1, 256):
seq(15, 7, 1)
```

See also: math.compose, math.convertbase, math.ndigits.

```
math.dirac (x [, eps])
```

The Dirac delta function, also known as the impulse function, returns 0 for all numbers x other than 0 , and infinity if $\mathrm{x}=0$, iff eps is set to zero which is the default.

If eps is set to any positive value x , returns $1 /\left(2^{*} \operatorname{eps}\right)^{*} \exp (-|x| / e p s)$ even if $x=0$.

## math.dms (x)

Converts a number representing a decimal number $x$ into its $\mathrm{TI}-30$ sexagesimal DMS representation and returns a number. For example: 10.5125 returns 10.3045, representing 10³0'45".

See also: math.dd, math.splitdms, math.todecimal, math.tosgesim.

```
math.eps ([x [, option]])
```

The function returns the machine epsilon, the relative spacing between the number $|x|$ and its next larger number in the machine's floating point system. If no argument is given, $x$ is set to 1 .

On x86 machines and with Agena numbers, i.e. C doubles, eps(1) and eps() return $2.2204460492503 e-016=2^{-52}$, and eps(2) returns 4.4408920985006e-016 $=2^{-51}$.

When given any second argument, the function computes a `mathematical' epsilon value that is also dependent on the magnitude of its argument x . It can be used in difference quotients, etc., for it prevents huge precision errors with computations on very small or very large numbers. The mathematical epsilon with respect to $x$ is equal to $\left.x^{*} \operatorname{sqrt(math} . e p s(x)\right)$.

See also: math.epsilon, math.nextafter.

```
math.epsilon (x [, method])
math.epsilon (f, x [, ...] [, iters=n])
```

In the first form, by default returns the relative spacing between $|x|$ and its next larger number on the machine's floating point system, taking into account the magnitude of its argument. In this case, the function works like math.eps with the
true option set, but is 20 percent faster. If $|x|<1$, you may choose a constant epsilon value yourself, e.g. Eps.

In the first form, you may choose between different methods to determine an epsilon value, where ulp = math.nextafter( $x$, infinity) - x:

| Method | Formula |
| :---: | :---: |
| 0 (default) | $x^{*}$ sqrt(ulp) |
| 1 | $x^{*} \operatorname{cbrt}($ ulp $)$ |
| 2 | sqit(ulp) * $(x+$ sqit(ulp) $)$ |
| 3 | cbrt(ulp) * $(x+$ cbrt(ulp) $)$ |

In the second form, by passing a function f and an argument x , the function determines an epsilon value by taking the function value $\mathrm{f}(\mathrm{x})$ into account, using a divided difference table. If f is multivariate, pass its further arguments tight after x .

## math.expminusone (x)

Returns a value equivalent to $\exp (\mathrm{x})-1$, with x a number. It is computed in a way that is accurate even if x is near 0 , since $\exp (\sim 0)$ and 1 are nearly equal.

The function can be used, for example, in financial mathematics, to calculate small daily interest rates, among other things.

See also: expx2, math.Inplusone.

```
math.exponent (x)
```

Returns the exponent e of a number x such that math.mantissa(x) * $2^{e}$ equals x . The result is identical to the second result returned by frexp. The function is around 20 percent faster but returns correct results only if your system supports IEEE 754 floating-point numbers, whereas frexp always works regardless of the internal representation.

See also: frexp, math.mantissa, math.uexponent.

```
math.fall (x, n)
```

The falling factorial function computes $x^{*}(x-1)^{\star}(x-2)^{*} \ldots{ }^{*}(x-n+1)$, with $x a$ number and n an integer. If n is negative, the rising factorial function (Pochhammer function) is computed.

See also: fact, math.pochhammer.

```
math.fdim (x, y [, a])
```

The function returns $\mathrm{x}-\mathrm{y}$ if its argument x , a number, is greater than or equal y , else it returns a, which is 0 by default.
math.fib (n)
Returns the $n$-th Fibonacci number, with $n$ a non-negative integer. If $n>76$, the function returns fail since the result is too large to be accurately represented. The defaults are: math. $\mathrm{fib}(0)=0$ and math. $\mathrm{fib}(1)=1$; with all other values computed by math.fib(n) := math.fib(n-2) + math.fib(n-1).

See also: math.fibinv.
math.fibinv (n)
For any non-negative integer $n$ returns the index $i$ of the Fibonacci number with fib(i) $<=\mathrm{n}<\mathrm{fib}(\mathrm{i}+1)$. The function is implemented in Agena and included in the lib/library.agn file.

See also: math.fib.
math.fld (x, y)
Returns the largest integer less than or equal to the real quotient $\frac{x}{y}$ of the numbers $x$ and y .

See also: \operator, math.cld.

```
math.flipsign (x, y)
```

Returns the number x with its sign flipped if y (a number) is negative. For example, $\operatorname{abs}(x)=$ flipsign $(x, x)$.

See also: math.copysign, math.signbit, sign.
math.floorpow2 (x)
Finds the largest power of 2 less than or equal to x , where x is a non-negative integer. If $x<2$, the result is $x$. If $x<0$, undefined will be returned. Examples: math.floorpow2(3) $\Rightarrow 2=2^{1}$, and math.floorpow2(8) $\Rightarrow 8=2^{3}$.

The function returns fail if $x \geq 2^{31}$.

See also: ilog2, math.ceillog2, math.ceilpow2, math.ispow2.

```
math.fpclassify (x)
```

For the given number x, returns

- 0 if x is undefined (= constant math.fp_nan),
- 1 if x is infinite, i.e. +/-infinity (= constant math.fp_infinite),
- 2 if x is subnormal (= constant math.fp_subnormal,
- 3 if $x$ is zero (= constant math.fp_zero),
- 4 if x is normal (= constant math.fp_normal), including irregular values $\geq 2^{52}$.

Thus, for example, `ordinary` numbers are represented by results greater than 2 .

The function returns fail if it could not determine the type of floating-point number (of C type double). It is a platform-independent port of C's fpclassify.

See also: math.isnormal, math.issubnormal.
math.fraction (x [, err])
Given a number $x$, this function outputs two integers and a number: the numerator n , the denominator d , and the accuracy epsilon, such that $\mathrm{x}:=\mathrm{n} / \mathrm{d}$ to the accuracy epsilon $:=|(x-n / d) / x| \leq e r r$.

The error err should be a non-negative number, and by default is 0 .

The function is implemented in Agena and included in the lib/library.agn file.
See also: div package.

```
math.frexp (x [, option])
```

Returns the sign $s$, the mantissa $m$ and the exponent $e$ of the number $x$, in this order, such that $s^{*} m^{*} 2^{e}=x$. The sign is -1 if $x$ is negative (including -0) and 1 otherwise. The mantissa is a float in the range $[0.5,1$ ) except for $\mathrm{x}=0$, where the result is 0 . The exponent is a negative or positive integer or zero.

If any option is given, then instead of the sign the sign bit $s$ will be returned: 1 if x is negative or -0 , and 0 otherwise. In this case $\mathrm{x}=\operatorname{signum}(-\mathrm{s}) * \mathrm{~m}^{*} 2^{\mathrm{e}}$.

The function works correctly only on IEEE 754-compliant systems.
See also: frexp, Idexp, ilog2, math.exponent, math.mantissa.

```
math.gcd (x, y)
```

Returns the greatest common divisor of the numbers x and y as a number. If x or y is not an integral, 1 will be returned. The function is implemented in Agena and included in the lib/library.agn file.

See also: math.lcm.

```
math.hEps
```

Deprecated. Represented the value $1.4901161193847656 e-12$, an epsilon value more or less in the middle of Eps and DoubleEps. See also: hEps constant, environ.kernel/hEps.
math.iscube ( $n$ )
Checks if a given integer $n$ is a perfect cube, i.e. if $\operatorname{cbrt}(\mathrm{n})^{\wedge} 3=n$.
See also: cbrt, cube, math.issquare.
math.isfib ( n )
Checks whether the non-negative integer n is a Fibonacci number.
See also: math.fib, math.fibinv.

```
math.isinfinity (x)
```

Returns -1 if its numeric argument x is -infinity, +1 if x is + infinity, or 0 if neither.
See also: finite, infinite.
math.isirregular (x)
Checks whether a number or complex number can be represented exactly on your system. I returns:

- false if $|x|<2^{52}$ : a number with decimal places can internally be represented as a number with decimal places, but not necessarily itself. With $n<52$, the spacing between two subsequent representable numbers is the fraction $2^{n-52}$.
- fail if $2^{52} \leq|x| \leq 2^{53}+1$ : representable numbers are exactly the integers; spacing between representable numbers is exactly 1 .
- true if $|x|>2^{53}+1$ : an integer mostly cannot be exactly represented; with $n>$ 52 , spacing is the integer $2^{n-52}$.

With complex $x$, checks whether at least the real or imaginary part evaluates to false or fail - according to the rule mentioned above - and returns that; otherwise if both parts evaluate to true, returns true.
math.isminuszero (x)
Returns true if x is -0 (minus zero) and false otherwise. See also: math.signbit.
math.isnormal (x)
Returns true returns true if a number is neither $+0,-0,+$ infinity, -infinity, undefined nor subnormal. The result is equal to the expression math.fpclassify $(x)=$ math.fp_normal.

With complex x , returns math.isnormal(real( x$)$ ) and math.isnormal(imag(x)).
See also: finite, math.isminuszero, math.issubnormal.

```
math.isordered (x, y)
```

Returns false if at least one of its arguments x and y - two numbers - is undefined, and true otherwise. See also: nan.

```
math.ispow2 (x)
```

Checks whether a given non-negative number $x$ is a power of base $2\left(x=2^{\log 2(x)}\right)$ and returns true or false. Also returns false if x is negative.

The function returns fail if its argument is $\pm$ infinity or undefined.

```
math.isprime (x)
```

Returns true, if the integral number x is a prime number, and false otherwise. Note that you have to take care yourself that x is an integer and is less than the largest integer representable on your system.

See also: math.nextprime, math.prevprime.

## math.isqrt (x)

Returns the integer square root of the number $x$ : the largest integer $m$ such that $m * m \leq x$.
math.issquare ( $n$ )
Checks if a given integer $n$ is a perfect square, i.e. if $\operatorname{sqrt}(\mathrm{n})^{\wedge} 2=n$. Any power of two is a perfect square, for example $n=1,4,9,16,25,36,49$, etc.

See also: sqrt, square, cube, math.iscube, math.ispow2.
math.issubnormal (x)
Checks whether the number x is subnormal, i.e. whether internally the leading digit of its mantissa is 0 . The function returns true or false. Subnormal numbers are very close to zero, have reduced precision and lead to excessive CPU usage. They are in the range $[-2.2250738585072009 \mathrm{e}-308,-4.9406564584124654 \mathrm{e}-324]$ and [4.9406564584124654e-324, 2.2250738585072009e-308]. 0, undefined and
+/-infinity are not subnormal. Please note that the next representable number after 0 (towards $+\infty$ ) is subnormal.

With complex $x$, returns math.issubnormal(real(x)) or math.issubnormal(imag(x)).

## See also: math.normalise, math.smallestnormal, math.two54, math.zerosubnormal.

```
math.koadd (x, y [, q])
```

The function adds x and y using Kahan-Ozawa round-off error prevention and returns two numbers: the sum of x and y plus the updated value of the correction variable q. The optional correction variable q should be 0 at first invocation, and the previously returned correction variable otherwise - if $q$ is not given, it defaults to 0 .

The following algorithm used is:

```
math.koadd := proc(s :: number, x :: number, q) is
    local sold, u, v, w, t;
    q := optnumber (q, 0);
    V := x - q;
    sold := s;
    s := s + v;
    if abs(x) < abs(q) then
        x, q := -q, x
    fi;
    u := (v - x) + q;
    if abs(sold) < abs(v) then
        sold, v := v, sold
    fi;
    w := (s - sold) - v;
    q := u + W;
    return s, q
end;
```

A typical usage should look like:

```
x, q -> 0;
y := 0.1;
while x < 1 do
    x, q := math.koadd(x, y, q)
od;
print(s + q);
```

See also: math.accu, stats.sumdata.

## math.largest

This constant represents the largest positive number representable in Agena. It is computed during start-up and may be different from the setting returned by environ.system, the latter statically compiled into the Agena binary. The smallest negative number (nearest to $-\infty$ ) is the negative of this constant, i.e. - math.largest.

## See also: math.lastcontint, math.smallest.

## math.lastcontint

This constant represents the largest integer i on the floating-point system such that i $1<>$ i. In other words: The constant represents the largest integer value that can be stored in an Agena number without loss of precision. On 32-bit systems (and higher), it is equal to $2^{53}=9,007,199,254,740,992$.

See also: math.largest.
math.lcm ( $\mathrm{x}, \mathrm{y}$ )
Returns the least common multiple of to numbers $x$ and $y$ as a number. The function is implemented in Agena and included in the lib/library.agn file.

See also: math.gcd.

```
math.lnabs (x)
```

Returns $\operatorname{In}(\mathbf{a b s}(\mathrm{x}))$ for numeric or complex x . With complex numbers, takes care of underflows.

```
math.lnplusone (x)
```

Returns a value equivalent to $\ln (1+x)$, with $x$ a number. It is computed in a way that is accurate even if $x$ is near zero.

It can be used, for example, in financial calculations, when computing small daily interest rates.

Example: $\ln (1.0000000000000001) \Rightarrow 0$, math.Inplus $1(0.0000000000000001) \Rightarrow$ 1e-016.

See also: math.expminusone.

```
math.logs (x, b)
```

The iterated logarithm of $\mathrm{x}, \log ^{\star}(\mathrm{x})$ (for `log star`) returns the number of times the logarithm function to a given base b must be iteratively applied on x until the result reaches or drops below 1. If $x<=1$, returns 0 . The algorithm is equivalent to:

```
logs := proc(x, b) is
    for i from 0 while x > 1 do
        x := log(x, b)
    od;
    return i
end;
```

math.mantissa (x)
Returns the mantissa $m$ of a number $x$ such that $m *{ }^{\wedge}$ math.exponent( $x$ ) equals $x$. The result is identical to the first result returned by frexp, and is in the range $[0.5,1$ ) (or zero when $x$ is zero). The function is around 20 percent faster but returns correct results only if your system supports IEEE 754 floating-point numbers, whereas frexp always works regardless of the internal representation.

See also: frexp, math.exponent, math.significand.

```
math.max (x [, ...])
```

Returns the maximum value among its arguments of type number.

```
math.min (x [, ...])
```

Returns the minimum value among its arguments of type number.

```
math.modinv (a [, m])
```

Computes the modular (multiplicative) inverse $\mathrm{a}^{-1}$ of an integer a (modulo m) such that $a^{*} a^{-1}=1$ (modulo m). $m$ is 257 by default. If $m$ is not prime, then not every non-zero integer a has a modular inverse - in this case the function returns undefined.

See also: \% operator, drem, iqr, symmod, math.modulus.

```
math.modulus (x, y)
```

The function is a plain binding to the C `\%` modulus operator. Both its arguments must be integers. The return is an integer. If $\mathrm{y}=0$, the function returns undefined.

See also: \% operator, bytes.mod32, drem, hashes.fibmod32, iqr, symmod, math.modinv, math.nearmod.

```
math.morton (x, y)
```

Interleaves the bits of integers $x$ and $y$, so that all of the bits of $x$ are in the even positions and y in the odd; the function can be used to linearising 2D integer co-ordinates, combining $x$ and $y$ into a single integer that can be compared easily. It has the property that a number is usually close to another if their x and y values are close.
math.mulsign ( $x, y$ )
Multiplies, not copies, its first argument with the sign of its second, and returns x * signum(y).

See also: math.copysign, math.flipsign, math.signbit, sign, signum.
math.ndigits (x [, b])
Returns the number of integer digits - without decimal places - in the number x to the base b . By default, b is 10 .

If b is -10 , counts the number of decimal places (fractional digits) in x , where x is considered to be of base 10. This feature is experimental and not failsafe.

See also: math.decompose, math.nthdigit.
math.nearbyint (x)
Returns x rounded to the nearest integer, returns the same result as round $(\mathrm{x}, 0$ ) does but is implemented differently and $5 \%$ faster. The function has been included for C math library compatibility reasons only.

See also: int, math.rint, math.trunc.

```
math.nearmod (x, m)
```

Returns the closest value to the given number $x$ divisible by the given modulus $m$, equivalent to round $(\mathrm{x} / \mathrm{m})$ * m. See also: \%, math.modulus.

```
math.nextafter (x, y)
```

Returns the next machine floating-point number of x in the direction toward y .
See also: +++ and --- operators, math.eps, math.ulp.
math.nextmultiple ( $\mathrm{n}, \mathrm{b}$ )
Returns the next multiple of an integer $n$ to the given base $b$, towards +infinity if $b$ is positive, and towards -infinity, if b is negative.

```
math.nextpower (x, base [, option])
```

By default returns the smallest power of base greater than x . If the third argument is true, then the smallest power of base greater than or equal to x will be returned.
math.nextprime (x)
Returns the smallest prime greater than the given number x .
See also: math.congruentprime, math.prevprime, math.isprime.
math.norm (x, a1:a2 [, b1:b2])
Converts the number $x$ in the scale [a1, a2] to one in the scale [b1, b2]. The second and third arguments must be pairs of numbers. If the third argument is missing, then $x$ is converted to a number in $[0,1]$. The return is a number.

See also: linalg.scale, math.wrap, stats.scale.
math.normalise (x [, option])
Checks whether its numeric argument x is subnormal and in this case normalises it, i.e. returns a non-zero normalised value $x^{*} 2^{64}$ that is close to $x$; otherwise returns its argument x unaltered. If any option is given, the unsigned high 4-byte word of the result will be returned, too.

With complex $x$, normalises both its real and imaginary part if necessary and returns the complex number math.normalise(real(x)) + I*math.normalise(imag(x)); the option is not supported in this case.

It is useful to prevent excessive CPU usage with values very close to zero.
For more information, see math.issubnormal.
See also: math.zeroin, math.zerosubnormal.

```
math.nthdigit (x, n)
```

Returns the $n$-th digit of the number $x$, with $n$ an integer. To evaluate an integer digit, n should be positive; for a decimal place, n should be negative.

The function is written in Agena and included in the lib/library.agn file.

## See also: math.ndigits.



Evaluates a piecewise-continuous function. cond ${ }_{1}$, etc. are relations evaluating to Booleans, and $f_{1}$, etc. numeric expressions. The arguments are checked from left to right and as soon as a condition cond ${ }^{2}$ is met, piecewise returns the respective value $f_{k}$. If no condition meets, the function returns fotherwise, and undefined if not given.

The implementation is far from perfect as all of its arguments are evaluated before executing the procedure. Better use the Boolean operator and and or, for example:

- math.piecewise( $x<2,-1, x<3,1$, infinity) and
- $\mathrm{x}<2$ and -1 or $\mathrm{x}<3$ and 1 or infinity
are equivalent, but the latter is around 15 times faster due to application of the McCarthy Rule.

```
math.pochhammer (x, n)
```

Computes the Pochhammer function (rising factorial), where both x and n are real numbers. It returns the number:

$$
\frac{\Gamma(\mathrm{x}+\mathrm{n})}{\Gamma(\mathrm{x})}
$$

See also: fact, math.fall.
math.powmod (x, p, m)
Computes $\mathrm{x} \wedge \mathrm{p} \% \mathrm{~m}$.
math.prevprime (x)
Returns the largest prime less than the given number x .
See also: math.nextprime, math.isprime.

```
math.quadrant (x)
```

This function returns the quadrant of an angle $x$ given in radians and returns an integer in [1, 4].
math.ramp (x)
For number x , gives x if $\mathrm{x}>0$ and 0 otherwise.
See also: heaviside, math.rectangular.
math.random ([m [, n]])
When called without arguments, returns a pseudo-random float with uniform distribution in the range $[0,1)$.

When called with two integers $m$ and $n$, math.random returns a pseudo-random integer with uniform distribution in the range $[m, n]$.

The call ‘math.random(n)`, for a positive \(n\), is equivalent to `math.random(1, n)'. The call `math.random(0)` produces an integer with all bits (pseudo) random.

This function uses the xoshiro256** algorithm to produce pseudo-random 64-bit integers, which are the results of calls with argument 0 . Other results (ranges and floats) are unbiased extracted from these integers.

Agena initializes its pseudo-random generator with the equivalent of a call to math.randomseed with no arguments, so that math.random should generate different sequences of results each time the program runs.
math. randoms ([m [, n]] [, option])
This function creates random numbers as Agena did before version 2.27.10.
When called without arguments, returns a pseudo-random real number in the range $(0,1)$. It can generate up to 2 * environ.maxlong unique random numbers in this interval.

When called with a number $m$, math.random returns a pseudo-random integer in the range $[1, m]$.

When called with two numbers $m$ and $n$, math.random returns a pseudo-random integer in the range [ $m, n$.

If option, any Boolean, is given, then the sequence of values returned should be arbitrary, otherwise it is always the same unless math.randomseed is called with other values.

See also: math.randomseed, skycrane.dice.
math.randomseed ([x, y])
When called with at least one argument, the integer parameters x and y are joined into a 128 -bit seed that is used to reinitialize the pseudo-random generator; equal seeds produce equal sequences of numbers. The default for y is zero.

When called with no arguments, Lua generates a seed with a weak attempt for randomness.

This function returns the two seed components that were effectively used, so that setting them again repeats the sequence.

To ensure a required level of randomness to the initial state (or contrarily, to have a deterministic sequence, for instance when debugging a program), you should call math.randomseed with explicit arguments.
math. randomseeds ([x, y])
Sets x and y as the `seeds` for the pseudo-random generator, as Agena did before version 2.27.10: equal seeds produce equal sequences of numbers. x and y must both be positive integers. It returns two new settings. The function does not check for $\mathrm{x}=0 \times 464 \mathrm{fffff}$ and $\mathrm{y}=0 \times 9068 \mathrm{ffff}$.

If called without arguments, the function returns the current seeds.
See also: math.random.
math.rectangular (x [, pi])
math.rectangular (x [, a [, b [, pi]]])
In the first form, computes the rectangular pulse function for number x :

$$
\text { math.rectangular }(x)=\left\{\begin{array}{cc}
1 & \text { if }|x|<0.5 \\
0.5 & \text { if }|x|=0.5 \\
0 & \text { if }|x|>0.5
\end{array}\right.
$$

In the second form, a represents the rising edge, and b the falling edge of the rectangular pulse function. By default, $a=-0.5$ and $b=+0.5$. The function then returns 0 if $\mathrm{x}<\mathrm{a}$ or $\mathrm{x}>\mathrm{b}$; 0.5 if ( $\mathrm{x}=\mathrm{a}$ or $\mathrm{x}=\mathrm{b}$ ) and $\mathrm{a}<>\mathrm{b}$, and 1 otherwise. If $p_{i}$ is the Boolean value true, the function computes the box distribution $\mathrm{Pi}(\mathrm{x})$ :

$$
\operatorname{Pi}(x)=\left\{\begin{array}{cc}
1 & \text { if }|x|<0.5 \\
\text { undefined } & \text { if }|x|=0.5 \\
0 & \text { if }|x|>0.5
\end{array}\right.
$$

See also: heaviside, math.clip, math.ramp, math.triangular, math. unitise, sinc.

```
math.relerror (a, b)
```

Computes the relative error $|b-a| /|a|$, handling case of undefined and infinity.
math.rempio2 (x [, option])
Conducts an argument reduction of $x$ into the range $|y|<\frac{\pi}{2}$ and returns $y=x$ $N * \frac{\pi}{2}$. If any option is given, then the function also returns $N$, or actually the last three digits of N . The number of operations conducted are independent of the exponent of the input.

The function is 60 percent faster than math.wrap, but returns a result different from x if its argument $|x|$ is already in the range $\frac{\pi}{4} . . \frac{\pi}{2}$.

This function is just a port to the underlying C function rem_pio2 which is used to compute sines, cosines and tangents.

See end of Chapter 11.1.2 for a comparison chart.

```
math.rint (x)
```

Rounds a (complex) float to a (complex) integer according to the current rounding method which you can query and set with environ.kernel/rounding.

See also: ceil, entier, int, mdf, round, math.nearbyint.

```
math.signbit (x)
```

Checks whether the number $x$ has its sign bit set and returns true or false. It is a plain binding to $\mathrm{C}^{\prime}$ s copysign function. For example, although $-0=0$, math.signbit( -0 ) $\Rightarrow$ true and math.signbit $(0) \Rightarrow$ false.

See also: math.copysign, math.flipsign, math.isminuszero, sign.
math.significand (x)
Returns the mantissa of number $x$ in a normalised form, in the range[1, 2), with math.significand $(\mathrm{x})=2^{*}$ math.mantissa( x$)=\operatorname{Idexp}(\mathrm{x},-\mathrm{ilog} 2(\mathrm{x})$ ). If x is 0 , the return is 0 .

See also: math.uexponent.

## math.sincos (x)

Returns both the sine and cosine for number or complex x as two numbers or complex numbers. The function is around 10 to $15 \%$ faster than calling the sin and cos operators separately.

See also: cos, sin, math.sincosfast, math.sincospi.

## math.sinhcosh (x)

For number $x$, returns both the hyperbolic sine and hyperbolic cosine as two numbers. The function is around 30 to $35 \%$ faster than calling the sinh and cosh operators separately.

With complex x, returns complex results.
See also: cosh, sinh.
math.sincospi (x [, option])
Returns both $\sin \left(\pi^{\star} x\right)$ and $\cos \left(\pi^{\star} x\right)$ for number $x$ with better precision than calling the respective standard operators. If option is true, than the tangent, i.e. $\tan \left(\pi^{\star} x\right)$ is returned too.

# See also: math.sincos, math.sinpi, math.cospi, math.tanpi. 

math.sinpi (x)
Returns $\sin \left(\pi^{*} x\right)$ for number $x$ with better precision than calling the respective standard operator.

See also: sin, math.sincos, math.sincospi, math.cospi, math.tanpi.

```
math.smallest
```

This constant represents the smallest positive number representable in Agena. It is computed during start-up and is different from the setting returned by environ.system, the latter statically compiled into the Agena binary.

See also: math.largest.

```
math.smallestnormal
```

This constant denotes the smallest positive normal number representable on your system.
math.splitdms (x)
Splits the number x representing a sexagesimal number in TI-30 DMS format into its parts and returns three numbers: the degrees, minutes, and seconds. For example: -10.3045 represents $-10^{\circ} 30^{\prime} 45^{\prime \prime}$.

The function is implemented in Agena and included in the lib/library.agn file.
See also: math.dd, math.dms, math.todecimal, math.tosgesim.
math.stirnum ( $\mathrm{n}, \mathrm{k}$, kind)
Computes either the Stirling number for $n, k$, of the first or the second kind. $k$ ind is 1 by default to compute the first kind; you can set it to 2 to evaluate the second kind.

```
math.tanpi (x)
```

Returns $\tan \left(\pi^{*} x\right)$ for number $x$ with better precision than calling the respective standard operator.

See also: tan, math.sincos, math.sincospi, math.sinpi, math.cospi.

```
math.todecimal (h [, m [, s]])
```

Converts a sexagesimal time value given in hours $h$, minutes $m$ and seconds s into its decimal representation. The optional arguments $m$ and $s$ default to 0 . If a
sexagesimal value is negative, then h should be negative, while m and s should be non-negative.

Example:

```
> math.todecimal(12, 30, 1): # half past noon and one second
12.500277777778
```

See also: clock.todec, math.todms, math.tosgesim.
math.todms (x)
Converts a number in DMS notation to its decimal representation, e.g. 10.3045, representing $10^{\circ} 30 ' 45$ ", returns 10.5125 .

See also: math.todecimal.
math.tohex (x)
Converts a non-negative integer $x$ in the range [0,255] to its hexadecimal representation, returned as a 2-character string.

See also: math.convertbase.
math.toradians (d [, m [, s]])
Returns the angle given in degrees $d$, minutes $m$ and seconds $s$, in radians. The optional arguments m and s default to 0 .

```
math.tosgesim (d)
```

Converts a decimal time value given by the number $d$ into its sexagesimal representation and returns three numbers: the hours, minutes, and seconds.

Example:

```
> math.tosgesim(12.500277777778):
12 30 1
```

The function is written in Agena and included in the lib/library.agn file.
See also: math.dms, math.todecimal, math.todms.

```
math.triangular (x)
math.triangular (x [, a [, b]])
```

In the first form, computes the triangular function of base length 1 for number x :

$$
\text { math.triangular }(x)=\left\{\begin{array}{cc}
1-|2 x| & \text { if }|x|<0.5 \\
0 & \text { if }|x| \geq 0.5
\end{array}\right.
$$

In the second form, by passing a left and a right border $a, b$, the function returns non-zero values in this range, and 0 otherwise, with $a=-0.5$ and $b=+0.5$ the defaults. Thus, the general formula used by the function is:
math.triangular( $\mathrm{x}, \mathrm{a}, \mathrm{b}):=\max \left(0,1-\mid 2^{*}(\mathrm{x}-\right.$ offset $\left.) / \mathrm{d} \mid\right)$,
where $d:=|b-a|$ and offset $:=a+d / 2$.
See also: heaviside, math.branch, math.clip, math.rectangular, math.unitise, math.wrap, sinc.
math.trunc ( x )
Returns x rounded to the nearest integer towards zero, returns the same result as int(x). The function has been included for $C$ math library compatibility reasons only.

See also: math.nearbyint.
math.two54
The constant represents $2^{54}$, a value with which subnormal numbers can be multiplied in order to become normal. See also: math.issubnormal.
math.uexponent (x [, option])
Computes the unbiased base-2 exponent of number $x$, i.e. returns math.exponent( x ) -1 , except for $\mathrm{x}=0$ and subnormal numbers where the result is -1023, and for $\mathrm{x}=$ undefined or $\mathrm{x}= \pm$ infinity returns 1024.

If any option is given, then returns sign(x)*math. uexponent(x), but for $x=$ undefined returns $0 \times 401=1025$, for $x=$-infinity returns -1024 , and for $\mathrm{x}=$ infinity returns +1024 . Due to the definition, returns 0 for $\mathrm{x}=0$ and subnormal x .

See also: bytes.getunbiased, math.significand, frexp.

```
math.ulp (x [, eps])
```

Computes the unit of least precision (ULP), the spacing between floating-point numbers, for number $x$, as a measure of accuracy in numeric calculations. It is equivalent to math.nextafter( $x$, infinity) - x .

If eps is given, the function also returns the number of ULPs - an integer - between x and $\mathrm{x}+\mathrm{eps}$.
math.unitise (x [, eps])
Returns 0 if its number argument x is zero or close to zero, and 1 otherwise:

- 0 if $|x| \leq e p s$,
- 1 if $|x|>$ eps.

With complex numbers $\mathrm{x}=\mathrm{a}+\mathrm{I} \mathrm{k}$, returns

- 0 if $|a| \leq e p s$ and $|b| \leq e p s$,
- 1 if $|a|>$ eps and $|b|>$ eps.

By default, eps is set to the constant Eps.
See also: heaviside, math.clip, math.rectangular, math.unitstep, math.zeroin.

```
math.unitstep (x [, eps])
```

For number x , gives 0 for $\mathrm{x}<0$ and 1 otherwise.
See also: heaviside, math.unitise.
math.wrap (x [, a [, b]])
Conducts a range reduction of the number $x$ to the interval $[a, b)$ and returns $a$ number. If $x \in[a, b)$, $x$ is simply returned.

In the second form, if $a$ is not given, $a$ is set to $-\pi$ and $b$ to $+\pi$. If $a$ is given but not $b$, $a$ is set to -a and b to +a , so a should be positive.

The result is equivalent to:

```
> dec x, a;
> dec b, a;
> a + (b + x symmod b) symmod b:
```

See also: \% operator, math.branch, math.clip, math.norm, math.rempio2, zx.reduce, end of Chapter 11.1.2 for a comparison chart.

```
math.xlnplusone (x)
```

Computes $\mathrm{x}-\ln (1+\mathrm{x})$ in a way that is accurate even if x is near zero. The algorithm is ten percent faster than simply returning x - math. Inplusone( x ).

```
math.zeroin (x)
```

Sets a number or complex number x to 0 if $|x| \leq$ DoubleEps. With a complex number $x$, return $0+I^{*} 0$ if its magnitude $|x| \leq$ DoubleEps or sets its respective parts to zero if their respective absolute values are less or equal to DoubleEps.

See also: math.chop, math.normalise, math.zerosubnormal.
math.zerosubnormal (x)
Checks whether its numeric argument x is subnormal and in this case returns 0 , otherwise returns its argument x . It is useful to prevent excessive CPU usage in case of arguments very close to zero. Note that result retains the sign of x .

With complex x , returns the complex number math.zerosubnormal(real(x)) + I*math.zerosubnormal(imag(x)).

For more information, see math.issubnormal, math.normalise, math.zeroin.
Comparison of some clipping functions:

```
gdi.plotfn([<< x -> math.rempio2(x) >>,
    << x -> math.wrap(x) >>,
    << x -> math.clip(x) >>,
    << x -> zx.reduce(x) >> ,
    << x -> math.branch(x) >>],
    -4, 4, -4, 4,
    colour=['red', 'navy', 'green', 'black', 'maroon']);
```



### 11.1.3 fastmath Library

As a plus package, this library is not part of the standard distribution and must be activated with the import statement, e.g. import fastmath.

The library provides procedures to approximate mathematical functions in the real domain. Despite its name, the package functions may not necessarily be faster than the standard functions and operators implemented in Agena.

## fastmath.cosfast (x)

Approximates $\boldsymbol{\operatorname { c o s } ( \mathrm { x } )}$ for number x , and returns a number. It is around 40 percent faster than cos.

See also: cos.
fastmath.hypotfast (x, y)
Returns the hypotenuse of the two numbers $x$ and $y$; the return is a number. The function is sixty percent faster than hypot, but prone two round-off errors.
fastmath.invroot (x [, degree [, n [, xhalf]]])
Approximates the inverse root 1/root(x, degree) using the Quake III method, and returns a number. $x$ is the radicand, degree the degree-th root which by default is 2 . $n$ is the number of iterations to be conducted and by default is $2^{\wedge}$ degree. xhalf is the internal equivalent of $x, 0.5^{*} x$ by default. The greater the degree, the less accurate is the result.

See also: fastmath.reciprocal, fastmath.sqroot.
fastmath.invsqrt (x)
Approximates the inverse square root 1/sqrt(x), using Quake's Fast Inverse Square Root method and returns a number. It is five percent faster than the inverse of the sqrt operator.

## fastmath.lbfast (x)

Approximates $\log 2(x)$ for number $x$, and returns a number. It is around a third faster than $\log 2$. If $\mathrm{x}<=0$, the result will be wrong.

See also: log2.
fastmath.reciprocal (x)
Approximates the reciprocal of its argument $x$ of type number. The return is a number. The function is purely experimental.

See also: fastmath.invroot, fastmath.sqroot.

## fastmath.sinfast (x)

Approximates $\boldsymbol{\operatorname { s i n }}(\mathrm{x})$ for number x , and returns a number. It is around 40 percent faster than sin.

## fastmath.sincosfast (x)

Returns both an approximation of the sine and cosine as two numbers. The function is around $10 \%$ faster than calling math.sincos.
fastmath.sqroot ( x )
Roughly approximates the square root of its argument x of type number. The returns are two numbers: guesses computed using C doubles and floats, in this order. The function is purely experimental.

See also: fastmath.invroot, fastmath.reciprocal, fastmath.sqrifast.
fastmath. sqrtfast (x)
Approximates the square root of its argument x of type number. The function is purely experimental.

See also: fastmath.sqroot.
fastmath.tanfast (x)
Approximates $\tan (x)$ for number $x$, and returns a number. It is around 40 percent faster than tan.

See also: tan.

## 11.2 bytes Library

As a plus package, this library is not part of the standard distribution and must be activated with the import statement, e.g. import bytes.

The library provides procedures for bit and byte twiddling.

### 11.2.1 General Functions

## bytes.bcd (n)

Returns the Binary coded decimal (BCD) representation of the non-negative integer n. From left to right, each decimal digit is converted to a four-bit representation ( $0=$ 0b0000, $9=0 \mathrm{~b} 1001$ ), and the resulting bit sequence is then returned as one decimal integer, e.g. decimal $102=000100000010 \Rightarrow B C D 258$.

By default, if only $n$ is given, the function converts the decimal integer to BCD. If true is passed as a second argument, $n$ is converted from BCD to its decimal integer representation.
bytes.castint (x, bits)
Casts number x to a C integer. The results may be platform-dependent.

| bits | Cast to |
| :--- | :--- |
| 8 | uint8_ $\dagger$ |
| 16 | uint16_t |
| 32 | uint32- $\dagger$ |
| 64 | uint64- $\dagger$ |
| -8 | int8 $\dagger$ |
| -16 | int16_ $\dagger$ |
| -32 | int32 $\dagger$ |
| -64 | int64_ $\dagger$ |

bytes.fpbtoint (x)
Converts a `floating point byte` generated by bytes.inttofpb back. This function is used to evaluate numbers transported to the Lua/Agena virtual machine. Please note that math.inttofpb(math.fpbtoint(x)) does not return x .
bytes.numhigh (x)
Returns the higher bytes of a number $x$ as an integer. The function does not support complex numbers.

See also: bytes.numwords, bytes.numlow.
bytes.numlow (x)
Returns the lower bytes of a number x as an integer. The function does not support complex numbers.

See also: bytes.numhigh, bytes.numwords, bytes.setlow.

```
bytes.numwords (x)
```

Returns both bytes.numhigh(x), bytes.numlow(x) plus the unbiased exponent (i.e. math.exponent(bytes_numhigh(x)) - 1, except for $\mathrm{x}=0->-1023$ ) as three results, in this order.

See also: bytes.setnumwords.
bytes.inttofpb (x)
Converts the integer x to a `floating point byte`, represented as (eeeeexxx), where the real value is ( 1 xxx ) * $2^{\wedge}$ (eeeee - 1 ) if eeeee $<>0$ and ( $x x x$ ) otherwise. This function is used to transport numbers to the Lua/Agena virtual machine.

See also: bytes.fpbtoint

## bytes.leadzeros (x)

Returns the number of leading zeros in the unsigned 32-bit integer $x$, and the modified value of $x$ after this operation, where all bits starting with the first non-zero bit in x are set to 1 .

See also: bytes.leastsigbit, bytes.mostsigbit, bytes.onebits, bytes.trailzeros.

```
bytes.leastsigbit (x)
```

Returns the position of the least significant bit (lsb) in the unsigned 32-bit integer x , here the smallest index of the first 1 -bit, counting from bit index 1 . If $x<1$, returns 0 .

See also: bytes.leadzeros, bytes.mostsigbit, bytes.onebits.

## bytes.mostsigbit (x)

Returns the position of the most significant bit (msb) in the unsigned 32-bit integer x , i.e. the largest index of a 1 -bit, counting from bit index 1 . If $x<1$, returns 0 .

See also: bytes.leadzeros, bytes.leastsigbit, bytes.mostsigbit.
bytes.onebits (x)
Returns the number of bits set in the unsigned 32-bit integer x .
See also: bytes.leadzeros, bytes.mostsigbit.

## bytes.optsize ( $n$ )

For a given number of bytes $n$, calculates the optimal number of bytes (places) in a C `array` (e.g. a memfile, numarray or even a string) if it shall be aligned on the 4or 8-byte word boundary.

See also: strings.strlen.
bytes.pack (fmt, v1, v2, ...)
Returns a binary string containing the values v1, v2, etc. packed (that is, serialised in binary form) according to the format string fmt.

The first argument to bytes.pack, bytes.packsize, and bytes.unpack is a format string, which describes the layout of the structure being created or read.

A format string is a sequence of conversion options. The conversion options are as follows:
<: sets little endian
>: sets big endian
=: sets native endian
$![n]$ : sets maximum alignment to $n$ (default is native alignment)
b: a signed byte (char)
в: an unsigned byte (char)
h: a signed short (native size)
н: an unsigned short (native size)
ı: a signed long (native size)
L: an unsigned long (native size)
j: a lua_Integer
v: a lua_Unsigned
т: a size_† (native size)
i $[\mathrm{n}]$ : a signed int with n bytes (default is native size)
I $[\mathrm{n}]$ : an unsigned int with n bytes (default is native size)
f: a float (native size)
d: a double (native size)
n: a lua_Number
cn : a fixed-sized string with n bytes
z: a zero-terminated string
$s[n]$ : a string preceded by its length coded as an unsigned integer with $n$
bytes (default is a size_t)
x: one byte of padding
Xop: an empty item that aligns according to option op (which is otherwise ignored)
' ' : (empty space) ignored
(A " $[\mathrm{n}] \mathrm{"}$ means an optional integral numeral.) Except for padding, spaces, and configurations (options "xX <=>!"), each option corresponds to an argument (in bytes.pack) or a result (in bytes.unpack).

For options "!n", "sn", "in", and "In", n can be any integer between 1 and 16. All integral options check overflows; bytes.pack checks whether the given value fits in the given size; bytes.unpack checks whether the read value fits in a Lua integer.

Any format string starts as if prefixed by "! $1=$ ", that is, with maximum alignment of 1 (no alignment) and native endianness.

Alignment works as follows: For each option, the format gets extra padding until the data starts at an offset that is a multiple of the minimum between the option size and the maximum alignment; this minimum must be a power of 2 . Options " c " and "z" are not aligned; option "s" follows the alignment of its starting integer.

All padding is filled with zeros by bytes.pack (and ignored by bytes.unpack).
See also: bytes.packsize, bytes.unpack, math.ispow2.

## bytes.packsize (fmt)

Returns the size of a string resulting from bytes.pack with the given format. The format string cannot have the variable-length options 's' or 'z'.

## bytes.reverse (x)

Reverses all the bits in the unsigned 32-bit integer x, flipping all bits from 0 to 1 and vice versa.
bytes.setnumhigh (x, i)
The function sets the higher bytes of the number $x$ to the unsigned 32-bit integer i, and returns the new number. It does not support complex numbers.

## See also: bytes.setnumlow, bytes.numhigh.

bytes.setnumlow (x, i)
The function sets the lower bytes of the number $x$ to the unsigned 32-bit integer i, and returns the new number. It does not support complex numbers.

See also: bytes.setnumhigh, bytes.numlow.
bytes.setnumwords (hx, lx)
Returns the number (C double) x represented by the unsigned 32-bit integers hx and $l_{x}$, i.e. $x=$ bytes.setnumwords(math.numhigh( $x$ ), math.numlow( $(x)$ ).

See also: bytes.numwords.
bytes.tobig (x [, order])
On Little Endian systems, converts the number x into its Big Endian representation and returns it. On Big Endian platforms, just returns x unaltered. If order is 4, then the function processes $x$ as an unsigned 4-byte integer. If order is -4 , the function treats $x$ as a signed 4-byte integer.

See also: bytes.tolittle, os.endian.
bytes.tobinary (x)
Converts a non-negative integer into its binary representation, a sequence of zeros and ones.

See also: math.convertbase.
bytes.tobytes (x [, nbytes [, false]])
If given no option, returns a sequence of eight bytes representing the number x in Little Endian order, i.e. the least-significant byte is the first entry in the resulting sequence. If nbytes is the number +4 or -4 , $x$ is a assumed to be an unsigned 4-byte integer or signed 4-byte integer, respectively, and a sequence of four bytes representing x in Little Endian representation will be returned. If nybtes is $+2, \mathrm{x}$ will be treated as an unsigned 2-byte integer, with a sequence of two bytes to be returned.

On Big Endian systems, conversion to Little Endian representation can be switched off by passing a third argument, the Boolean value false.

See also: getbit, getbits, getnbits, bytes.tonumber.
bytes.tolittle (x [, order])
On Big Endian systems, converts the number x into its Little Endian representation and returns it. On Little Endian platforms, just returns $x$ unaltered. If order is 4, then the function processes $x$ as an unsigned 4-byte integer. If order is -4 , the function treats x as a signed 4-byte integer.

See also: bytes.tobig, os.endian.
bytes.tonumber (s)
Takes a sequence s of two, four or eight numbers representing bytes and converts it into an Agena number. Regardless of your platform, the order of bytes in s is assumed to be Little Endian.

If s contains eight bytes, it is assumed to represent a $C$ unsigned double. If it contains four bytes, an unsigned four-byte integer is assumed; and with two bytes, an unsigned two-byte integer is assumed.

See also: bytes.tobytes.

## bytes.trailzeros (x)

Returns the number of trailing zeros in the unsigned 32-bit integer $x$, and the modified value of $x$ after this operation, where all bits starting with the least significant bit in x are set to 1 .

See also: bytes.leadzeros, bytes.leastsigbit, bytes.mostsigbit, bytes.onebits.
bytes.unpack (fmt, s [, pos])
Returns the values packed in string s (see bytes.pack) according to the format string fmt. An optional pos marks where to start reading in s (default is 1). After the read values, this function also returns the index of the first unread byte in s.

### 11.2.2 cast Functions

The bytes package provides the 'cast' userdata data structure representing an Agena number as both a C double (i.a. Agena number) and its two higher and lower 32-bit unsigned integer representations, along with functions to query and assign its individual components.

Example:

```
> a := bytes.cast(-Pi):
cast(-3.1415926535898 : 3221823995, 1413754136)
> hx := bytes.gethigh(a) :
3221823995
> hx >>> 31: # sign bit (1 = minus, 0 = plus)
1
> bytes.sethigh(a, hx && 0x7fffffff): # absolute value
3.1415926535898
```

bytes.cast ([x])
bytes.cast ([hx, lx])
Creates a userdata structure of type 'cast' that stores the Agena number 0 or x and its integer representation as two unsigned 32-bit integers. Technically, the userdata represents the C union (see source file src/sunpro.h):

| Big-Endian platforms | Little-Endian platforms |
| :--- | :--- |
| typedef union \{ | typedef union \{ |
| double value; | double value; |
| struct \{ | struct \{ |
| uint32_t msw; | uint 32_t lsw; |
| uint32_t lsw; | uint32_t msw; |
| \} parts; <br> ieee_double_shape_type; | parts; <br> ieee_double_shape_type; |

If no argument is given, then the userdata represents zero (0), alternatively you can set it to number x (first form).

You may also initialise the userdata by passing both its unsigned 32-bit integer word hx and unsigned 32-bit integer lower word 1x (second form).

See also: bytes.getdouble, bytes.gethigh, bytes.getlow, bytes.getwords, bytes.setdouble, bytes.setwords.
bytes.getdouble (a)
Returns the floating point element of 'cast' userdata a, i.e. a number.

## bytes.gethigh (a)

Returns the higher unsigned 32-bit integer representation of a number from 'cast' userdata a.

See also: bytes.getlow, bytes.getwords.

## bytes.getlow (a)

Returns the lower unsigned 32-bit integer representation of a number from 'cast' userdata a.

See also: bytes.gethigh, bytes.getwords.
bytes.getunbiased (a)
Returns the unbiased exponent of the double x represented by 'cast' userdata a. Equals math.exponent $(x)$ - 1, except for $x=0$ where the result is -1023 . If $|x|<1$, the result is always negative.

See also: bytes.gethigh, bytes.getlow, bytes.getwords, math.uexponent.
bytes.getwords (a)
Returns both the higher and lower unsigned 32-bit integer representations of a number from 'cast' userdata a.

See also: bytes.getdouble, bytes.gethigh, bytes.getlow.
bytes.setdouble (a, x)
Sets the floating point element of 'cast' userdata a and returns the higher and lower unsigned 32 -bit integer representations, in this order.

See also: bytes.setwords.
bytes.sethigh ( $\mathrm{a}, \mathrm{hx}$ )
Sets the higher unsigned 32-bit integer element hx of 'cast' userdata a. The return is the corresponding floating point representation, i.e. a number.

See also: bytes.setdouble, bytes.setlow.
bytes.setlow (a, lx)
Sets the lower unsigned 32 -bit integer element $1 x$ of 'cast' userdata a. The return is the corresponding floating point representation, i.e. a number.

See also: bytes.setdouble, bytes.sethigh.
bytes.setwords (a, hx, lx)
Sets the higher and lower unsigned 32 -bit integer elements hx and $\mathrm{lx}_{\mathrm{x}}$ of 'cast' userdata $a$. The return is the corresponding floating point representation, i.e. a number.

See also: bytes.setdouble, bytes.sethigh, bytes.setlow.

### 11.2.3 IEEE754 Functions

The bytes package provides the 'ieee' userdata data structure representing an Agena number as both a C double (i.a. Agena number) and its components sign bit, biased exponent and high- and low-word mantissa. See bytes.ieee for details.

Example:

```
> import bytes
exp10 := proc(x) is
> x *:= log2(10);
> local i := round(x);
local f := bytes.ieee(0);
> bytes.setieee(f, expo = i + 1023);
> x -:= i;
> return bytes.getieee(f, 'double') *
> (1.0 + x*(0.69314718055994530941723212145818 +
> x*(0.24022650695910071233355126316333 +
                x*(0.055504108664821579953142263768622 +
                x*(0.0096181291076284771619790715736589 +
                x*(0.0013333558146428443423412221987996 +
                x*(0.00015403530393381609954437097332742 +
                x*(0.00001525273380405984028002543901201 +
                x*(0.0000013215486790144309488403758228288 +
                x*0.00000010178086009239699727490007597745)))!)))))
>end;
```

bytes.ieee ([x])
bytes.ieee ([signbit, exponent, high_mantissa, low_mantissa])
Creates a userdata structure of type 'ieee' that stores the Agena number 0 or x and allows read and write access to its components sign bit signbit, its biased exponent, the high-word part of the mantissa high_mantissa and its low-word part high_mantissa. Technically, the userdata represents the C union (see source file src/sunpro.h):

| Big-Endian platforms | Little-Endian platforms |
| :---: | :---: |
| typedef union \{ | typedef union \{ |
| double v; | double v; |
| struct \{ | struct \{ |
| uint64_t sign : 1; | uint64_t mantissa_low : 32; |
| uint64_t exponent : 11; | uint64_t mantissa_high : 20; |
| uint64_t mantissa_high : 20; | uint64_t exponent : 11; |
| uint64_t mantissa_low : 32; | uint64_t sign : 1; |
| \} c; | \} c; |
| \} double_ieee754; | \} double_ieee754; |

If no argument is given, then the userdata represents zero (0), alternatively you can set it to number x (first form).

You may also initialise the userdata by passing both its sign bit, exponent, and the high and low parts of the mantissa (second form).

## bytes.setieee (a, options)

Sets components in 'leee' structure a. Accepted options are one or more pairs:

- 'double': any Agena number,
- 'signbit' ': the sign bit, 1 for minus, 0 for plus,
- 'expo': the biased exponent, an unsigned 4-byte integer,
- ' high ' : high-word part of the mantissa,
- 'low': low-word part of the mantissa.


## Example:

```
> bytes.setieee(a, double=Pi, signbit=1); # sets -Pi to 'ieee' object a
```

bytes.getieee (a [, options])
Returns the components of 'ieee' structure a. If only a is given, then its five components number, sign bit, exponent, mantissa high-word and mantissa low-word are returned, in this order.

If one or more of the following strings are passed as options, then the requested components will be returned in the order given by the user:

- 'double': any Agena number,
- 'signbit' : the sign bit, 1 for minus, 0 for plus,
- 'expo': the biased exponent, an unsigned 4-byte integer,
- 'high ' : high-word part of the mantissa,
- 'low': low-word part of the mantissa.


## Example:

```
> bytes.getieee(a, 'double', 'signbit'):
-3.1415926535898 1
```

Following are specialised functions for 'ieee' data:
bytes.setieeesignbit (a, bit [, option])
Sets the sign bit of ieee structure a to bit, which is either 1 for minus or 0 for plus. If any option is given, the function returns the updated values for double, sign bit, exponent, high and low-word mantissa, in this order.
bytes.setieeeexpo (a, e [, option])
Sets the biased exponent of ieee structure a to non-negative integer e. If any option is given, the function returns the updated values for double, sign bit, exponent, high and low-word mantissa, in this order.
bytes.setieeehigh (a, hi [, option])
Sets the high-word of the mantissa of ieee structure a to non-negative integer hi. If any option is given, the function returns the updated values for double, sign bit, exponent, high and low-word mantissa, in this order.
bytes.setieeelow (a, lo [, option])
Sets the high-word of the mantissa of ieee structure a to non-negative integer lo. If any option is given, the function returns the updated values for double, sign bit, exponent, high and low-word mantissa, in this order.
bytes.setieeedouble (a, v [, option])
Sets the floating-point component in ieee structure a to Agena number v. If any option is given, the function returns the updated values of the sign bit, exponent, high and low-word mantissa in a, in this order.
bytes.getieeedouble (a)
Returns the floating-point component in ieee structure a, an Agena number.

### 11.2.4 32-bit Integer Operations

The following functions process 32-bit signed and unsigned integers.
Please note, that by default, Agena including the functions listed below, work in unsigned mode. You can switch to signed operations by issuing

```
> environ.kernel(signedbits = true);
```

on the command line or in a (library) file.
bytes.add32 (a, b [, …])
Adds two or more numbers a, b, ... using 4-byte unsigned integer arithmetic. The return is an integer.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits = true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: \&+ operator.
bytes.sub32 (a, b [, …])
Subtracts two or more numbers $a, b, \ldots$ using 4-byte unsigned integer arithmetic. The return is an integer.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits = true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: \&- operator.
bytes.mul32 (a, b [, ...])
Multiplies two or more numbers $a, b, \ldots$ using 4-byte unsigned integer arithmetic. The return is an integer.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits $=$ true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: \&* operator.
bytes.muladd32 (a, b [, ...])
Multiplies two numbers $a, b$, and adds further numbers $c, \ldots$ using 4-byte unsigned integer arithmetic. The return is the integer $\mathrm{a}^{*} \mathrm{~b}+\mathrm{c}+\ldots$

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits = true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: bytes.add32, bytes.mul32.
bytes.div32 (a, b [, ...])
Divides two or more numbers $a, b, \ldots$ using 4-byte unsigned integer arithmetic. The return is an integer.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits $=$ true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: \&/ operator.
bytes.mod32 (a, b)
Takes the modulus a \% b (with \% the C modulus operator, not Agena's \%), using 4 -byte unsigned integer arithmetic. The return is an integer.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits = true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

See also: math.modulus.

## bytes.divmod32 (a, b)

Returns the quotient and remainder of the 4-byte division a/b.
See also: bytes.div32, bytes.mod32.
bytes.and32 (...)
Conducts a binary AND operation on all the arguments (none, one or multiple signed or unsigned 32-bit integers) and returns an integer.

See also: \&\& operators.
bytes.arshift32 (x, n)
Returns the 32-bit signed or unsigned integer x shifted n bits to the right. The number n may be any representable integer. Negative displacements shift to the left.

This shift operation is what is called arithmetic shift. Vacant bits on the left are filled with copies of the higher bit of $x$, thus preserving the sign of $x$; vacant bits on the right are filled with zeros. In particular, displacements with absolute values higher than 31 result in zero or OxFFFFFFFF (all original bits are shifted out).

See also: $\lll$ and $\ggg$ operators, bytes.shift32.
bytes.extract 32 ( $n$, field [, width])
Returns the unsigned number formed by the bits field to field + width - 1 from n. Bits are numbered from 0 (least significant) to 31 (most significant). All accessed bits must be in the range $[0,31]$.

The default for width is 1 .
Signed 32-bit integers $n$ are not supported.
See also: bytes.replace32.
bytes.isint32 ( n )
Checks whether the given number $n$ is in the range of a signed or an unsigned 4-byte integer and returns true or false.

To check in which mode Agena is, check the environ.kernel/signedbits setting. It should usually be unsigned.

If you are in unsigned mode, the argument should be in the range 0 .. environ.kernel().maxulong $=0 . .4^{\prime} 294^{\prime} 967^{\prime} 295$.

If you are in signed mode, $n$ should be in the range environ.kernel().minlong environ.kernel().maxlong $=-2^{\prime} 147^{\prime} 483^{\prime} 647 . .2^{\prime} 147^{\prime} 483^{\prime} 647$.

Example:

```
> import bytes
> environ.kernel().signedbits: # we are in unsigned mode (C uint32_t's).
false
> bytes.isint32(4'294'967'295):
true
> bytes.isint32(4'294'967'295 + 1):
false
```

bytes.mask32 (n)
Returns an integer with the first n bits set to one, e.g. bytes.mask $32(3) \rightarrow 7$.
bytes.nand32 (...)
Conducts a binary complementary OR operation on all the arguments (none, one or multiple signed 32-bit integers) and returns an integer. There is no `unsigned` mode available, as the results would be of no use.

See also: nand.

## bytes.nextbit (mask)

Gets and clears the next bit from the unsigned 4-byte mask, starting with the most significant bit. The function returns the modified value of mask and the respective bit position $0 . .31$.

```
bytes.nor32 (...)
```

Conducts a binary complementary OR operation on all the arguments (none, one or multiple signed 32-bit integers) and returns an integer. There is no `unsigned` mode available, as the results would be of no use.

See also: nor.
bytes. not32 (x)
Conducts a binary NOT operation on the signed or unsigned 32-bit integer x and returns an integer.

See also: ~~ operator.

## bytes.numto32 (x)

Converts a number $x$ to its signed or unsigned 4-byte integer representation. Note that very large values (positive or negative) might overflow, e.g. bytes.numto $32\left(2^{\wedge} 32+1\right) \Rightarrow 1$. The result may differ across platforms in overflow situations.

You can switch from unsigned to signed arithmetic by setting environ.kernel(signedbits $=$ true), and from signed to unsigned arithmetic by environ.kernel(signedbits = false).

## See also: math.uexponent.

```
bytes.or32 (...)
```

Conducts a binary OR operation on all the arguments (none, one or multiple signed or unsigned 32-bit integers) and returns an integer.

See also: || operator.

## bytes.parity32 (x)

Determines the parity of the unsigned 4-byte integer $x$, i.e. the number of 1 -bits in $x$ modulo 2.

Returns 0 if x is of even parity, and 1 in case of odd parity.
See also: hashes.parity.
bytes.replace32 (n, v, field [, width])
Returns a copy of $n$, an unsigned 32-bit integer, with the bits field to field + width - 1 replaced by the value $v$.

Signed 32-bit integers $n$ are not supported.
See bytes.extract32 for details about field and width.
bytes.rotate32 (x, n)
Rotates the bits in the 32-bit integer x n displacements to the right if $\mathrm{n}>=0$, or n places to the left if $\mathrm{n}<0$. The return is a 32-bit integer.

Internally the function uses unsigned 32-bit integers by default. You can change this to signed integers by calling environ.kernel with the 'signedbits' option.

See also: $\lll<$ and $\ggg>$ operators.

## bytes.shift32 (x, n)

Shifts the bits in the 32-bit integer x n displacements to the left if $\mathrm{n}<0$, and to the right if $n>0$.

Internally the function uses unsigned 32-bit integers by default. You can change this to signed integers by calling environ.kernel with the 'signedbits' option.

See also: $\lll$ and $\ggg$ operators, bytes.arshift32.
bytes.xnor32 (...)
Conducts a binary complementary exclusive-OR operation on all the arguments (none, one or multiple signed 32-bit integers) and returns an integer. There is no `unsigned` mode available, as the results would be of no use.

See also: xnor.
bytes.xor32 (...)
Conducts a binary exclusive-OR operation on all the arguments (none, one or multiple signed or unsigned 32-bit integers) and returns an integer.

See also: ^ ^ operator.

## 11.3 mapm - Arbitrary Precision Library

As a plus package, in Solaris, Linux, Mac OS X, and Windows, this library is not part of the standard distribution and must be activated with the import statement, e.g.
import mapm.
In OS/2 and DOS, the package is built into the binary executable and does not need to be activated with import.

The package provides functions to conduct arbitrary precision mathematics with real numbers. It uses Mike's Arbitrary Precision Math Library, written by Michael C. Ring.

Standard operators like $+,-, *, /, \uparrow, \%,<,=,>$, and unary minus are supported.

All function names in this library begin with the letter $x$.
The package uses its own kind of numbers which are different from Agena numbers: use mapm.xnumber and mapm.xtonumber to convert between them.

By default, the precision is set to 17 digits, but you can change this any time with the mapm.xdigits function, see example below:

It is always advised to pass numbers as strings if possible. This is because Agena uses C doubles which are not $100 \%$ precise.

```
> import mapm;
> mapm.xdigits(100); # precision set to 100 digits
> a := mapm.xnumber('0.5');
> a*mapm.Pi:
1.57079632679489662
> b := mapm.xnumber(0.5):
0.500000000000000000
> b*mapm.Pi:
1.57079632679489662
```

You cannot directly compare MAPM numbers with Agena numbers:

```
>a-b=0:
false
> a - b = mapm.xnumber (0):
true
```

See also: The long package implementing 80-bit floating-point arithmetic, described in Chapter 11.15.

The mathematical functions are:

| Function | Meaning | Function | Meaning |
| :---: | :---: | :---: | :---: |
| mapm.xabs | absolute value | mapm.xfactorial | factorial |
| mapm.xarccos | arc cosine | mapm.xidiv | integer division |
| mapm. xarccosh | inverse hyperbolic cosine | mapm.xin | natural logarithm |
| mapm.xadd | addition | mapm.xlog | logarithm of given base |
| mapm.xarcsin | inverse sine | mapm.xlog2 | base-2 logarithm |
| mapm.xarcsinh | inverse hyperbolic sine | mapm.xlog10 | common logarithm |
| mapm.xarctan | inverse tangent | mapm.xmul | multiplication |
| mapm. xarctan2(x, y) | 4 quadrant inverse tangent | mapm.xpow | power |
| mapm. xarctanh | hyperbolic inverse tangent | mapm.xsign | sign |
| mapm.xcbrt | cubic root | mapm.xsin | sine |
| mapm.xcos | cosine | mapm.xsincos | sine and cosine |
| mapm.xcosh | hyperbolic cosine | mapm.xsinh | hyperbolic sine |
| mapm.xdiv | division | mapm.xsqrt | square root |
| mapm.xerf | error function | mapm.xsub | subtraction |
| mapm.xerfc | complementary error function | mapm.xtan | tangent |
| mapm.xhypot (x, y [, prec]) | hypotenuse with optional precision | mapm.xtanh | hyperbolic tangent |
| mapm.xterm ( $c, x, n$ ) | computes $\mathrm{C}^{*} \mathrm{x}^{\wedge} \mathrm{n}$ | mapm.xfma $(x, y, z)$ | fused multiply-add |
| mapm.xexp | exponential function |  |  |
| mapm.xexp2 | base-2 exponentation |  |  |
| mapm.xexp 10 | base-10 exponentation |  |  |

Most of the mapm functions accept a second argument - a non-negative integer giving the individual precision.

The package provides the following metamethods:

| Operator | Name | Description |
| :--- | :--- | :--- |
| + | '_-add' | addition |
| - | '_-sub' | subtraction |
| $*$ | '_-mul' | multiplication |
| $/$ | '_-div' | division |
| $\%$ | '_-mod' | modulus |
| $\wedge$ | '_-pow' | power with any exponent |
| $* *$ | '__ipow' | power with integer exponent |


| Operator | Name | Description |
| :---: | :---: | :---: |
| - | '__unm' | unary minus |
| < | '__lt' | less-than |
| $=$ | '__eq' | equals |
| <= | '__le' | less-or-equal |
| abs | '__abs' | absolute value |
| sign | '__sign' | sign |
| recip | '__recip' | reciprocal |
| sqit | '__sqrt' | square root |
| square | '__square' | square ( $x^{\wedge} 2$ ) |
| cube | '__cube' | cube ( $\mathrm{x}^{\wedge} 3$ ) |
| In | '__ln' | natural logarithm |
| exp | '__exp' | exponential function |
| sin | '__sin' | sine |
| cos | '__cos' | cosine |
| tan | '-_tan' | tangent |
| arcsin | '__arcsin' | arcus sine |
| arccos | '__arccos' | arcus cosine |
| arctan | '__arctan' | arcus tangent |
| sinh | '__sinh' | hyperbolic sine |
| cosh | '__cosh' | hyperbolic cosine |
| tanh | '__tanh' | hyperbolic tangent |
| n/a | '__gc' | garbage collection |
| n/a | '__tostring' | conversion to a string, e.g. for the pretty printer |

Other functions are:

| Function | Meaning | Function | Meaning |
| :--- | :--- | :--- | :--- |
| mapm.xceil | ceil function | mapm. <br> xexponent | exponent |
| mapm.xfloor | floor function | mapm.xinv | reciprocal |
| mapm.xiseven | test for even <br> number | mapm.xisint | check for an <br> integral |
| mapm.xisodd | test for odd number | mapm.xmod | modulus |
| mapm.xround | rounds downwards <br> to the nearest <br> integer | mapm.xneg | negates a number |
| mapm. <br> xcompare(x, y) | comparison, returns <br> -1 if $x<y, 0$ if $x=y$, <br> and 1 if $x>y$ | mapm.xnumber | converts an Agena <br> number or a string <br> representing a <br> number to an <br> arbitrary precision <br> number |


| Function | Meaning | Function | Meaning |
| :--- | :--- | :--- | :--- |
| mapm.xdigits | sets the number of <br> digits used in all sub- <br> sequent calcula- <br> tions. With no argu- <br> ment, returns the <br> current setting. <br> (default is 17) | mapm. <br> xtonumber | converts an arbitrary <br> precision number to <br> an Agena number. <br> A second optional <br> argument $n$ gives <br> the precision for this <br> specific number, <br> with $n>0$. |
| mapm. <br> xdigitsin | significant digits | mapm.xtostring | converts an arbitrary <br> precision number to <br> a string |
| mapm.xchebyt <br> $(n, x)$ | n-th Chebyshev <br> polynomial of the <br> first kind at point $x$ |  |  |

Available constants with precision of 1,000 digits are:

| Constant | Value | Comment |
| :---: | :---: | :---: |
| mapm.Pi | $\pi$ |  |
| mapm.Pi2 | $2 \pi$ |  |
| mapm.PiO2 | $\pi / 2$ |  |
| mapm.PiO4 | $\pi / 4$ |  |
| mapm.PiO180 | $\pi / 180$ | radians per degree |
| mapm.InvPi2 | 1/(2r) |  |
| mapm.InvPiO4 | $4 / \pi$ |  |
| mapm.InvPiSqO4 | $4 / / \pi^{2}$ |  |
| mapm.E | $E=\exp (1)$ |  |
| mapm.sqıt2 | $\sqrt{2}$ |  |
| mapm.sqit3 | $\sqrt{3}$ |  |
| mapm.In2 | $\ln (2)$ |  |
| mapm.Invin2 | $1 / \ln (2)$ |  |
| mapm.Invsqrt2 | $1 / \sqrt{2}$ |  |
| mapm.Phi | $(1+\sqrt{5}) / 2$ | Golden Ratio |
| mapm.InvPhi | 1/((1+ $\left.\left.{ }^{5}\right) / 2\right)$ | inverse Golden Ratio |
| mapm.InvPhiSq | $(1 /((1+\sqrt{5}) / 2))^{2}$ |  |
| mapm.InPhi | $\ln (1+\sqrt{5}) / 2$ | logarithm of Golden Ratio |
| mapm.InvinPhi | $1 / \ln (1+\sqrt{5}) / 2$ | inverse |
| mapm.naught mapm.nought | 0 | zero |
| mapm.one | 1 |  |
| mapm.two | 2 |  |
| mapm.three | 3 |  |
| mapm.four | 4 |  |
| mapm.five | 5 |  |
| mapm.six | 6 |  |
| mapm.seven | 7 |  |


| Constant | Value | Comment |
| :--- | :--- | :--- |
| mapm.eight | 8 |  |
| mapm.nine | 9 |  |
| mapm.ten | 10 |  |
| mapm.eleven | 11 |  |
| mapm.twelve | 12 |  |
| mapm.fifty | 50 |  |
| mapm.hundred | 100 |  |
| mapm.thousand | 1,000 |  |
| mapm.half | 0.5 |  |
| mapm.quarter | 0.25 |  |
| mapm.tenth | 0.1 |  |
| mapm.fifth | 0.2 |  |
| mapm.hundredth | 0.01 |  |
| mapm.thousandth | 0.001 |  |

These constants have been defined in source file lib/mapm.agn.

## 11.4 mp - GNU Multiple Precision Arithmetic Library

As a plus package, the mp package is not part of the standard distribution and must be activated with the import statement, i.e. import mp.

The mp library is a binding to the GMP library providing multiple functions to conduct signed and unsigned integer arithmetic of arbitrary precision.

The package provides various metamethods for easy entry of calculations, too.
Signed and unsigned integers - `mpints` for short in this context - are represented by mp userdata objects which can be passed to the functions and operators described below.

OS/2, Solaris, Linux and UNIX users may have to install the original GMP 6.1 library separately in order for this binding to work. The package is not available for Mac OS X. In order for this binding to work on Intel CPUs, you may need at least a Sandybridge processor.

```
> import mp
> a, b := mp.uint(1), mp.uint(2) # unsigned integers
> a + b:
mp (3)
> a, b := mp.sint(2), mp.sint(3) # signed integers
> a * b:
mp (6)
```


### 11.4.1 Creation of Signed and Unsigned Integers

```
mp.uint (n)
```

mp.uint (numstr [, base])

Creates an unsigned integer object (mpz_† GMP userdata object) from an unsigned integer $n$, or a string numstr representing an unsigned integer.

If you pass a string you may indicate whether it is in decimal format by passing the optional second argument 10, and if its is in hexadecimal encoding, pass 16, which is the default.

See also: mp.sint, mp.setstring.

```
mp.sint (n)
mp.sint (numstr [, base])
```

Like mp.uint, but creates a signed integer mpz_† GMP userdata object.

### 11.4.2 Signed and Unsigned Integer Arithmetic

The following operators and functions can be applied both on signed and unsigned mpints:
mp.add ( $a, b$ )
Adds two mpints $a, b$, and returns a new mpint. Used by __add metamethod, i.e.: $\operatorname{mp} \cdot \operatorname{add}(\mathrm{a}, \mathrm{b})=\mathrm{a}+\mathrm{b}$.
mp. subtract (a, b)
Subtracts two mpints a, b and returns a new mpint. Used by $\qquad$ sub metamethod, i.e.: mp.subtract $(a, b)=a-b$.
mp.multiply (a, b)
Multiplies two mpints a, b and returns a new mpint. Used by __mul metamethod, i.e.: mp.multiply $(a, b)=a *$ b.

```
mp.divide (a, b)
```

Divides two mpints $a, b$ and returns a new mpint. Used by __div metamethod, i.e.: mp.divide $(a, b)=a / b$.

```
mp.addmul (r, a, b)
```

Multiplies two mpints $a, b$, adds the result to $r$ and returns the updated value of $r$ : i.e.: mp.addmul( $r, a, b)<=>r+:=a *$ b.
mp.submul ( $\mathrm{r}, \mathrm{a}, \mathrm{b}$ )
Multiplies two mpints $a, b$, subtracts the result from $r$ and returns the updated value of $r$ : i.e.: mp.submul( $r, a, b$ ) <=> r $-:=a$ * $b$.
mp.modulus ( $\mathrm{r}, \mathrm{a}, \mathrm{b}$ )
Computes the modulus of two mpints $a, b$ and returns a new mpint. Used by __mod metamethod, i.e.: mp.subtract $(a, b)=a \% b$.

## mp.neg (a)

Returns -a, with a an mpint, as a new mpint. Used by __unm metamethod, i.e. mp.neg(a) $<=>-a$.

```
mp.mul2exp (a, b)
```

Computes $a * 2 \wedge b$, with $a, b$ mpints, and returns the result in a new mpint. The operation is equivalent to a left shift by b bits.
mp.tdiv (a, b)
Returns both quotient and remainder of $a / b$, with $a, b$ units, both rounded towards zero.

```
mp.tdivq (a, b)
```

Divides two mpints $\mathrm{a}, \mathrm{b}$ and returns the resulting quotient as a new mpint, rounded towards zero.

```
mp.tdivr (a, b)
```

Divides two mpints $a, b$ and returns the resulting remainder as a new mpint, rounded towards zero.

## mp.powm (a, b, c)

With three units, computes $\left(\mathrm{a}^{\wedge} \mathrm{b}\right) \% \mathrm{c}$ and returns the result as a new mpint.

```
mp.root (a, n)
```

Computes the truncated integer part of the n-th root of a, with a an mpint, n a number, and returns the result as a new mpint.

## mp.log2 (a)

Like ilog2, but for mpint a.

### 11.4.3 Number Theoretic Functions

mp.testprime (a [, reps])
Checks whether mpint $a$ is a prime and returns:

- 0 if a is no prime,
- 1 if a is probably prime,
- 2 if a is definitely prime.

The accuracy of the result can be controlled by the optional second parameter reps which by default is 15 , with reasonable values between 15 and 50 .
mp.nextprime (a)
Returns the next prime to mpint a, as a new mpint.
mp.gcd (a, b)
Returns the greatest common divisor of mpints a and $b$, as a new mpint.
mp.gcdext (s, t, a, b)
Returns the greatest common divisor of mpint a and mpint band returns the result.
In addition the function sets mpints $s$ and $t$ to coefficients satisfying $a^{*} s+b^{*} t=$ (the return).
mp.lcm (a, b)
Returns the least common multiple of mpints a and b, as a new mpint.
mp.invert (a, b)
Computes the inverse of mpint a modulo mpint $b$ and returns a mpint.
mp.jacobi (a, b)
Computes the Jacobi symbol $(a / b)$ of the mpints $a, b$, which is defined only if $b$ is odd. The return is a new mpint.
mp.legendre ( $a, p$ )
Computes the Legendre symbol $(a / p)$ of the mpints $a, b$, which is defined only if $p$ is an odd positive prime. The return is a new mpint.

```
mp.kronecker (a, b)
```

Computes the Jacobi symbol ( $\mathrm{a} / \mathrm{b}$ ) for mpints $\mathrm{a}, \mathrm{b}$, with the Kronecker extension $(a / 2)=(2 / a)$ with odd $a$, and $(a / 2)=0$ with even $a$. The return is a new mpint.

## mp.remove ( $\mathrm{a}, \mathrm{b}$ )

Removes all occurrences of the factor a from b returns the result as a new mpint.

```
mp.factorial (n)
```

Returns the factorial of number n (_not_mpint) as a new mpint.
mp.fib ( n )
Returns the n-th Fibonacci number, with n a number (_not_mpint), and returns a new mpint.

## mp.lucas ( n )

Sets the n-th Lucas number, with n a number (_not_ mpint), and returns a new mpint.

## mp.primorial (n)

Returns the primorial of number n (_not_mpint), i.e. the product of all positive prime numbers $<=n$. The return is a new mpint.

```
mp.binomial (n, k)
```

Computes the binomial coefficient $n$ (an mpint) over $k$ (a number) and returns the result as a new mpint.

### 11.4.4 Bitwise Operations

## mp.andint (a, b)

Conducts a bitwise-and, 'a and b', with $a, b$ mpints, and returns the result as a new mpint.

```
mp.orint (a, b)
```

Conducts a bitwise-or, ‘a or b’, with a, b mpints, and returns the result as a new mpint.

## mp.xorint (a, b)

Conducts a bitwise-xor, ` a xor b`, with a, b mpints, and returns the result as a new mpint.

## mp.com (a)

Computes the one's complement of mpint a and returns the result as a new mpint.

```
mp.scan0 (a, n)
mp.scan1 (a, n)
```

Scan mpint a, starting from bit n (a number, not an mpint), towards more significant bits, until the first 0 or 1 bit (respectively) is found. The functions return the index of the found bit. Bit positions start from 0.
mp.popcount (a)
Computes the population count of mpint a, i.e. the number of 1 bits in the binary representation, and returns the result a number.

```
mp.mostsigbit (a)
```

Returns the position of the most significant bit (msb) as a number, counting from bit position number 0. If all bits are cleared, i.e. zero, returns -1 .

## mp.leastsigbit (a)

Returns the position of the least significant bit (Isb) in a number, counting from bit position number 0. If all bits are cleared, i.e. zero, returns -1.

```
mp.hamdist (a, b)
```

Computes the hamming distance between mpint a and mpint b, i.e. the number of positions a and b have different bit values. The count will be returned as a number.

## mp.setbit ( $\mathrm{r}, \mathrm{n}$ )

Sets bit $n$ in mpint $r$. The function returns nothing. $n$ is an integer position counting from 0 .

```
mp.getbit (r, n)
```

Returns bit $n$ in mpint $r$. The function returns a number. $n$ is an integer position counting from 0 .

```
mp.clrbit (r, n)
```

Clears bit n in mpint r . The function returns nothing. n is an integer position counting from 0.

```
mp.combit (r, n)
```

Conducts a bitwise complement ( ${ }^{n}$ not` operation) on bit number $n$ in mpint $r . n$ is an integer position counting from 0 . The function returns nothing.

### 11.4.5 Miscellaneous

```
mp.tonumber (a)
```

Returns the numeric value in mpint a as a number.
mp.tostring (a)
Returns the numeric value in mpint a as a string.
mp.swap (a, b)
Swaps the values in mpints a and b. The function returns nothing.
mp.cmp (a, b)
Compares $a$ and $b$ and returns a positive number if $a>b, 0$ if $a=b$, and a negative number if $\mathrm{a}<\mathrm{b}$.

```
mp.cmpabs (a, b)
```

Compares the absolute values of $a$ and $b$ and returns a positive number if $a>b, 0$ if $a=b$, and a negative number if $a<b$.
mp.iseven (a)
Checks whether mpint a represents an even integer and returns true or false.

## mp.isodd (a)

Checks whether mpint a represents an odd integer and returns true or false.

## mp.setstring (str)

Receives a string str and converts it to an mpint.
See also: mp.getstring, mp.uint, mp.sint.

```
mp.getstring (a)
```

Returns the string in mpint a that was previously stored to it by calling the mp.setstring function.

See also: mp.setstring, mp.tostring.

```
mp.sizeinbase (a)
```

Returns the size of a measured in number of digits in the given base, an integer. base can vary from 2 to 62 and should be even.
mp.attrib (a)
Returns various information on mpint a, in a dictionary.

## 11.5 mpf - GNU Multiple Precision Floating-Point Reliable Library

As a plus package, the mpf package is not part of the standard distribution and must be activated with the import statement, i.e. import mpf.

The mpf library is a binding to the MPFR library providing multiple functions to conduct floating-point arithmetic of arbitrary precision.

The package also provides various metamethods for easy entry of calculations.
MPFR floats are represented by mpf userdata objects which can be passed to the functions and operators described below.

OS/2, Solaris, Linux and UNIX users may have to install the original GMP 6.1 and MPFR 4.1 libraries separately in order for this binding to work. The package is not available for Mac OS X. In order for this binding to work on Intel CPUs, you may need at least a Sandybridge processor.

Examples:

```
> import mpf
> a, b := mpf.new(2), mpf.new(3) # define 2.0 & 3.0 as two MPFR floats
> a * b: # conduct multiplication
mpf(6.00000000000000000000000000000000000000000)
> sin(mpf.Pi): # compute sine of Pi
mpf(1.883041077660785116745909548456034940273e-39)
> mpf.precision(32); # reduce precision
> sin(mpf.Pi):
mpf(1.8830410775e-39)
> mpf.log2(mpf.new(8)): # compute base-2 logarithm of 8
mpf(3.0000000000)
```

Following are all available operators, mathematical and general functions.

| Operator | Functionality | Operator | Functionality |
| :---: | :--- | :---: | :--- |
| + | addition | exp | exponential function to the <br> base E $=2.71828 .$. |
| - | subtraction | sin | sine |
| $*$ | multiplication | cos | cosine |
| /an | tangent |  |  |
| a | division | exponentiation | cosh |
| $(-)$ | unary minus | hyperbolic sine |  |
| abs | absolute value | tanh | hyperbolic tangent |
| sign | sign | arcsin | inverse sine |
| sqrt | square root | arccos | inverse cosine |
| In | natural logarithm | arctan | inverse tangent |


| Operator | Functionality |
| :---: | :--- |
| isnonzero | test for a non-zero |
| iszero | test for zero |
| $=$ | equality check |
| $<$ | less-than relation |
| $<=$ | less-than-or-equal relation |
| $>$ | greater-than relation |
| $>=$ | greater-than or equal relation |


| Function | Arguments | Functionality |
| :---: | :---: | :---: |
| mpf.agm | 2 MPFR values | arithmetic-geometric mean |
| mpf.ai | 1 MPFR value | Airy function |
| mpf.arctan2 | 2 MPFR values | inverse tangent |
| mpf.beta | 2 MPFR values | Beta function |
| mpf.recsart | 1MPFR value | inverse square root |
| mpf.cbrt | 1 MPFR value | cubic root |
| mpf.ceil | 1 MPFR value | rounds up to the next higher or equal representable integer |
| mpf.copysign | 2 MPFR values | like math.copysign |
| mpf.cot | 1 MPFR value | cotangent |
| mpf.csc | 1 MPFR value | cosecant |
| mpf. digamma | 1 MPFR value | Digamma function |
| mpf.dim | 2 MPFR values a, b | returns $a-b$ if $a>b, 0$ if $a<=b$, or undefined of $a$ or $b$ is undefined |
| mpf.eint | 1 MPFR value | exponential integral |
| mpf.erf | 1 MPFR value | error function |
| mpf.erfc | 1 MPFR value | complementary error function |
| mpf.exp10 | 1 MPFR value | exponential to base 10 |
| mpf.exp2 | 1 MPFR value | exponential to base 2 |
| mpf.floor | 1 MPFR value | rounds to the next lower or equal representable integer |
| mpf.fma | 3 MPFR values | fused multiply-addition |
| mpf.fmod | 2 MPFR values | see: fmod |
| mpf.fms | 3 MPFR values | fused multiply-subtraction |
| mpf.gamma | 1 MPFR value | Gamma function |
| mpf.hypot | 2 MPFR values | hypotenuse |
| mpf.isfinite | 1 MPFR value | check for a finite value, unlike undefined or infinity |
| mpf.isinfinite | 1 MPFR value | check for infinity |
| mpf. isundefined | 1 MPFR value | check for undefined |
| mpf.j0 | 1 MPFR value | first kind Bessel function of order 0 |
| mpf.j1 | 1 MPFR value | first kind Bessel function of order 1 |
| mpf.jn | 2 MPFR values plus one integer for the order | first kind Bessel function of order $n$ |


| Function | Arguments | Functionality |
| :---: | :---: | :---: |
| mpf.y0 | 1 MPFR value | second kind Bessel function of order 0 |
| mpf.yl | 1 MPFR value | second kind Bessel function of order 1 |
| mpf.yn | 2 MPFR values plus one integer for the order | second kind Bessel function of order $n$ |
| mpf. 1 i2 | 1 MPFR value | real part of the dilogarithm of its argument |
| mpf.lgamma | 1 MPFR value | logarithm of the Gamma function |
| mpf.log10 | 1 MPFR value | logarithm to the base 10 |
| mpf.log2 | 1 MPFR value | logarithm to the base 2 |
| mpf.modf | 2 MPFR values | see: modf. |
| mpf. nexttoward | 1 MPFR value | works like `math.nextafter`, but for MPFR values; does not change its argument |
| mpf.random | none | returns a uniformly distributed random float on the interval $[0,1]$ |
| mpf.round | 1 MPFR value | rounds to nearest representable integer, rounding halfway cases away from zero |
| mpf.sec | 1 MPFR value | secant |
| mpf.signbit | 1 MPFR value | checks the sign bit and returns true (value is negative) or false |
| mpf.trunc | 1 MPFR value | rounds to the next representable integer toward zero |
| mpf.zeta | 1 MPFR value | Riemann Zeta function |
| mpf.Zero | 1 signed integer | returns an MPFR +0 or -0 , depending on sign of its argument |
| mpf. Inf | 1 signed integer | returns an MPFR +infinity or -infinity, depending on sign of its argument |
| mpf.Nan | none | returns MPFR undefined |
| mpf.max | 2 MPFR values | returns the maximum of two values |
| mpf.min | 2 MPFR values | returns the minimum of two values |
| mpf.Ln2 | n/a | MPFR constant $\operatorname{In}(2)$ |
| mpf.Pi | n/a | MPFR constant Pi |
| mpf.Euler | n/a | MPFR constant $\gamma=0.57721566490 . .$. |
| mpf.Catalan | n/a | MPFR constant $\lambda=0.91596559417 . .$. |

See also: The long package implementing 80-bit floating-point arithmetic, described in Chapter 11.15.

General functions:
mpf.clone (x)
Clones an MPFR value and returns it. The rounding mode of the MPFR value returned will be the current one, not necessarily the one with which the value to be duplicated has been created.

## mpf.new (x)

Creates an MPFR floating-point object from a number $x$, or a string x representing a number. For best accuracy, you should pass strings instead of numbers, as numbers are rounded before converted to an MPFR value.
mpf.precision ([x])
Gets or sets the overall precision, in bits. If an integer x in the range 2 .. $2,147,483,647$ is being passed, the function sets the precision for all values subsequently allocated.

If no argument is given, the current setting will be returned.
The default precision at invocation of the package is 128 .

```
mpf.rounding ([rmode])
```

Gets or sets the current rounding mode. If a string rmode is passed, the function sets the rounding mode for all values subsequently allocated. Valid settings for rmode are the strings:

- 'rndn ', round to nearest, with ties to even;
- 'rndz', round toward zero;
- 'rndu', round toward +infinity;
- 'rndd ', round toward -infinity.

If no argument is given, the current rounding mode will be returned.
The default rounding mode at invocation of the package is 'rndn', i.e. rounding to nearest.

```
mpf.swap (x, y)
```

Swaps the values in MPFR values x and y . The function returns nothing.

```
mpf.tonumber (x)
```

Converts an MPFR value x into an Agena number.

```
mpf.tostring (x)
```

Converts an MPFR value x into a string.

## 11.6 divs - Library to Process Fractions

As a plus package, this library is not part of the standard distribution and must be activated with the import statement, e.g. import divs.

The library provides basic arithmetic to calculate with fractions. To create a fraction, use divs.divs which accepts mixed, improper and proper fractions. The package implements metamethods so that the common addition, subtraction, division, and unary minus operators can be used.

The + operator adds two fractions, or a number and a fraction in any order.
The - operator subtracts two fractions, or a number and a fraction in any order.
The * operator multiplies two fractions, or a number and a fraction in any order.

The / operator divides two fractions, or a number and a fraction in any order.
The ^ operator exponentiates two fractions, or a number and a fraction in any order.

The ** operator raises a fraction to an integer power, in this order.
The abs operator returns the absolute value of a fraction and returns a fraction.

The sign operator returns the sign of a fraction and returns a number.
The sqit operator returns the square root of a fraction and returns a fraction. If the resulting fraction could not be evaluated with absolute precision, it returns a number.

The In operator returns the natural logarithm of a fraction and returns a fraction. If the resulting fraction could not be evaluated with absolute precision, it returns a number.

The $\exp$ operator returns the value of $\mathbf{E}$ to the power of the given fraction and returns a fraction. If the resulting fraction could not be evaluated with absolute precision, it returns a number.

The sin operator returns the sine of a fraction and returns a fraction in radians. If the resulting fraction could not be evaluated with absolute precision, it returns a number (in radians).

The cos operator returns the cosine of a fraction and returns a fraction in radians. If the resulting fraction could not be evaluated with absolute precision, it returns a number (in radians).

The tan operator returns the tangent of a fraction and returns a fraction in radians. If the resulting fraction could not be evaluated with absolute precision, it returns a number (in radians). It returns undefined if poles have been encountered.

The arctan operator returns the arcus tangent of a fraction and returns a fraction in radians. If the resulting fraction could not be evaluated with absolute precision, it returns a number (in radians). It returns undefined if poles have been encountered.

The int operator returns the integer quotient of the numerator of a fraction divided by its denominator.

The numerators and denominators should all be integers.
The return always is an improper fraction. There are also two functions to convert fractions to decimals and vice versa.

Examples:

```
> import divs;
> divs.divs(1, 2, 3) + divs.divs(1, 3):
2
> divs.divs(1, 2) * divs.divs(1, 3):
divs(5, 6)
> divs.divs(1, 2) * divs.divs(1, 3):
divs(1, 6)
> 2 * divs.divs(1, 3):
divs(2, 3)
> divs.todec(divs.divs(1, 2)):
0.5
> divs.todiv(ans):
div(1, 2) 0
```

Relations: Two fractions can be compared with the $<,<=,=,==, \sim=,>=$, and > operators.

The following operators are also supported: arcsin, arccos, arcsec, sinh, cosh, tanh, recip, and $\sim<>$.

Functions:
divs.denom (a)
This function returns the denominator of the fraction a of the user-defined type 'divs' and returns it as a number.

The function is written in Agena and is included in the lib/divs.agn file.
See also: divs.numer.

```
divs.divs ([x, ] y, z)
divs.divs ([x:]y:z)
```

This function defines a fraction and returns it as a value of the user-defined type 'div' if $z$ is not 1 , with proper metamethods added. It returns a number if $z$ equals 1 , and undefined if $z$ is 0 .

In the first form: if all three arguments are given, representing a mixed fraction $x \frac{y}{z}$, the function converts it into an improper fraction and returns it. If only $y$ and $z$ are given, the function returns a reduced improper or proper fraction $\frac{x}{y}$.

The second form allows to pass $x, y$, and $z$ as a nested pair x:y:z, representing a mixed fraction, or the pair $y: z$ representing an improper or proper fraction.

In both forms, $x, y$, and $z$ should be integers.
The function is written in Agena and is included in the lib/divs.agn file.

```
divs.equals (a, b [, option])
```

This function checks two fractions $a, b$ for equality. Alternatively, either a or b may be simple Agena numbers. The result is either true or false. If any non-null option is given, the function checks for approximate equality (see approx function). Note that the equality operators $=,==$, and $\sim=$ cannot check values of different types.

The function is written in Agena and is included in the lib/divs.agn file.
divs.numer (a)
This function returns the numerator of the fraction a of the user-defined type 'divs ' and returns it as a number.

The function is written in Agena and is included in the lib/divs.agn file.
See also: divs.denom.

```
divs.todec (a)
```

This function converts a fraction a of the user-defined type 'divs' to a float and returns it.

The function is written in Agena and is included in the lib/divs.agn file.
See also: divs.todiv.

```
divs.todiv (x)
```

This function converts a number $x$ to an improper fraction of the user-defined type 'divs' and returns it. The second return is the accuracy (see math.fraction for further information).

The function is written in Agena and is included in the lib/divs.agn file.
See also: divs.todec, math.fraction.

## 11.7 dual - Dual Numbers

As a plus package, the dual package is not part of the standard distribution and must be activated with the import statement, i.e. import dual.

This library provides basic support for dual numbers which are related to complex numbers, but instead of an imaginary unit i with $\mathrm{i}^{2}=-1$, we have a nilpotent $\varepsilon$ unit with $\varepsilon^{2}=0$.

Dual numbers are used with automatic differentiation, and other applications.
The package provides basic arithmetic operators via and also some transcendent functions, in cases, through metamethods.

To define a dual number, e.g. $1+2 \varepsilon$, type:

```
> import dual
> a := dual.dual(1, 2)
> a:
1+2e
```

Add a to $3+4 \varepsilon$ :

```
> b := dual.dual(3, 4)
> a+b:
4+6e
```

Square root:

```
> sqret(ans):
```

$2+1.5 e$

The following lists all available operators and functions and the results, with two dual numbers $\mathrm{p}=\mathrm{a}+\mathrm{b} \varepsilon$ and $\mathrm{q}=\mathrm{c}+\mathrm{d} \varepsilon$ :

| Operation | Call | Real Part | Dual Part |
| :---: | :---: | :---: | :---: |
| Unary minus | -p | -a | -b |
| Addition | $p+q$ | $a+c$ | $b+d$ |
| Subtraction | $p-q$ | $a-c$ | $b-d$ |
| Multiplication | $p^{*}$ q | $a^{*} c$ | $a^{*} d+b^{*} c$ |
| Division | $p / q$ | a/c | (b*c - $\left.\mathrm{a}^{*} \mathrm{~d}\right) /\left(c^{*} \mathrm{c}\right)$ |
| Reciprocal | $1 / p$ | 1/a | -b/(a**2) |
| Exponentiation | $p^{\wedge} \mathrm{q}$ | $a^{\wedge} \mathrm{c}$ | $a^{\wedge} c^{*}\left(d^{*} \ln a+b^{*} c / a\right)$ |
| Square | square $p$ | $\mathrm{a}^{* *} 2$ | 2*a*b |
| Cube | cube P | a**3 | 3*b*a**2 |
| Absolute value | abs p | abs a | n/a |
| Sign | sign p | $\begin{aligned} & 1 \text { 1, if } a>0 \text { or } a=0 \\ & \text { and } b>0 \\ & -1, \text { if } a<0 \text { or } \\ & a=0 \text { and } b<0 \\ & 0 \text {, otherwise } \end{aligned}$ | n/a |
| Exponential function | $\exp p$ | exp a | b*exp a |
| Natural logarithm | $\ln \mathrm{p}$ | In a | b/a |
| Base-2 logarithm | log2 | $\log 2(\mathrm{a})$ | b/a/log(2) |
| Base-10 logarithm | $\log 10$ | $\log 10(a)$ | b/a/log(10) |
| $\exp (\mathrm{x})-1$ | exp- <br> minusone | expminusone(a) | $\mathrm{b}^{*} \exp (\mathrm{a})$ |
| $\ln (\mathrm{x}+1)$ | Inplusone | Inplusone(a) | $\mathrm{b} /(1.0+\mathrm{a})$ |
| Square root | sqit p | sqrit a | 0.5*a[2]/sqit a |
| Hypotenuse | hypot p | hypot(a, b) | ./. |
| Sine | $\sin \mathrm{p}$ | $\sin a$ | $\mathrm{b}^{*} \cos \mathrm{a}$ |
| Cosine | $\cos p$ | $\cos a$ | -b*sin a |
| Tangent | $\tan \mathrm{p}$ | tan a | $\mathrm{b} /\left(\cos (\mathrm{a})^{* *} 2\right)$ |
| Arcus sine | $\arcsin \mathrm{p}$ | arcsin a | b/hypot3(a) |
| Arcus cosine | $\arccos p$ | $\arccos a$ | -b/hypot3(a) |
| Arcus tangent | $\arctan p$ | arctan a | $b /\left(1+a^{*} a\right)$ |
| Hyperbolic sine | sinh $p$ | sinh a | $b^{*}$ cosh a |
| Hyperbolic cosine | cosh p | cosh a | $\mathrm{b}^{*} \sinh \mathrm{a}$ |
| Hyperbolic tangent | tanh p | tanh a | $\mathrm{b}^{*} \operatorname{sech}(\mathrm{a})^{\wedge} 2$ |
| Inverse hyperbolic sine | arcsinh | $\operatorname{arcsinh}(\mathrm{a})$ | $b^{*}\left(1 / s q r^{\prime \prime}\left(a^{\wedge} 2+1\right)\right)$ |
| Inverse hyperbolic cosine | arccosh | $\operatorname{arccosh}(\mathrm{a})$ | $b^{*}\left(1 / s q r^{\prime \prime}\left(a^{\wedge} 2-1\right)\right)$ |
| Inverse hyperbolic tangent | arctanh | $\operatorname{arctanh}(\mathrm{a})$ | $b^{*}\left(1 /\left(1-a^{\wedge} 2\right)\right)$ |
| Error function | erf | erf(a) | $\mathrm{b}^{*} 2 / \mathrm{sqrt}(\mathrm{Pi})$ * $\exp \left(-(\mathrm{a})^{\wedge} 2\right)$ |
| Complementary error function | erfc | erfc(a) | $\mathrm{b}^{*}-2 / \mathrm{sqrt}(\mathrm{Pi})^{*} \exp \left(-(\mathrm{a})^{\wedge} 2\right)$ |
| Scaled complementary error function | erfcx | erfcx(a) | $\begin{aligned} & 2 * a * \operatorname{expx2(a)} * \operatorname{erfc}(a) \\ & 2 / \mathrm{sqlt}(\mathrm{Pi}) \end{aligned}$ |
| Equality | $p=q$ | $a=c$ and $b=d$ | n/a |


| Operation | Call | Real Part | Dual Part |
| :--- | :--- | :--- | :--- |
| Relation $<$ | $\mathrm{p}<\mathrm{a}$ | $\mathrm{a}<\mathrm{c}$ | $\mathrm{n} / \mathrm{a}$ |
| Relation $<=$ | $\mathrm{p}<=\mathrm{q}$ | $\mathrm{a}<=\mathrm{c}$ | $\mathrm{n} / \mathrm{a}$ |
| Relation $>$ | $\mathrm{p}>\mathrm{q}$ | $\mathrm{a}>\mathrm{c}$ | $\mathrm{n} / \mathrm{a}$ |
| Relation $>=$ | $\mathrm{p}>=\mathrm{q}$ | $\mathrm{a}>=\mathrm{c}$ | $\mathrm{n} / \mathrm{a}$ |

## 11.8 clock - Clock Package

This package contains mathematical routines to perform basic operations on time values, i.e. hours, minutes, and seconds.

As a plus package, it is not part of the standard distribution and must be activated with the import statement, e.g. import clock.

A time value is always defined by the clock.tm constructor. You may apply the ordinary,,$+- *$ and / operators in order to add, subtract, multiply or divide values. The relations $<,<=,=,>=$, and $>$ are also supported.

Also, the following operators can be used for sexagesimal arithmetic - but please beware of round-off errors, for they convert a sexagesimal argument to decimal, apply the operator, and convert the result back to sexagesimal.

The ^ operator exponentiates sexagesimals, or sexagesimals and numbers, and returns a sexagesimal.

The abs operator determines the absolute value of a sexagesimal and returns a sexagesimal.

The sign operator returns the sign of a sexagesimal and returns a number.
The sqit operator returns the square root of a sexagesimal and returns a sexagesimal. If the sexagesimal is negative, it returns undefined.

The In operator returns the natural logarithm of a sexagesimal and returns a sexagesimal. If the sexagesimal is non-negative, it returns undefined.

The $\exp$ operator returns the value of $\mathbf{E}$ to the power of the given sexagesimal and returns a sexagesimal.

The sin operator returns the sine of a sexagesimal and returns a sexagesimal, in radians.

The cos operator returns the cosine of a sexagesimal and returns a sexagesimal, in radians.

The tan operator returns the tangent of a sexagesimal and returns a sexagesimal, in radians. It returns undefined if poles have been encountered.

The arctan operator returns the arcus tangent of a sexagesimal and returns a sexagesimal, in radians. With poles, it returns undefined.

By default, all time values are properly adjusted to a normalised representation if the value of the environment variable _clockAdjust is not changed. If it
clockAdjust is set to a value different from true, then this normalisation is switched off.

All functions are implemented in Agena and included in the lib/clock.agn file.
A typical example might look like this:

```
> import clock alias
add, adjust, div, mul, sub, pow, tm, todec, totm
```

Subtract 10 hours and fifteen minutes from 20 hours and 15 minutes:

```
> tm(20, 15, 0) - tm(10, 15, 0):
tm(10, 0, 0)
```

61 seconds are automatically converted to 1 minute and 1 second:

```
> tm(0, 61):
tm(0, 1, 1)
```

Turn off normalisation:

```
> _clockAdjust := null
> tm(0, 61):
tm(0, 0, 61)
```

Turn on normalisation again:

```
> __clockAdjust := true
```

The functions provided by the package are:

```
clock.add (t1, t2 [, \cdots.])
```

The function adds two or more values of type $\mathbf{t m}$. The return is a value of type $\mathbf{t m}$.

```
clock.adjust (t)
```

The function adjusts the representation of tm values in a time object t by applying the rules described in the description of clock.tm.
clock.sub (t1, t2 [, ...])
The function subtracts two or more values of type tm. The return is a value of type tm.

```
clock.sgstr (x [, d])
```

Converts a float or `tm` value x into its sexagesimal string representation of the format hh:mm:ss. The colon to separate hours, minutes, and seconds can be changed by passing another optional delimiter a of type string.

See also: clock.totm.

```
clock.tm (min)
clock.tm (min, sec)
clock.tm (hrs, min, sec)
```

This function is used to define time values, where hrs , min, sec are numbers.
In the first form, minutes are defined. The return is a value of type tm of the form tm(0, min, 0).

In the second form, both minutes and seconds are defined. The return is a value of type tm of the form $\mathrm{tm}(0, \mathrm{~min}, \mathrm{sec})$.

In the third form, both hours, minutes, and seconds are defined and returned as a value of type tm of the form tm(hrs, min, sec). (hrs may be set to 0 .)

By default, if min $>59$ and / or if sec $>59$, proper adjustments are made before the time value will be returned. If $\min >59$ the call to time returns $t m$ (hrs +1 , min $60, \mathrm{sec}$ ). If sec $>59$ the call to time returns tm (hrs, min +1 , sec -60 ). The default is set by the global variable _clockAdjust which is assigned true at initialisation of the package if it has not already been set false before the clock package has been loaded.
hrs might be any non-negative number.
If _clockAdjust is set false then no adjustments are made to the arguments. You can use clock.adjust to apply the adjustments described above.

```
clock.todec (t)
```

Converts a tm value t into its decimal representation of type number.
See also: clock.totm, math.todecimal.

```
clock.totm (t)
```

Converts a tm value t in decimals (of type number) into its tm representation. The return is of type tm.

See also: clock.todec.

## 11.9 astro - Astronomy Functions

As a plus package, the astro package is not part of the standard distribution and must be activated with the import statement, e.g. import astro.

```
astro.cdate (x)
```

Converts a Julian date, represented by the float x, into its Gregorian calendar date representation, returning seven values in the following order: the year, the month, the day, the decimal fraction of the day - in the range $[0,1)$-, the hour, minute, and second.

See also: astro.jdate, os.date, os.isdst.

```
astro.cweek (y, m, d)
```

Returns the calendar week for the given year (y), month (m), and day (d), an integer in the range 1 .. 53 , determined according to the ISO 8601 standard, and the corresponding year as the second result. The second result is not necessarily equal to $y$, e.g. the calendar week of January 1, 2016 is calendar week 53 of 2015, and the calendar week of December 31, 2013 is week 1 of 2014.

If the passed date does not exist, the function issues an error.
See also: astro.lastcweek, os.date.

```
astro.cweekmonsun (y, cw)
```

Computes the Gregorian dates of the Monday and Sunday for a given calendar week cw and year y and returns four numbers: the year, the month, the day, and the fraction of day - in his order. In case of a non-existing calendar week cw, the function issues an error.

See also: astro.cweek, os.date.

```
astro.dectodms (x, orientation)
```

Converts co-ordinates x in decimal degrees (a number) to the form degree, minute, second, and their orientation ' N ', 'S', 'W', or 'E' (DMS format). You must also specify whether to compute latitude or longitude values, by passing the strings 'lat' Or 'lon', respectively for orientation.

The return are three numbers and the orientation, a string.
See also: astro.dmstodec.

```
astro.dmstodec (degree, minute, second, hour, orientation)
```

Converts co-ordinates in DMS format consisting of degree, minute, second, (all numbers) and their orientation ' N ', 'S', 'W', or ' $E$ ' (a single-character string) to their corresponding decimal degree representation (DegDec format). The return is a number.

See also: astro.dectodms.
astro.hdate (jd)
Converts the Julian date ja to the corresponding year, month and day in the Jewish calendar, in this order. The fraction of day, the hour, minute and second are also returned.

See also: astro.jdate, os.date with the '*j' format.

```
astro.isleapyear (x)
```

Returns true if the given year x (a number) is a leap year, and false otherwise.

```
astro.lastcweek (y [, flag])
```

Computes the last calendar week of the year $y$. If flag is not given, the function returns either the number 52 or 53, and the given year y. If flag is given, then calendar week 1 and $\mathrm{y}+1$ will be returned if December 31 of the given year y is either a Monday, Tuesday or Wednesday, otherwise it works as if $f$ lag has not been passed.

See also: astro.lastcweek, os.date.
astro.jdate (year, month, day [, hour [, minute [, second]]])
Converts a Gregorian date represented by year, month, day and optionally hour, minute, and second (all numbers) to the corresponding Julian date. The return is a number, or fail if the date or time is of a wrong format.

By definition, the base 0 of the Julian date is January 1, 4713 BC, noon GMT. However, since the function takes no account of the date(s) of adoption of the Gregorian calendar, astro.jdate(0) does not return this date.

The defaults for hour, minute, and second are 0 .
See also: astro.cdate, os.date, os.isdst.
astro.moon (year, month, day, hour, lon, lat)
Provides an easier-to-use interface to astro.moonriseset. and astro.moonphase.

The first four arguments represent the year, month, day, and hour, all of type number. Longitudes and latitudes can be given in form of two tables lon, lat containing degrees (a number), minutes (a number), seconds (a number), and the orientation (the single character 'N', 'S', 'W', or 'E').

The return is a table with the indices 'riseset', containing the rise and set times of the Moon in 'tm' representation, and the index 'phase' which holds the computed Lunar phase (a float and an integer).

See astro.moonriseset and astro.moonphase for further information.
The function uses the ‘tm` time notation of the clock package. You do not have to readlib clock before.

The function is written in Agena and included in the astro.agn file.
Example for Düsseldorf:

```
> astro.moon(2013, 1, 7, 0, [7, 6, 0, 'E'], [50, 43, 48, 'N']):
[phase ~ [0.2995659104481, 7], riseset ~ [tm(2, 27, 0), tm(11, 50, 0)]]
```

astro.moonphase (year, month, day [, hour])
Takes a year, a month, a day, and optionally an hour (all numbers) and returns the moon phase as a real number in the range $[0,1]$, where 0 is new moon and 1 is full Moon; and an integer in the range [0, 7], where 0 indicates new moon and 4 indicates full moon. If hour is not given, it is set to 0 .

See also: astro.moon.
astro.moonriseset (year, month, day, lon, lat)
Returns the times of Lunar rise and set in GMT. Receives the year, month day, the longitude and latitude lon and lat (all of type number) and returns two numbers: the GMT rise time in a decimal, and the GMT set time also in a decimal.

Use clock.totm to convert the rise and set times to sexagesimal format, or try astro.moon.

## Example for Düsseldorf:

```
> astro.moonriseset(2013, 1, 8,
    astro.dmstodec(6, 46, 58, 'E'), astro.dmstodec(51, 13, 32, 'N')):
3.7666666666667 12.566666666667
astro.sun (year, month, day, lon, lat)
Provides an easier-to-use interface to astro.sunriseset.
```

year, month, and day must be integers. Longitudes and latitudes can be given in form of two tables lon, lat, containing degrees (a number), minutes (a number), seconds (a number), and the orientation (the single-character string 'N', 'S', 'W', or 'E').

The return is a table with the indices 'riseset', 'civil', 'astro', and 'nautical' containing the rise and set times in 'tm` representation. The index 'south' holds the time where the Sun is at south.

See astro.sunriseset for further information.

The function uses the `tm` time notation of the clock package. The function uses the 'tm` time notation of the clock package. You do not have to readlib clock before.

The function is written in Agena and included in the astro.agn file.
Example for Düsseldorf:

```
> astro.sun(2013, 1, 7, [6, 46, 58, 'E'], [51, 13, 32, 'N']):
[astro ~ [tm(5, 34, 5.1483689555826), tm(17, 44, 22.952745470386)],
civil ~ [tm(6, 56, 25.738372228174), tm(16, 22, 2.3627421977944)],
nautical ~ [tm(6, 14, 13.023074498407), tm(17, 4, 15.078039927568)],
riseset ~ [tm(7, 35, 19.775508661645), tm(15, 43, 8.325605764323)],
south ~ tm(11, 39, 14.050557212984)]
```

astro.sunriseset (year, month, day, lon, lat)
Returns the sunrise/sunset times in UTC for years starting with 1800 A.D. to 2099 A.D. It is a workhorse function, maybe you would like to use astro.sun for a more convenient interface.
year, month and day, all integers, are the values of the day to evaluate. lon is the longitude (west/east), and lat the latitude (west/east), both in decimal degrees of type float of the location that is of interest. Use astro.dmstodec to convert co-ordinates containing degrees (integer), minutes (integer), and seconds (integer or float), and the orientation to decimal degrees.

## Example for Düsseldorf:

```
> astro.sunriseset(2013, 1, 7,
> astro.dmstodec(6, 46, 58, 'E'), astro.dmstodec(51, 13, 32, 'N')):
7.5888265301838 15.718979334935 0 6.9404828811745 16.367322983944 0
6.2369508540273 17.070855011091 0 5.5680967691543 17.739709095964 0
```

11.653902932559

The first and second returns are the sunrise/sunset times which are considered to occur when the Sun's upper limb is 35 arc minutes below the horizon (this accounts for the refraction of the Earth's atmosphere).

The third return is 0 , if the rises and sun sets in a day; +1 if the Sun is above the specified `horizon` 24 hours, -1 if the Sun is below the specified `horizon` 24 hours.

The fourth and fifth returns are start and end times of civil twilight. Civil twilight starts/ends when the Sun's centre is 6 degrees below the horizon.

The sixth return is 0 , if the rises and sun sets in a day; +1 if the Sun is above the specified `civil twilight horizon` 24 hours, -1 if the Sun is below the specified `horizon` 24 hours.

The seventh and eighth returns are the start and end times of nautical twilight. Nautical twilight starts/ends when the Sun's centre is 12 degrees below the horizon.

The ninth return is 0 , if the rises and sun sets in a day; +1 if the Sun is above the specified `nautical twilight horizon` 24 hours, -1 if the Sun is below the specified `horizon` 24 hours.

The tenth and eleventh returns are the start and end times of astronomical twilight. Astronomical twilight starts/ends when the Sun's centre is 18 degrees below the horizon.

The twelfth return is 0 , if the rises and sun sets in a day; +1 if the Sun is above the specified `nautical twilight horizon` 24 hours, -1 if the Sun is below the specified "astronomical twilight horizon` 24 hours.

The thirfeenth return is the time when the Sun is at south (in decimal UTC).
All times returned are given in decimal hours of type number. Use clock.totm to convert them into 'tm' notation.

## See also: astro.sun, astro.moon.

```
astro.taiutc ([jd])
```

Returns the TAI-UTC lookup table value of leap seconds for a given Julian date jd; if no argument is given, then the value for the current system date is computed. TAl stands for International Atomic Time. The function returns 0 for Gregorian dates before 1961.

In the future, you may have to add further values to the source code of this function which also includes the URL of the respective file to be checked. The function is written in Agena and included in the astro.agn file.

See also: os.date ('*j' format).

### 11.10 cordic - Numerical CORDIC Library

As a plus package, this library is not part of the standard distribution and must be activated with the import statement, e.g. import cordic.

The CORDIC algorithm (CORDIC stands for COordinate Rotation Dlgital Computer) also known as the `Volder's algorithm', is used to calculate hyperbolic, trigonometric, logarithmic, and root functions, on hardware not featuring multipliers, requiring only addition, subtraction, bitshift and table lookup.

The algorithm, similar to one published by Henry Briggs around 1624, has been developed in 1959 by Kack E. Volder to improve an aviation system. According to Wikipedia, it has not only been used in pocket calculators, but also in x87 FPUs, in CPUs prior to Intel 80486 - and in Motorola's 68881, in signal and image processing, communication systems, robotics, and also 3D graphics - and other applications.

This binding to John Burkardt's CORDIC implementation uses additon, subtraction, table lookups, multiplication, divisions, and the absolute function.

The package accepts and returns Agena numbers only.

Available functions are:

```
cordic.carccos (x)
```

Returns the inverse cosine operator in radians.

```
cordic.carcsin (x)
```

Returns the inverse sine operator in radians.

```
cordic.carctan2 (y, x)
```

Returns the arc tangent of $\mathrm{y} / \mathrm{x}$ in radians, but uses the signs of both parameters to find the quadrant of the result.
cordic.carctanh (x)
Returns the inverse hyperbolic tangent of x in radians.

```
cordic.ccbrt (x)
```

Returns the cubic root of the number x .

```
cordic.ccos (x)
```

Returns the cosine of $x$ in radians.

```
cordic.ccosh (x)
```

Returns the hyperbolic cosine of x in radians.
cordic.cexp (x)
Returns $e^{x}$, the exponential function to the base $e=2.718281828459$...
cordic.chypot ( $\mathrm{x}, \mathrm{y}$ )
Returns $\sqrt{x^{2}+y^{2}}$, the hypotenuse.
cordic.cln (x)
Returns the natural logarithm of x .
cordic.cmul ( $\mathrm{x}, \mathrm{y}$ )
Returns $x^{*} y$, i.e. the product of $x$ and $y$.
cordic.csin (x)
Returns the sine of x in radians.
cordic.csinh (x)
Returns the hyperbolic sine of x in radians.
cordic.csqrt (x)
Returns the square root of $x$.
cordic.ctan (x)
Returns the tangent of x in radians.
cordic.ctanh (x)
Returns the hyperbolic tangent of x in radians.

### 11.11 zx - Sinclair ZX Spectrum Functions

As a plus package, the $\mathbf{z x}$ package is not part of the standard distribution and must be activated with the import statement, i.e. import zx .

### 11.11.1 Introduction

This package implements various Sinclair ZX Spectrum mathematical functions.

Most of the functions use the same algorithms and Chebyshev polynomials of degree 6, 8, or 12 as implemented in the Sinclair ZX Spectrum ROM, with similar accuracy.

All functions are based on those published on the book `The Complete Spectrum ROM Disassembly`, written by Dr. Ian Logan \& Dr. Frank O'Hara, pp. 217.

In general, the procedures are mostly slower and also less precise than their Agena pendants. By default, the fully expanded and simplified polynomials are hard-wired into the library's C code. By passing the optional last argument true, however, the polynomials are processed iteratively in real-time, using the $\mathbf{z x}$.genseries function which imitates the Z80 assembler subprocedure `series generator`.

You may query the respective Chebyshev coefficient vectors by calling zx.getcoeffs, and globally change them with zx.setcoeffs. Range reduction is performed by zx.reduce.

The names of all ZX Spectrum `clones` are written in capital letters, to not collide with Agena's built-in operators.

The $C$ source file src/zx.c contains exact information on the precision of the functions.

### 11.11.2 Original ZX Spectrum Functions

zx.ABS (x)
Returns the absolute magnitude of the number x. The function does not use Chebyshev polynomials.

See also: abs.
zx.ACS (x)
Computes the ZX Spectrum inverse cosine of its numeric argument x and returns a number. If $x \notin[-1,1]$, undefined will be returned.

See also: arccos.
zx.ADD (x, y)
Returns $\mathrm{x}+\mathrm{y}$.
See also: zx.DIV, zx.MUL, zx.SUB.
zx.AND ( $\mathbf{x}, \mathrm{y}$ )
Returns x if y is non-zero and the value zero otherwise. Strings are not supported. The function does not use Chebyshev polynomials.

See also: zx.NOT, zx.OR.
zx.ASN (x)
Computes the ZX Spectrum inverse sine of its numeric argument x and returns a number. If $x \notin[-1,1]$, undefined will be returned.

See also: arcsin.
zx.ATN (x)
Computes the $Z X$ Spectrum inverse tangent of its numeric argument $x$ and returns a number.

See also: arctan.
zx.cos (x)
Computes the ZX Spectrum cosine of its numeric argument $x$ and returns $a$ number.

See also: cos.
zx.DIV ( $\mathrm{x}, \mathrm{y}$ )
Returns $\mathrm{x} / \mathrm{y}$. With $\mathrm{y}=0$, the result is undefined.
See also: zx.ADD, zx.MUL, zx.SUB.
zx.EXP (x)
Computes the ZX Spectrum exponential function of the number x to the base $\mathbf{E}=$ $\exp (1)$. It looses precision, however, if its argument is greater than the constant $\mathbf{E}$.

See also: exp. zx.LN.
zx.INT (x)
Rounds its numeric argument $x$ downwards to the nearest integer. The function does not use Chebyshev polynomials.

See also: entier.
zx.LN (x)
Computes the $Z X$ Spectrum natural logarithm of the number $x$. If $x \leq 0$, undefined will be returned.

See also: In, zx.EXP.
zx.MUL (x, y)
Computes $x^{*} y$.
See also: zx.ADD, zx.DIV, zx.SUB.
zx.NOT (x)
Returns 1 if its numeric argument x is 0 , and 0 otherwise. The function does not use Chebyshev polynomials.

See also: not, zx.AND, zx.OR.
zx.OR (x, y)
Returns the number x if the number y is 0 , and 1 otherwise. Strings are not supported. The function does not use Chebyshev polynomials.

See also: or, zx.AND, zx.NOT.
zx.PI
The constant $\pi$ in the ZX Spectrum precision (supposedly C float).
zx.POW ( $\mathrm{x}, \mathrm{y}$ )
Returns the $Z X$ Spectrum exponentiation $x \uparrow y$, with $x$ and $y$ numbers, and returns $a$ number.

Internally, the $Z X$ Spectrum and this function treats $x \uparrow y$ like $\exp \left(\ln (x)^{*} y\right)$. If $x<0$ then undefined will be returned.

As with $\mathbf{z x}$.EXP, the function is quite imprecise if $x>E$ (the constant).

See also: ** and ${ }^{\wedge}$ operators, $\mathbf{z x}$.SQR.
zx.SGN (x)
Returns -1 if the number $x$ is negative, 0 if $x$ is zero, and 1 if $x$ is positive. If $x$ is undefined, undefined will be returned. The function does not use Chebyshev polynomials.

See also: sign, signum.
zx.SIN (x)
Computes the $Z X$ Spectrum sine of its numeric argument $x$ and returns a number.

See also: sin, zx.COS, zx.TAN.
zx.SQR (x)
Returns the $Z X$ Spectrum square root of its numeric argument $x$ and returns $a$ number. If $x<0$, undefined will be returned.

See also: sqrt, zx.POW.
zx.SUB (x, y)
Computes $\mathrm{x}-\mathrm{y}$.

See also: zx.ADD, zx.DIV, zx.MUL.
zx.TAN (x)
Computes the ZX Spectrum tangent of its numeric argument $x$ and returns $a$ number.

See also: tan, zx.COS, zx.SIN.

### 11.11.3 Auxiliary Functions

## zx.genseries (x, s)

Receives a number $x$ in the range $[-1,1]$ and a sequence of coefficients and returns the value of the corresponding Chebyshev polynomial. If $x$ is out of range, no error will be returned. This is an exact clone of the $Z X$ Spectrum ROM `series generator` Z80 assembler subroutine.
zx.getcoeffs ()
The function returns the current Chebyshev coefficient vectors for various package functions. The return is a dictionary of four numeric sequences:

| Key | Used by | Indirectly used by | Default size |
| :--- | :--- | :--- | :--- |
| 'SIN' $^{\prime}$ | zx.SIN | zx.COS and zx.TAN | 6 |
| 'ATN' $^{\prime}$ | zx.ATN | zx.ACS and $\mathbf{\text { zx.ASN }}$ | 12 |
| 'LN' $^{\prime}$ | zx.LN | zx.SQR and zx.POW | 12 |
| 'EXP' $^{\prime}$ | zx.EXP | zx.SQR and $\mathbf{z x . P O W ~}$ | 8 |

See also: zx.setcoeffs.

```
zx.setcoeffs (n, s)
```

Globally sets Chebyshev coefficients to the package's environment. You can change existing coefficients, reduce or enlarge their respective number down to one or up to 256 values. Internally, the coefficients are treated as $C$ doubles, the shipped defaults have the precision of C floats.

The first argument n must be the string 'Sin', 'ATn', 'Ln', or 'exp'. The second argument s must be a sequence of one to 256 numbers.

For the meanings of the first argument, see $\mathbf{z x}$.getcoeffs.
Please note that the respective zx functions must be called with the last argument true in order to revert to the (changed) coefficient vectors as they use hard-wired expanded polynomials by default.

See also: $\mathbf{z x}$.getcoeffs.
zx.reduce (x)
Reduces a number $x$ to another number $v$ in the range $[-1,1]$ where $\sin (v)=\sin (\pi$ $* v / 2$ ) for multiples or fractions of $\pi$, and returns $v$. Please note that even if $x \in[-1,1]$, $v$ will be calculated - see inrange for range checks.

The function imitates the ZX Spectrum ROM 'reduce argument' Z80 assembler subroutine which is used to prepare calls to ZX Spectrum's sine and cosine subroutines. Example:

```
> zxsin := proc(x) is
> local w, z;
> w := zx.reduce(x);
> z := 2 * w**2 - 1;
> return w * zx.genseries(z, zx.getcoeffs().SIN)
> end;
> zxCos := << x -> zxsin(x + Pi/2) >>;
```

See also: math.wrap, end of Chapter 11.1.2 for a comparison chart.

### 11.12 calc - Calculus Package

This package contains mathematical routines to perform basic calculus numerically. Since the functions do not work symbolically, please beware of round-off errors. As a plus package, it is not part of the standard distribution and must be activated with the import statement, e.g. import calc.

A typical example might look like this:

```
> import calc;
```

Define a function $\mathrm{f}:=\mathrm{x} \rightarrow \sin (\mathrm{x})$ :

```
> f := << x -> sin(x) >>
```

Determine all its zeros over $[-5,5]$ :

```
> calc.zeros(f, -5, 5):
seq(-3.1415926535898, 0, 3.1415926535898)
```

Differentiate it at point 0 and also return an error estimate:

```
> calc.diff(f, 0):
```

$0.99999999999963 \quad 1.8503717573394 \mathrm{e}-010$

Compare it:

```
> cos(0):
```

1

Integrate it over $[0, \pi]$ :

```
> calc.gtrap(f, 0, Pi):
1.9999999938721
```

Summary of functions:
Basic Calculus:
calc.aitken, calc.fminbr, calc.fmings, calc.iscont, calc.limit, calc.regulafalsi, calc.sections, calc.zeroin, calc.zeros.

Differentiation:
calc.diff, calc.eulerdiff, calc.isdiff, calc.maximum, calc.minimum, calc.xpdiff.

## Integration:

calc.gauleg, calc.gtrap, calc.intde, calc.intdei, calc.intdeo, calc.integ, calc.simaptive.

Integrals:
calc.Ci, calc.Chi, calc.dawson, calc.Ei, calc.En, calc.fresnelc, calc.fresnels, calc.ibeta, calc.igamma, calc.igammc, calc.invibeta, calc.scaleddawson, calc.Shi, calc.Si, calc.Ssi, calc.w.

Sums \& Products:
calc.prod, calc.fsum.
Interpolation:
calc.cheby, calc.chebyt, calc.chebycoeffs, calc.clampedspline, calc.clampedsplinecoeffs, calc.interp, calc.linterp, calc.nakspline, calc.naksplinecoeffs, calc.neville, calc.newtoncoeffs, calc.polyfit, calc.polygen, calc.savgol, calc.savgolcoeffs, calc.smoothstep.

## Distances

calc.arclen, calc.eucliddist, calc.sinuosity.

## Miscellaneous:

calc.Ai, calc.Bi, calc.bernoulli, calc.dilog, calc.euler, calc.gaussian, calc.lambda, calc.polylog, calc.Psi, calc.weier, calc.zeta.

The functions:

```
calc.Ai (x)
```

The Airy wave function returns both the first independent solution to the differential equation $y^{\prime \prime}(x)=x^{*} y$ and its first derivative, for any real $x$.

See also: calc.Bi.
calc.aitken (f, x0 [, eps [, iter]])
The function finds the limit of the sequence $x_{n+1}=f\left(X_{n}\right)$ with initial $x_{0}$ and tolerance eps, with a maximum of iter iterations, using Aitken extrapolation. f is a univariate function. eps by default is DoubleEps and iter is 20.

It returns either the approximated limit $a$ and the first derivative at $a, \mathrm{f}^{\prime}(a)$, if successful, and undefined twice otherwise. The third return is the number of iterations taken to compute the result.

Example: calc.aitken $\left(\ll x->1 / 2^{*}(x+2 / x) \gg, 1\right) \sim=\operatorname{sqrt}(2)$.
See also: times.
calc.arclen (f, a, b)
The function returns the arc length (curvilinear length) of a function f in one real between the points a and b.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.eucliddist, calc.sinuosity.
calc.bernoulli (n [, eps])
Computes the n -th Bernoulli number Bn and returns a number. n should be a non-negative integer. eps is an internal bailout value and by default equals DoubleEps.

See also: calc.euler.
calc.Bi (x)
The Airy wave function returns both the second independent solution to the differential equation $y^{\prime \prime}(x)=x^{\star} y$ and its first derivative, for any real $x$.

See also: calc.Ai.
calc.Ci (x)
Computes the cosine integral and returns it as a number. x must be a number.
See also: calc.Si, calc.Chi, calc.Shi, calc.Ssi.

```
calc.cheby (f, a, b, n [, \cdots.] [, option])
```

Returns a function computing the Chebyshev interpolant for a given point. f is the univariate or multivariate function to be interpolated, a and b represent the domain of the definition, n is the order of the interpolant. As a rule of thumb, the wider the domain, the larger $n$ should be. If $f$ has more than one argument, then all arguments except the first are passed right after $n$.

You may optionally pass the deriv=k option as the very last argument to compute either the first $(k=1)$, second $(k=2)$, third $(k=3)$, fourth $(k=4)$ or fifth $(k=5)$ derivative, where $k$ defaults to 0 , i.e. the function itself.

Using this function may speed up numeric computations significantly if the expression to be evaluated consists of many subexpressions - and if accuracy is not of primary concern. When computing derivatives, it is 10 times faster than calc.xpdiff and - depending on the expression type-also more accurate.

## Example:

```
> # get derivative of ln(x), i.e. 1/x
> g := calc.cheby(<< x -> ln x >>, 1, 10, 50, deriv = 1);
> g(5):
0.20000000000002
```

See also: calc.chebycoeffs, calc.diff, calc.savgol, calc.xpdiff.

```
calc.chebycoeffs (f, a, b, n)
```

Computes Chebyshev interpolation coefficients used internally by calc.cheby. f is a univariate function for which coefficients shall be computed, a and b represent the domain of the definition, n is the order of the interpolant.

The return is a table of the Chebyshev coefficients, indexed from 1 to $n$, with key 'domain' representing the domain a:b (a pair). As a rule of thumb, the larger the domain, the larger n should be. See also: calc.savgolcoeffs.

```
calc.chebyt (n, x)
```

Computes the $n$-th Chebyshev polynomial of the first kind, evaluated at $x$, with $n a$ non-negative integer and x a number. The return is equal to $\cos (\mathrm{n} * \arccos (\mathrm{x}))$.

```
calc.Chi (x)
```

Computes the hyperbolic cosine integral and returns it as a number. x must be a number.

See also: calc.Si, calc.Ci, calc.Shi, calc.Ssi.

```
calc.clampedspline (obj, da:db)
calc.clampedspline (obj, da:db, a)
calc.clampedspline (obj, da:db, a, coeffs)
```

Evaluates the clamped cubic spline for a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$, at a single value a (a number) of the independent variable x.

The boundary conditions are passed as a pair of numbers da:db, where da is the derivative of the function at the left border, and db is the derivative of the function at the right border.

In the first form, returns a univariate function which can be called with a number to obtain the value of the interpolating polynomial. For best performance, use this first form.

In the second form, the function computes the coefficients of the linear, quadratic, and cubic terms itself in each call.

In the third form, the function expects the coefficients coeffs of the linear, quadratic, and cubic terms as a sequence of three sequences, in this order, and each containing numbers. The fourth argument may be obtained by calling calc.clampedsplinecoeffs.

In the second and third form, the function returns the value of the interpolating polynomial, a number, at the specified value a of the independent variable $x$.

In general, the function returns fail if the structure contains less than two pairs.
See also: calc.interp, calc.clampedsplinecoeffs, calc.nakspline, calc.neville.

```
calc.clampedsplinecoeffs (obj, da:db)
```

Determines the coefficients for the clamped cubic spline for a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$. The return can be used to speed up execution of calc.clampedspline.

The boundary conditions are passed as a pair of numbers da:db, where da is the derivative of the function at the left border, and db is the derivative of the function at the right border.

The function returns fail if the structure less than two pairs.
See also: calc.clampedspline.
calc.curvature (f, x [, ...])
Determines the curvature of a real univariate or multivariate function at a given point. Curvature in this context is defined as the rate of change of direction of a point that moves on a curve. The result is the number $\mathrm{f}^{\prime \prime}(\mathrm{x}, \cdots) /\left(1+\mathrm{f}^{\prime}(\mathrm{x}, \cdots)^{2}\right)^{3 / 2}$.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.sinuosity.

```
calc.dawson (x)
```

Computes Dawson's integral for a number x . The return is the number

$$
e^{-x^{2}} \int_{0}^{x} e^{t^{2}} d t
$$

See also: calc.scaleddawson, expx2.

```
calc.diff (f, x [, \cdots.] [, options])
```

Computes the value of the first derivative of a function f at a point x , and also returns the absolute error as a second return.

If the option deriv=$n$ is given, where n may be 1,2 , or 3 , the n -th derivative is calculated, with $n=1$ the default. If $n=0$, then the function value at $f(x)$ is determined.

If the eps=h option is given, the epsilon value h (a positive number preferably close to zero) is used to determine the difference quotient; otherwise it is automatically determined by calling math.epsilon with x .

If the absolute error is quite large, it may either indicate non-differentiability of f at x , ... , or that the derivative could not be computed with sufficient precision.

The algorithm is based on Conte and de Boor's `Coefficients of Newton form of polynomial of degree \(3^{`}\), and computes symmetric difference quotients.

See also: calc.cheby, calc.differ, calc.isdiff, calc.eulerdiff, calc.xpdiff.

```
calc.differ (f, x [, ...] [, options])
```

Computes the derivative of a univariate or multivariate function f at point x ( $a$ number). The second, etc. arguments to f may be given right after argument x .

If the option deriv $=\mathrm{n}$ is given, where n may be 1,2 , or 3 , the n -th derivative is calculated, with $n=1$ the default. If $n=0$, then the function value at $f(x)$ is determined.

If the eps $=\mathrm{h}$ option is given, the epsilon value h (a positive number preferably close to zero) is used to determine the difference quotient; otherwise it is automatically determined by calling math.epsilon for $x$.

This function actually is just a simple wrapper to calc.eulerdiff if deriv=1 or no deriv option has been given, and to calc.xpdiff otherwise, thus automatically choosing the best method to compute the derivative.

The function is implemented in Agena and included in the lib/calc.agn file.

```
calc.dilog (x)
```

Computes the dilogarithm (Spence's) function for a number $x$. The return is the number

$$
\mathrm{Li}_{2}(\mathrm{x})=\sum_{\mathrm{k}=1}^{\infty} \frac{\mathrm{z}^{\mathrm{k}}}{\mathrm{k}^{2}}
$$

See also: calc.polylog.
calc.Ei (x)
Computes the exponential integral

$$
\mathrm{Ei}(\mathrm{x})=-\int_{-x}^{\infty} \frac{\mathrm{e}^{-t}}{\dagger} d t
$$

for a number $x$. The return is a number ${ }^{20}$, and undefined if $x=0$.

```
calc.En (n, x)
```

Evaluates the exponential integral

$$
E_{n}(x)=-\int_{1}^{\infty} \frac{e^{-x t}}{t^{n}} d t
$$

for non-negative $n$ (an integer) and real x . The return is a number.

```
calc.eucliddist (f, a, b [, ...])
```

Computes the Euclidian distance, i.e. the straight-line distance, of two points (a, $f(a)$ ) and ( $b, f(b)$ ) on a curve defined by a function $f$ in one real, in the Euclidean plane. $a, b$ must be numbers. If $f$ is multivariate, its second, third, etc. argument are passed after b.

See also: |- operator, hypot, calc.sinuosity.
calc.euler ( n [, eps])
Computes the n -th Euler number En and returns a number. n should be a non-negative integer. eps is an internal bailout value and by default equals DoubleEps.

See also: calc.bernoulli.

[^1]```
calc.eulerdiff (f, x [, \cdots.]] [, option])
```

Computes the first (second, third, see below) derivative of the univariate or multivariate function f at real point x , a number.

If the option eps $=\mathrm{h}$ is given, the epsilon value h (a positive number preferably close to zero) is used internally for the computation, its default is math.epsilon(x).

The second, etc. arguments to $£$ may be given right after argument $x$.
The return is the imaginary part of $f(x+\mid * h) / h$, or fail if $f$ did not evaluate to the complex plane. The function does not check whether f is differentiable at $\mathrm{x}, \ldots$, you may call calc.isdiff before.

If the deriv=2 option is passed, then the second derivative is determined, deriv=3 computes the third derivative. The quality of the second and third derivatives are close to, but not as good as, the one of calc.xpdiff. (The first derivatives of eulerdiff are still better than those of xpdiff.)

This function as at least three times faster than calc.xpdiff. See also: calc.diff.
The idea has been taken from the Euler Math Toolbox, thus its name.
See also: calc.differ, calc.diff, calc.xpdiff.

```
calc.fminbr (f, a, b [, tol])
```

Estimates the minimum location of a univariate function $£$ through one-dimensional search over a given range [a, b], with $a, b$ numbers, using Golden section search combined with parabolic interpolation. The acceptable tolerance tol defaults to Eps. Returns the abscissa (x-axis) value where a minimum has been found, a number.

If there are multiple minima in the range, the function returns an arbitrary one. This function is rather basic, see calc.minimum and calc.maximum for alternatives.

See also: calc.fmings.

```
calc.fmings (f, a, b [, tol])
```

Like calc.fminbr, but performs Golden section search only.
Given $a$ function $f$ with $a$ single local minimum in the interval [a, b], with $a, b$ numbers, returns the abscissa value (x-axis) where a minimum has been found. The acceptable tolerance tol defaults to DoubleEps.

```
calc.fprod (f, a, b)
```

Computes the product of $f(a), \cdots, f(b)$, with $f$ a function, $a$ and $b$ numbers. If $a>b$, then the result is 1 .

See also: calc.fsum.
calc.fresnelc (x)
Computes the Fresnel integral $C(x)=\int_{0}^{x} \cos \left(\frac{\pi}{2} t^{2}\right) d t$ and returns it as a number.

```
calc.fresnels (x)
```

Computes the Fresnel integral $S(x)=\int_{0}^{x} \sin \left(\frac{\pi}{2} t^{2}\right) d t$ and returns it as a number.

```
calc.fsum (f, a, b [, ...])
```

Computes the sum of $f(a), \cdots, f(b)$, with $£$ a function, $a$ and $b$ numbers. If $£$ requires two or more arguments, the second, third, etc. argument must be passed after b. If a $>\mathrm{b}$, then the result is 0 . The function uses Kahan-Babuška round-off error prevention. Examples:

```
> calc.fsum(<< n, x -> (x**n)/fact(n) >>, 0, 100, 1):
2.718281828459
> calc.fsum(<< x, n -> ( }\mp@subsup{\textrm{x}}{}{**}\textrm{n})/\operatorname{fact}(\textrm{n})>>, 0, 100, 1)
5050
```

See also: qsumup, sumup, calc.fprod, stats.cumsum, stats.fsum.
calc.gauleg (f, a , b [, n, [, eps]])
Performs Gauss-Legendre integration of a real univariate function $f$ over the interval a .. b with n sample points over the whole range, and precision eps. n defaults to 50 and eps to DoubleEps. It is seven times faster than calc.integ with similar precision.
calc.gaussian (x [, a [, b [, c]]])
Computes the Gaussian function $\frac{a}{2 c^{2}} e^{-(x-b)^{\wedge} 2}$ at a real or complex point $x$, with $a$, $b, c$ being (real) numbers. By default, $a=1, b=0, c=\frac{1}{\sqrt{2}}$. The return depends on the type of $x$.

See also: expx2.
calc.gd (x)
Computes Gudermannian function for any number or complex number x, i.e.

$$
\operatorname{gd}(x)=\int_{t=0}^{x} \frac{1}{\cosh (t)} d t=\arctan (\sinh (x)) .
$$

The type of return depends on $x$.
Wikipedia: `The Gudermann function relates circular functions and hyperbolic functions without explicitly using complex numbers.' The function is written in the Agena language.

See also: calc.logistic, calc.sigmoid.

```
calc.gtrap (f, a, b [, eps])
```

Integrates the function $f$ on the interval $[a, b]$ using a bisection method based on the trapezoid rule and returns a number. By default the function quits after an accuracy of eps $=$ Eps has been reached. You may pass another numeric value for eps if necessary.

See also: calc.intde, calc.intdei, calc.intdeo, calc.integ, calc.simaptive.
calc.ibeta (x, a, b)
Evaluates the incomplete beta integral defined by

$$
\frac{\Gamma(a+b)}{\Gamma(a) \Gamma(b)} \int_{0}^{x} f^{a-1}(1-t)^{b-1} d t
$$

from 0 to $x$. Both a and $x$ must be positive numbers. See also: calc.invibeta.

```
calc.igamma (x, a)
```

Evaluates the incomplete gamma integral defined by

$$
\frac{1}{\Gamma(a)} \int_{0}^{x} e^{-t} t^{a-1} d t
$$

Both a and x must be positive numbers. See also: calc.igammac.
calc.igammac ( $x, a$ )
Evaluates the complemented incomplete gamma integral defined by

$$
\frac{1}{\Gamma(a)} \int_{x}^{\infty} e^{-t} t^{a-1} d t
$$

Both a and x must be positive numbers. See also: calc.igamma.
calc.intde (f, a, b [, eps])
Integrates the function $f$ on the interval $[a, b]$, with a and $b$ numbers, using Double Exponential (DE) Transformation, also known as Tanh-sinh quadrature.
f needs to be analytic over [a, b]. eps is the relative error requested excluding cancellation of significant digits, and by default is equal to le-15. Specifically, eps means: (absolute error) / ( $\int_{a}^{b} f(x) \mid d x$ ).
The return is 1) the approximation to the integral, or fail if evaluation failed, and 2) an estimate err of the absolute error, where

- err $\geq 0$ : normal termination,
- err < 0: abnormal termination, i.e. an convergent error has been detected: 1) $f(x)$ or $\frac{d}{d x}^{n} f(x)$ has discontinuous points or sharp peaks over $[a, b]$ (you must divide the interval $[a, b]$ at these points). 2) The relative error of $f(x)$ is greater than eps. 3) $f(x)$ has an oscillatory factor and the frequency of the oscillation is very high.

This function is four times faster than calc.gtrap and also much more accurate. It can be applied on any polynomial, exponential or trigonometric function, logarithm, power function, and most special functions.

See also: calc.gauleg, calc.gtrap, calc.intdei, calc.intdeo, calc.integ, calc.simaptive.

```
calc.intdei (f, a, [, eps])
```

Integrates the non-oscillatory function f on the interval $[\mathrm{a}, \infty]$, with a a number, using Double Exponential (DE) Transformation, also known as Tanh-sinh quadrature.
f needs to be analytic over $[a, \infty]$. eps is the relative error requested excluding cancellation of significant digits, and by default is equal to le-15. Specifically, eps means: (absolute error) / ( $\left.\int_{a}^{b} f(x) \mid d x\right)$.

The return is either the approximation to the integral, or fail if evaluation failed, and an estimate err of the absolute error. For further information see calc.intde.

See also: calc.gtrap, calc.intde, calc.integ, calc.simaptive.
calc.intdeo (f, a, [, omega [, eps])
Integrates the oscillatory function $f$ on the interval $[a, \infty]$, with a a number, using Double Exponential (DE) Transformation, also known as Tanh-sinh quadrature.
f needs to be analytic over $[a, \infty]$. omega is the oscillatory factor of f and by default is 1 . eps is the relative error requested excluding cancellation of significant digits, and by default is equal to le-15. Specifically, eps means: (absolute error)/( $\int_{a}^{b} f(x) \mid d x$ ). The return is either the approximation to the integral, or fail if evaluation failed, and an estimate err of the absolute error. For further information see calc.intde.

See also: calc.gtrap, calc.intde, calc.intdei, calc.integ, calc.simaptive.
calc.integ (f, a, b [, omega [, eps [, n]]])
This function is a wrapper around calc.intde, calc.intdei, and calc.intdeo. If eps is not given, it is le-15 by default. If omega is not given, it is 1 . The return is the integral value and the error margin, both are numbers.

If b is not infinity, the function calls calc.intde and returns its results.
If b is infinity, the function first calls calc.intdei and returns its results, if intdei does not evaluate to fail. Otherwise, calc.intdeo is called.

If the function should internally switch to another algorithm in order to compute a result successfully, n denotes the number of sample points to evaluate. n by default is set to $(b-a)^{*} 20$, i.e. 20 samples per unit.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.gauleg, calc.gtrap, calc.intde, calc.intdei, calc.intdeo, calc.simaptive.

```
calc.interp (obj)
calc.interp (obj, a)
calc.interp (obj, a, coeffs)
```

In the first form, computes a Newton interpolating polynomial and returns it as a univariate function. The interpolation points are passed in a table obj, with each point being represented by the pair $\mathrm{x}_{k}: \mathrm{y}_{\mathrm{k}}$.

Example:

```
> f := calc.interp([ 0:0, 1:3, 2:1, 3:3 ]);
```

Call fat point 10 :

```
> f(10):
85
```

In the second and third form, it evaluates the Newton form of the polynomial which interpolates a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$, at a single value a (a number) of the independent variable.

In the second form, the function computes the coefficients automatically in each call, which slows down this variant.

In the third form, by passing a sequence coeffs of coefficients (numbers), the function uses the coefficients passed, avoiding their (re-)computation. The third argument may be obtained by calling calc.newtoncoeffs.

Both in second and third form, the function returns the value of the interpolating polynomial, a number, at the specified value a of the independent variable. It is advised to use the first form to benefit from maximum speed.

Example:

```
> calc.interp([ 0:0, 1:3, 2:1, 3:3 ], 10):
88
```

See also: calc.cheby, calc.clampedspline, calc.linterp, calc.nakspline, calc.neville, calc.newtoncoeffs, calc.polyfit, calc.savgol.
calc.invibeta (y, a, b)
Evaluates the inverse of the incomplete beta integral such that

$$
y=\text { calc.ibeta(x, a, b). }
$$

See also: calc.ibeta.
calc.iscont (f, x [, ‥] [, option])
The function returns true if a real function f is continuous at the given point, and false otherwise. If $f$ requires only one argument, $x$ is a number. If $f$ requires two or more arguments, the second, third, etc. argument of f must be passed right after x.

If the option eps $=\mathrm{h}$ is given as the last argument, the epsilon value h (a positive number preferably close to zero) is used for the approximate equality check with the left and right limit; otherwise it is automatically determined by calling math.eps with x and any option given. See calc.limit for an example.

See also: calc.isdiff.

```
calc.isdiff (f, x [, \cdots.] [, option])
```

The function returns true if a real function f is differentiable at the given point x , of type number, and false otherwise. If $£$ requires two or more arguments, the second, third, etc. argument (all of type number) - of f must be passed right after x .

If the option eps $=\mathrm{h}$ is given as the last argument, the epsilon value h (a positive number preferably close to zero) is used for the approximate equality check with the left and right limit; otherwise it is automatically determined by calling math.epsilon(x). See calc.limit for an example.

A function is differentiable at $x, \ldots$ if it is continuous at $x$ and if the left- and rightsided difference quotients are equal.

See also: calc.diff, calc.iscont, calc.xpdiff.
calc.lambda (v, x [, eps])
Computes the Lambda function and its derivative of (positive) integral order v for argument x :

$$
\begin{gathered}
\Lambda_{v}(x)=2^{v} \Gamma(v+1) \\
\Lambda_{v}^{\prime}(x)=\frac{2 v}{x}\left(\Lambda_{v-1}(x)-\Lambda_{v}(x)\right)
\end{gathered}
$$

$\Gamma$ is the Gamma function, and $J_{v}$ is the Bessel function of the first kind (Agena function besselj). The function also returns the actual order processed, which may differ from the input v . eps is a bailout value and by default is DoubleEps.
calc.limit (f, x [, $\cdot \cdot]$ [, options])
The function returns the limit, a number, of a real function f at the given point x ( $a$ number). If the limit does not exist, undefined will be returned.

If f is multivariate, the second, third, etc. argument of f must be passed right after $x$.

Options may be given as the very last arguments, their order does not matter.

If the eps=h option is given, the epsilon value h (a positive number preferably close to zero) is used for the approximate equality check of the left and right limit; otherwise it is automatically determined by calling math.eps with x and any option.

If the side='left' option is given, the left-sided limit is determined. If the side='right' option is given, the right-sided limit is determined. If the side='both' option is given, the left and right-sided limit, in this order, will be returned. If the side='all' option is given, the limit, the left-sided, and the right-sided limit will be returned, in this order.

For example, if the function is $f(x, y):=|x|+y$, with $x=1, y=3$, and eps $=1 e-4$, the call for the left-sided limit would be:

```
> calc.limit(<< x, y -> abs(x) + y >>, 0, 3, eps = 1e-4, side='left'):
3
```

calc.linterp (obj)

Returns a function that conducts a Lagrange interpolation for a given sequence or table obj of numeric pairs $x: y$ where $x$ and $y$ denote a point in the plane. It is often said that Lagrange interpolation is suited for theoretical purposes only, since it is rather slow.

See also: calc.interp, calc.polyfit.
calc.logistic (x [, max [, k [, x0]]])
Computes the logistic function, having a characteristic `S`-shaped curve or sigmoid curve, for any number $x$, according to the formula

$$
L(x)=\frac{m a x}{1+e^{-k\left(x-x_{0}\right)}},
$$

where max is the curve's maximum value, k its steepness, and x 0 the x -value of the sigmoid's midpoint. By default, max $=1, k=1$, and $\times 0=0$, computing the sigmoid function. If only $x$ is given, it works like calc.sigmoid.

The result is a number between - but excluding - 0 and max.
See also: calc.gd, calc.logit, calc.sigmoid.
calc.logit (x)
Computes the inverse sigmoid or logistic function according to the formula

$$
\operatorname{logit}(x)=\frac{\ln (x)}{\ln (1+x)}=2 \operatorname{arctanh}(2 x-1)
$$

If $x=0$, the function will return -infinity, and if $x=1$ the result will be +infinity.
See also: calc.logistic, calc.probit, calc.sigmoid.

```
calc.maximum (f, a, b, [step [, eps]])
```

Returns all possible maximum locations of the univariate function f on the interval [a, b]. The function divides the interval [a, b] into smaller intervals [a, a+step], [a+step, $a+2{ }^{*}$ step], $\cdots$, [b-step, b], with step $=0.1$ if step is not given. It then looks for possible maximum locations $x$ in these smaller intervals and checks whether the first derivative of f at x is 0 .
f must be differentiable on $[a, b]$. The procedure returns two sequences.
The accuracy of the procedure is determined by eps, with eps = Eps as a default. If a possible extreme location x matches the condition $\mathrm{f}^{\prime}(\mathrm{x})=0$ with this accuracy, it is included in the first sequence that the procedure returns. If the test fails and eps $\leq$ Eps, then an accuracy of le-5 is used for a second test. If it succeeds, x is included into both the first and the second sequence, indicating to the user that the first test failed.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.fminbr, calc.fmings, calc.minimum.

```
calc.minimum (f, a, b, [step [, eps]])
```

Returns all possible minimum locations of the univariate function $f$ on the interval [a, b]. The function divides the interval $[a, b]$ into smaller intervals $[a, a+s t e p],[a+s t e p$, $\mathrm{a}+2^{*}$ step], $\cdots,[b-$ step, b], with step $=0.1$ if step is not given. It then looks for possible minimum locations x in these smaller intervals and checks whether the first derivative of f at x is 0 .
£ must be differentiable on [a, b]. The procedure returns two sequences.
The accuracy of the procedure is determined by eps, with eps = Eps as a default. If a possible extreme location $\times$ matches the condition $\mathrm{f}^{\prime}(\mathrm{x})=0$ with this accuracy, it is included in the first sequence that the procedure returns. If the test fails and eps $\leq$ Eps, then an accuracy of le-5 is used for a second test. If it succeeds, x is included into both the first and the second sequence, indicating to the user that the first test failed.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.fminbr, calc.fmings, calc.maximum.

```
calc.nakspline (obj)
calc.nakspline (obj, a)
calc.nakspline (obj, a, coeffs)
```

Evaluates the `not-a-knot` cubic spline for a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$, at a single value a (a number) of the independent variable.

In the first form, returns a univariate function which can be called with a number to obtain the value of the interpolating polynomial. This is the recommended usage due to its run-time behaviour.

In the second form, the function computes the coefficients of the linear, quadratic, and cubic terms itself in each call.

In the third form, the function expects the coefficients coeffs of the linear, quadratic, and cubic terms as a sequence of three sequences, in this order, and each containing numbers. The third argument may be obtained by calling calc.naksplinecoeffs.

In the second and third form, the function returns the value of the interpolating polynomial, a number, at the specified value a of the independent variable.

In general, the function returns fail if the structure contains less than four pairs.
See also: calc.clampedspline, calc.interp, calc.naksplinecoeffs, calc.neville.

```
calc.naksplinecoeffs (obj)
```

Determines the coefficients for the `not-a-knot cubic spline for a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$. The return can be used to speed up execution of calc.nakspline.

The function returns fail if the structure contains less than four pairs.
See also: calc.nakspline.

```
calc.neville (obj)
calc.neville (obj, a)
```

In the first form, returns a function that conducts an Aitken-Neville interpolation for a given sequence or table obj of numeric pairs $x_{k}: y_{k}$ where $x_{k}$ and $y_{k}$ denote a point in the plane.

In the second form, evaluates the polynomial which interpolates a given sequence or table obj of points represented by pairs of the form $x_{k}: y_{k}$ at $a$ single value a ( $a$ number) of the independent variable, using Aitken-Neville interpolation, and returns a number.

Example:

```
> calc.neville([1:1, 2:2, 3:3], 2):
2
```

See also: calc.clampedspline, calc.interp, calc.nakspline.

```
calc.newtoncoeffs (obj)
```

Returns a sequence of the coefficients of type number of the Newton form of the polynomial which interpolates a given table or sequence obj of pairs representing the points $x_{k}: y_{k}$. The return can be used to speed up execution of calc.interp.

See also: calc.interp.

```
calc.polyfit (obj, n)
```

For an $n$-th-degree polynomial of a sample of Cartesian pairs $x_{k}: y_{k}$, returns $a$ sequence of coefficients of descending degree, using polynomial regression. $x_{k}, y_{k}$ are numbers and degree $n$ must be a positive integer. Example:

```
> coeffs := calc.polyfit(seq( 1:0, 2:3, 3:1 ), 2):
seq(-2.5, 10.5, -8.0000000000001)
```

The return may be passed to calc.polygen to generate a polynomial function, e.g.:

```
> p := calc.polygen(coeffs);
```

There is no limit on the degree, but a degree of 7 or more is not regarded appropriate.

The function tries to reproduce polynomial trend lines known from spreadsheet applications and internally uses Kahan-Ozawa-Summation for better accuracy.

See also: calc.interp, calc.linterp, calc.polygen.


```
calc.polygen (obj)
```

 coefficients $c_{n}, c_{n-1}, \cdots, c_{2}, c_{1}$ and returns it as a new function $\ll x->p(x) \gg$, where $x$ and the return $p(x)$ represent numbers. You may alternatively pass the coefficients in a table, sequence or register obj.

The function internally uses 80-bit precision floats.
Example: The Taylor series expansion of the sine function, with order 8, is:

$$
\sin (x)=x-\frac{1}{3!} x^{3}+\frac{1}{5!} x^{5}-\frac{1}{7!} x^{7}+\ldots
$$

So the coefficients in descending [sic !] order are:

```
> coeffs := [1, 0, -1/fact(3), 0, +1/fact(5), 0, -1/fact(7)];
```

This generates the function:

```
> taylorsine := calc.polygen(coeffs);
> taylorsine(1), sin(1):
0.84146825396825 0.8414709848079
```

See also: calc.polyfit.

```
calc.polylog (n, x)
```

Returns the polylogarithm of order $n$ (an integer greater or equals -1 ) at a real point x . The return is a number, or fail if $\mathrm{n}<-1$ for this situation is not implemented. The polylogarithm of order $n$ is defined by the series:

$$
\operatorname{Lin}_{n}(x)=\sum_{k=1}^{\infty} \frac{x^{k}}{k^{n}}
$$

See also: calc.dilog.

## calc.probit (x)

Computes the inverse of the cumulative distribution function of the standard normal distribution:

$$
\operatorname{probit}(x)=\sqrt{2} \operatorname{erf}^{-1}(2 x-1) .
$$

If $x=0$, the function will return -infinity, and if $x=1$ the result will be + infinity.
See also: calc.logit,inverf.
calc.Psi (x)
Computes the Psi (digamma) function, the logarithmic derivative of the gamma function, for a number x . The return is the number calc.xpdiff(Ingamma(x), x).

## See also: gamma, Ingamma.

```
calc.regulafalsi (f, a, b [, eps])
```

Tries to determine the root of the univariate function f in the borders a and b and returns it as a number if successful, and null otherwise.

The precision eps by default is Eps.
See also: calc.zeroin, calc.zeros.
calc.savgol (f [, options])
Computes a Savitzky-Golay filter for the univariate function f to `smooth` its data by returning a factory interpolating f at a given point $\mathrm{x}_{0}$. preventing large oscillations between sample points.

It fits successive subsets of neighbouring data with a low-degree polynomial using the linear least-square method. By default, 15 equally-spaced points to the left of $x_{0}$ and 15 equally-spaced points to the right of $x_{0}$ are examined.

You can change this 'window' by passing another odd value with the 'points' option. All adjacent points are separated by distance eps which is le-5 by default. You can change the distance with the 'eps' option, e.g. eps=0.1 which unless you want to compute a derivative, see below, might be a much more useful value.

Alternatively it can also compute derivatives of any degree $n$ by passing the option deriv=n. The larger the degree $n$ of the derivative, however, the less accurate the results will become.

The degree d of the smoothing least-square polynomial is 3 by default and can be changed by the degree $=d$ option. Recommended degrees are $d=2$ or 4 , with $d$ not exceeding 6.

The function automatically determines the most suitable settings for the window and the spacing eps of its points, but you can switch this off by passing the adaptive=false Option (default is adaptive=true).

Example: Compute the first, second and third derivative of $\sin (x)$ and evaluate at $x=$ $\frac{\pi}{2}$ :

```
> import calc
> f := << x -> sin x >>
> f' := calc.savgol(f, deriv = 1)
> f'' := calc.savgol(f, deriv = 2)
> f''' := calc.savgol(f, deriv = 3)
```

```
> f(Pi/2), f'(Pi/2), f''(Pi/2), f'''(Pi/2):
1 -6.3527471044073e-017 -1.0000000010326 4.3874822912549e-007
```

See also: calc.cheby, calc.interp, calc.savgolcoeffs.

```
calc.savgolcoeffs (nleft, nright, deriv, polydeg)
```

Returns the normalised Savitzky-Golay filter coefficients as a register. nleft is the number of leftward observations to be examined, while nright is the number of rightward ones.
deriv is the order of the derivative desired ( 0 for the smoothed function, 1 for the first derivative, asf.).
polydeg is the order of the smoothing polynomial, with 2 or 4 being recommended values, but not exceeding 6 .

See also: calc.chebycoeffs, calc.savgol.
calc.scaleddawson (x)
Implements the Scaled Dawson Integral w_im( x ) $=$ 2*calc.dawson( x$) /$ sqrt(Pi) for real x.

See also: calc.dawson, calc.w.
calc.sections (f, $a, b$, step)
Returns all intervals where a function has a change in sign. f must be a function, a the left border of the main interval, b its right border, and step the step size. The return is a sequence of pairs denoting the found subintervals. The function uses Adapted Neumaier summation to prevent round-off errors, the same used by numeric for loops with fractional step sizes.

See also: calc.zeros.
calc.Shi (x)
Computes the hyperbolic sine integral and returns it as the number

$$
\operatorname{Shi}(x)=\int_{0}^{x} \frac{\sinh t}{t} d t
$$

x must be a number.
See also: calc.Ci, calc.Chi, calc.Si, calc.Ssi.
calc.Si (x)
Computes the sine integral

$$
\operatorname{Si}(x)=\int_{t=0}^{x} \frac{\sin (t)}{t} d t=\int_{t=0}^{x} \operatorname{sinc}(t) d t
$$

and returns it as a number. x must be a number.
See also: calc.Ci, calc.Chi, calc.Shi, calc.Ssi, sinc.

```
calc.sigmoid (x)
```

Computes the sigmoid, i.e. standard logistic, function,

$$
S(x)=\frac{1}{1+e^{-x}}
$$

having a characteristic `S`-shaped curve or sigmoid curve, for any number x. The result is a number between - but excluding - 0 and 1 .

See also: calc.gd, calc.logistic, calc.logit.

```
calc.simaptive (f, a, b [, h_min [, eps]])
```

Integrates the function $f$ on the interval $[a, b]$ using Simpson-Simpson Adaptive Quadrature and returns a number. The function returns fail, if no suitable subinterval of length greater than min_h could be found for which the estimated error falls below eps.

The function is thrice as fast as calc.integ, but is not suited with singularities at or within the borders.

By default, h_min is 1e-7, and eps is Eps/2, where Eps is the global system variable Eps.

See also: calc.gauleg, calc.gtrap, calc.intde, calc.intdei, calc.intdeo, calc.integ.

```
calc.sinuosity (f, a, b)
```

Computes the ratio of the curvilinear length (along the curve) and the Euclidean distance (straight line) between the end points a and $b$, of the curve defined by a function f in one real. $\mathrm{a}, \mathrm{b}$ must be numbers.
sinuosity does not check whether f has an inflection point in the given range $[\mathrm{a}, \mathrm{b}]$. The function is implemented in Agena and included in the lib/calc.agn file.

See also: calc.arclen, calc.curvature, calc.eucliddist.

```
calc.smoothstep (x, n)
calc.smoothstep (x, 'perlin')
```

In the first form, the function receives a non-negative integer $n$ and any number x and returns 0 if $\mathrm{x}<0,1$ if $\mathrm{x}>1$, and smoothly interpolates between 0 and 1 , using an $\left(2^{\star}{ }_{n}+1\right)^{\text {th }}$-degree Hermite polynomial otherwise.

The slope of the smoothstep function is zero at both edges, so the result is differentiable over the whole real domain.

Wikipedia: `Smoothstep is a family of sigmoid-like interpolation and clamping functions commonly used in computer graphics and video game engines`, for example to naturally accelerate or decelerate an object.

In the second form, if the string 'perlin' is passed, the function computes the 'smootherstep` polynomial $6 x^{5}-15 x^{4}+10 x^{3}$ for $0<x<1$, which has zero 1st- and 2nd-order derivatives at $\mathrm{x}=0$ and $\mathrm{x}=1$, as suggested by computer scientist Prof. Kenneth Perlin. If given, n may be any integer as it is not evaluated in this case.

See also: heaviside, math.clip, math.rectangular, math.unitise.

```
calc.softsign (x)
```

Computes the Softsign function $\frac{x}{1+|x|}$.

```
calc.Ssi (x)
```

Computes the shifted sine integral and returns it as a number. x must be a number.
See also: calc.Ci, calc.Chi, calc.Shi, calc.Si.

```
calc.variance (f, a, b [, relative [, n [, eps]]]])
```

Returns a positive integer that indicates whether a function f in one real changes slowly or rapidly on the given interval $[a, b]$, with $a, b$ numbers. The larger the result, the larger is its rate of change.

By default,

- the result is relative, i.e. given per unit on the abscissa (true for relative, false for absolute),
- there are $n=10$ sample points per unit, and
- the bail-out value eps - a positive value close to zero - is Eps.

Internally, the function uses adaptive integration with trapezoidal rule and counts the number of trapezoids evaluated. Note that the results are estimates.
calc.w (z [, eps])
Implements the scaled complex complementary error function $\mathrm{W}(\mathrm{z})=$ $\exp \left(-z^{\wedge} 2\right)^{\star} \operatorname{erfc}\left(-I^{\star} z\right)$ (Faddeeva function) for number or complex number z. The return is a complex value. By default, the precision eps is DoubleEps, and can be any other non-negative number.

See also: calc.scaleddawson.
calc.weier (x, a, b [, eps])
Implements the Weierstraß function for the given number $x$ and parameters $a, b$ (also numbers), with $0<\mathrm{x}<1$ and $\mathrm{ab} \geq 1$, b an odd positive integer - a function that is continuous but non-differentiable everywhere:

$$
\sum_{n=0}^{\infty} a^{n} \cos \left(b^{n} x\right)
$$

The precision is given by its fourth optional argument, eps, which is Eps by default.
The function internally uses Kahan-Ozawa-Summation for better accuracy.

```
calc.xpdiff (f, x [, \cdots.] [, options])
```

Like calc.diff, but uses Richardson's extrapolation method to compute symmetric difference quotients. f is a univariate or multivariate function to be inspected at point x (a number). The second, etc. arguments to f may be given right after argument $x$.

The return of the procedure is the derivative of f at $\mathrm{x}, \ldots$, - a number - and the absolute error. If the absolute error is quite large, it may indicate non-differentiability of f at $\mathrm{x}, \ldots$. If the function could not determine a result if x is near an undefined domain, it automatically calls calc.diff, which is more robust in this situation but returns less precise results.

If the option deriv $=\mathrm{n}$ is given, where n may be 1,2 , or 3 , the n -th derivative is calculated, with $n=1$ the default. If $n=0$, then the function value at $f(x)$ is determined.

If the option eps $=\mathrm{h}$ is given, the epsilon value h (a positive number preferably close to zero) is used for the relative error check. If the option delta $=g$ is given, the delta value $g$ (a positive number preferably close to zero) is used for the absolute error check, otherwise they both default to math.epsilon(x).
xpdiff produces better results with powers and trigonometric functions than calc.diff.

See also: calc.diff, calc.differ, calc.eulerdiff, calc.isdiff.

```
calc.zeroin (f, a, b [, eps])
```

Determines the root of the univariate function f in the borders a and b and returns a number if successful, and null otherwise.

The precision eps by default is Eps.

In general, the function will even return accurate results where calc.regulafalsi fails to do so - or even cannot find a root at all -, but the runtime behaviour compared to calc.regulafalsi depends on the following conditions:

1. the interval should not be too far from the origin,
2. the width of the interval should not be too small.

If both conditions are met, then the function can be faster than calc.regulafalsi.
The algorithm uses bisection combined with linear or quadric inverse interpolation, followed by applying Regula Falsi to the estimate done by the previous actions.

See also: calc.regulafalsi, calc.zeros.
calc.zeros (f, a, b, [step [, eps]])
Returns all roots of a function f in one variable on the interval $[\mathrm{a}, \mathrm{b}]$ in a sequence. If it could not find a root, it returns null.

The function divides the interval $[\mathrm{a}, \mathrm{b}$ ] into smaller intervals [a, a+step], [a+step, a+2*step], … [b-step, b], with step=0.1 if step is not given. It then looks for changes in sign in these smaller intervals and if it finds them, determines the roots using a modified regula falsi method.

The accuracy of the regula falsi method is determined by eps, with eps = Eps as a default. f must be differentiable on $[\mathrm{a}, \mathrm{b}]$.

The function is implemented in Agena and included in the lib/calc.agn file.
See also: calc.regulafalsi, calc.sections, calc.zeroin.

## calc.zeta (x)

Computes the Riemann Zeta function for real $\mathrm{x}>1$ and returns the number:

$$
\sum_{k=2}^{\infty} k^{-x}+1
$$

### 11.13 linalg - Linear Algebra Package

This package provides basic functions for Linear Algebra. As a plus package, it is not part of the standard distribution and must be activated with the import statement, e.g. import linalg.

There are two constructors available to define vectors and matrices, linalg.vector and linalg.matrix. Except of these two procedures, the package functions assume that the geometric objects passed have been created with the above mentioned constructors.

The package includes a metatable linalg.vmt defined in the lib/linalg.agn file with metamethods for vector addition, vector subtraction, and scalar vector multiplication. Further functions are provided to compute the length of a vector with the abs operator and to apply unary minus to a vector.

The table linalg.mmt defines metamethods for matrix addition, subtraction and multiplication with a scalar. It is assigned via the lib/linalg.agn file, as well.

The vector function allows to define sparse vectors, i.e. if the component $n$ of $a$ vector $v$ has not been physically set, and if $\mathrm{v}[\mathrm{n}]$ is called, the return is 0 and not null.

The dimension of the vector and the dimensions of the matrix are indexed with the 'dim' key of the respective object. You should not change this setting to avoid errors. Existing vector and matrix values can be overwritten but you should take care to save the correct new values.

Equality checks of vectors or matrices should always be conducted with the strict equality operator $==$ or the $\sim=$ approximate equality operator instead of the Cantor-like $=$ equality operator ${ }^{21}$. For inequality use the not operator combined with $==$ or $\sim=$.

A sample session:

```
> import linalg alias
```

Define two vectors in two fashions: In the simple form, just pass all components explicitly:

[^2]```
> a := vector(1, 2, 3):
[ 1, 2, 3 ]
```

In a more elaborate form, indicate the dimension of the vector to be created and only pass the vector components that are not zero in a table:

```
> b := vector(3, [1~2]):
[ 2, 0, 0 ]
```

Check whether $a$ and $b$ are parallel and have the same direction:

```
> abs(a+b) = abs(a) + abs(b):
false
```

Addition:

```
> a + b:
[ 3, 2, 3 ]
```

Subtraction:

```
> a - b:
[ -1, 2, 3 ]
```

Scalar multiplication:

```
> 2 * a:
[ 2, 4, 6 ]
> crossprod(a, b):
[ 0, 6, -4 ]
```

Find the vector x which satisfies the matrix equation $\mathrm{Ax}=\mathrm{b}$. In this example, we will solve the equation $\left[\begin{array}{ccc}1 & 2 & -4 \\ 2 & 1 & 3 \\ -3 & 1 & 6\end{array}\right] * x=\left[\begin{array}{c}-6 \\ 5 \\ -2\end{array}\right]$. The linalg.matrix constructor expects row vectors.

```
> A := matrix([1, 2, -4], [2, 1, 3], [-3, 1, 6]):
[ 1, 2, -4 ]
[ 2, 1, 3 ]
[ -3, 1, 6 ]
> b := vector(-6, 5, -2):
[ -6, 5, -2 ]
> backsubs(A, b):
[ 2, -2, 1 ]
```

The linalg operators and functions are:

```
s1 + s2
```

Adds two vectors or matrices s1, s2. The return is a new vector or matrix. This operation is done by applying the $\qquad$ _ada metamethod.

```
s1 = s2
```

Subtracts two vectors or matrices s1, s2. The return is a new vector or matrix. This operation is done by applying the $\qquad$ sub metamethod.

## k * s <br> s * $k$ <br> m 1 * m2

Multiplies a number k with each element in vector or matrix s, or multiplies the matrix m 1 with matrix m 2 . The return is a new vector or matrix. This operation is done by applying the $\qquad$ mul metamethod.

## s L k

Divides each element in the vector s by the number $k$ The return is a new vector. This operation is done by applying the __div metamethod.

## abs (v)

Determines the length of vector v. This operation is done by applying the $\qquad$ abs metamethod to $v$.

## qsumup (v)

Raises all elements in vector v to the power of 2 . The return is the sum of these powers, i.e. a number. This operation is done by applying the __qsumup metamethod to v.
linalg.add ( v , w)
Determines the vector sum of vector vand vector w. The return is a vector.
See also: linalg.sub.
linalg.augment (...)
Joins two or more matrices or vectors together horizontally. Vectors are supposed to be column vectors. The matrices and vectors must have the same number of rows.

The return is a new matrix.
See also: linalg.stack.
linalg.backsub (A)
linalg.backsub (A, v)
Performs backward substitution on a system of linear equations.

In the first form, a must be an augmented $\mathrm{m} \times \mathrm{n}$ lower triangular matrix with $\mathrm{m}+1=$ n . In the second form, a is an lower triangular square matrix and va right-hand side vector.

The return is the solution vector.

The function issues an error if a is not upper triangular. You may change the tolerance to detect `zeros` by setting the global system variable Eps to another value.

See also: linalg.gsolve, linalg.rref.

## linalg.backsubs (A, b)

The function has been deprecated. Please use linalg.gsolve instead.
linalg.checkmatrix (A [, B, ‥] [, true])
Issues an error if at least one of its arguments is not a matrix. If the last argument is true, then the matrix dimensions are returned as a pair, else the function returns nothing.

Contrary to linalg.checkvector, the dimensions will not be checked if you pass more than one matrix.

```
linalg.checksquare (A)
```

Issues an error if A is not a square matrix. It returns nothing. See linalg.issquare for information on how this check is being done.
linalg.checkvector (v [, w, ..] ])
Issues an error if at least one of its arguments is not a vector. In case of two or more vectors it also checks their dimensions and returns an error if they are different.

If everything goes fine, the function will return the dimensions of all vectors passed.

See linalg.isvector for information on how the check is being done.
linalg.coldim (A [, ...])
Determines the column dimension of the matrix $A$. The return is a number.

If you pass more than one argument, then a time-consuming check whether A is a matrix, is skipped.

A more direct way of determining the column dimension is right (A.dim).
See also: linalg.rowdim.
linalg.column (A, n)
Returns the n-th column of the matrix or row vector a as a new vector.
See also: columns, linalg.submatrix.
linalg.crossprod (v, w)
Computes the cross-product of two vectors $v, w$ of dimension 3 . The return is $a$ vector.
linalg. det (A)
Computes the determinant of the square matrix A. The return is a number. With singular matrices, it returns 0 .
linalg.diagonal (v)
Creates a square matrix a with all vector components in v put on the main diagonal. The first element in v is assigned $\mathrm{A}[1][1]$, the second element in v is assigned A[2] [2], etc. Thus the result is a dim(v) $x$ dim(v)-matrix.

See also: linalg.getdiagonal.
linalg.dim (A)
Determines the dimension of a matrix or a vector A. If A is a matrix, the result is a pair with the left-hand side representing the number of rows and the right-hand side representing the number of columns. If A is a vector, the size of the vector is determined.
linalg.dotprod (v, w)
Computes the vector dot product of two vectors v, w of same dimension. The vectors must consist of Agena numbers. The return is a number.

```
linalg.forsub (A)
linalg.forsub (A, v)
```

Performs forward substitution on a system of linear equations.

In the first form, a must be an augmented $\mathrm{m} \times \mathrm{n}$ upper triangular matrix with $\mathrm{m}+1=$ n . In the second form, A is an upper triangular square matrix and v a right-hand side vector.

The return is the solution vector.

The function issues an error if A is not upper triangular. You may change the tolerance to detect `zeros` by setting the global system variable Eps to another value.

See also: linalg.backsub, linalg.rref.
linalg.getdiagonal (A)
Returns the diagonal of the square matrix a as a vector.
See also: linalg.diagonal.

```
linalg.gsolve (A [, true])
linalg.gsolve (A, v [, true])
```

Performs Gaussian elimination on a system of linear equations.

In the first form, a must be an augmented $m \times n$ matrix with $m+1=n$. In the second form, a is a square matrix and va right-hand side vector.

The return is the solution vector. It returns infinity if an infinite number of solutions has been found, and undefined if no solutions exists. It returns fail if it could not determine whether no or an infinite number of solutions exist.

If the Boolean value true is given as the last argument, the reduced linear system is also returned as an (augmented) upper triangular matrix.

See also: linalg.backsub, linalg.forsub, linalg.rref.
linalg.hilbert ( n [, x$]$ )
Creates a generalised $n x$ n Hilbert matrix $H$, with $H[i, j]:=1 /(i+j-x)$. If $x$ is not specified, then x is 1 . ( n and x must be numbers.)
linalg.identity ( $n$ )
Creates an identity matrix of dimension $n$ with all components on the main diagonal set to 1 and all other components set to 0 .
linalg.inverse (A)
Returns the inverse of the square matrix A.
linalg.isallones (A)
Checks whether the vector or matrix A contains only ones and returns true or false.
See also: linalg.iszero.
linalg.isantisymmetric (A)
Checks whether the matrix a is an antisymmetric matrix. If so, it returns true and false otherwise.
linalg.isdiagonal (A)
Checks whether the matrix A is a diagonal matrix. If so, it returns true and false otherwise.
linalg.isidentity (A)
Checks whether the matrix A is an identity matrix. If so, it returns true and false otherwise.
linalg.ismatrix (A)
Returns true if A is a matrix, and false otherwise. To avoid costly checks of the passed object, the function only checks whether a is a sequence with the user-defined type 'matrix'.
linalg.issquare (A)
Returns true if A is a square matrix, i.e. a matrix with equal column and row dimensions, and false otherwise.
linalg.issymmetric (A)
Checks whether the matrix a is a symmetric matrix. If so, it returns true and false otherwise.
linalg.isvector (A)
Returns true if $A$ is a vector, and false otherwise. To avoid costly checks of the passed object, the function only checks whether a is a sequence with the user-defined type 'vector'.
linalg.iszero (A)
Checks whether the vector or matrix A contains only zeros and returns true or false.

See also: linalg.isallones.
linalg.ludecomp (A [, n])
Computes the LU decomposition of the square, non-singular matrix $A$ of order $n$. If $n$ is missing, it is determined automatically, i.e. $n:=$ left(A.dim).

The return is the resulting matrix, the permutation vector as a vector, and a number where this number is either 1 for an even number of row interchanges done during the computation, or -1 if the number of row interchanges was odd. If the matrix is singular, an error will be issued.

```
linalg.matrix (obj
linalg.matrix (m, n [, lv])
```

In the first form, creates a matrix from the given structures $\circ b j_{k}$. The structures are considered to be row vectors. Valid structures are vectors created with linalg.vector, tables or sequences.

In the second form, with $m$ and $n$ integers, creates $a_{m} \times \mathrm{n}$ matrix and optionally fills it row by row with the elements in the table or sequence 1 v . 1 v must not include structures. If $1 v$ is not given, the matrix is filled with zeros.

The return is a table of the user-defined type 'matrix' and a metatable linalg.mmt assigned to the matrix. The table key 'dim' contains a pair with the dimensions of the matrix: the left-hand side specifies the number of rows, the right-hand side the number of columns.

See also: linalg.vector, utils.readcsv.
linalg.maeq ( $A, B$ )
This function checks matrix A and matrix в for approximate equality. The return is either true or false. The function uses Donald Knuth's approximation method to compare matrix elements (see the approx function for information on how this works).

You can change the accuracy threshold epsilon with the environ.kernel/eps function.

See also: $\sim=$ and $\sim<>$ metamethods, approx, linalg.meeq, linalg.vaeq.
linalg.meeq (A, B)
This function checks matrix A and matrix в for strict equality. The return is either true or false.

See also: == metamethod, linalg.maeq, linalg.veeq.
linalg.mmap (f, A [, ‥])
This function maps a function f to all the components in the matrix a and returns a new matrix. The function must return only one value. See linalg.vmap for further information.
linalg.mmul (A, B)
This function multiplies an $m \times n$ matrix A with an $n \times p$ matrix $B$. The return is $a n m \times p$ matrix. See also: * metamethod.
linalg.mulrow (A, i, s)
Multiplies each element of row i in matrix a with the scalar s and returns a new matrix.

See also: linalg.swapcol, linalg.swaprow, linalg.mulrowadd.
linalg.mulrowadd (A, i, j, s)
Returns a copy of matrix a with each element in row j exchanged by the sum of this element and the respective element in row i multiplied by the number s .

See also: linalg.swapcol, linalg.swaprow, linalg.mulrowadd.

```
linalg.mzip (f, A, B [, ...])
```

This function zips together two matrices $A$, в by applying the function f to each of its respective components. The result is a new matrix $m$ where each element m[i, j] is determined by $\left.m[i, j]:=f_{A}[i, j], B[i, j]\right)$. If the $f$ has more than two arguments, then its third to last argument must be given right after B .
$A$ and $B$ must have the same dimension.

See also: linalg.vzip, linalg.mmap, linalg.mzip.
linalg.norm (A)
linalg.norm (v [, n])
The function returns the norm of a matrix or vector.

In the first form, the function returns the infinity norm of a matrix A. It is the maximum row sum, where the row sum is the sum of the absolute values of the elements in a given row.

In the second form, it returns the $n$-norm of a vector $v$, where $n$ is a positive integer. (The n-norm of a vector is the $n$-th root of the sum of the magnitudes (absolute values) of each element in v raised to the $n$-th power.) If $n$ is infinity, the return is the infinity norm, i.e. the maximum magnitude of all elements $v$.
linalg.reshape (A, m [, n])
Returns an $m \mathrm{x} n$ matrix whose elements are taken from the matrix $A$. The elements of the matrix are accessed in column-major order. If $n$ is omitted, it is set to 1 .

Example:

```
> a := linalg.matrix(3, 2, [1, 2, 3, 4, 5, 6]):
[ 1, 2]
[ 3, 4
[5, 6 ]
> reshape(a, 2, 3):
[ 1, 3, 5 ]
[2, 4, 6]
```

linalg.rowdim (A [, ...])

Determines the row dimension of the matrix A. The return is a number.
If you pass more than one argument, then a time-consuming check whether A is a matrix, is skipped.

A more direct way of determining the column dimension is left (A.dim).
See also: linalg.coldim.
linalg.rref (A [, v])
Returns the reduced row echelon form of any $m \mathrm{Xn}$ matrix A .

If a vector v is given, the function computes the reduced row echelon form of the augmented matrix a|v. In this case, a and v must have equal dimensions.

See also: linalg.gsolve.

```
linalg.scalarmul (v, n)
linalg.scalarmul (n, v)
```

Performs a scalar multiplication by multiplying each element in vector v by the number n . The result is a new vector.

## linalg.scale (A)

Normalises the (non-null) columns of a matrix A in such a way that, in each column, an element of maximum absolute value equals 1 . The return is a new matrix where the normalised vectors are delivered in the corresponding columns.

See also: math.norm, stats.scale.

```
linalg.stack (...)
```

Joins two or more matrices or vectors together vertically. Vectors are supposed to be row vectors. The matrices and vectors must have the same number of columns.

The return is a new matrix.

See also: linalg.augment.
linalg.submatrix (A, p [, r])
linalg.submatrix (A, p:q [, r:s])
In the first form, returns column p from matrix A as a new row vector.
In the second form, returns columns p to q as a new matrix.
An optional third argument may be given to limit the extraction of the columns to the specified row $r$ or rows $r$ to $s$.

With the second and third arguments, you may mix numbers with pairs.
See also: linalg.column.
linalg.swapcol (A, p, q)
Swaps column p in matrix a with column q. p, q must be positive integers. The result is a new matrix.

See also: linalg.swaprow, linalg.mulrow, linalg.mulrowadd.
linalg.swaprow (A, p, q)
Swaps row $p$ in matrix A with row $q$. p, q must be positive integers. The result is a new matrix.

## See also: linalg.swapcol, linalg.mulrow, linalg.mulrowadd.

linalg.sub ( $v$, w)
Subtracts vector w from vector v. The result is a new vector.

See also: linalg.add.

```
linalg.trace (A)
```

Computes the trace of a square matrix a and returns a number.
linalg.transpose (A)
Computes the transpose of a $m \times n$-matrix a and thus returns an $n \times m$-matrix.

```
linalg.vector (a1, a2, ...)
linalg.vector ([a1, a2, \cdots.])
linalg.vector (seq(a1, a2, ...))
linalg.vector (n, [a1, a2, \cdots.])
linalg.vector (n, [ ])
```

Creates a vector with numeric components a1, a2, etc. The function also accepts a table or sequence of elements a1, a2, etc. (second and third form).

In the fourth form, $n$ denotes the dimension of the vector, and $a_{k}$ might be single values or key~value pairs. By a metamethod, vector components not explicitly set automatically default to 0 . This allows you to create memory-efficient sparse vectors and thus matrices.

In the fifth form, a sparse zero vector of dimension $n$ will be returned.
The result is a table of the user-defined type 'vector' and the linalg.vmt metatable assigned to allow basic vector operations with the operators +, -, *, unary minus and abs. The table key 'dim' contains the dimension of the vector created.

See also: linalg.matrix.
linalg.vaeq (a, b)
This function checks vector a and vector b for approximate equality. The return is either true or false. The function uses Donald Knuth's approximation method to compare vector elements (see the approx function for information on how this works).

You can change the accuracy threshold epsilon with the environ.kernel/eps function.

See also: ~= metamethod, approx, linalg.veeq, linalg.maeq.

```
linalg.veeq (a, b)
```

This function checks vector a and vector b. for strict equality. The return is either true or false.

See also: == metamethod, linalg.meeq, linalg.vaeq.
linalg.vmap (f, v [, ...])
This operator maps a function f to all the components in vector v and returns a new vector. The function f must return only one value.

If function f has only one argument, then only the function and the vector are passed to linalg.vmap. If the function has more than one argument, then all arguments except the first are passed right after the name of the vector.

Examples:

```
> vmap(<< x -> x^2 >>, vector(1, 2, 3) ) :
[1, 4, 9 ]
> vmap(<< (x, y) -> x > y >>, vector(1, 0, 1), 0): # 0 for y
[ true, false, true ]
```

See also: linalg.vzip, linalg.mmap, linalg.mzip.
linalg.vzip (f, v1, v2 [, $\cdots]$ )
This function zips together two vectors by applying the function $f$ to each of its respective components. The result is a new vector $v^{\prime}$ where each element $v^{\prime}[\mathrm{k}]$ is determined by $\mathrm{v}^{\prime}[\mathrm{k}]:=\mathrm{f}(\mathrm{v} 1[\mathrm{k}], \mathrm{v} 2[\mathrm{k}])$.
v1 and v2 must have the same dimension. The third to last argument to f must be given right after v2.

See also: linalg.vmap, linalg.vzip, linalg.mmap.
linalg.zerovector ( n )
Creates a zero vector of length n with all its components physically set to 0 . If you want to create a sparse zero vector of dimension $n$, use: linalg.vector ( $n$, [ ] ).

### 11.14 stats - Statistics

This package contains procedures for statistical calculations and operates completely on tables. As a plus package, it is not part of the standard distribution and must be activated with the import statement, e.g. import stats.

You might want to use utils.readcsv to read distributions from a file.

Summary of functions:
Averages:
stats.accu, stats.amean, stats.ema, stats.gema, stats.gmean, stats.gsma, stats.gsmm, stats.hmean, stats.iqmean, stats.median, stats.mean, stats.midrange, stats.qmean, stats.sma, stats.smm, stats.trimean, stats.trimmean.

Combinations:
stats.cartprod, stats.numbcomb, stats.numpart, stats.numbperm.
Deviations:
stats.ad, stats.chauvenet, stats.durbinwatson, stats.ios, stats.mad, stats.md, stats.sd, stats.spread, stats.ssd, stats.var.

Density:
stats.cdf, stats.nde, stats.ndf, stats.pdf.

## Extrema:

stats.colnorm, stats.extrema, stats.minmax, stats.peaks, stats.rownorm, stats.smallest.

## Occurrences:

stats.countentries, stats.freqd, stats.isall, stats.isany, stats.mode, stats.obcount, stats.obpart.

Ranges:
stats.fivenum, stats.iqr, stats.percentile, stats.prange, stats.qcd, stats.quartiles.

Sums:
qsumup, sumup, stats.cumsum, stats.fsum, stats.moment, stats.sumdata, stats.sumdataln, stats.var.

Probability density functions :
stats.cauchy, stats.cdfnormald, stats.chisquare, stats.fratio, stats.gammad, stats.gammadc, stats.invnormald, stats.normald, stats.probit, stats.studentst.

## Miscellaneous:

stats.acf, stats.acv, stats.checkcoordinate, stats.dbscan, stats.deltalist, stats.fprod, stats.herfindahl, stats.issorted, stats.kurtosis, stats.neighbours, stats.scale, stats.skewness, stats.sorted, stats.tovals.

The functions:
A general note: almost all of the statistics functions ignore the undefined value should it be part of a distribution. Any non-numeric values in a distribution are replaced with zeros. Most of the following functions also process numarrays.

To reduce round-off errors, it is always a good idea to sort structures before applying stats functions that sum up data, see stats.sorted and numarray.sorted.
stats.accu ([true])
Returns a factory that computes the running mean, variance, median, and absolute deviation by mere accumulation of individual observations.

If the first optional argument true is passed, then sample values are computed (division by the number of observations - 1), otherwise population values are computed (division by the number of observations).

If the resulting factory is called without any argument, the current results are returned in a table.

If the resulting factory is called with a number, i.e. an observation, it is added to the accumulators.

While the mean and variance computed are correct, the median and the absolute deviation are approximations only. The function ignores non-finite values, i.e. undefined and +/-infinity.

You may use this function if a distribution is too large to be stored in a structure.
The idea has been taken from the Stat package shipped with Digital Equipment Corporation Critical Mass Modula-3. 2.10.1.
stats.acf (obj, lag, [, option [, m [, s]]])
Returns the autocorrelation of a distribution obj (a table, sequence or numarray) of numbers at a given lag, a non-negative integer. If any third argument option different from null is passed, then the un-normalised autocorrelation will be returned. The return is a number,

$$
\sum_{i=1}^{n-l a g}\left(\text { obj }_{i}-\mu\right)\left(\text { obj }_{j+\operatorname{lag}}-\mu\right)
$$

where n is the number of observations, and $\mu$ is the arithmetic mean of the distribution. If no option is passed, the sum is divided by the variance of obj multiplied by $n$, yielding a normalised result. The function uses Kahan-Ozawa round-off error prevention.

To speed up computation times significantly, you may also pass a precomputed mean m and the sum s of all values in the distribution.

It may be used to detect periodicy in a time series.
A distribution is autocorrelated if stats.acf returns a negative or positive value significantly different from zero. The - normalised - return is in the range $[-1,1]$, where +1 denotes perfect autocorrelation and -1 with 1 perfect anti-correlation. A negative correlation indicates that higher values of a distribution are related to lower values.

See also: stats.acv.

```
stats.acv (obj, p, [, option])
```

Depending on the type of the observation obj, returns a table, sequence or numarray of autocorrelations starting with lag $=0$, through and including the given number p of lags. If any third argument option is passed, then un-normalised autocorrelations are returned. For the formula and numeric method used, see stats.acf.
stats.ad (obj [, option])
Computes the absolute (or mean) deviation of all the values in a table, sequence or numarray obj, i.e. the mean of the equally likely absolute deviations from the arithmetic mean $\mu$ :

$$
\left.\frac{1}{n} \sum_{i=1}^{n} \right\rvert\, \text { obj }_{i}-\mu \mid
$$

The return is a number.

If any second non-null argument is given, then the variation coefficient will be returned:

$$
\left.\frac{1}{n} \sum_{i=1}^{n} \right\rvert\, \text { obj }_{i}-\mu|/|\mu|
$$

Absolute deviation is more robust than standard deviation since it is less sensitive to outliers. The function uses Kahan-Babuška round-off error prevention.

If obj is empty or entirely consists of undefineds, fail will be returned. The function ignores undefineds, if obj features at least one number.

Please note that if obj includes non-numbers, where undefined is considered a number, they are interpreted as zeros which might unexpectedly influence the result.

The function returns fail if obj contains less than two elements.
See also: stats.ios, stats.mad, stats.md, stats.sd.

## stats.amean (obj)

Divides each element in a table, sequence or numarray obj by the size of obj and sums up the quotients to finally return the arithmetic mean. It is equivalent to:

$$
\sum_{i=1}^{n} \frac{o b j_{i}}{n}
$$

By dividing each element before summation, the function avoids arithmetic overflows and also uses the Kahan-Babuška algorithm to prevent round-off errors during summation. Thus the function is more robust but also significantly slower than stats.mean.

If obj is table, it is assumed to be an array, non-positive integral keys (including strings, etc.) are ignored.

The function returns fail if obj contains less than two elements.
If obj is empty or entirely consists of undefineds, fail will be returned. The function ignores undefineds, if obj features at least one number.

Please note that if obj includes non-numbers, where undefined is considered a number, they are interpreted as zeros which might unexpectedly influence the result.

See also: stats.accu, stats.gmean, stats.hmean, stats.mean, stats.qmean, stats.sma, stats.trimmean.
stats.bell ( n )
Returns the $n$-th Bell number, i.e. counts the possible partitions of a set.

```
stats.cartprod (l)
```

Creates a factory that each time it is called, returns a tuple in the Cartesian product of a table of two or more tables 1 , or a sequence of two or more sequences 1 . The type of the result is the same as the type of the input. The structures in 1 may be of different size but must be non-empty.

```
stats.cauchy (x, a, b)
```

The cauchy[a, b] distribution has the probability density function:

$$
1 /\left(\pi^{\star} b^{\star}\left(1+((x-a) / b)^{2}\right)\right), b>0 .
$$

See also: stats.chisquare, stats.fratio, stats.normald, stats.studentst.

```
stats.cdf (a, b [, \mu [, \sigma]])
```

Computes the cumulative density function between the lower bound a and the upper bound b . If the mean $\mu$ is not given, it defaults to 0 ; if the standard deviation $\sigma$ is not given, it defaults to 1 .

The return is the number:

$$
\frac{1}{\sigma \sqrt{2 \pi}} \int_{a}^{b} e^{\frac{-(x-\mu)^{2}}{2 \sigma^{2}}} d x
$$

See also: stats.nde, stats.ndf, stats.pdf.
stats.cdfnormald (x)
Implements the cumulative density function for the standard normal distribution. The return is the number:

$$
\frac{1}{\sqrt{2 \pi}} \int_{t=-\infty}^{x} e^{\frac{-t^{2}}{2}} d t
$$

See also: stats.invnormald, stats.normald.
stats.chauvenet (obj [, x] [, option, ...])
Receives a table or sequence obj of normally distributed numbers and checks them for outliers using the formula:

$$
\mathrm{p}:=\mathrm{n} \text { * } \operatorname{erfc}((|\mathrm{x}-\mu| / \mathrm{sd}),
$$

where n is the number of observations in a distribution, x a sample of it, $\mu$ the arithmetic mean $\mu=\sum_{i=1}^{n} \frac{\mathrm{obj}_{\mathrm{i}}}{\mathrm{n}}$, dev the standard deviation $\mathrm{sd}=\sqrt{\frac{1}{n} \sum_{i=1}^{n}\left(\mathrm{obj}_{\mathrm{i}}-\mu\right)^{2}}$. If at least obj and x is given, the function checks whether the number x is an outlier by conducting a 1-pass check and returns true or false.

If obj but not x is passed, however, the procedure iterates obj again and again as long as it does not find an outlier, and returns the outliers in a structure, its type defined by the type of obj.

By default, if $p<0.5$, where 0.5 is the magical Chauvenet number, an outlier is detected. If you pass the option bailout $=c$, then $c$, a non-negative number, will be the threshold.

If you pass the option jump=true, as soon as an outlier is detected, it is removed from the distribution and then the whole evaluation process is restarted immediately with a reduced distribution along with a re-computed mean and deviation.

If you do not, all remaining items are also checked according to the current criteria - after the last item has been checked, only then the outliers are removed from the distribution, the mean and deviation are re-computed and another iteration begins.

If you pass the option mean $=\mathrm{f}$, where f is a procedure, then the mean $\mu$ is determined by $f$. The default is $f=$ stats.amean, i.e. the arithmetic mean.

If you pass the option dev=f, where $f$ is a procedure, then the deviation dev is determined by $f$. The default is $f=$ stats.sd, the standard deviation.
if you pass the option outlier='lower' or outlier='upper', then the function only checks for lower or upper outliers, respectively.

Further information: `Cleaning Data the Chauvenet Way`, by Lily Lin and Paul D. Sherman, published at the South East SAS Users Group's website http://www.sesug.org.

The function is implemented in Agena and included in the lib/stats.agn file.

```
stats.checkcoordinate (c [, procname])
```

The function checks whether the given co-ordinate c is a pair $x$ : $y$ with both its left-hand and right-hand side $x$ and $y$ being numbers. If a second argument, a string, is given, then error messages of stats.checkcoordinate refer to the given procedure procname as the function issuing the error. Otherwise the error message includes a reference to stats.checkcoordinate.

The function returns the numbers x and y and issues an error otherwise.
stats.chisquare ( $\mathrm{x}, \mathrm{nu}$ )
The chisquare[nu] distribution has the probability density function:

$$
x^{\wedge}((n u-2) / 2) \exp (-x / 2) / 2^{\wedge}(n u / 2) / \Gamma(n u / 2)
$$

with $\mathrm{x}>0$ and nu a positive integer.
See also: stats.cauchy, stats.fratio, stats.normald, stats.studentst.
stats.colnorm (obj)
Returns the largest absolute value of the numbers in the table, sequence or numarray obj, and the original value with the largest absolute magnitude. If obj includes undefineds, they are ignored. If the structure obj consists entirely of one or more undefineds, then the function returns the value undefined twice. If the structure is empty, fail will be returned.

See also: stats.scale, stats.rownorm.
stats.countentries (obj [, f [, ...]])
Counts the number of occurrences of each entry in a table or sequence obj and returns a dictionary with its respective key the entry and its value the number of occurrences.

You might optionally pass a procedure f to be mapped on the structure before counting begins on the thus modified structure. If f has more than one argument, then its second to last argument must be given right after f .

The function is implemented in Agena and included in the lib/stats.agn file.

See also: countitems, bags package.
stats.cumsum (obj)
Returns a structure of the cumulative sums of the numbers in the table, sequence or numarray obj.

The type of return is determined by the type of obj.
The function returns fail if obj contains less than one element. It may also return a structure containing undefined and/or infinity if obj includes non-numbers.

See also: sumup, calc.fsum, stats.fsum, stats.sumdata.

```
stats.dbscan (obj, eps, minpts [, option])
```

The functions finds clusters in a sequence obj of n-dimensional points and returns a table with the individual clusters along with their respective points.

It also returns a register of the size of the whole distribution listing the cluster number associated with each point, where the point in this case is represented by its integral position in the sequence obj.

The co-ordinates of points in obj may be represented by pairs (2-dimensional space, only), sequences (any space), or vectors created by linalg.vector (any space).
eps is the maximum allowed distance between two points that shall belong to the same neighbourhood. minpts is the minimum number of points that shall constitute a neighbourhood.

By specifying the 'select' option along with a function returning a Boolean, e.g. 'select':<< x -> right x < 1 >>, only points satisfying the given criterion are examined.

By specifying the 'method' option, you can control how the function determines clusters: 'method':'original' uses the classic one, 'method':'modified' uses a much faster and memory-saving implementation that contrary to the original method immediately flags neighbours of neighbours as being visited and thus does not examine them again in further passes. The default is 'original'.

See also: stats.neighbours.
stats.deltalist (obj [, option])
Returns a structure of the deltas of neighbouring elements in the table, sequence or numarray obj. If the value true is given as an option, then absolute differences are returned.

The type of return is determined by the type of obj.
Please note that the difference between undefined and a number is undefined, and that the difference between infinity and a number is $\pm$ infinity.

The function returns fail if obj contains less than two elements.
See also: stats.ios.

## stats.durbinwatson (obj)

The Durbin-Watson test detects the autocorrelation in the residuals from a linear regression and returns

$$
d=\sum_{i=2}^{n}\left(o b j_{i}-o b j_{i-1}\right)^{2} / \sum_{i=1}^{n} o b j_{i}^{2}
$$

If $d$ is equal to 2 , it indicated the absence of autocorrelation. If $d$ is less than 2 , it indicates positive autocorrelation; if $d$ is greater than 2 it indicates negative autocorrelation and that the observations are very different from each other. If $d$ is less than 1, the regression should be checked. The function uses Kahan-Babuška roundoff prevention. obj may be a table, sequence or numarray.
stats.ema (obj, k, alpha [, mode [, y0star]])
Computes the exponential moving average of a table or sequence obj up to and including its $k$-th element.

The smoothing factor alpha is a rational number in the range $[0,1]$.
The function supports two algorithms: If mode is 1 (the default), then the algorithm

```
r := alpha * obj[k];
s := 1 - alpha;
for i from k - 1 to 1 by -1 do
    r +:= alpha * s ^ i * obj[i]
od;
r := r + s ^ k * y0star;
```

is used to compute the result r . In mode 1, you can pass an explicit first estimate y0star, otherwise the first value y0star is equal to the sample moving average of obj. If mode is 2 , then the formula

```
r := obj[k];
for i from k - 1 to 1 by -1 do
    r +:= alpha * (obj[i] - r)
od;
```

is applied.

The result is a number.
See also: stats.gema.
stats.extrema (obj, delta)
Expects a sequence or table obj of points $x_{k}: y_{k}$ and the number delta and determines the local minima and maxima.

A value $y_{k}$ is considered an extrema if the difference to its surrounding is at least delta. The function returns two structures of pairs, i.e. points, the first one including the local minima, the second one the local maxima.

The type of the structures is determined by the type of obj.
The function is implemented in Agena and included in the lib/stats.agn file.
stats.fivenum (obj)
Returns a sequence of the first quartile, the median, and the third quartile of a distribution obj, in this order. obj may be a table, sequence or numarray. If the number of observations is five or more, the sequence also includes the minimum and the maximum observation, along with the arithmetic mean.

The first and third quartiles are computed according to the NIST rule, see stats.percentile for further information.

If the elements in obj are not sorted in ascending order, the function automatically sorts them non-destructively, and any non-numeric values are converted to zeros.

See also: stats.quartiles.
stats.fprod (f, obj [, a [, b [, ...]]])
Applies the function $£$ onto all elements in the table, sequence or numarray obj and then multiplies the results. The return is the number:

$$
\prod_{i=a}^{b} \mathrm{f}_{\mathrm{f}(\mathrm{Ob}, \mathrm{i})}
$$

If $a$ is not given, $a$ is set to 1 . If $b$ is not given, $b$ is set to the number of elements in obj. If f is a multivariate function, its second, third, etc. argument must be passed after b.

See also: calc.fsum, stats.fsum, stats.sumdata.
stats.fratio (x, nu1, nu2)
The Fisher's F distribution, also known as fratio distribution, has the probability density function

$$
\begin{gathered}
\Gamma((\mathrm{nu} 1+\mathrm{nu} 2) / 2) / \Gamma(\mathrm{nu} 1 / 2) / \Gamma(\mathrm{nu} 2 / 2)^{\star}(\mathrm{nu} 1 / \mathrm{nu} 2)^{\wedge}(\mathrm{nu} 1 / 2) * \\
\mathrm{x}^{\wedge}((\mathrm{nu}-2) / 2) /\left(1+(\mathrm{nu} / \mathrm{nu})^{\star}{ }_{\mathrm{x}}\right) \wedge((\mathrm{nu} 1+\mathrm{nu} 2) / 2)
\end{gathered}
$$

with $\mathrm{x}>0$, nu1 and nu2 positive integers.
See also: stats.cauchy, stats.chisquare, stats.normald, stats.studentst.

```
stats.freqd (s, p [, n])
stats.freqd (s, p [, option])
```

For sample s, the function computes a frequency distribution function that each time it is called, returns both the start of the respective subinterval (not the class number) defined by pair p and step size or number of classes and the number of occurrences in this subinterval/class. If the distribution has been completely traversed, two nulls are returned.

For more information on the arguments to be passed and the values returned, please refer to the description of stats.obcount.

Example:

```
> s := seq(-1, 0, 0.1, 0.2, 0.3, 0.4, 1, 1.1, 2, 2.1)
> stats.obcount(s, 0:2, 0.5):
[0 ~ 5, 0.5 ~ 0, 1 ~ 2, 1.5 ~ 1] [-1, 2.1]
> f := stats.freqd(s, 0:2, 0.5);
> f():
0 5
> f():
0.5 0
```

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.obcount.
stats.fsum (f, obj [, a [, b [, …]]])
Applies the function f onto all elements in the table, sequence or numarray obj and then sums up the results using Kahan-Babuška round-off error prevention. The return is the number:

$$
\sum_{i=a}^{b} f\left(0 b_{j}\right)
$$

If $a$ is not given, $a$ is set to 1 . If $b$ is not given, $b$ is set to the number of elements in obj. If f is a multivariate function, its second, third, etc. argument must be passed after b.

See also: calc.fsum, stats.fprod, stats.sumdata.
stats.gammad ( $\mathrm{x}, \mathrm{a}, \mathrm{b}$ )
The Gamma distribution function returns the integral from zero to real x of the gamma probability density function and returns the number:

$$
\frac{a^{b}}{\Gamma(b)} \int_{0}^{x} t b-1 \quad e^{-a t} d t
$$

where a * $\mathrm{x}>0, \mathrm{~b}>0$. See also: stats.gammadc.
stats.gammadc ( $\mathrm{x}, \mathrm{a}, \mathrm{b}$ )
The complemented Gamma distribution function returns the integral from x to infinity of the gamma probability density function and returns the number:

$$
\frac{a^{b}}{\Gamma(b)} \int_{x}^{\infty} t^{b-1} e^{-a t} d t
$$

where $a^{*} x>0, b>0$. See also: stats.gammadc.
stats.gema (obj, k, alpha [, mode [, y0star]])
Like stats.ema, but returns a function that, each time it is called, returns the exponential moving average, starting with sample $\mathrm{obj}^{2}[\mathrm{k}]$, and progressing with sample $o b j[k+1]$, obj $[k+2]$, etc. with subsequent calls. It return null if there are no more samples in obj. It is much faster than stats.ema with large distributions.

The smoothing factor alpha is a rational number in the range $[0,1]$.

The function supports two algorithms: If mode is 1 (the default), then the algorithm

```
r := alpha * obj[k];
s := 1 - alpha;
for i from k - 1 to 1 by -1 do
    r := r + alpha * s ^ i * obj[i]
od;
r := r + s ^ k * y0star;
```

is used to compute the result. In mode 1, you can pass an explicit first estimate y0star, otherwise the first value y0star is equal to the sample moving average of obj.

If mode is 2 , then the formula

```
r := obj[k];
for i from k - 1 to 1 by -1 do
    r := r + alpha * (obj[i] - r)
od;
```

is applied to the period.
The result is a number.
stats.gini (obj [, 'sorted'])
Measures the inequality in a distribution given by the table, sequence or numarray obj by applying Gini's formula

$$
\sum_{i=1}^{n} \sum_{j=1}^{n}\left|x_{i}-x_{j}\right| / 2 n^{2} \mu,
$$

where n is the number of occurrences and $\mu$ the arithmetic mean.
All members of obj should be numbers. infinity's or undefined's are ignored.
It returns a number $r$ indicating the absolute mean of the difference between every pair of observations, divided by the arithmetic mean of the population, with $0 \leq r \leq 1$ , where 0 indicates that all observations are equal, and (a theoretical value of) 1 indicates complete inequality. It is assumed that all observations are non-negative.

If the option 'sorted' is given then the function assumes that all elements in obj are already sorted in ascending order - thus computing the result much faster.

To compute the normalised Gini coefficient, multiply the result by $n /(n-1)$.
See also: stats.herfindahl.

## stats.gmean (obj)

Returns the geometric mean of all numeric values in table, sequence or numarray obj. It is a measure of central tendency. Its formula is:

$$
\left(\prod_{i=1}^{n} b_{i}\right)^{1 / n}
$$

The function returns fail if obj contains less than two elements.
The geometric mean should be applied on positive values that are interpreted to their products, e.g. rates of growth, instead of their sums, only. Otherwise, undefined may be returned.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.amean, stats.hmean, stats.mean, stats.qmean.

```
stats.gsma (obj, k, p)
stats.gsma (obj, k, p, b)
```

Like stats.sma, but returns a function that, each time it is called, returns the simple moving mean, starting with sample $k$, and progressing with sample $k+1, k+2$, etc. If $k>$ size obj, then the function returns null. It is much faster than stats.sma with large distributions.

```
stats.gsmm (obj, k, p)
stats.gsmm (obj, k, p, b)
```

Like stats.smm, but returns a function that, each time it is called, returns the simple moving median, starting with sample $k$, and progressing with sample $k+1, k+2$, etc. If $k>$ size $\left(\mathrm{obj}^{\mathrm{j}}\right.$ ), then the function returns null. It is much faster than stats.smm with large distributions.

The function automatically non-destructively sorts the distribution obj if it is unsorted.

## stats.herfindahl (obj)

Returns the normalised Herfindahl-Hirschman index of a distribution obj (a table, sequence or numarray), an indicator of the amount of competition in economy. A value of 0 means that there is absolute competition, i.e. that all companies have the same share, and 1 means that there is a monopoly.
The normalised index h is defined as:

$$
H=\sum_{i=1}^{n}\left(\frac{O b j_{i}}{s}\right)^{2}, \text { where } s=\sum_{i=1}^{n} \text { obj }_{i} \Rightarrow h=\frac{H-1 / n}{1-1 / n}
$$

It is also a good measure to determine the stability of a distribution, with a value tending to zero indicating that the number of outliers is quite low, and a value tending to 1 that there is at least an extreme outlier.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.gini.

## stats.hmean (obj)

Returns the harmonic mean of all numeric values in table, sequence or numarray obj as a number. It is useful with rates and ratios, as it provides the best average. It is defined as follows:

$$
\mathrm{n} / \sum_{\mathrm{i}=1}^{\mathrm{n}} \frac{1}{\mathrm{obj}_{\mathrm{i}}}
$$

The function returns fail if obj contains less than two elements.
The harmonic mean should be applied on observations containing relations to a unit, e.g. speed.

The function internally uses Kahan-Babuška summation to compensate for rounding errors.

See also: stats.amean, stats.gmean, stats.mean, stats.qmean.

## stats.invnormald (y)

Evaluates the inverse of the Normal distribution function by returning the argument, $x$, for which the area under the Gaussian probability density function (integrated from $-\infty$ to $x$ ) is equal to $y$.

See also: stats.cauchy, stats.chisquare, stats.fratio, stats.normald, stats.studentst.

```
stats.ios (obj [, option])
```

Sums up absolute differences between neighbouring entries in a table, sequence or numarry obj, divides by the number of its elements minus 1 , and returns the number:

$$
\frac{1}{n-1} \sum_{i=2}^{n}\left|o b j_{i}-o b j_{i-1}\right|
$$

The function returns fail if obj contains less than two elements.

If any second non-null argument is given, the function first normalises the distribution to the range ( $-\infty, 1$ ] (see stats.scale), determines the difference list, sums up its absolute differences and divides the sum by the number of occurrences minus 1 to make a distribution comparable to other ones.

This indicator is quite useful to find out how stable or volatile a preferably unsorted distribution is.

See also: stats.ad, stats.deltalist, stats.sd, stats.var.

```
stats.iqmean (obj)
```

Returns the arithmetic mean of the interquartile range of the distribution obj using Kahan-Babuška round-off error prevention. The return is a number. obj may be a table, sequence or numarray.

If a distribution is unsorted, the function automatically sorts it non-destructively, and any non-numeric observations are converted to zeros.

The interquartile range comprises all observations that reside between the first and third quartiles.
See also: stats.iqr, stats.midrange.

```
stats.iqr (obj [, a [, b]])
```

Without a and b given, the function determines the interquartile range (IQR), i.e. the difference of the third and first quartile. stats.iqr is useful for determining the variability in a distribution obj (a table, sequence or numarray).

You may optionally pass a lower and upper percentile $a, b$, both in the range [0, 100). If $a$ is missing, it is set to 25 . If $b$ is missing it is set to $100-\mathrm{a}$.

It returns the number
stats.percentile(obj, b) - stats.percentile(obj, a)

If obj is unsorted, the function sorts it non-destructively. It is implemented in Agena and included in the lib/stats.agn file.

See also: stats.midrange, stats.percentile, stats.qcd, stats.quartiles.

```
stats.isall (obj [, eps])
```

Checks whether all elements in a table or sequence obj are non-zero and returns true or false. If the second argument eps, a non-negative number, is passed, the function returns true if all observations $x$ in obj satisfies the condition $\operatorname{abs}(x)>$ eps. By default eps is 0 .

The function returns fail with empty structures or structures that contain one element only.

See also: and operator, stats.isany.

```
stats.isany (obj [, eps])
```

Checks whether at least one element in a table or sequence obj is non-zero and returns true or false. If the second argument eps, a non-negative number, is passed, the function returns true if at least one observations $x$ in obj satisfies the condition $\operatorname{abs}(x)>$ eps. By default eps is 0 .

The function returns fail with empty structures or structures that contain one element only.

See also: or operator, stats.isall.

```
stats.issorted (obj [, f])
```

Checks whether all values in a table, sequence or numarray obj of numbers are stored in ascending order and returns true or false. If a value in obj is not a number, it is ignored.

If obj is a table, you have to make sure that it does not contain holes. If it contains holes, apply tables.entries on obj.

If f is given, then it must be a function that receives two structure elements to determine the sorting order. See sort for further information.

See also: sort, sorted, skycrane.sorted, stats.sorted.

```
stats.kurtosis (obj)
```

The function determines the kurtosis, a measure of flatness or peakedness of symmetric and unimodal distributions.

To quote Wikipedia, a higher value means that the distribution has `a sharper peak and fatter tails, ` while a lower value indicates `the distribution has a more rounded peak and thinner tails. '

The function computes the result by computing the fourth moment around the mean of a distribution, divided by the fourth power of the standard deviation.

The function returns fail if obj contains less than two elements.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.skewness.

```
stats.mad (obj [, option])
```

Returns the median of the absolute deviations of all numeric values in table, sequence or numarray obj from obj's median, and returns the number:

$$
\text { stats.median( } \left.\bigvee_{i=1}^{\text {size obj }} \mid \text { obj }_{i}-\text { stats.median(obj) } \mid\right)
$$

If any second non-null argument is given, then the variation coefficient will be returned:

$$
\text { stats.median( } \bigvee_{i=1}^{\text {size obj }} \mid \text { obj }_{i}-\text { stats.median(obj) } \mid \text { )/ stats.median(obj). }
$$

Median absolute deviation is quite robust if a distribution contains a small number of outliers.

If obj is unsorted, it automatically sorts it before determining the result.
If obj contains less than two elements or entirely consists of undefineds, fail will be returned. The function ignores undefineds, if obj features at least one number.

Please note that if obj includes non-numbers, where undefined is considered a number, they are interpreted as zeros which might unexpectedly influence the result.

## See also: stats.ad, stats.md, stats.median.

```
stats.md (obj [, option])
```

Computes the median deviation of all the values in a table, sequence or numarray obj, i.e. the mean of the equally likely absolute deviations from the median med:

$$
\left.\frac{1}{n} \sum_{i=1}^{n} \right\rvert\, \text { obj }_{i}-\text { med } \mid
$$

The return is a number.
If any second non-null argument is given, then the variation coefficient will be returned:

$$
\sqrt{\left.\frac{1}{n} \sum_{i=1}^{n} \right\rvert\, \text { obj }_{i}-\mathrm{med} \mid} /|\mathrm{med}|
$$

See also: stats.mad.

## stats.mean (obj)

Returns the arithmetic mean of all numeric values in table, sequence or numarray obj as a number. It is equivalent to:

$$
\frac{1}{n} \sum_{i=1}^{n} o b j_{i}
$$

thus the function - as opposed to stats.amean - first computes the sum of the observations and then divides it by the number of elements.

If obj is table, it is assumed to be an array, non-positive integral keys (including strings, etc.) are ignored.

The function returns fail if obj contains less than two elements.
For a more robust but slower version, please have a look at stats.amean.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.accu, stats.amean, stats.gmean, stats.hmean, stats.meanmed, stats.qmean.

```
stats.meanmed (obj [, option])
```

Returns both the arithmetic mean and the median of all numeric values in table, sequence or numarray obj as numbers. If any option is given, the quotient of the mean and the median will be returned.

See also: stats.accu, stats.amean, stats.meanvar, stats.median.
stats.meanvar (obj [, option])
Returns both the arithmetic mean and the variance - in this order - of the distribution obj using an algorithm developed by B. P. Welford to prevent round-off errors.

By default, the population variance will be returned unless you pass the Boolean value true for option to compute the sample variance. obj may be a table, sequence or numarray.

See also: stats.meanmed.
stats.median (obj)
Returns the median of all numeric values in table, sequence or numarray obj as a number. If obj is unsorted, it automatically sorts it before determining the median.

If obj contains less than two elements or entirely consists of undefineds, fail will be returned. The function ignores undefineds, if obj features at least one number.

Please note that if obj includes non-numbers, where undefined is considered a number, they are interpreted as zeros which might unexpectedly influence the result.

The median is the middle element of a distribution if its size is odd, or the average of its middle elements it is size is even.

See also: stats.accu, stats.mad, stats.meanmed.
stats.midrange (obj [, option])
Returns both the arithmetic mean and the variance - in this order - of the distribution obj, a table, sequence or numarray.

Computes the sum of the minimum and maximum value of a distribution obj, divided by two.

If the option 'sorted' is given, the observation is not traversed; instead the first and the last entry is taken to compute the mean. If the observation is empty or has only one element, fail will be returned.

See also: stats.iqr, stats.minmax.
stats.minmax (obj [, 'sorted'])
Returns a table with the minimum of all numeric values in table, sequence or numarray obj as the first value, and the maximum as the second value. If the option 'sorted' is passed than the function assumes that all values in obj are sorted in ascending order so that execution is much faster.
stats.minmax returns fail if a sequence or table of less than two elements has been passed. If obj consists entirely of undefined entries, $[-\infty, \infty]$ or $\boldsymbol{s e q}(-\infty, \infty)$ are returned.

See also: stats.midrange.

```
stats.mode (obj)
```

Returns all values in the sequence or table obj with the largest number of occurrence, i.e. highest frequency. If there is more than one value with the highest frequency, they are all returned.

The type of return is determined by the type of its argument. If the given structure is empty, it is simply returned.

The function is implemented in Agena and included in the lib/stats.agn file.
stats.moment (obj [, p [, $\mathbf{x}_{\mathrm{m}}$ [, option]]])
Computes the moment p of the given table, sequence or numarray obj about any origin $\mathrm{x}_{\mathrm{m}}$ for a full population and returns a number. It is equivalent to:

$$
\frac{1}{n} \sum_{i=1}^{n}\left(o b j_{i}-x_{m}\right)^{p}
$$

If only obj is given, the moment $p$ defaults to 1 , and the origin $x_{m}$ defaults to 0 . If given, the moment $p$ and the origin $x_{m}$ must be numbers. If obj contains less then two observations, fail will be returned.
if option is given and is true, the sample moment

$$
\frac{1}{n-1} \sum_{i=1}^{n}\left(\text { obj }_{i}-x_{m}\right)^{p}
$$

is computed.
See also: qmdev, stats.sumdata.
stats.nde (x [, [ $\mu,[\sigma]])$
Computes $e^{\frac{-(x-\mu)^{2}}{2 \sigma^{2}}} ; \mu$ and $\sigma$ default to 0 and 1 , respectively.
See also: stats.ndf, stats.pdf.
stats.ndf ([ $\sigma$ ])
Computes $\frac{1}{\sqrt{2 \pi}}$ if $\sigma$ is not given, and $\frac{1}{\sigma \sqrt{2 \pi}}$ otherwise, and issues an error if $\sigma \leq 0$.
See also: stats.nde, stats.pdf.

```
stats.neighbours (obj, idx, eps [, power [, indices]])
```

Determines all neighbours of a given n-dimensional point in a distribution obj that lie in a certain Euclidian distance eps. idx is the position of the point of interest in the distribution - a positive integer -, and not the point itself. eps is any positive number, power is a positive integer with which the respective Euclidean distances and eps shall be raised before a comparison is conducted, its default is 2 .

The return is a sequence with the nearby points. If the fifth argument indices is true, however, then not the points but their positions in the distribution are returned.

The points may be represented either as pairs (2-dimensional space), sequences of co-ordinates (n-dimensional space), or any n-dimensional vectors created by the linalg.vector function.

See also: linalg.norm, stats.dbscan.
stats.normald (x [, $\mu$ [, $\sigma]$ ])
The normal distribution has the probability density function:

$$
\exp \left(-(x-\mu)^{2} / 2 / \sigma^{2}\right) / \sqrt{2 \pi \sigma^{2}}
$$

$\sigma$ is the standard deviation and must be positive. $\mu$ defaults to 0 , and $\sigma$ to 1 .
See also: stats.cauchy, stats.chisquare, stats.fratio, stats.invnormald, stats.studentst.

```
stats.numbcomb (n, r)
stats.numbcomb (s,r)
```

In the first form, counts the number of combinations of $n$ things taken $r$ at a time. In the second form, the function counts the number of combinations all the elements in the set $s$ taken $r$ at a time. The set may include data of any type.

If $n$ or $r$ are non-integral or negative, the function returns undefined.
The function is implemented in Agena and included in the lib/stats.agn file.
See also: binomial, fact, stats.numbperm.
stats.numbpart ( $n, r$ )
Computes the number of partitions of $n$, the partition numbers, taken $r$ at a time. By default, $\mathrm{r}=\mathrm{n}$.

```
stats.numbperm (n, r)
stats.numbperm (s,r)
```

In the first form, counts the number of permutations of $n$ things taken $r$ at a time. In the second form, the function counts the number of permutations of all the elements in the set s taken $r$ at a time. The set may include data of any type.

If $n$ or $r$ are non-integral or negative, the function returns undefined.
The function is implemented in Agena and included in the lib/stats.agn file.

See also: binomial, fact, stats.numbcomb.

```
stats.obcount (s, p, n [, f])
stats.obcount (s, p [, option])
```

The function counts occurrences in an observation.
In the first form, it first divides a numeric range defined by the pair p and its step size n into its respective classes.

In the second form, if the option is classes=k, it first divides a numeric range defined by the pair p into k classes. If no option is passed, it automatically computes the number of classes according to the formula

$$
1+3.3 * \ln (\text { size of range } p \text { ), }
$$

with no upper limit. (It is suggested to choose between 5 or 30 classes.)
With both forms, all occurrences in the distribution s (a sequence) are then sorted into these subranges/classes and the function finally counts all elements in them. If the optional fourth argument $f$, a function, is given, then an occurrence or a part of an occurrence is first converted according to the function definition before the correct subinterval is being determined.

The function returns a table with the keys the respective left borders of the subranges and the values the number of counts in the respective subranges. It always also returns a second table which may include all those elements in s which are not part of the overall range defined by $p$. If all numbers in $s$ fit into $p$, an empty table will be returned.

If an element in s equals the right border of a subinterval, then it is considered to be part of the next subinterval. But if an element in s equals the right border of the overall interval $p$, it is considered part of the last subinterval.

The function issues an error if it encounters a non-number in s, or if the left border in $p$ is greater or equals to the right border in $p$.

The function is implemented in Agena and included in the lib/stats.agn file.
An example:

```
> s := seq(0.1, 0.2, 0.3, 0.4, 1, 1.1, 2, 2.1);
> stats.obcount(s, 0:2, 1):
[0 ~ 4, 1 ~ 3] [2.1]
```

See also: stats.freqd, stats.obpart.

```
stats.obpart (s, p, n [, f [, g]])
stats.obpart (s, p, option [, f [, g]])
```

The function sorts occurrences into subintervals (classes).
In the first form, it divides a numeric range defined by the pair $p$ and its step size $n$ into its respective subintervals, and sorts all occurrences in the distribution s (a sequence) into these classes.

In the second form, if the option is class=k, divides a numeric range defined by the pair $p$ into $k$ classes. If the option null, the function automatically computes the number of classes according to the formula

$$
1+3.3 * \ln (\text { size of range p) }
$$

with no upper limit. (It is suggested to choose between 5 or 30 classes.)
If the fourth argument $£$, a function, is given, then an occurrence or a part of an occurrence is first converted according to the function definition before the correct subinterval is being determined. If f is null, no conversion is done.

If the fifth argument g , a function, is given, then it is applied on an occurrence or part of it before it is inserted into the subinterval that already has been determined.

The function returns a table with the keys the respective left borders of the subranges and the values sequences with the respective occurrences. It always also returns a second table which may include all those elements in swich are not part of the overall range defined by $p$.

If an element in s equals the right border of a subinterval, then it is considered to be part of the next subinterval. But if an element in s equals the right border of the overall interval $p$, it is considered part of the last subinterval.
The function issues an error if a distribution or part of it is not or could not be converted to a number, or if the left border in $p$ is greater or equals to the right border in p .

The function is implemented in Agena and included in the lib/stats.agn file.

## See also: stats.obcount.

Examples:

```
> s := seq(1.1, 1.2, 2.4, 2.5, 2.6, 3.1);
> stats.obpart(s, 1:4, 1):
[seq(1.1, 1.2), seq(2.4, 2.5, 2.6), seq(3.1)]
```

Given are timestamps and running times in seconds:

```
> s := seq('12:30:05.017':3, '12:31:57.235':4);
```

To convert a timestamp into its decimal representation, so that stats.obpart can sort an occurrence into a subinterval, we define the following function:

```
> import clock
> f := proc(x) is
> local hrs, min, sec;
> hrs, min, sec :=
    strings.match(left(x), '(%d%d):(%d%d):(%d%d\.%d%d%d)');
    return clock.todec(clock.tm( # returns a number
        tonumber(hrs), tonumber(min), tonumber(sec)))
    end;
> stats.obpart(s, 12.4:12.6, 1/60, f):
[12.4 ~ seq(), ..., 12.5 ~ seq(12:30:05.017:3),
12.516667 ~ seq(12:31:57.235:4), ...] []
```

We only want to insert the running times in milliseconds, but not the timestamps:

```
> g := << x -> right(x)*1k >>;
> stats.obpart(s, 12.4:12.6, 1/60, f, g):
[12.4 ~ seq(), ..., 12.5 ~ seq(3000), 12.516667 ~ seq(4000), ...]
```


## See also: stats.obcount.

```
stats.pdf (x [, \mu [, \sigma]])
```

Computes the probability density function for the normal distribution at the numeric value x . The defaults are $\mu=0$, with standard deviation $\sigma=1$, thus determining the standard normal distribution.

The return is the number:

$$
\frac{1}{\sigma \sqrt{2 \pi}} e^{\frac{-(x-\mu)^{2}}{2 \sigma^{2}}}
$$

See also: stats.cdf, stats.nde, stats.ndf.
stats.peaks (obj, delta [, dv])
The function returns all peaks and valleys of a distribution obj consisting of two-dimensional numeric co-ordinates represented as pairs xk:yk. obj may be a table or sequence. A point is considered an extremum if the `vertical` difference to its surrounding is at least delta, a positive number. By default, if $d v$ is not given or is 1, the direct neighbours of each point are considered, otherwise the dv-th neighbours to the left and the right of each point are checked.

Depending on the type of 0 , the first return is a structure including all valleys represented as pairs xk:yk, and the second return is a structure of the peaks as pairs xk:yk.

See also: stats.extrema.
stats.percentile (obj, p [, option])
Returns the value below which a certain percent p of the elements in obj fall.
obj must be a table, sequence or numarray, $p$ an integer in the range $0 \leq p<100$. If no option is given, then the percentile is determined by computing the nearest rank (rank $=\mathrm{p} / 100$ * size obj $+1 / 2$, `Wikpedia method`). If option is the string 'nist', then the method proposed by NIST is used (rank = p/100 * (size obj +1 )); if the string 'excel' is given for option, then the algorithm used by Excel is used (rank $=\mathrm{p} / 100$ *(size obj -1) +1 ).

The function issues an error if obj is empty. It is implemented in Agena and included in the lib/stats.agn file.

## See also: whereis, stats.quartiles.

stats.prange (obj [, a [, b]])
Returns all elements in a table, sequence or numarray obj from the a-th percentile rank up but not including the b-th percentile rank. a and b must be positive integers in the range [0.. 100). If a and $b$ are not given, $a$ is set to 25 , and $b$ to 75 . If $b$ is not given, it is set to 100-a. The type of return is determined by the type of obj. If the elements in obj are not sorted in ascending order, the function automatically sorts them non-destructively, and any non-numeric values are converted to zeros.

## stats.probit (x)

Implements the quantile function associated with the standard normal distribution, or in other words: the inverse of the cumulative distribution function of the standard normal distribution for number x . It returns the number $\sqrt{2} \operatorname{erf}^{-1}(2 x-1)$.

```
stats.qcd (obj [, a [, b]])
```

Without a and b given, the function determines the interquartile range (IQR) of a distribution obj (a table, sequence or numarray), i.e. the difference of the third (= Q3) and first ( = Q1) quartile divided by the sum of the third and first quartile:

$$
\frac{Q_{3}-Q_{1}}{Q_{3}+Q_{1}}
$$

You may optionally pass a lower and upper percentile a, b, both in the range [0, 100). If $a$ is missing, it is set to 25 . If $b$ is missing it is set to $100-\mathrm{a}$.

If obj is unsorted, the function sorts it non-destructively. It is implemented in Agena and included in the lib/stats.agn file.

See also: stats.iqr, stats.percentile, stats.quartiles.

```
stats.qmean (obj)
```

Returns the quadratic mean (root mean square) of all numeric values in table, sequence or numarray obj as a number. If obj is table, it is assumed to be an array, non-positive integral keys (including strings, etc.) are ignored. It can be used to measure the magnitude of a quantity which variates are positive and negative, e.g. sinusoids.

It is equivalent to:

$$
\sqrt{\frac{1}{n} \sum_{i=1}^{n} o b j_{i}^{2}}
$$

The function returns fail if obj contains less than two elements.
The function is implemented in Agena and included in the lib/stats.agn file.

See also: stats.amean, stats.gmean, stats.hmean, stats.mean.

```
stats.quartiles (obj)
stats.quartiles (obj [, pos])
```

In the first form, it returns the first, second, and third quartile of table, sequence or numarray obj. The first and third quartiles are computed according to the NIST rule, see stats.percentile for further information.

It also determines the lower outlier limit $L_{1}$, where $L_{1}=$ first quartile - 1.5 times the interquartile range of obj, and the upper outlier limit $U_{1}$, where $U_{1}=$ third quartile + 1.5 times the interquartile range of obj. If a value $x$ in obj is equal to $L_{1}$ or $U_{1}$, then $x$ will be returned. If $L_{1}$ is not included in obj, then the next largest value to $L_{1}$ will be returned. If $U_{1}$ is not included in obj, then the next smallest value to $U_{1}$ is computed.

Finally it computes the interquartile range, i.e. third quartile - first quartile. The order is: first quartile, median, third quartile, ${ }^{\prime} L_{1}{ }^{`}, U_{1}$ ', and the interquartile range.

In the second form, if either the integer 1,2 , or 3 is passed for the optional second argument pos, the first, second, or third quartile will be returned as a number, respectively.

If the elements in obj are not sorted in ascending order, the function automatically sorts them non-destructively, and any non-numeric values are converted to zeros.

The number of values in obj should be at least 12, better are 20 or more values. if the number of values is less than 2 , fail will be returned.

See also: whereis, stats.fivenum, stats.iqr, stats.percentile, stats.qcd.

```
stats.rownorm (obj)
```

Returns the sum of the absolute values of the numbers in the table, sequence or numarray obj. If obj includes undefineds, they are ignored. If the structure consists entirely of one or more undefineds, then the function returns undefined. If the structure is empty, fail will be returned.

See also: stats.scale, stats.colnorm.

```
stats.scale (obj [, option])
```

The procedure normalises the numbers in the table or sequence obj in such a way that an element of maximum absolute value equals 1, thus scaling a distribution to the range $(-\infty, 1]$ by dividing all observations by this maximum element.

When given a second option, the function normalises all its observations to the range $[0,1]$. See math.norm for further details.

The normalised numbers are returned in a new table or sequence, depending on the type of obj.

If the maximum absolute value is 0 , the function returns fail.
See also: math.norm, linalg.scale.

```
stats.sd (obj [, sample [, option]])
```

Returns the standard deviation of all numeric values in table, sequence or numarray obj as a number. If obj is a table, it is assumed to be an array, non-positive integral keys (including strings, etc.) are ignored.

If sample is not given or is not true, it returns the population standard deviation:

$$
\sigma=\sqrt{\frac{1}{n} \sum_{i=1}^{n}\left(\mathrm{obj}_{i}-\mu\right)^{2}}
$$

where $\mu$ is the arithmetic mean of a distribution.
If sample is given and is true, the (unbiased) sample standard deviation will be returned:

$$
\sigma=\sqrt{\frac{1}{n-1} \sum_{i=1}^{n}\left(\mathrm{obj}_{i}-\mu\right)^{2}}
$$

If the return is a small number, it indicates that the points in a distribution are close to its mean m . A large value indicates that its points are rather spread out. Contrary to variance, standard deviation is expressed in the same units as the data.
Standard deviation is less robust to outliers than absolute deviation.

The function returns fail if obj contains less than two elements.
If any third non-null argument is given, then the coefficient $\sigma / \| \mu \mid$ will be returned to make different distributions comparable.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: qmdev, stats.ad, stats.chauvenet, stats.ios, stats.mad, stats.var.

## stats.skewness (obj)

Returns the sample skewness, a measure of the asymmetry of the probability distribution represented by the table or sequence obj of numbers. Returns 0 if a distribution is symmetric, a negative value if the left tail is longer, and a positive value if the right tail is longer.

It computes the third moment about the mean and divides it by the third power of the standard deviation.

The function returns fail if obj contains less than two elements.
The function is implemented in Agena and included in the lib/stats.agn file.

See also: stats.kurtosis.

```
stats.sma (obj, k, p)
stats.sma (obj, k, p, b)
```

In the first form, computes the simple moving average of a table or sequence obj by averaging the last p numbers from the structure ( p is also known as the `period`) including sample k, i.e.:

$$
\frac{1}{\mathrm{p}} \sum_{i=k-p+1}^{k} o b j_{i} \quad \text { (financial form) }
$$

In the second form, by passing the Boolean value true for argument $b$, the mean is taken from an equal number of values on either side of $k$, including $k$. Thus $p$ must be an odd number:

$$
\frac{1}{\mathrm{p}} \sum_{\mathrm{i}=\mathrm{k}-\mathrm{p} \backslash 2}^{\mathrm{k}+\mathrm{p} \backslash 2} \mathrm{obj}_{\mathrm{i}} \quad \text { (scientific form) }
$$

It returns undefined, if either the left or right end of the sublist to be evaluated is not part of obj. The function does not accept structures including the value undefined.

By dividing each element before summation, the function avoids arithmetic overflows and also uses Kahan-Babuška summation to prevent round-off errors during summation.
stats.gsma is the iterator version of this function which traverses large distributions much faster.

See also: stats.amean, stats.gsma, stats.gsmm, stats.smm.

```
stats.smallest (obj [, k])
```

Returns the $k$-th smallest element in the numeric table, sequence or numarray obj. If $k$ is not given, it is set to 1 .

```
stats.smm (obj, k, p)
stats.smm (obj, k, p, b)
```

In the first form, computes the simple moving median of a table or sequence obj by sorting the last p numbers from the structure ( p is also known as the `period`) including sample $k$, and then taking its median.

In the second form, by passing the Boolean value true for argument $b$, the simple moving median is determined by sorting an equal number of values on either side of $k$, including $k$, and then taking the median. Thus $p$ must be an odd number.

The function is more robust than stats.sma to outliers in a period.

It returns undefined, if either the left or right end of the sublist to be evaluated is not part of obj. The function does not accept structures including the value undefined.

The function automatically non-destructively sorts the distribution obj if it is unsorted.
stats.gsmm is the iterator version of this function which traverses large distributions much faster.

See also: stats.amean, stats.gsma, stats.gsmm, stats.sma.

```
stats.sorted (obj [, true] [, options])
```

Sorts the table or sequence obj of numbers in ascending order and non-destructively up to and around twice as fast as sort if the structure contains (around) more than seven elements. It also ignores undefined's. The type of return is defined by the type of the input.

If an element in obj is not a number, it is replaced with the number 0 before sorting.
By default, the function internally uses a recursive implementation of the Quicksort algorithm combined with a fallback to Heapsort in ill-conditioned situations, called Introsort.

You may exclusively use an iterative variant of the Quicksort algorithm by passing the second argument true or the string 'pixelsort', which may be faster on some older systems, especially with elements in completely random or in (nearly) ascending order. If the option 'nrquicksort' is given, an alternative non-recursive algorithm described by Niklaus Wirth is being used. If the option 'heapsort' is passed, the function uses the Heapsort algorithm. If the option 'quicksort' is given, a traditional recursive Quicksort algorithm is being used.

See also: sort, sorted, skycrane.sorted, stats.issorted, numarray.sort.

## stats.spread (obj)

Computes the population spread, i.e. the variance, of a distribution obj of numbers, and returns a number. The result is equal to:

$$
\frac{1}{n} \sum_{i=1}^{n} o b j_{i}^{2}-\frac{1}{n^{2}}\left(\sum_{i=1}^{n} o b j_{i}\right)^{2}
$$

The function is around 10 percent faster than stats.var but is more susceptible to numeric overflows if the magnitudes of the observations are very large.

The function is implemented in Agena and included in the lib/stats.agn file.
stats.standardise (obj [, option])
Standardises a distribution by subtracting the arithmetic mean $\mu$ from each observation and then dividing by the population standard deviation (default) $\sigma$ of the distribution:

$$
\mathrm{obj}_{\mathrm{i}} \rightarrow \frac{\mathrm{obj} j_{i}-\mu}{\sigma}
$$

Depending on the type of its argument obj, the return is either a new table or sequence of the respective quotients, preserving the original order of the observations. You may alternatively divide by the sample standard deviation by passing the optional value true as the second argument, obj may be a table, sequence or numarray.
stats.studentst (x [, nu])
The Student's t-distribution has the probability density function:

$$
\Gamma((\mathrm{nu}+1) / 2) / \Gamma(\mathrm{nu} / 2) / \sqrt{\mathrm{nu}^{\star} \pi} /\left(1++^{2} / \mathrm{nu}\right)^{\wedge}((\mathrm{nu}+1) / 2)
$$

with nu a positive integer.

## See also: stats.cauchy, stats.chisquare, stats.fratio, stats.normald.

```
stats.sum (obj)
stats.sum (f, obj [, ...])
```

The function has been deprecated, please use stats.sumdata instead.

```
stats.sumdata ([f, ] obj [, p [, xm [, ..]]]])
```

Sums up all the powers $p$ of the given table, sequence or numarray obj of $n$ elements about the origin $x_{\mathrm{m}}$ and returns a number. It is equivalent to:

$$
\sum_{i=1}^{n}\left(\text { obj }_{i}-x_{m}\right)^{p}
$$

If only obj is given, the power p defaults to 1 , and the origin $\mathrm{x}_{\mathrm{m}}$ defaults to 0 . If given, p and $\mathrm{x}_{\mathrm{m}}$ must be numbers. If obj is empty, the function returns fail.

If a function f is given, it only sums up the values in obj satisfying f , which should return a Boolean. If $f$ has more than one argument, then its second to last argument must be given right after $\mathrm{x}_{\mathrm{m}}$.

## Examples:

```
> import stats;
> stats.sumdata(<< x -> x > 2 >>, seq(1, 2, 3, 4)):
7
> stats.sumdata(<< x, y -> x + y > 2 >>, seq(1, 2, 3, 4), 1, 0, 1):
9
```

The function uses Kahan-Babuška round-off error prevention.

## See also: math.koadd, sumup, stats.cumsum, stats.fsum, stats.moment, stats.sumdataln.

```
stats.sumdataln ([f, ] obj [, p [, xm [, \cdots.]]])
```

Sums up all the natural logarithms of the powers $p$ of the given table, sequence or numarray obj of $n$ elements about the origin $x_{m}$ and returns a number. It is equivalent to:

$$
\sum_{i=1}^{n} \ln \left(\left(o b j_{i}-x_{m}\right)^{p}\right)
$$

If only obj is given, the power $p$ defaults to 1 , and the origin $x_{m}$ defaults to 0 . If given, $p$ and $x_{m}$ must be numbers. If obj is empty, the function returns fail.

If a function f is given, it only sums up the values in obj satisfying f , which should return a Boolean. If $f$ has more than one argument, then its second to last argument must be given right after $\mathrm{x}_{\mathrm{m}}$. For examples, please see stats.sumdata.
stats.tovals (obj)
Converts all string values in the structure obj to Agena numbers or complex numbers and returns a new structure. The type of return is determined by the type of obj.

```
stats.trimean (obj [, p])
```

If $p$ is not given, the function determines the 1st quartile Q1 and the 3rd quartile Q3 along with the median $Q 2$ of a distribution obj and returns the trimean ( $Q 1+2 * Q 2$ + Q3)/4 along with the median. obj may be a table, sequence or numarray.

If $p$, an integer in the range [0.. 100) is given, instead of the first and third quartiles the p-th and 100 - p-th percentile ranks are the lower and upper margins in the computation.

When compared to the median, the trimean is a means to determine whether a distribution is biased in its first or second half. If the distribution is not sorted, it
automatically sorts it non-destructively, where any non-numeric elements are set to 0 .

See also: stats.iqr, stats.trimmean, stats.winsor.
stats.trimmean (obj, f)
Returns the arithmetic mean of the interior of a distribution obj (a table, sequence or numarray), where the number $f \in[0,1)$ determines the fraction of the data that is to be excluded from the margins.

The number p of data to be excluded from obj is always rounded down to the nearest even number. The function then does not take into account $\mathrm{p} / 2$ points from the left margin and $\mathrm{p} / 2$ points from the right margin when calculating the average using Kahan-Babuška round-off error prevention. The function does not sort the distribution.

The return is a number. It returns fail, if the distribution includes less than two elements.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.amean, stats.winsor.
stats.var (obj [, sample [, option]])
Returns the variance of all numeric values in table, sequence or numarray obj as a number. If obj is a table, it is assumed to be an array, non-positive integral keys (including strings, etc.) are ignored.

If sample is not given or does not evaluate to true, the population variations will be returned, where $\mu$ is the arithmetic mean of a distribution:

$$
\sigma^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(\text { obj }_{i}-\mu\right)^{2}
$$

If sample is given and is true, the (unbiased) sample variance will be returned:

$$
\sigma^{2}=\frac{1}{n-1} \sum_{i=1}^{n}\left(\text { obj }_{i}-\mu\right)^{2}
$$

If option of any type is passed, the variation coefficient $\sigma^{2} /|\mu|$ is determined to make different distributions comparable.

The function returns fail if obj contains less than two elements.

The function is implemented in Agena and included in the lib/stats.agn file.
See also: stats.ad, stats.ios, stats.mad, stats.sd, stats.spread.
stats.weights (obj)
stats.weights (x [, ...])
In the first form, the function inserts all the elements in sequence obj into a new sequence and returns it.

In the second form, it inserts all the given arguments into a new sequence and returns it.

In both forms, only numbers and pairs are accepted in the sequence or argument list. In case of a pair $x: n, x$ denotes an observation and $n$, a non-negative integer, denotes the number of occurrence of $x$, so $x$ is inserted $n$ times into the new sequence.
stats.winsor (obj [, n])
Returns the winsorised mean of all numeric values in table or sequence obj.
The function first replaces the first n percent of a distribution at the low and high end with the most extreme remaining values, and then calculates the arithmetic mean of the entire modified distribution. By default, n is 10 .

The winsorised mean is more resistant to outliers than the traditional arithmetic mean.

See also: stats.trimean, stats.trimmean.

## stats.zscore (obj)

Returns a univariate function ${ }^{`} z(x)^{\prime}$ computing the $z$-score (standard score) of a sample $x$ in the table, sequence or numarray obj - the number of standard deviations x is above or below the mean according to the formula: $\mathrm{z}(\mathrm{x})=(\mathrm{x}-\mu) / \delta$, where $\mu$ denotes the arithmetic mean of obj, and $\delta$ its standard deviation.

The resulting function returns a positive number if $x$ is above the mean and $a$ negative number if it is below. It does, however, not check whether $x$ is part of obj. The result is computed using Kahan-Babuška round-off error prevention for $\mu$ and $\delta$.

The function is implemented in Agena and included in the lib/stats.agn file.

### 11.15 long - 80-Bit Floating-Point Arithmetic

This package implements 80-bit floating-point numbers and arithmetic. It is at least 80 times faster than the mapm package with the same precision.

Note that 80-bit floating-point arithmetic provided by this new package is still at least 12 times slower than Agena's built-in 64-bit arithmetic so it is useful only if you need extended precision with 19 significant digits and a range of approximately $3.65 \times 10^{-4951}$ to $1.18 \times 10^{4932}$.

As a plus package, it is not part of the standard distribution and must be activated with the import statement, e.g. import long. Example:

```
> import long;
> a, b := long.double(1), long.double(2)
> a + b:
longdouble(3.0000000000000000000)
> exp(a):
longdouble(2.7182818284590452354)
> long.tonumber(ans): # convert back to Agena number (64-bit)
2.718281828459
```

Note that relational operators such like $=$ or $<>$ cannot compare longdoubles with numbers as they are different types, and the result would always be false. Arithmetic binary operators, however, such like + , \%, however, can process a mix of numbers and longdoubles and return a longdouble as the result. Also, most unary operators and functions with one or two arguments can process both longdoubles and ordinary Agena numbers.

Creation, Conversion, Iteration:

## long.double (x)

Creates a longdouble from the ordinary Agena number $x$, returning a userdata of type longdouble with the longdouble metatable attached.
x may also be a string representing a number - with constants, you might prefer this to avoid round-off errors. For a predefined set of constants, also check the end of this subchapter.
long.tonumber ( x )
Converts the longdouble x into an ordinary Agena number, losing precision.

```
long.tostring (x [, format])
```

Converts the longdouble x into a string with 19 fractional digits by default. You can pass a string format that includes the ld specifier to control the output, e.g.

```
> long.tostring(long.Pi, "%.15ld"):
```

returns

### 3.141592653589793

long. count ([start [, step [, stop]]])
Returns an iterator function that, each time it is called, returns a new longdouble.
If no argument is given, the first number returned by the iterator is 0 , the next call returns 1, the next one 2, and so forth. This means that the longdouble returned with each call is increased by 1.

If only start is given, the first value returned by the iterator is start, the next call returns start +1 , the next one start +2 , and so forth. This means that the longdouble returned with each call is increased by 1.

If start and step are given, the first value returned by the iterator is start, the next call returns start + step, the next one start $+2^{*}$ step, and so forth. This means that the number returned with each call is increased by step, which may be negative. In the latter case the next value returned will be less than the current returned value.

If stop is given, the iterator returns null if the counter value exceeds stop. Default is + long.infinity.

If start or step are not longdoubles or numbers, the factory issues an error.
If start or step are non-integral, the function applies Neumaier summation to avoid round-off errors.

Example:

```
> import long;
> f := long.count(long.double(1), long.double(-0.1), long.double(-1));
> while c := f() do print(c) od; # counts down
```

A note in advance: All the functions and most of the operators are also available as functions which names always start with "long.x". So, for example, the sin operator is also available as the function long.xsin, and the math.chop function has the alias math.xchop.

Basic Arithmetic Operations:
$\mathbf{x} \pm \mathbf{y}$
The operator computes $\mathrm{x}+\mathrm{y}$, i.e. performs an addition.
$\mathbf{x}=\mathrm{y}$
The operator computes x-y, i.e. performs a subtraction.

## $\mathbf{x}$ * $\mathbf{y}$

The operator computes $x$ * y, i.e. performs a multiplication.
$\mathbf{x}$ / y
The operator computes x/y, i.e. performs a division.
$\mathbf{x} \boldsymbol{\perp}$
The operator computes $x \backslash_{\text {y }}$, i.e. performs an integer division.
$\mathbf{x}$ 응 $\mathbf{y}$
The operator computes x \% y, i.e. returns the modulus.
$\mathbf{x}$ 人 $\mathbf{y}$
The operator computes $\mathrm{x}{ }^{\wedge}{ }_{\mathrm{y}}$, i.e. raises x to the power of y , where y represent any arithmetic number.

## x ** y

The operator computes $x{ }^{* *} y$, i.e. raises $x$ to the power of $y$, where $y$ represent an integer.
recip (x)
The operator returns the inverse $1 / x$.
abs (x)
The operator will return the absolute value of x .

## sign (x)

Determines the sign of x . The result of the operator is determined as follows:

- 1 , if $x>0$,
- -1 , if $x<0$,
- undefined, if $x=$ undefined,
- O otherwise, even for -0.


## signum (x)

Determines the sign of $x$. The result of the operator is determined as follows:

- 1, if $x \geq 0$
-     - 1 otherwise.

```
long.copysign (x, y)
```

Returns a longdouble with the magnitude of $x$ and the sign of $y$, i.e. $\operatorname{abs}(x)$ * $\operatorname{sign}(y)$. If $y$ is 0 , then its sign is considered to be 1 .

## long.exponent ( x )

Returns the exponent $e$ of $x$ such that long.mantissa(x) * $2^{e}$ equals x .

## long.fma ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ )

Performs the fused multiply-add operation (x * y) + z, with the intermediate result not rounded to the destination type, to improve the precision of a calculation.

```
long.fmod (x, y)
```

Computes the remainder from the division of numerator x by denominator y . The return value is $\mathrm{x}-\mathrm{n}^{*} \mathrm{y}$, where n is the quotient of x divided by y , rounded towards zero to an integer.

## long.hypot (x, y)

Returns $\sqrt{x^{2}+y^{2}}$. It is the length of the hypotenuse of a right triangle with sides of length $x$ and $y$, or the distance of the point ( $x, y$ ) from the origin. The function is slower but more precise than using sqrt along with square, avoiding over- and underflow.

## long.hypot2 (x)

Returns $\sqrt{1+\mathrm{x}^{2}}$, avoiding over- and underflow.

## long.hypot3 (x)

Returns $\sqrt{1-x^{2}}$, avoiding over- and underflow.

## long.hypot 4 (x)

Returns $\sqrt{x^{2}-y^{2}}$, avoiding over- and underflow.

```
long.koadd (x, y [, q])
```

The function adds x and y using Kahan-Ozawa round-off error prevention and returns two longdoubles: the sum of $x$ and $y$ plus the updated value of the correction variable q. The optional correction variable q should be 0 at first invocation, and the previously returned correction variable otherwise - if q is not given, it defaults to 0 .

A typical usage should look like:

```
> x, q -> long.double(0);
> y := long.double('0.1');
> while x < long.double(1) do
    x, q := long.koadd(x, y, q)
od;
print(s + q);
```

long.fdim (x, y)

Computes $\mathrm{x}-\mathrm{y}$ if $\mathrm{x}>\mathrm{y}$, and return 0 otherwise.

## long.mantissa (x)

Returns the mantissa $m$ of $x$ such that $m *{ }^{\wedge}$ long.exponent(x) equals $x$. See also: long.significand.

## long.modf (x)

Returns the integral part of x and its fractional part. The integral part is rounded towards zero. Both the integral and fractional part of the return have the same sign as x . The sum of the two values returned equals x .

## long.pytha (a, b)

Computes the Pythagorean equation $c^{2}=a^{2}+b^{2}$, without undue underflow or overflow, for longdoubles or numbers $a, b$.

## long.pytha4 (a, b)

Computes $a^{2}-b^{2}$, without undue underflow or overflow, for longdoubles or numbers a, b.

## long.significand (x)

Returns the mantissa of $x$ in a normalised form, in the range[1, 2), with long.significand( x ) $=2$ *long.mantissa( x ) $=$ long.ldexp( x , -long.ilog2( x )). If x is 0 , the return is 0 .

## Relations:

A note in advance: The 80-bit infinity representation is represented by the constant long.infinity and not infinity, and that of "undefined" is long.undefined.
$\mathbf{x}$ 三 $\mathbf{y}$
The binary operator returns true if x is exactly equal to y , and false otherwise.

## x <> Y

The binary operator returns true if x is not exactly equal to y , and false otherwise.

## $\mathbf{x}$ ~= $y$

The binary operator returns true if x is approximately equal to y , and false otherwise. See also long.approx.

## $\mathbf{x}$ <br> ~<> Y

The binary operator returns false if x is approximately equal to y , and trueotherwise.

## $\mathbf{x} \leq \mathrm{y}$

The binary operator returns true if x is less than y , and false otherwise.

## $\mathrm{x} \leq=\mathrm{Y}$

The binary operator returns true if x is less than or equal to y , and false otherwise.

## $\mathbf{x} \geq \mathbf{y}$

The binary operator returns true if x is greater than y , and false otherwise.

## $\mathbf{x} \geq=\mathrm{y}$

The binary operator returns true if x is greater than or equal to y , and false otherwise.

```
long.isequal (x, y)
```

Compares x with y and returns true if $\mathrm{x}=\mathrm{y}$, and false otherwise.
long.isunequal ( $\mathrm{x}, \mathrm{y}$ )
Compares x with y and returns true if $\mathrm{x}<>\mathrm{y}$, and false otherwise.

```
long.isless (x, y)
```

Compares x with y and returns true if $\mathrm{x}<\mathrm{y}$, and false otherwise.

```
long.islessequal (x, y)
```

Compares x with y and returns true if $\mathrm{x}<=\mathrm{y}$, and false otherwise.

```
long.approx (x, y [, eps])
```

Compares the x and y and checks whether they are approximately equal. If eps is omitted, Eps is used.

The algorithm uses a combination of simple distance measurement ( $|x-y| \leq e p s$ ) suited for values `near` 0 and a simplified relative approximation algorithm developed by Donald H. Knuth suited for larger values $(|x-y| \leq e p s * \max (|x|$, $|\mathrm{y}| \mathrm{I})$, that checks whether the relative error is bound to a given tolerance eps.

The function returns true if x and y are considered equal or false otherwise. If both a and b represent infinity, the function returns true. The same applies to a and b being -infinity or undefined.

```
long.fmax (x, y)
```

Returns x if $\mathrm{x}>\mathrm{y}$, and y otherwise.
long.fmin ( $x, y$ )
Returns x if $\mathrm{x}<\mathrm{y}$, and y otherwise.

Powers and Roots:
square ( x )
The operator squares x and returns $\mathrm{x} * 2$.
cube ( $x$ )
The operator raises $x$ to the power of 3 .

## $\mathbf{x}$ squareadd $\mathbf{c}$

The operator computes $x^{\wedge} 2+c$, preventing round-off errors. See also long.fma.

```
sqrt (x)
```

Returns the square root of x .

If x is a number and negative, the operator returns undefined.

```
long.cbrt (x)
```

Returns the cubic root of the number $x$.
long.root (x [, n])
Returns the non-principal $n$-th root of $x$. n must be an integer and is 2 by default. Note that since the function computes the non-principal root.

```
invsqry (x)
```

The operator computes the inverse square root x, i.e. $1 /$ sqri(x).

Exponentiation \& Logarithms:

```
antilog2 (z)
```

The operator computes $2^{2}$, i.e. 2 raised to the power of $z$.

```
antilog10 (z)
```

The operator computes $10^{2}$, i.e. 10 raised to the power $z$.

## $\exp (x)$

Exponential function; the operator returns the value $e^{\mathrm{x}}$, with e Euler's number.

## long.expminusone (x)

Returns a value equivalent to $\exp (x)$ - 1. It is computed in a way that is accurate even if $x$ is near 0 , since $\exp (\sim 0)$ and 1 are nearly equal.
$\ln (x)$
Natural logarithm of $x$ with the base $e^{1}$. If $x$ is non-positive, the operator returns undefined.

## long.lnplusone (x)

Returns a value equivalent to $\ln (1+x)$. It is computed in a way that is accurate even if x is near zero.

## $\log (x, b)$

The operator returns the logarithm of x to the base b .

## long.log2 (x)

Returns the base-2 logarithm of x .
long.ilog2 (x)
Returns the integral base-2 logarithm of x .

## long.log10 (x)

Returns the base-10 logarithm of x .

Trigonometric Functions and Operators:
$\sin (x)$
The operator returns the sine of x (in radians).
$\cos (x)$
The operator returns the cosine of x (in radians).
$\tan (x)$
The operator returns the tangent of $x$ (in radians).

## long.csc (x)

The function returns the secant of x (in radians), i.e. $1 / \sin (\mathrm{x})$.

```
long.sec (x)
```

The function returns the secant of x (in radians), i.e. $1 / \cos (\mathrm{x})$.

```
long.cot (x)
```

The function returns the cotangent of x (in radians), i.e. $1 / \tan (\mathrm{x})$.
sinc ( $x$ )
The operator returns the un-normalised cardinal sine of $x$ (in radians), i.e. $\boldsymbol{\operatorname { s i n }}(\mathrm{x}) / \mathrm{x}$, with sinc(long.double(0)) = long.double(1).

## Hyperbolic Trigonometric Functions and Operators:

sinh (x)
The operator returns the hyperbolic sine of x (in radians).
cosh (x)
The operator returns the hyperbolic cosine of $x$ (in radians).

## $\tanh (x)$

The operator returns the hyperbolic tangent of x (in radians).

Inverse and Inverse Hyperbolic Trigonometric Functions and Operators:

## $\arccos (x)$

The operator returns the inverse cosine operator ( $x$ in radians).

## long.arccosh (x)

The function computes the inverse hyperbolic cosine of x (in radians).

## arcsin (x)

The operator computes the inverse sine operator (in radians).

## long.arcsinh (x)

The function returns the inverse hyperbolic sine of $x$ (in radians).

## $\arctan (x)$

The operator computes the inverse tangent operator (in radians).

## long.arctanh (x)

The function returns the inverse hyperbolic tangent of x (in radians).

## long.arccsc (x)

The function returns the inverse cosecant of $x$ (in radians).
$\operatorname{arcsec}(x)$
The operator returns the inverse secant of $x$ (in radians).

## long.arccot (x)

The function returns the inverse cotangent of x (in radians).

## Error Functions:

```
long.erf (x)
```

Returns the error function of number $x$. It is defined by $\operatorname{erf}(x)=\frac{2}{\sqrt{\pi}} \int_{t=0}^{x} e^{-\dagger \wedge} 2$.

## long.erfc (x)

Returns the complementary error function of x . It is defined by $\operatorname{erfc}(\mathrm{x})=1-\operatorname{erf}(\mathrm{x})$.

Rounding \& Related:

## long.ceil (x)

Rounds upwards to the nearest integer larger than or equal to x .

## entier (x)

The operator rounds x downwards to the nearest integer. Same as:

## long.floor (x)

Rounds x downwards to the nearest integer. Also: long.floor(x) $=$ ceil $(x)=-e n t i e r(-x)$.

## int (x)

The operator rounds x to the nearest integer towards zero.

## frac (x)

The operator returns the fractional part of $x$, i.e. $x-\operatorname{int}(x)$, preserving the sign.

```
long.round (x [, d])
```

Rounds x to its d -th digit, using the round-half-up method. If a is omitted, the longdouble is rounded to the nearest integer. If a is positive, the function rounds to the $d$-th fractional digit. If $d$ is negative, it rounds to the $d$-th integral digit. long.round treats positive and negative values symmetrically, and is therefore free of sign bias.

```
long.chop (x [, eps [, method [, n]]]])
```

Shrinks x more or less near zero to exactly zero, using one of several methods, passed as an integer. The default for eps is DoubleEps. The standard method is 0 for hard shrinking. Integral $n$ is used in the SmoothGarrote method.
$\left.\left.\begin{array}{|c|l|c|l|}\hline \text { method } & \text { Comment } & \text { Value } & \text { Domain } \\ \hline 0 & \text { "Hard", performs hard shrinking } & 0 & |x| \leq e p s \\ x & 0 & |x|>e p s\end{array} \right\rvert\, \begin{array}{l}|x| \leq e p s \\ |x|>e p s\end{array}\right]$

Method 2 has not been implemented.

Checks:
nonzero (x)
Checks whether x is not 0 . The operator returns true or false.
zero (x)
Checks whether x is 0 , respectively. The operator returns true or false.
even (x)
Checks whether x is even. The operator returns true if x is even, and false otherwise. With non-integral numbers, the operator returns false.
odd (x)
The operator checks whether x is odd. The operator returns true if x is odd, and false otherwise. With non-integral longdoubles, the operator returns false.

## float (x)

Checks whether $x$ has a fraction, i.e. not integral, and returns true or false.
With +/-infinity and undefined, returns false.

## integral (x)

Checks whether x is integral, i.e. does not contain a fraction, and returns true or false.

With $+/$-infinity and undefined, returns false.

```
finite (x)
```

The operator checks whether x is neither $\pm$ infinity nor undefined. The operator returns true or false.
nan (x)
Checks whether x evaluates to undefined. The operator returns true or false.

## Miscellaneous:

```
long.eps ([x [, option]])
```

The function returns the machine epsilon, the relative spacing between $|x|$ and its next larger longdouble in the machine's floating point system. If no argument is given, $x$ is set to 1 .

When given any second argument, the function computes a `mathematical epsilon value that is also dependent on the magnitude of its argument x. It can be used in difference quotients, etc., for it prevents huge precision errors with computations on very small or very large numbers. The mathematical epsilon with respect to x is equal to x * sqri(long.eps( x )).

```
long.gsolve (A)
long.gsolve (A, v)
```

Performs Gaussian elimination on a system of linear equations.
In the first form, a must be an augmented $m \times n$ matrix created with linalg.matrix with $\mathrm{m}+1=\mathrm{n}$. In the second form, A is a square matrix and v a right-hand side vector, created with linalg.vector.
linalg.matrix and linalg.vector accept standard Agena numbers only, so the input is 64 -bit precision but the output is 80 -bit.

The return is the solution vector with longdoubles. It returns infinity if an infinite number of solutions has been found, and undefined if no solutions exists. It returns fail if it could not determine whether no or an infinite number of solutions exist.

Example:

```
> import linalg, long
> A := linalg.matrix([1, 1, 1, 2], [6, -4, 5, 31], [5, 2, 2, 13]):
[ 1, 1, 1, 2 ]
[ 6, -4, 5, 31 ]
[ 5, 2, 2, 13 ]
> long.gsolve(A):
[longdouble(3.000000..), longdouble(-2.000000..), longdouble(0.999999..)]
```


## long.nextafter ( $\mathbf{x}, \mathrm{y}$ )

Returns the next machine floating-point number of x in the direction toward y .
long.norm (x, a1:a2 [, b1:b2])
Converts x in the scale $\left[\mathrm{a} 1, \mathrm{a}_{2}\right.$ ] to one in the scale $[\mathrm{b} 1, \mathrm{~b} 2$. The second and third arguments must be pairs of longdoubles. If the third argument is missing, then x is converted to a longdouble in [0, 1].
long.rempio2 (x [, option])
Conducts an argument reduction of x into the range $|\mathrm{y}|<\frac{\pi}{2}$ and returns $\mathrm{y}=\mathrm{x}$ $N * \frac{\pi}{2}$. If any option is given, then the function also returns $N$, or actually the last three digits of N . The number of operations conducted are independent of the exponent of the input.

## long.unm (x)

Negates a number or longdouble x and returns it, same as the expression -x .

```
long.wrap (x [, a [, b]])
```

Conducts a range reduction $x$ to the interval $[a, b)$. If $x \in[a, b)$, $x$ is simply returned.
In the second form, if $a$ is not given, $a$ is set to $-\pi$ and $b$ to $+\pi$. If $a$ is given but not $b$, $a$ is set to -a and b to +a , so a should be positive.

## long.signbit (x)

Checks whether x has its sign bit set and returns true or false. For example, although $-0=0$, long.signbit $(-0) \Rightarrow$ true and long.signbit $(0) \Rightarrow$ false.

## long.frexp (x)

Returns the mantissa $m$ and the exponent $e$ of $x$ such that $x=m 2^{e}$. e should be integral, and the value of $m$ is in the range $[0.5,1$ ) (or zero when $x$ is zero). The operation is bijective, i.e. long.Idexp(long.frexp(x)) = x.
long.ldexp (m, e)
Returns $m 2^{e}$ (e should be integral).
long.multiple (x, y [, option])
Checks whether $x$ is a multiple of $y$, i.e. whether $x / y$ evaluates to an integral, and returns true or false.

Also returns true with $\mathrm{x}=0$ and any non-zero y .
If $y$ is zero, long.undefined or +/-long.infinity, the function returns fail.
By passing the optional third argument true, a tolerant check is done, with subnormal x or y first converted to zero, and a subsequent approximate equality check to the nearest integer of $x / y$. The tolerance value internally used is the value of DoubleEps at the time of the function call.

In most cases, it may suffice to just call integral(x/y).

IEEE:
long.fpclassify (x)
For the given x , returns

- long.fp_nan if x is undefined,
- long.fp_infinite if x is infinite, i.e. +/-infinity,
- long.fp_subnormal if $x$ is subnormal,
- long.fp_zero if $x$ is zero,
- long.fp_normal if $x$ is normal, including irregular values $\geq 2^{52}$.


## long.isundefined (x)

Returns true if long.fpclassify $(\mathrm{x})=$ long.fp_nan, and false otherwise.

```
long.isinfinite (x)
```

Returns true if long.fpclassify(x) = long.fp_infinite, and false otherwise.

```
long.iszero (x)
```

Returns true if long.fpclassify(x) = long.fp_zero, and false otherwise.

```
long.isnormal (x)
```

Returns true if long.fpclassify $(\mathrm{x})=$ long.fp_normal, and false otherwise.

## long.issubnormal (x)

Returns true if long.fpclassify $(\mathrm{x})=$ long.fp_subnormal, and false otherwise.

## long.isfinite (x)

Returns true if long.fpclassify(x) $<>$ long.fp_nan and long.fpclassify(x) $<>$ long.fp_infinite, and false otherwise.

Available constants are:

| Constant | Value | Comment |
| :--- | :--- | :--- |
| long.Pi | $\pi$ |  |
| long.Pi2 | $2 \pi$ |  |
| long.PiO2 | $\pi / 2$ |  |
| long.PiO4 | $\pi / 4$ | radians per degree |
| long.PiO180 | $\pi / 180$ |  |
| long.InvPi2 | $1 /(2 \pi)$ |  |
| long.InvPiO4 | $4 / \pi$ |  |
| long.InvPiSqO4 | $4 / / \pi^{2}$ |  |
| long.E | $\mathrm{E}=\mathrm{exp}(1)$ |  |
| long.sqrt2 | $\sqrt{2}$ |  |
| long.sqrt3 | $\sqrt{3}$ |  |
| long.In2 | $\ln (2)$ |  |
| long.Invln2 | $1 / \ln (2)$ | Golden Ratio |
| long.Invsqrt2 | $1 / \sqrt{2}$ |  |
| long.Phi | $(1+\sqrt{5}) / 2$ | logarithm of Golden Ratio |
| long.InvPhi | $1 /((1+\sqrt{5}) / 2)$ | inverse |
| long.InvPhiSq | $1 /((1+\sqrt{5}) / 2))^{2}$ | zero |
| long.InPhi | $\ln (1+\sqrt{5}) / 2$ |  |
| long.InvlnPhi | $1 / \ln (1+\sqrt{5}) / 2$ |  |
| long.naught | 0 |  |
| long.nought | 0 |  |
| long.one | 1 |  |
| long.two | 2 |  |
| long.three | 3 |  |
| long.four | 4 |  |
| long.five | 5 |  |
| long.six | 6 |  |
| long.seven | 7 |  |
| long.eight | 8 |  |
| long.nine | 9 |  |
| long.ten | 10 |  |
| long.eleven | 11 |  |
| long.twelve | 12 |  |
| long.fifty | 50 |  |
| long.hundred | 100 |  |
| long.thousand | 1,000 |  |
| long.half | 0.5 |  |
| long.quarter | 0.25 |  |
| long.tenth | 0.1 |  |
| long.fifth | 0.2 |  |
| long.hundredth | 0.01 |  |
| long.thousandth | 0.001 |  |
| long.threequarter | 0.75 |  |
| long.third | $1 / 3$ |  |
|  |  |  |


| Constant | Value | Comment |
| :--- | :--- | :--- |
| long.sixth | $1 / 6$ |  |
| long.eighth | 0.125 |  |
| long.twelfth | $1 / 12$ |  |
| long.sixteenth | 0.0625 |  |
| long.infinity | infinity |  |
| long.undefined | undefined |  |

These constants have all been defined in source file lib/long.agn.

Chapter Twelve

## Input \& Output

## 12 Input \& Output

## 12.1 io - Input and Output Facilities

The I/O library provides two ways for file manipulation.

Summary of functions:
Opening and closing files:
io.open, io.close.
Reading data:
io.input, io.lines, io.read, io.readfile, io.readlines.
Writing data:
io.output, io.write, io.writefile, io.writelines.
File positions:
io.eof, io.filepos, io.move, io.seek, io.skiplines.
File locking:
io.lock, io.unlock.
File buffering:
io.setvbuf, io.sync
Interaction with applications:
io.pcall, io.popen, io.close
Keyboard interaction:
io.anykey, io.getkey, io.kbdgetstatus, io.keystroke
Windows clipboard interaction
io.getclip, io.putclip.

## Miscellaneous:

## io.clearerror, io.ferror, io.fileno, io.filesize, io.isfdesc, io.mkstemp, io.nlines, io.isopen, io.tmpfile, io.truncate.

Usage:

1. The first one uses file handles; that is, there are operations to set a default input file and a default output file, and all input/output operations are over these default files. File handles are values of type userdata and are used as in the following example:

Open a file and store the file handle to the name fh :

```
> fh := io.open('d:/agena/src/change.log'):
file(7803A6F0)
```

Read 10 characters:

```
> io.read(fh, 10):
Change Log
```

Close the file:

```
> io.close(fh):
true
```

In the following descriptions of the io functions, file handles are indicated with the argument filehandle.

The table io provides three predefined file handles with their usual meanings from C: io.stdin, io.stdout, and io.stderr.
2. The second style uses file names passed as strings like 'd:/agena/lib/library.agn'. File names are always indicated with the argument filename in this chapter.

Unless otherwise stated, all I/O functions return null on failure (plus an error message as a second result) and some value different from null on success.
io.anykey ()
Checks whether a key is being pressed and returns either true or false. A common usage is as follows:

```
> while io.anykey() = false do od; # wait until a key has been pressed
```

The function works in the OS/2, Solaris, Linux, DOS, and Windows editions only. On Lion, the function sometimes echoes the key being pressed. On other systems, it returns fail.

See also: io.getkey, io.read.
io.clearerror (filehandle)
Clears the end-of-file and error indicators for the file denoted by filehandle. The function returns nothing.

## See also: io.eof, io.ferror.

io.close ([filehandle, ...])
Closes one or more files. Note that files are automatically closed when their handles are garbage collected, but that takes an unpredictable amount of time to happen.

Without a filehandle, closes the default output file.
The function also deletes the file handles and the corresponding filenames from the io.openfiles table if the files could be properly closed.

The function returns true on success and false otherwise. With pipes, also returns the exit code of the application run.

See also: io.open, io.popen.

```
io.eof (filehandle)
```

Checks whether the end of the file denoted by filehandle has been reached and returns true or false.

See also: io.clearerror, io.ferror.

```
io.ferror (filehandle)
```

Checks the error indicator for the file denoted by filehandle and returns true if set or false if not set.

See also: io.clearerror, io.eof.

```
io.fileno (filehandle)
```

Returns the file descriptor, an integer, associated with the stream referenced by filehandle, which is of type userdata/file. It is useful for informative purposes, only.

The return cannot be used as a substitute to filehandle in calls to io functions, and which require a handle of type userdata/file.

The function issues an error if filehandle is not of type userdata/file or if does not reference an open file.

See also: io.isfdesc.
io.filepos (filehandle)
Returns the current position in the file denoted by its file handle filehandle, and returns a non-negative number.

See also: io.seek.

```
io.filesize (filehandle)
```

Returns the size of an open file denoted by its file handle filehandle and returns the number of bytes as a non-negative integer.

```
io.getclip ()
```

Returns the contents of the Windows clipboard as a string. If the clipboard could not be accessed, it returns fail plus an error string. It also returns fail and an error string, if the clipboard contains a binary object.

The function is available in the Windows edition only.
See also: io.putclip.
io.getkey ([anything])
If no argument is given, waits until a key is pressed and returns its ASCll number. If any argument is passed, the function waits until a key is pressed, but returns nothing.

The function is available in the OS/2, Solaris, Linux, Mac OS X, DOS, and Windows editions only.

See also: io.anykey, io.read.
io.infile (filename, pattern)
io.infile (filehandle, pattern)
Checks whether the file given by the name filename or the file denoted by its descriptor filehandle includes a pattern of type string, and returns true or false. The function supports pattern matching.

See also: io.readfile, utils.findfiles.

```
io.input (filehandle)
io.input (filename)
io.input ()
```

When called with a file name, it opens the named file (in text mode), and sets its handle as the default input file. When called with a file handle, it simply sets this file handle as the default input file. When called without parameters, it returns the current default input file.

In case of errors this function raises the error, instead of returning an error code.

```
io.isfdesc (filehandle)
```

Checks whether filehandle is a valid file handle. Returns true if filehandle is an open file handle, or false if filehandle is not a file handle.

See also: io.fileno, io.isopen.

```
io.isopen (filehandle)
```

Checks whether filehandle references an open file. Returns true if $f$ ilehandle is an open file handle, or false if filehandle is not a file handle. Thus it also returns false if filehandle is not of type userdata/file. Contrary to io.isfdesc, it also detects invalid file positions caused by files too large or if the stream referenced by filehandle does not support file positioning.

Please note that the function cannot detect whether a file has been opened by another application.

The function is five times slower than io.fdesc.

See also: io.fileno, io.isfdesc.
io.kbdgetstatus ()
OS/2 only: Get status information about the keyboard. The function returns a table with the contents of the KBDINFO structure after the call to the C API function KbdGetStatus. See http://www.edm2.com/index.php/KbdSetStatus_(FAPI) for the meaning of the results.

## io.keystroke (c)

Windows only: emulates a keystroke for the given ASCII value (an integer) c and dumps the character representing c to the currently active window. For security, newlines, carriage returns, and CTRL-Z's will not be accepted as input.

```
io.lines (filename)
io.lines (filehandle)
io.lines ()
```

In the first form, the function opens the given file denoted by string filename in read mode and returns an iterator function that, each time it is called, returns a new line from the file.

In the second form, the function opens the given file in read mode and returns an iterator function that, each time it is called, returns a new line from the file.

Therefore, the construction

```
for keys line in io.lines(f) do body od
```

will iterate over all lines of the file denoted by $£$, where f is either a file name or file handle. When the iterator function detects the end of file, it returns null (to finish the loop) and automatically closes the file if a filename is given. In case of a file handle, the file is not closed.

The call io.lines() (without a file name) iterates over the lines of the default input file. In this case it does not close the file when the loop ends.

See also: io.readlines.

```
io.lock (filehandle)
io.lock (filehandle, size)
```

The function locks the file given by its handle filehandle so that it cannot be read or overwritten by other applications.

In the first form, the entire file is locked in UNIX-based systems. In Windows, only $2^{63}$ bytes are locked, so you have to use the second form described below in Windows after the file has become larger than $2^{63}$ bytes ( $=8,589,934,592$ GBytes).

In the second form the function locks size bytes from the current file position. Locked blocks in a file may not overlap. size may be larger than the current file length.

The function returns true on a successful lock, and false otherwise.

Note that other applications that do not use the locking protocol may nevertheless have read and write access to the file.

See also: io.unlock.

```
io.maxopenfiles ([n])
```

In Solaris, Linux Mac OS X and Windows, returns the maximum number of open files, minus 2 for stdin \& stdout, if no argument is given - or sets the maximum number of files that are allowed to be opened simultaneously if an integer $n$ is given.

On OS/2 and DOS, returns the maximum number of open files, but you cannot change this number.

On the platforms given above, when n is not given, returns undefined in case of errors. On all other platforms, the function always returns undefined.

```
io.mkstemp (template)
```

The function creates a unique temporary filename from the given template, $a$ string, which must always end with six (capital) x's and returns it as a string. It also creates a file of the same name, but does not open it.

Example: io.mkstemp('filexxxxxx').
See also: io.tmpfile, os.remove, os.tmpdir, os.tmpname.
io.move (filehandle, $n$ )
Moves the current file position of the open file denoted by its filehandle either to the left or the right.

If n is a positive integer, then the file position is moved n characters to the right, if it is a negative integer, it is moved $n$ characters to the left. If $n$ is zero, the position is not changed at all.

The function returns true on success and false otherwise.
See also: io.seek.

```
io.nlines (filename)
```

io.nlines (filehandle)

The function counts the number of lines in the (text) file denoted by filename or filehandle and returns a non-negative integer.

See also: io.skiplines.
io.open (filename [, mode])
This function opens a file, given by the string filename, in the mode specified in the string mode. It returns a new file handle of type userdata/file. The function does not lock the file (see io.lock).

The function also enters the newly opened file into the io.openfiles table in the following format: [filehandle $\sim$ [filename, mode]].

In case of errors, the function quits with an error.
The mode string can be any of the following:

- 'r', 'read': read mode (the default);
- 'w', 'write': write mode only; if the file already exists, it is truncated to zero length;
- 'a', 'append': append mode;
- 'r+': update mode (both reading and writing), all previous data is preserved; the initial file position is at the beginning of the file;
- 'w+': update mode (reading and writing), all previous data is erased;
- 'a+': append update mode (reading and appending), previous data is preserved, writing is only allowed at the end of file.

The mode string may also have a 'b' at the end, which is needed in some systems to open the file in binary mode. This string is exactly what is used in the standard C function fopen.

See also: io.close, io.lock.
io.output ([filehandle])
Similar to io.input but operates over the default output file.
io.pcall (prog [, mode])
Starts programme prog (passed as a string) in a separated process, sends and receives data to this programme via stdout - if mode is ' $r$ ', or mode is not given -, or writes data to this programme if mode is 'w'. After communication finishes, the connection is automatically closed.

The return is a sequence of strings containing the result sent back by the application.

The function thus is a combination of io.popen, io.readlines, and io.pclose, has been written in Agena, and is included in the main Agena library (lib/library.agn).

This function is system dependent and is not available on all platforms.
See also: remove, select, os.execute.

```
io.popen ([prog [, mode]])
```

Starts programme prog in a separated process and returns a file handle that you can use to read data that is sent from this programme (if mode is ' $r$ ', the default) via stdout, or to write data to this programme (if mode is 'w').

Use io.close to close the connection.
The following example shows how to receive the output of the UNIX `Is` command:

```
> p := io.popen('ls -l', 'r'):
file(779509B8)
> for keys i in io.lines(p) do print(i) od;
total }191
drwxrwxrwx 1 user group 0 Oct 12 17:00 OS2
-rw-rw-rw- 1 user group 24481 Oct 13 18:23 aauxlib.c
-rw-rw-rw- 1 user group 6205 Aug 10 02:26 aauxlib.h
-rw-rw-rw- 1 user group 16067 Oct 12 23:42 aauxlib.o
> io.close(p):
true 0
```

This function is system dependent and is not available on all platforms.
See also: os.execute, io.close, io.pcall.

```
io.putclip (str)
```

Copies the string str to the Windows clipboard. If the clipboard could not be accessed, it returns fail plus an error string. It only returns fail, if something else went wrong, and true on success.

The function is available in the Windows edition only.
See also: io.getclip.

```
io.read (filehandle [, format])
```

io.read ()
In the first form, reads the file with the given filehandle, according to the given formats, which specify what to read. For each format, the function returns a string (or a number) with the characters read, or null if it cannot read data with the specified format. When called without formats, it uses a default format that reads the entire next line (see below).

The available formats are

- ' ${ }_{\mathrm{n}}$ ': reads a number; this is the only format that returns a number instead of a string. Hexadecimal numbers and numbers in scientific E notation are accepted, too. It also processes floats that include the decimal point separator of the current locale that may be different from a dot.
- '*a': reads the whole file, starting at the current position. On end of file, it returns the empty string ${ }^{22}$.
- '*1': reads the next line (skipping the end of line), returning null on end of file. This is the default format.
- '*L' : reads the next line keeping the end-of-line character.
- number: reads a string up to this number of characters, returning null on end of file. If number is zero, it reads nothing and returns an empty string, or null on end of file.

In the second form, the function reads from the default input stream (usually the keyboard) and returns a string or number.

Note that you can write to stdin by passing the constant io.stdin as a file handle.

```
See also: io.lines, io.readfile, io.readlines, skycrane.readcsv, utils.readcsv, utils.readxml.
```

io.readfile (filename [, removenlcr [, pattern [, flag]]])
io.readfile (filhandle [, removenlcr [, pattern [, flag]]])
Reads the entire file with name filename or the file denoted by its handle filehandle in binary mode and returns it as a string. Note that contrary to io.readlines, the function also returns carriage returns (ASCll code 13).

If a second argument removenlcr is the Boolean value true, has been passed, then the function removes all newlines and if existing all carriage returns at the end of each line. If it is false, no such deletions are performed.

If the optional third argument pattern is given, the function only returns the whole contents of a file if the string pattern has been found in the file. Pattern matching is supported.

If the optional fourth argument flag is false, the function returns the whole file contents file if the string pattern has not been found in the file.

See also: io.infile, io.read, io.readlines, io.writefile.

[^3]```
io.readlines (filename [, options])
io.readlines (filehandle [, options])
```

Reads the entire file with name filename or file handle filehandle and returns all lines in a table.

If a string consisting of one or more characters is given as a further argument, then all lines beginning with this string are ignored. If the option true is passed, then diacritics in the file are properly converted to the console character set, provided you use code page 1252. You can mix the options in any order. The function automatically deletes carriage returns (ASCII code 13) if included in the file.

You can also pass a function of one variable: in this case the function is applied on all the lines being read in and the function call results are inserted into the resulting table instead of the original lines. A line is only transformed if the line has not been skipped, see the string option mentioned above. Example:

```
> # convert all lines to upper-case, but skip all lines starting with '1':
> io.readlines(filename, '1', << x -> upper x >>):
```

An error is issued if the file could not be found.
If you use file handles, you must open the file with io.open before applying io.readlines, and close it with io.close thereafter.

## See also: io.lines, io.read, io.readfile, utils.readcsv, utils.readxml, skycrane.readcsv.

io.rewind (filehandle)
Sets the current file position of the open file denoted by its filehandle to the beginning of the file. It returns the current file position, the number 0, at success, and null plus an error string otherwise.

See also: io.move, io.seek, io.toend.
io.seek (filehandle [, whence [, offset]])
Sets and gets the file position, measured from the beginning of the file, to the position given by offset plus a base specified by the string whence, as follows:

- 'set ': base is position 0 (beginning of the file);
- 'cur': base is current position;
- 'end': base is end of file.

In case of success, io.seek returns the final file position, measured in bytes from the beginning of the file. If this function fails, it returns null, plus a string describing the error.

The default value for whence is 'cur', and for offset is 0 . Therefore, the call io.seek(file) returns the current file position, without changing it; the call io.seek (file, 'set') sets the position to the beginning of the file (and returns 0); and the call io.seek (file, 'end') sets the position to the end of the file, and returns its size.

See also: io.move, io.rewind, io.skiplines, io.toend.

```
io.setvbuf (filehandle, mode [, size])
```

Sets the buffering mode for an output file. There are three available modes:

- 'no': no buffering; the result of any output operation appears immediately.
- 'full': full buffering; output operation is performed only when the buffer is full or when you explicitly flush the file (see io.sync).
- 'line': line buffering; output is buffered until a newline is output or there is any input from some special files (such as a terminal device).

For the last two cases, sizes specifies the size of the buffer, in bytes. The default is an appropriate size.

```
io.skiplines (filehandle, n)
io.skiplines (filename, n)
```

The function skips the given number of lines and sets the file position to the beginning of the line that follows the last line skipped.

If a file name is passed, then with each call to io.skiplines the search always starts at the very first line in the file. The function automatically closes the file if a file name has been passed and returns the result (see below).

If you use a file handle, then lines can be skipped multiple times, always relative to the current file position. With a file handle, io.skiplines does not close the file.

The second argument $n$ may be any non-negative number. If $n$ is 0 , then the function does nothing and does not change the file position.

The function returns two values: the non-negative number of lines actually skipped and the non-negative number of characters skipped in this process, including newlines and carriage returns.

See also: io.nlines, io.seek.

```
io.sync (filehandle)
io.sync ()
```

In the first form, saves any written data to the file denoted by filehandle. In the second form, the function flushes the default output.

```
io.tmpfile ()
```

Returns a handle to a temporary file. The file is opened in update mode and it is automatically removed when the programme ends.

See also: io.mkstemp, os.tmpdir, os.tmpname.

```
io.toend (filehandle)
```

Sets the current file position of the open file denoted by its filehandle to the end of the file. It returns the current file position, a number indicating the size of the file, at success, and null plus an error string otherwise.

See also: io.move, io.rewind, io.seek.
io. unlock (filehandle [, size])
The function unlocks the file given by its handle filehandle so that it can be read or overwritten by other applications again. If size is given, the function, only the given number of bytes is unlocked, starting from the current file position.

The function returns true on a successful unlock, and false otherwise.
For more information, see io.lock.

```
io.write (...)
```

io.writeline (...)
Write the value of each of its arguments to standard output if the first argument is not a file handle, or to the file denoted by the first argument, a file handle. Except for the file handle and the 'delim' option described below, all arguments must be strings, numbers, Booleans or null. To write other values, use tostring or strings.format.
io.writeline adds a new line at the end of the data written, whereas io.write does not.

By default, no character is inserted between neighbouring values. This may be changed by passing the option 'delim':<str> (i.e. a pair, e.g.'delim':'।') as the last argument to the functions with <str> being a string of any length. Remember that in the function call, a shortcut to 'delim': <str> is delim ~ <str>.

The functions return true on success, and false otherwise.
Hint: If you work in DOS-like systems, such like DOS, Windows, or OS/2, and if the text to be written includes line breaks, you may wonder why the resulting file will be larger than the number of characters in the text. This is because the operating system adds a further control code, i.e. carriage return, in front of each line break. To avoid this, open the file in binary mode, e.g. io.open (filename, 'wb').

Examples:
Write a string to the console. Note that in the first statement, no newline is added to the output, as opposed to the second and third statements.

```
> io.write('Gauden Dach !')
Gauden Dach !
> io.write('Gauden Dach !', '\n')
Gauden Dach !
> io.writeline('Gauden Dach !')
Gauden Dach !
```

Write strings to the console:

```
> io.writeline('Bet', 'to\'n', '16.', 'Johrhunnert', 'geef', 'dat', 'hier',
> 'baben', 'anne', 'Küst', 'nix', 'anneres', 'as', 'Platt.')
Betto'n16.JohrhunnertgeefdathierbabenanneKüstnixanneresasPlatt.
```

Use a white space as a separator:

```
> io.writeline('Bet', 'to\'n', '16.', 'Johrhunnert', 'geef', 'dat', 'hier',
> 'baben', 'anne', 'Küst', 'nix', 'anneres', 'as', 'Platt.',
> delim=' ')
Bet to'n 16. Johrhunnert geef dat hier baben anne küst nix anneres as
Platt.
```

Write a string to a new file called 'd:/newfile.txt': First we have to create the new file with io.open and the 'w' (write) option.

```
> fh := io.open('d:/newfile.txt', 'W'):
file(7803A6F0)
```

Write some text to the file.

```
> io.write(fh, 'Gouden Dach !'):
true
> io.writeline(fh, '\nBet', 'to\'n', '16.', 'Johrhunnert', 'geef', 'dat',
> 'hier', 'baben', 'anne', 'Küst', 'nix', 'anneres', 'as', 'Platt.',
> delim=' '):
true
```

Finally, the file will be closed.

```
> io.close(fh):
true
```

Note that you can also write to stdin, stdout and stderr by passing the constants io.stdin, io.stdout or io.stderr as a file handle.

See also: io.writefile, print, skycrane.formatline, skycrane.scribe, skycrane.tee.

```
io.writefile (filename, ...)
io.writefile (filehandle, ...)
```

In the first form, creates a new file filename denoted by its first argument (a string) and writes all of the given strings or numbers starting with the second argument in binary mode to it. To write other values, use tostring or strings.format. After writing all data, the function automatically closes the new file.

In the second form, the function writes its arguments to the open file denoted by its handle filehandle.

By default, no character is inserted between neighbouring strings. This may be changed by passing the option 'delim': <str> (i.e. a pair, e.g. 'delim':'|') as the last argument to the function with <str> being a string of any length.
If the file fn already exists, it is overwritten without warning.
The function returns the total number of bytes written, and issues an error otherwise. It is around twice as fast than using a combination of io.open, io.write, and io.close.

See also: save, io.readfile.

## 12.2 binio - Binary File Package

This package contains functions to read data from and write data to binary files.

Summary of functions:
Opening and closing files:
binio.open, binio.close, binio.isfdesc.
Reading data:
binio.lines, binio.readbytes, binio.readchar, binio.readlong, binio.readlongdouble, binio.readnumber, binio.readshortstring, binio.readstring.

Writing data:
binio.writebytes, binio.writechar, binio.writeline, binio.writelong, binio.writelongdouble, binio.writenumber, binio.writeshortstring, binio.writestring.

File positions:
binio.eof, binio.filepos, binio.rewind, binio.seek, binio.toend.
File locking:
binio.lock, binio.unlock.

File buffering:
binio.sync.
Miscellaneous:
binio.length.

The binio package always uses file handles that are positive integers greater than 2. (Note that the io package uses file handles of type userdata.) The positive integer will be returned by the binio.open function and must be used in all package functions that require a file handle.

A typical example might look like this:

Open a file and return the file handle:

```
> fh := binio.open('c:/agena/lib/library.agn'):
3
```

Determine the size of the file in bytes:

```
> binio.length(fh):
46486
```

Close the file.

```
> binio.close(fh):
true
```

binio supports metamethods. The metatable used by the package is called `BINIOFILE*`. By default, only __gc and __tostring methods are supported. Check the end of Chapter 6.19 on how to add further methods.

The binio functions are:
binio.close (filehandle [, filehandle2, ...])
Closes the files identified by the given file handle(s) and returns true if successful, and issues an error otherwise. The function also deletes the file handles and the corresponding filenames from the binio.openfiles table if the file could be properly closed.

See also: binio.open.

```
binio.eof (filehandle)
```

Checks whether the end of the file denoted by filehandle has been reached and returns true or false.

```
binio.filepos (filehandle)
```

Returns the current file position relative to the beginning of the file as a number. In case of an error, it quits with this error.

```
binio.isfdesc (filehandle)
```

Checks whether filehandle is a valid file handle. Returns true if filehandle is an open file handle, or false if filehandle is not a file handle.

## binio.length (filehandle)

The function returns the size of the file denoted by filehandle in bytes. In case of an error, it quits with this error.

```
binio.lines (filehandle [, n] [, true])
```

Creates an iterator function that beginning from the current file position, with each call will return a new line from the file pointed to by the handle filehandle.

By default, the function traverses the file up to its end. If the second argument $n$ is a positive integer, it will read the next n characters from the current file position (default is infinity $=$ end of file). The function generally ignores carriage returns (ASCII code 13) and does not return newlines (ASCII code 10).

If the last argument is the Boolean value true, all embedded zeros (ASCll Code 0) will be replaced with white spaces, and the traversal of the file will continue. By default, zeros are not ignored, so if one is found, the traversal will stop.

The iterator function returns a string, and null if the end of the file has been reached. It also returns null if the last argument is not true and an embedded zero has been found in the file.

The iterator function does not close the file at the end of traversal, use binio.close to accomplish this.
binio.lock (filehandle)
binio.lock (filehandle, size)
The function locks the file given by its handle filehandle so that it cannot be read or overwritten by other applications.

In the first form, the entire file is locked in UNIX-based systems. In Windows, only $2^{63}$ bytes are locked, so you have to use the second form in Windows after the file has become larger than $2^{63}$ bytes ( $=8,589,934,592$ Gbytes).

In the second form the function locks size bytes from the current file position. Locked blocks in a file may not overlap. size may be larger than the current file length.

The function returns true on a successful lock, and false otherwise.
Note that other applications that do not use the locking protocol may nevertheless have read and write access to the file.

See also: binio.unlock.

```
binio.open (filename, 'a')
binio.open (filename [, anything else])
```

Opens the given file denoted by filename and returns a file handle (a number).
If it cannot find the file, it creates it and leaves it open for further binio operations.
In the first form, by passing the 'a' or 'append' option, and if the file already exists, it opens the file and sets the current file position to the end of the file so that nothing will be overwritten later on.

In the second form, if the file already exists, it opens the file and sets the current file position to the beginning of the file. In subsequent write operations, the contents of the file will thus be overwritten and the programmer has to ensure its integrity himself. (Use binio.toend to append to the file in this case or pass the 'a' option.)

The file is always opened in both read and write modes.
If an optional second argument except ' $a$ ' or 'append' is given, the file is opened in read mode only. Thus, if the file does not yet exist, the function returns an error.

The function also enters the newly opened file into the binio.openfiles table.
See also: binio.close, binio.lock, binio.unlock, os.exists.
binio.readbytes (filehandle [, bytes] [, options])
By default, the function reads environ.kernel('buffersize') bytes from the file denoted by filehandle and returns them as a sequence of integers. You may change the kernel buffer size value to any other values in order to read less or more bytes.

If bytes is given, the function reads bytes bytes from the file denoted by filehandle and returns them as a sequence of integers.

The function increments the file position thereafter so that the next bytes in the file can be read with a new call to various binio.read* functions.

If the end of the file has been reached, null will be returned. In case of an error, it quits with the respective error.

By default, the function reads in all bytes of a file, including newlines (ASCll 10) or carriage returns (ASCII 13). You can change this by setting the ignore option and passing a string of explicit bytes that shall be skipped, e.g.:

```
> binio.readbytes(fh, ignore=" .\n"); # skip white space, dot & newline
```

Also by default, the function reads in embedded zeros and treats them as every other byte. If you pass the eof option and set it to true, then the function quits if it
encounters an embedded zero in the file. The file pointer is automatically reset to the position of the embedded zero. The default is false, i.e. the whole file is read in.

The function is much faster when working on a larger number of bytes.
See also: binio.writebytes, bytes.tonumber, stack.readbytes, strings.tochars.

```
binio.readchar (filehandle)
binio.readchar (filehandle, offset)
```

In the first form, the function reads a byte from the file denoted by filehandle from the current file position and increments the file position thereafter so that the next byte in the file can be read with a new call to binio.read* functions.

In the second form, at first the file position is changed by offset bytes (a positive or negative number or zero) relative to the current file position. After that, the byte at the new file position is read. Next, the file position is being incremented thereafter so that the next byte in the file can be read with a new function call.

If the byte is successfully read, it will be returned as a number. If the end of the file has been reached, null will be returned. In case of an error, the function quits.
binio.readindex (filehandle , $k$ [, type [, offset]])
The function assumes that all values in the binary file pointed to be filehandle are of the same type and reads the $k$-th one. By default, the function reads numbers (C doubles). You may pass the third argument type to determine another type. Valid types are the strings 'char' (see binio.writechar), 'long' (see binio.writelong), 'number' (the default, see binio.writenumber), 'shortstring' (see binio.writeshortstring) or 'string' (see binio.writestring). Longdoubles are not supported.

You may pass an optional offset from the beginning of the file as the fourth argument, which by default is 0 . If given, the file position is moved the offset's +1 byte in the file before searching for the given index and reading the value of interest. This feature supports a self-defined file header.

See also: binio.readbytes, binio.readchar, binio.readlong, binio.readnumber, binio.readshortstring, binio.readstring, binio.writeindex.

```
binio.readlong (filehandle [, offset])
```

The function reads a signed $C$ value of type int32_t from the file denoted by filehandle from the current file position and returns it. If there is nothing to read, the function returns null. Note that the number to be read should have been written to the file using the binio. writelong function.

In the second form, before reading the actual value, at first the file position is changed by offset bytes (a positive or negative number or zero) relative to the current file position.

## See also: binio.writelong.

```
binio.readlongdouble (filehandle [, offset])
```

The function reads a longdouble from the file denoted by filehandle from the current file position and returns it. If there is nothing to read, the function returns null. Note that the longdouble to be read should have been written to the file using the binio.writelongnumber function. See the long package for further information on 80-bit floating point values.

In the second form, before reading the actual value, at first the file position is changed by offset bytes (a positive or negative number or zero) relative to the current file position.

The function is not supported on Big Endian systems.
See also: binio.writelongdouble.

```
binio.readnumber (filehandle [, offset])
```

The function reads an Agena number from the file denoted by filehandle from the current file position and returns it. If there is nothing to read, the function returns null. Note that the number to be read should have been written to the file using the binio. writenumber function.

In the second form, before reading the actual value, at first the file position is changed by offset bytes (a positive or negative number or zero) relative to the current file position.

See also: binio.writenumber.

## binio.readshortstring (filehandle)

The function reads a string of up to 255 characters from the file denoted by filehandle from the current file position and returns it. If there is nothing to read, the function returns null.

Note that the string to be read should have been written to the file using the binio. writeshortstring function, as this function also stores the length of the string in a special way to the file.

See also: binio.writeshortstring.

```
binio.readstring (filehandle)
```

The function reads a string of any length from the file denoted by filehandle from the current file position and returns it. If there is nothing to read, the function returns null.

Note that the string to be read should have been written to the file using the binio.writestring function, as this function also stores the length of the string in a special way to the file.

See also: binio.writestring.
binio.rewind (filehandle [, pos])
Sets the file position to the beginning of the file denoted by filehandle.
If pos, a non-negative integer is given, the function resets the file pointer to the position pos relative to the beginning of the file.

The function returns the new file position as a number in case of success, and quits with an error otherwise.

See also: binio.toend, binio.seek.

## binio.seek (filehandle, position)

The function changes the file position of the file denoted by filehandle position bytes relative to the current position. position may be negative, zero, or positive.

The return is true if the file position could be changed successfully, or issues an error otherwise.

See also: binio.rewind, binio.toend.

## binio.sync (filehandle)

Flushes all unwritten content to the file denoted by the handle filehandle. The function returns true if successful, false if stdin or stdout should be closed, and issues an error otherwise (e.g. if the file was not opened before or an error during flushing occurred).

## binio.toend (filehandle)

Sets the file position to the end of the file denoted by filehandle so that data can be appended to the file without overwriting existing data. The function returns the file position as a number in case of success, and issues an error otherwise.

See also: binio.rewind, binio.seek.

```
binio.unlock (filehandle)
binio.unlock (filehandle, size)
```

The function unlocks the file given by its handle filehandle so that it can be read or overwritten by other applications again.

The function returns true on a successful unlock, and false otherwise.

For more information, see binio.lock.

```
binio.writebytes (filehandle, s)
```

The function writes all integers in the sequence s to the file denoted by filehandle at its current position. The function returns true in case of success and fail if the sequence is empty.

The integers in s should be integers number with $0 \leq$ number $<256$, otherwise number \% 256 will be stored to the file.

Internally, the bytes are stored as $C$ unsigned char's.

See also: binio.readbytes, math.tobytes, strings.tobytes.

```
binio.writechar (filehandle, number [, ...])
```

The function writes the given Agena number, and optionally more numbers, to the file denoted by filehandle at its current position. The function returns true in case of success and quits with an error otherwise.

All number(s) should be integers with $0 \leq$ number $<256$, otherwise number $\% 256$ will be stored to the file.

Internally, the bytes are stored as a C unsigned char.
binio.writeindex (filehandle, k, type, value [, offset])
The function assumes that all values in the binary file pointed to by filehandle are of the same type and writes the $k$-th one.

The third argument type specifies the type to be written. Valid types are the strings 'char' (see binio.writechar), 'long' (see binio.writelong), 'number' (see binio.writenumber), 'shortstring' (see binio.writeshortstring) or 'string' (see binio.writestring). Longdoubles are not supported.

The fourth argument specifies the actual value to be written.
You may pass an optional offset from the beginning of the file as the fifth argument, which by default is 0 . If given, the file position is moved to the offset's + 1 byte before writing a value. This feature allows for a self-defined file header.

See also: binio.writebytes, binio.writechar, binio.writelong, binio.writenumber, binio.writeshortstring, binio.writestring, binio.readindex.

```
binio.writeline (filehandle, ...)
```

Writes one or more strings to the file denoted by its file handle filehandle, separated by newlines.

The function is written in the Agena language and is included in the lib/library.agn file.

```
binio.writelong (filehandle, number [, ...])
```

The function writes the given Agena number, and optionally more numbers, to the file denoted by filehandle at its current position. The number(s) should be integers with environ.minlong < number < environ.maxlong, otherwise the result is not defined.

The function returns true in case of success and quits with an error otherwise.
Internally, the numbers are stored as signed $C$ int32_t in Big Endian notation. Use binio.readlong to read values written by writelong back into Agena as readlong transforms the value back into the proper Endian format used by your machine.
binio.writelongdouble (filehandle, number [, ..•])
The function writes the given longdouble number, and optionally more longdoubles, to the file denoted by filehandle at its current position. The function returns true in case of success and issues an error otherwise. The function is not supported on Big Endian systems. See also: binio.readlongdouble.
binio.writenumber (filehandle, number [, ...])
The function writes the given Agena number, and optionally more numbers, to the file denoted by filehandle at its current position. The function returns true in case of success and issues an error otherwise. The numbers are always stored in Big Endian notation. The binio.readnumber function conducts proper conversion to Little Endian if Agena runs on a Little Endian machine.

```
binio.writeshortstring (filehandle, string [, ...])
```

The function writes the given string, and optionally more strings, to the file denoted by filehandle at its current position. The strings can be of length 0 to 255.

The function returns true in case of success and issues an error otherwise. Internally, writeshortstring at first writes the length of the respective string as a C unsigned char and after this it stores the string without a trailing null character to the file. If you call binio.readstring later, Agena very efficiently returns the string.

See also: binio.readshortstring.
binio.writestring (filehandle, string [, ...])
The function writes the given string, and optionally more strings, to the file denoted by filehandle at its current position.

The function returns true in case of success and quits with an error otherwise. Internally, writestring first writes the length of the respective string as a C long int and then the string without a null character to the file. This information is then read by the binio.readstring function to efficiently return the string.

See also: binio.readstring.

## 12.3 xbase - Library to Read and Write xBase Files

As a plus package, in Solaris, Linux, Mac OS X, and Windows, this library is not part of the standard distribution and must be activated with the import statement, e.g. import xbase.

This package provides basic functions to read and write dBASE III+ compliant files.
A typical session may look like this:

```
> import xbase alias;
> new('test.dbf', data=Number);
> f := open('test.dbf', 'write');
> writenumber(f, 1, 1, Pi);
> readvalue(f, 1, 1):
3.1415926535898
> close(f):
true
```

Limitations:

1. The xBase data types currently supported are: Number, Float (dBASE IV 2.0), Binary Double (dBASE 7), String, Date, and Logical.
2. Only files with extension .dbf are supported. Searching and sorting functions are not available, and any .ndx, or .idx index files or *.dbt files will be ignored.
3. Files with sizes greater than 2 GBytes are not supported.
xbase.attrib (filehandle)
returns a table with various information on the xBase file pointed to by filehandle.

| Table key | Meaning |
| :--- | :--- |
| 'codepage' | Code page used. |
| 'fieldinfo' | A table of tables that describe the respective fields in <br> consecutive order: title, xBase native type (see below), Agena <br> type, total number of bytes occupied by the field in the file. <br> With numbers, the number of decimals following the decimal <br> point (its scope) given. |
| 'fields' | Number of fields in the file. |
| 'filename' | Name of the xBase file (relative). |
| 'headerlength' | Length of the header in the xBase file. |
| 'lastmodified' | UTC date of the last write access, coded as an integer. |
| 'records' | Number of records stored in the file. |
| 'recordlength' | Number of bytes occupied by each record. |
| 'version' | dBASE version number (see xbase.new) |
| 'versionname' | dBASE version name (a string, see xbase.new) |

xBase native types recognised are: 'C' for String, 'N' for Number, 'F' for Float, 'L' for Logical, 'D' for Date, and 'O' for a binary Double and 'I' for a binary 4-byte signed integer. 'B' indicates a .DBT block number and ' $M$ ' a memo field. See xbase.new for further information.

For known version numbers, see xbase.new, as well. To check for dBASE 7, binary-and the result with Ob1 11 and check for result 4, e.g. result $\& \& 0 b 111=4$.

See also: xbase.fieldtype, xbase.filepos.

```
xbase.close (filehandle)
```

Closes a connection to the xBase file pointed to by filehandle. No more data can be read or written to the xBase file until you open it again using xbase.open. The function returns true if the file could be closed, and false otherwise.

```
xbase.field (filehandle, row [, 'set'])
```

The function has been deprecated. Please use xbase.readdbf instead.

See also: xbase.ismarked, xbase.readdbf, xbase.readvalue, xbase.record.

```
xbase.fields (filehandle)
```

Returns the number of fields per record contained in the xBase file denoted by filehandle.

See also: xbase.attrib, xbase.records.
xbase.fieldtype (filehandle, field)
Determines the dBASE data type of the given field in the open file denoted by filehandle. The function returns a one-character string, or the string '?' if it is unknown. See xbase.new for the meaning of the return.

See also: xbase.attrib.

```
xbase.filepos (filehandle)
```

Returns the current file position in the file denoted by filehandle and returns it as a number.

See also: xbase.attrib.

```
xbase.header (filehandle)
```

Returns three sequences: the header field names of the file denoted by filehandle, the corresponding Agena type names, and the respective single-character dBASE types.

See also: xbase.attrib.

```
xbase.ismarked (filehandle, record)
```

Checks whether a record in a file denoted by filehandle has been marked as to be deleted and returns true or false.

Please make sure that the file has been opened in write, append, or read/write mode before, otherwise the result may be undefined.

See also: xbase.mark.
xbase.isopen (filehandle)
Checks whether filehandle points to an open xBase file (opened by the same Agena session) and returns true or false.
xbase.isvoid (filehandle, record, field)
Checks whether the value at record number record and field number field from the file pointed to by filehandle has been deleted.

The function returns either true or false.

See also: xbase.ismarked, xbase.mark, xbase.purge, xbase.readvalue.
xbase.kernel ([options])
The function sets defaults for the binary representation and layout of binary doubles and binary time stamps in dBASE Level 7 files:

| Setting | Default | Description |
| :--- | :--- | :--- |
| DoubleIsBigEndian | true | If set to false, binary doubles shall be <br> represented in Little Endian notation. By default, <br> binary doubles are Big Endian. |
| LongIsBigEndian | false | If set to true, binary doubles shall be represented <br> in Big Endian notation. By default, binary integers <br> are Little Endian. |
| TimestampIsDouble | false | If set to true, binary time stamps are represented <br> as a binary 8-byte double; by default time and <br> date are represented by two 4-byte signed <br> integers, with the endianness depending on the <br> setting of Long1IsBigEndian. |

If no argument is given, the current settings are returned.

```
xbase.lock (filehandle)
xbase.lock (filehandle, size)
```

The function locks the file given by its handle filehandle so that it cannot be read or overwritten by other applications.

In the first form, the entire file is locked in UNIX-based systems. In Windows, only $2^{63}$ bytes are locked, so you have to use the second form in Windows after the file has become larger than $2^{63}$ bytes ( $=8,589,934,592$ GBytes).

In the second form the function locks size bytes from the current file position. Locked blocks in a file may not overlap. size may be larger than the current file length.

The function returns true on success and false otherwise.

Note that other applications that do not use the locking protocol may nevertheless have read and write access to the file.

See also: xbase.unlock.

```
xbase.mark (filehandle, row [, flag])
```

Marks the record number row, an integer, in the file denoted by its filehandle, as deleted.

Returns true if a record has been marked successfully, and false otherwise.
The actual data is not physically deleted, however, xbase.readvalue, xbase.record, xbase.field, and xbase.readdbf do not return it. Use xbase.purge to delete entries.

If flag is false, a formerly marked record is activated (`undeleted`) again.
Please make sure that the file has been opened in write, append, or read/write mode before, otherwise the result may be undefined.

See also: xbase.ismarked.

```
xbase.new (filename, desc}\mp@subsup{\mp@code{1}}{1}{[, code page] [, version] [, desc}\mp@subsup{2}{2}{\prime, \cdots., desc
``` creates a new xBase file with the file name filename.
desc \(_{\mathrm{k}}\) are k fields (columns) the xBase file will contain. code page indicates the code page to be used (see below) \({ }^{23}\).

In its header, the function designates the resulting file as a dBASE III+ file without memo .DBT file.
desc \(\mathrm{c}_{\mathrm{k}}\) must be a pair of the following form:
1. field_name : data_type
where field_name is a string and the name of the field to be added, and data_type is one of the strings 'Logical', 'Date', 'Float', 'Number', 'Double', 'Long', 'Complex', 'Byte', 'Decimal' or 'Character', i.e. the xBase data type of the values to be stored later.

Examples:
```

new('dbase.dbf', 'logical':'Logical') Or
new('dbase.dbf', logical='Logical') for short for a Boolean.

```

A Boolean (which in xBase is equal to a `Logical`) will always consist of one character ' T ', ' F ' for true and false.

An xBase Number will have a standard length of 19 places with a default scale of 15 digits, whereas an xBase Float consists of 20 places with a scale of 18 digits (scale: numbers following the decimal point). Numbers are stored in xBase files as strings with ANSI C double precision. The scale may be in [0, 15] with xBase Numbers, and in \([0,18]\) with xBase Floats.

An xBase Character (string) will have a default length of 64 characters. The minimum length of a string is 1 , the maximum length of a string may be 254 characters. Longer strings will be truncated.

A date will always consist of eight digits of the format YYYMMDD.
A dBase Level 7 Double represents an Agena number (integral or fractional) that is stored in either binary Big Endian or Little Endian format of eight bytes to an xBase file. The default is Big Endian, but you can change this when writing or reading files, see xbase.kernel.

A dBase Level 7 Long represents a signed 4-byte integer that is stored in either binary Big Endian or Little Endian format to an xBase file. The default is Little Endian, but you can change this when writing or reading files, see xbase.kernel.

\footnotetext{
\({ }^{23}\) Note that code pages are a Foxpro extension.
}

There are three proprietary nonstandard types: Type 'complex' represents a complex number, stored in 16 bytes, type 'Byte' represents an unsigned integer in the range 0 .. 255, stored in just one byte, and the experimental type 'Decimal' stores numbers as signed 4-byte C floats (note that these are highly inaccurate). All of these three types are represented in Little Endian notation.
1. field_name : data_type : length
where field_name and data_type are the same as mentioned above, and length is the maximum length of the item to be added. length must be a positive integer. With numbers, length denotes the number of digits after the decimal point to be stored.
When passing a length value, you may leave out the quotes for data_type values.

Examples:
```

new('dbase.dbf', 'value':'Number':5) Or
new('dbase.dbf', value=Number:5) for short for a float with five decimal places.

```

Supported xBase data types are:
\begin{tabular}{|c|c|c|c|c|}
\hline Type & data_type name & Agena type & Write function & dBASE version \\
\hline Logical & 'Logical' Or 'L' & boolean & xbase.writeboolean & III+ \\
\hline Number & \begin{tabular}{l}
'Number' Or \\
'Numeric' Or 'N'
\end{tabular} & number & xbase.writenumber & III+ \\
\hline Float & 'Float' Or 'F' & number & xbase.writefloat & IV 2.0 \\
\hline Double & 'Double' Or '0' & number & xbase.writedouble & 7 \\
\hline Long & 'Long' Or 'I' & number & xbase.writelong & 7 \\
\hline Character & 'Character' Or 'C' & string & xbase.writestring & III+ \\
\hline Date & 'Date' Or 'D' & string & xbase.writedate & III+ \\
\hline Timestamp & '@' & numbers & xbase.writetime & 7 \\
\hline OLE & 'G' & & n/a & ? \\
\hline Memo & 'M' & & n/a & ? \\
\hline Binary & 'B' & & n/a & ? \\
\hline Complex & 'Complex' Or 'c' & complex & xbase.writecomplex & prop. \\
\hline Byte & 'Byte' Or 'b' & number & xbase.writebyte & prop. \\
\hline Decimal & 'Decimal' Or 'f' & number & xbase.writedecimal & prop. \\
\hline
\end{tabular}

\footnotetext{
codepage should be a pair of the form 'codepage' ' n , with n an integer in [0,255].
}

Valid codepages are:
\begin{tabular}{|c|c|c|}
\hline n & Meaning & Code page \\
\hline \(0 \times 01\) & DOS USA & 437 \\
\hline Ox02 & DOS Multilingual & 850 \\
\hline \(0 \times 03\) & Windows ANSI & 1.252 \\
\hline \(0 \times 04\) & Standard Macintosh & 10.000 \\
\hline \(0 \times 64\) & Eastern Europe DOS & 852 \\
\hline 0x65 & Nordic DOS & 865 \\
\hline 0x66 & Russian DOS & 866 \\
\hline \(0 \times 67\) & Icelandic DOS & 861 \\
\hline 0x68 & Kamenicky (Czech) DOS & 895 \\
\hline 0x69 & Mazovia (Polish) DOS & 620 \\
\hline 0x6a & Greek DOS & 437G \\
\hline 0x6b & Turkish DOS & 857 \\
\hline 0x78 & Traditional Chinese (Republic of China (Taiwan), Hong Kong SAR) & 950 \\
\hline 0x79 & Korean Windows & 949 \\
\hline 0x7A & Chinese Simplified (Singapore, PRC) & 936 \\
\hline 0x7B & Japanese Windows & 932 \\
\hline 0x7C & Thai Windows & 874 \\
\hline 0x7D & Hebrew Windows & 1.255 \\
\hline 0x7E & Arabic Windows & 1.256 \\
\hline 0x96 & Russian Macintosh & 10.007 \\
\hline \(0 \times 97\) & Eastern European Macintosh & 10.029 \\
\hline 0x98 & Greek Macintosh & 10.006 \\
\hline 0xc8 & Eastern Europe Windows & 1.250 \\
\hline 0xc9 & Russian Windows & 1.251 \\
\hline Oxca & Turkish Windows & 1.254 \\
\hline Oxcb & Greek Windows & 1.253 \\
\hline
\end{tabular}

If no code page has been passed, it is set to \(0 \times 00\).
Example for Eastern European Macintosh:
```

new('dbase.dbf', text=string:255, code page=0x97);

```
version should be a pair of the form 'version' \(: n\), with \(n\) an integer in \([0,255]\).
dBASE version numbers are:
```

x xxx x 001 = 0x?1 not used
0000 0 010 = 0x02 FoxBASE
0000 0 011 = 0x03 FoxBASE+/dBASE III PLUS, no memo
x xxx x 100 = 0x?4 dBASE 7
0000 0 101 = 0x05 dBASE 5, no memo
011 0 000 = 0x30 Visual FoxPro
011 0 001 = 0x31 Visual FoxPro, autoincrement enabled
0 011 0 010 = 0x32 Visual FoxPro, Varchar, Varbinary, or Blob-enabled
0 100 0 011 = 0x43 dBASE IV SQL table files, no memo
0 110 0 011 = 0x63 dBASE IV SQL system files, no memo
111 1 011 = 0x7B dBASE IV, with memo
000 0 011 = 0x83 FoxBASE+/dBASE III PLUS, with memo
000 1 011 = 0x8B dBASE IV, with memo
10001 110=0x8E dBASE IV with SQL table
1 100 1 011 = 0xCB dBASE IV SQL table files, with memo
110 0 101 = 0xE5 Clipper SIX driver, with SMT memo
111 0 101 = 0xF5 FoxPro 2.x (or earlier) with memo
1111 1 011 = 0xFB FoxBASE (with memo?)
| ||| | |||
| ||| | ||| Bit flags (not used in all formats)
| ||| | ||| --------------------------------------
| ||| | +++-- bits 2, 1, 0, version (x03 = level 5, x04 = level 7)
| ||| +------ bit 3, presence of memo file
| +++-------- bits 6, 5, 4, presence of dBASE IV SQL table
+------------ bit 7, presence of .DBT file

```

The default is \(0 \times 03=3\) decimal for dBASE III+. If at least one of the given fields is of dBASE data type 'Double' ( = 'B' or 'O') or type 'timestamp', then the version number is automatically changed to \(0 x ? 4=4\) decimal \(=\) dBASE Level 7 . This allows dBASE files created with Agena and containing binary Doubles to be imported into LibreOffice 5.x. Current versions of Excel still cannot read Visual Fox Pro dbf files with Doubles or Longs, so you might pass the version option.

\section*{See also: xbase.open.}

\section*{xbase.open (filename [, mode])}

Opens an xBase file of the name filename for reading or writing, or both.
In the first form, the file is opened for reading only.
In the second form, if mode is either 'write', 'w', 'append', or 'r+', the file is opened for reading while new data sets may be added to the end of the file.

If mode is 'read' or 'r', the file is opened for reading only.
The return is a file handle to be used by all other xBase package functions.
See also: xbase.close, xbase.lock, xbase.new.
```

xbase.purge (filehandle, record, field)

```

Overwrites the specified field in the given record of the file denoted by its handle filehandle with asterisks, thus physically deleting the original content. The return is true if deletion succeeded, and false otherwise. After successful completion, a subsequent call to xbase.isvoid would return true.

See also: xbase.isvoid, xbase.mark, xbase.wipe.
```

xbase.readdbf (filename [, option])
xbase.readdbf (filehandle [, option])

```

In the first form, opens an xBase file denoted by its filename in read mode, returns all its records and fields, and closes it. In the second form, it reads the contents of the open file denoted by its handle filehandle.

If the xBase file contains more than one field, the data will be returned as a sequence of sequences, whereas if the file contains only one field, all values are returned in one sequence only.

If the option fields \(=x\) with \(x\) a positive number is given, only the given column \(x\) is extracted, and the return is a sequence of the column values. If the option fields=obj with obj a table or sequence of positive numbers is given, only the given fields in the records are returned, and the return is a sequence of sequences.

If a record has been marked as being deleted, the function ignores the record.
See also: xbase.field, xbase.ismarked, xbase.readvalue, xbase.record.
```

xbase.readvalue (filehandle, record, field)

```

Reads a value at record number record and field number field from the file pointed to by filehandle.

Supported values are of xBase type Logical, Number, Float, binary double, Date, Timestamp and String. Also Binary, Memo and OLE .DBT block numbers are supported, as well as type Complex, Byte and Decimal. If a number could not be read from the file, the function returns 0 . On Little Endian systems, you might have to convert Big Endian binary doubles back to Little Endian by calling bytes.tolittle; see also os.endian.

If record has been marked as being deleted, the function returns null.

See also: xbase.field, xbase.ismarked, xbase.record, xbase.isvoid.
```

xbase.record (filehandle, line)

```

Returns all values in the given record line (a number) of the file denoted by filehandle and returns them in a sequence.

If record has been marked as being deleted, the function returns null.
See also: xbase.field, xbase.ismarked, xbase.readdbf, xbase.readvalue.
```

xbase.records (filehandle)

```

Returns the number of records contained in the xBase file denoted by filehandle, including the ones marked as to be deleted or being completely void.

See also: xbase.attrib, xbase.fields.
```

xbase.sync (filehandle)

```

Writes any unwritten content to the xBase file pointed to by filehandle. The function either returns true if flushing succeeded or nothing had be flushed, or fail otherwise.

Please make sure that the file has been opened in write, append, or read/write mode before, otherwise the result may be undefined.
```

xbase.unlock (filehandle)
xbase.unlock (filehandle, size)

```

The function unlocks the file given by its handle filehandle so that it can be read or overwritten by other applications again.

The function returns true on success and false otherwise.

For more information, see xbase.lock.
```

xbase.wipe (filehandle, record)

```

In an xBase file denoted by filehandle, deletes all fields of the given record, a positive integer by overwriting all fields with asterisks. It also marks the record as deleted (see xbase.mark for further information).

To ensure performance, the function does not lock the file before deleting data you may want to manually call xbase.lock before and xbase.unlock thereafter. Also, it does not flush the file.

The function returns nothing.
The function has been written in Agena, see lib/xbase.agn.

\section*{See also: xbase.mark, xbase.purge.}
xbase.writeboolean (filehandle, record, field, value)
Writes the Boolean value true or false (4th argument) to the file denoted by filehandle to record number record and field number field. fail and null are not supported.

When creating the dBASE file with xbase.new, pass the ' L ' data type descriptor for the respective fields.

The return is true if writing succeeded, and false otherwise.
```

xbase.writebyte (filehandle, record, field, value)

```

Writes the integer value in the range 0 .. 255(4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the ' b ' data type descriptor for the respective fields.

The integer is stored in binary format of just one byte (unsigned C char).
A proprietary extension, applications that import dBASE files - such as Microsoft Excel - do not support this type.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writefloat, xbase.writelong, xbase.writenumber, xbase.new.
xbase.writecomplex (filehandle, record, field, value)
Writes the complex number value (4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the 'c' data type descriptor for the respective fields.

The complex number is stored in Little Endian binary format of sixteen bytes (two C doubles, converted to two C uint64_t).

A proprietary extension, applications that import dBASE files - such as Microsoft Excel - do not support this type.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

\section*{See also: xbase.writefloat, xbase.writelong, xbase.writenumber, xbase.new.}
```

xbase.writedate (filehandle, record, field, value)

```

Writes the string or number value (4th argument), representing an integer - or a string representing an integer - in the range19000101 \(<x<99991231\) and denoting a date, to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the 'D' data type descriptor for the respective fields.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writetime.
```

xbase.writedecimal (filehandle, record, field, value)

```

Writes the number value (4th argument) as a signed 4-byte Little Endian float to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the ' \(f\) ' data type descriptor for the respective fields.

A proprietary extension, applications that import dBASE files - such as Microsoft Excel - do not support this type.

Note that 4-byte floats are inherently inaccurate, so when reading them back into Agena you will find significant round-off errors due to stray bits.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.
```

xbase.writedouble (filehandle, record, field, value)

```

Writes the number value (4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the 'o' (letter O) data type descriptor for the respective fields.

The number is stored in binary format of eight bytes (C double, converted to a C uint64_t). By default, doubles are written in Big Endian representation. You can change this to Little Endian by setting
```

> xbase.kernel(DoubleIsBigEndian = false);

```

A dBASE 7 extension, some applications that import dBASE files - such as Microsoft Excel - do not support binary numbers, but LibreOffice 5.x and beyond does.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writefloat, xbase.writelong, xbase.writenumber, xbase.new.
xbase.writefloat (filehandle, record, field, value)
Writes the number value (4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the ' \(\mathrm{F}^{\prime}\) data type descriptor for the respective fields.

The number is stored with a total of 20 digits, including a maximum of 18 digits following the decimal point (scale).

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writedouble, xbase.writenumber, xbase.new.
```

xbase.writelong (filehandle, record, field, value)

```

Writes the number value (4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the ' I' data type descriptor for the respective fields.

The function automatically truncates Agena numbers containing decimal places to their integral part and issues an error if the numeric range [-2'147'483'647, \(+2^{\prime} 147^{\prime} 483^{\prime} 647\) ] is exceeded.

By default, longs are written in Little Endian representation. You can change this to Big Endian by setting
```

> xbase.kernel(LongIsBigEndian = true);

```

A dBASE 7 extension, some applications that import dBASE files - such as Microsoft Excel - do not support binary numbers, but LibreOffice 5.x and beyond does.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writedouble, xbase.writefloat, xbase.writenumber, xbase.new.
xbase.writenumber (filehandle, record, field, value)
Writes the number value (4th argument) to the file denoted by filehandle to record number record and field number field.

The function automatically determines whether the respective field is of xBASE type Numeric ('N'), Float ('F'), binary Long ('I'), or Binary Double ('O') (letter O). Concerning ' \(O\) ' and 'I', read the remarks on Endianness in the description of xbase.writedouble. It also writes the proprietary formats 'b' for byte (see xbase.writebyte) and 'c' for complex numbers (see xbase.writecomplex).

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error may have occurred.

See also: xbase.writedouble, xbase.writefloat, xbase.writelong, xbase.new.
```

xbase.writestring (filehandle, record, field, value)

```

Writes the string value (4th argument) to the file denoted by filehandle to record number record and field number field.

When creating the dBASE file with xbase.new, pass the 'c' data type descriptor for the respective fields.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error might have occurred.
```

xbase.writetime (filehandle, record, field,
y, m, d [, h [, m [, s [, ms]]]])

```

Writes the timestamp given by the year \(y\), month \(m\), day \(d\), and optionally hour \(h\), minute mm , second s , and milliseconds ms to the file denoted by filehandle to record number record and field number field.

By default, hours, minutes, seconds, and milliseconds default to 0 . Milliseconds must be an integer in the range [0, 999].

When creating the dBASE file with xbase.new, pass the ' e' data type descriptor for the respective fields.

The return is true if writing succeeded, and false otherwise. Note that the return false only indicates that an error might have occurred.

By default, the timestamp internally is represented by two signed 32-bit integers in Little Endian representation. You can change this to Big Endian representation by setting:
```

> xbase.kernel(LongIsBigEndian = true);

```

If the timestamp shall be represented by a binary double - the Julian Date, but the documentation available on dBASE Level 7 files is contradictory - you can set:
> xbase.kernel(TimestampIsDouble = true);
The endianness of the double is Big Endian by default. You can change this to Little Endian by setting:
```

> xbase.kernel(DoubleIsBigEndian = false);

```

See also: xbase.writedate.

\section*{12.4 ads - Agena Database System}

As a plus package, this simple database is not part of the standard distribution and must be activated with the import statement, e.g. import ads.

Agena is a database for storing and accessing strings and currently supports three `base` types:
1. Sorted `databases` with a key and one or more values,
2. sorted `lists` which store keys only,
3. unsorted `sequences` to hold any value (but no keys).

With databases and lists, each record is indexed, so that access to it is very fast. If you store data with the same key multiple times in a database, the index points to the last record stored, so you always get a valid record.

Sequences do not have indexes, so searching in sequences is rather slow. However, all values can be read into the Agena environment rapidly (using ads.getall).

The Agena Database System (ADS) pays attention to both file size and fast I/O operation. To reduce file size, the keys (and values) are stored with their actual lengths (of C type int32_t, so keys and values can be of almost unlimited size) and they are not extended to a fixed standard length. To fasten I/O operations, the length of each key (and value) is also stored within the base file.

The following terms are used in this chapter:
\begin{tabular}{|c|l|}
\hline Section & Description \\
\hline header & \begin{tabular}{l} 
various information on the data file, including the maximum \\
number of possible records, the actual number of records, and \\
the type of the base (database, list, or sequence).
\end{tabular} \\
\hline index & \begin{tabular}{l} 
only with databases and lists: area containing all file positions of \\
the actual records. The index section is always sorted. Sequences \\
do not contain an index section.
\end{tabular} \\
\hline records & key-value pairs with databases, and keys with lists or sequences.
\end{tabular}

A sample session:
First activate the package:
```

> import ads alias

```

Create a new database (file c:\test.agb) including all administration data like number of records, etc.:
```

> createbase('c:/test.agb');

```

Open the database for access. The variable fh is the file handle which refers to the database file (c: \test.agb) and is used in nearly all ads functions.
```

> fh := openbase('c:/test.agb');

```

Put an entry into the database with key `Duck` and value `Donald`.
```

> writebase(fh, 'Duck', 'Donald');

```

Check what is stored for `Duck`.
```

> readbase(fh, 'Duck'):
Donald

```

Show information on the database:
```

> attrib(fh):
keylength ~ 31 \# Maximum length for key
type ~ 0 \# database type, 0 for relational database
stamp ~ AGENA DATA SYSTEM \# name of database
indexstart ~ 256 \# begin of index section in file
commentpos ~ 0 \# position of a description, 0 because none
version ~ 300
maxsize ~ 20000

# end of index section

creation ~ 2008/01/18-19:00:50
columns ~ 2
columns
size ~ 1 \# number of actual entries

```

Close the database. After that you cannot read or write any entries any longer. Use the open function if you want to have access again.
```

> closebase(fh);

```

On all ads database types, you may use the following procedures:

\section*{ads.attrib (filehandle)}

Returns a table with all attributes of the `base` file. The table includes the following keys:
\begin{tabular}{|l|l|l|}
\hline Key & Description & Type \\
\hline 'columns' & The number of columns in the base. & number \\
\hline 'commentpos' & \begin{tabular}{l} 
The position of a comment in the base. If no \\
comment is present, its value is 0.
\end{tabular} & number \\
\hline 'creation' & \begin{tabular}{l} 
The date of creation of the base. The return is a \\
formatted string including date and time.
\end{tabular} & string \\
\hline 'indexstart' & the first byte in the base file of the index section. & number \\
\hline 'indexend' & the last byte in the base file of the index section. & number \\
\hline 'keysize' & the maximum length of the record key. & number \\
\hline 'maxsize' & total number of data sets allowed. & number \\
\hline 'size' & \begin{tabular}{l} 
the actual number of valid data sets (see ads.sizeof \\
as a shortcut).
\end{tabular} & number \\
\hline 'stamp' & The base stamp at the beginning of the file. & string \\
\hline 'type' & Indicator for database (0), list (1), or sequence (2). & number \\
\hline 'version' & The base version. & number \\
\hline 'description' & The description, empty string if not present & string \\
\hline
\end{tabular}

If the file is not open, attrib returns false.
See also: ads.free, ads.sizeof.
ads.clean (filehandle)
Physically deletes all entries that have become invalid (i.e. replaced by new values) from the database or list. The file index section is adjusted accordingly and the file shrunk to the new reduced size.

If there are no invalid records, false will be returned. If all records could be deleted successfully, true will be returned. If the file is not open, the result is fail. If a file truncation error occurred, clean quits with an error. The function issues an error if the file contains a sequence.
ads.closebase (filehandle [, filehandle2, ...])
Closes the base(s) identified by the given file handle(s) and returns true if successful, and false otherwise. false will be returned if at least one base could not be closed. The function also deletes the file handles and the corresponding filenames from the ads.openfiles table.
```

ads.comment (filehandle)
ads.comment (filehandle, comment)
ads.comment (filehandle, '')

```

In the first form, the function returns the comment stored to the database or list if present. The return is a string or null if there is no comment.

In the second form, ads.comment writes or updates the given comment to the database or list and if successful, returns true. The comment is always written to the end of the file. If it could not successfully add or update a comment, the function quits with an error.

In the third form, by passing an empty string, the existing comment is entirely deleted from the database or list.

If filehandle points to a sequence, an error will be issued and no comment is written. fail will be returned, if the file is not open.

Internally, the position of the comment is stored in the file header. See ads.attrib ['commentpos'].
ads.createbase (filename
[, number_of_records [, type [, number_of_columns
[, length_of_key [, description]]]]])
ads.createbase (filename
[, number_of_records [, type [, length_of_key [, description]]]])
Creates and initialises the index section of a new base with the given number of columns. It returns the file handle as a number, and closes the created file.

The first form defines a database, the second form is used to create sequences and lists.

Arguments / Options:
\begin{tabular}{|l|l|}
\hline filename & The path and full name of the base file. \\
\hline number_of_records & \begin{tabular}{l} 
The maximum number of records in the base. Default is \\
20,000. If you pass 0, fail will be returned and the base is \\
not created.
\end{tabular} \\
\hline type & \begin{tabular}{l} 
By default, the type is 'database'. If you pass the string 'list', \\
then a list will be created. The string 'seq' will create a \\
sequence. If the type passed is not known, fail will be \\
returned and no base is created.
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline number_of_columns & \begin{tabular}{l} 
The number of columns in a database. Default: 2 (key \\
and value). If the base is not a database, do not pass any \\
value (see second form). If the number of columns is \\
non-positive, fail will be returned and no base will be \\
created.
\end{tabular} \\
\hline length_of_key & \begin{tabular}{l} 
The maximum length of the base key. Note that internally, \\
the length is incremented by 1 for the terminating 10 \\
character. Default: 31 including the terminating 10 \\
character.
\end{tabular} \\
\hline description & \begin{tabular}{l} 
A string with a description of the contents of the base. A \\
maximum of 75 characters is allowed (including the 10 \\
character). If the string is too long, it will be truncated. \\
Default: 75 spaces.
\end{tabular} \\
\hline
\end{tabular}
ads.createseq (filename)
Creates a sequence with the given filename (a string). The function is written in Agena and can be used after issuing import ads.
```

ads.desc (filehandle)
ads.desc (filehandle, description)

```

In the first form, returns the description of a base stored in the file header. If no description has explicitly been written, the function returns the empty string.

In the second form, ads.desc sets or overwrites the description section of a database or list. Pass the description as a string. If the string is longer than 75 characters, fail will be returned and there are no changes to the base file. If the file is not open, fail will be returned, as well. If it was successful, the return is true.
```

ads.expand (filehandle [, n])

```

Increases the maximum number of datasets by \(n\) records ( \(n\) an integer). By default, n is 10. Internally, all data sets are shifted, so that the index section in the data file can be extended. Thus, the greater \(n\), the faster shifting will be if the function is called many times, which is significant for large files.

The function returns fail if the file is not open, and true otherwise. It issues an error if the file contains a sequence.

\section*{ads.filepos (filehandle)}

Returns the current position of the file denoted by filehandle. See also: ads.attrib.
```

ads.free (filehandle)

```

Determines the number of free data sets and returns them as an integer. If the base has not open, it returns fail. See also: ads.attrib.
```

ads.getall (filehandle [, option])

```

Converts an ADS sequence to a set and returns this set. The function automatically initialises the set with the number of entries in the ADS sequence. If the file is not open, fail will be returned.

If any option is given, an Agena sequence will be returned with the entries in the order of their physical presence in the database file; if one and the same entry is stored multiple times, it is also returned multiple times in the sequence.

See also: ads.getkeys, ads.getvalues.
```

ads.getkeys (filehandle)

```

Gets all valid keys in a database or list and returns them in a table. Argument: file handle (integer). If the file is not open, fail will be returned. If the base is empty, null will be returned. The function issues an error if the file contains a sequence.

See also: ads.get, ads.getvalues.
ads.getvalues (filehandle [, column])
By default, gets all valid entries in the second column in a database and returns them in a table. If the optional argument column is given, the entries in this column are returned. Argument: file handle (integer). If the file is not open or if the column does not exist, fail will be returned. If the base is empty, null will be returned. With lists, the return is always null.

See also: ads.get, ads.getkeys.
```

ads.index (filehandle, key)

```

Searches for the given key (a string) in the base pointed to by filehandle and returns its file position as a number. If their are no entries in the set, the function returns null. If the file is not open, fail will be returned.
```

ads.indices (filehandle)

```

Returns the file positions of all valid datasets as a table.

If the file is not open, indices returns fail. If there are no entries in the base, the return is an empty table, otherwise a table with the indices will be returned. The function issues an error if the file contains a sequence.

See also: ads.retrieve, ads.invalids, ads.peekin, ads.index.
```

ads.invalids (filehandle)

```

Returns the file positions of all invalid records in a database as a table.

If the file is not open, invalids returns fail. If no invalid entries are found, the return is an empty table. See also ads.retrieve. Note that the function also works with lists. However, since lists never contain invalid records, an empty table will always be returned with lists.

With sequences, the function issues an error.
```

ads.iterate (filehandle [, key])

```

Iterates sequentially and in ascending order over all keys in the database or list. With databases, both the next key and its corresponding value are returned. With lists, only the next key is returned.

The very first key can be accessed with an empty string or null (or by only passing filehandle). If there are no more keys left, the function returns null. If the database is empty, null will be returned as well. If the file is not open, the function returns fail.

Example:
```

> s, t := ads.iterate(fh, '');
> s, t := ads.iterate(fh, s);

```

With ADS sequences, the function returns an iterator function that when called returns the next entry in it.
```

ads.lock (filehandle)
ads.lock (filehandle, size)

```

The function locks the file given by its handle filehandle so that it cannot be read or overwritten by other applications.

In the first form, the entire file is locked in UNIX-based systems. In Windows, only \(2^{63}\) bytes are locked, so you have to use the second form in Windows after the file has become larger than \(2^{63}\) bytes ( \(=8,589,934,592\) GBytes).

In the second form the function locks size bytes from the current file position. Locked blocks in a file may not overlap. size may be larger than the current file length.

Note that other applications that do not use the locking protocol may nevertheless have read and write access to the file.

See also: ads.unlock.
ads.openbase (filename [, anything])
Opens the base with name filename and returns a file handle (a number). If it cannot find the file, or the base has not the correct version number, the function
returns fail. The base is opened in both read and write mode.
If an optional second argument is given (any valid Agena value), the base is opened in read mode only.

The function also enters the newly opened file into the ads.openfiles table.

\section*{ads.openfiles}

A global table containing all files currently open. Its keys are the file handles (integers), the values the file names (strings). If there are no open files, ads.openfiles is an empty table.
```

ads.peekin (filehandle, position)

```

Returns both the length of an entry (including the terminating \(\backslash 0\) character) and the entry itself at the given file position as two values (an integer and a string). The function is save, so if you try to access an invalid file position, the function will exit returning fail. It issues an error if the file contains a sequence.

See also: ads.index, ads.retrieve.
```

ads.rawsearch (filehandle, key [, column])

```

With databases, the function searches all entries in the given column for the substring key and returns all respective keys and the matching entries in a table. If column is omitted, the second column is searched. The value for column must be greater than 0 , so you can also search for keys.

With lists and sequences, the function always returns null. If the base is empty, null will be returned.

If the file is not open or the column does not exist, the function returns fail.
See also: ads.read, ads.getvalues.
```

ads.readbase (filehandle, key)

```

With databases, the function returns the entry (a string) to the given key (also a string). With lists and sequences, the function returns true if it finds the key, and false otherwise.

If the file is not open, read returns fail. If the base is empty, null will be returned. The function uses binary search.

See also ads.rawsearch.
```

ads.remove (filehandle, key)

```

With databases, the function deletes a key-value pair from the database; with lists, the key is deleted. Physically, only the key to the record is deleted, the key or key-value pair still resides in the record section but cannot be found any longer.

The function returns true if it could delete the data set, and false if the set to be deleted was not found. If the file is not open, delete returns fail. The function issues an error if the file contains a sequence.

If you want to physically delete all invalid records, use ads.clean.
```

ads.retrieve (filehandle, position)

```

Gets a key and its value from a database or list (indicated by its first argument, the file handle) at the given file position (an integer, the second argument). Two values are returned: the respective key and its value. With lists, only the key will be returned.

The function is save, so if you try to access an invalid file position, the function will exit and return fail.

If the file is not open, retrieve returns fail. The function issues an error if the file contains a sequence.

See also ads.indices, ads.invalids.
```

ads.sizeof (filehandle)

```

Returns the number of valid records (an integer) in the base pointed to be filehandle. If the base pointed to by the numeric filehandle is not open, the function returns fail.
```

ads.sync (filehandle)

```

Flushes all unwritten content to the base file. The function returns true if successful, and fail otherwise (e.g. if the file was not opened before or an error during flushing occurred).
```

ads.unlock (filehandle)
ads.unlock (filehandle, size)

```

The function unlocks the file given by its handle filehandle so that it can be read or overwritten by other applications again. For more information, see ads.lock.
```

ads.writebase (filehandle, key [, value1, value2, ...])

```

With databases, the function writes the key (a string) and the values (strings) to the database file pointed to by filehandle (an integer). If value is omitted, an empty string is written as the value.

With lists, the function writes only the key (a string) to the database file. If you pass values, they are ignored. If the key already exists, nothing is written or done and true will be returned. Thus, lists never contain invalid records.

In both cases, the index section is updated. If a key already exists, its position in the index section is deleted and the new index position is inserted instead (in this case there is no re-shifting). This does not remove the actual key-value pair in the record section. The function always writes the new key-value pair to the end of the file. (The file position after the write operation has completed is always 0.)

If the maximum number of possible records is exceeded, the base is automatically expanded by 10 records. You do not need to do this manually.
write returns the true if successful. If the file is not open, write returns fail.

\section*{12.5 xml - XML Parser}

As a plus package, the xml package is not part of the standard distribution and must be activated with the import statement, e.g. import xml. It is available for Solaris, OS/2, DOS, Mac OS X, Linux, and Windows only.

Since the XML package actually is the LuaExpat binding with some few Agena-specific modifications, large portions of this subchapter have been taken from the LuaExpat documentation.

\subsection*{12.5.1 Introduction}

XML/LuaExpat is a SAX XML parser based on the Expat library. SAX is the Simple API for XML and allows programmes to:
- process a XML document incrementally, thus being able to handle huge documents without memory penalties;
- register handler functions which are called by the parser during the processing of the document, handling the document elements or text.

With an event-based API like SAX the XML document can be fed to the parser in chunks, and the parsing begins as soon as the parser receives the first document chunk. XML/LuaExpat reports parsing events (such as the start and end of elements) directly to the application through callbacks. The parsing of huge documents can benefit from this piecemeal operation.

XML/LuaExpat is distributed as a library.

\subsection*{12.5.2 Parser objects}

Usually SAX implementations base all operations on the concept of a parser that allows the registration of callback functions. XML/LuaExpat offers the same functionality but uses a different registration method, based on a table of callbacks.

This table contains references to the callback functions which are responsible for the handling of the document parts. The parser will assume no behaviour for any undeclared callbacks.

\subsection*{12.5.3 Shortcuts}
```

xml.decode (str)

```

Reads a string str containing an XML stream and converts it into a dictionary. Its return is rather raw, but it can cope with situations where one and the same XML object is present multiple times on the same hierarchy.
```

xml.decodexml (str)

```

Reads a string str containing an XML stream and converts it into a dictionary.

The function provides some checking (basic syntax and balanced tags), and supports namespaces, XML and DOCTYPE declarations, comments and processing instructions. If a XML tag includes hyphens or colons, then they are converted to underscores in the corresponding Agena dictionary key.

The data must be included in an envelope.
The function also returns processing instructions in the sattr tag.
The function is written in Agena and included in the lib/xml.agn file.
The function does not cope well if one and the same XML object is present multiple times on the same hierarchy. Use utils.decodexml or xml.decode instead.
xml.readxml (filename)
Reads an XML file and returns its data in an Agena dictionary. The data must be included in an envelope.

See also: utils.readcsv, utils.readxml, xml.decode, xml.decodexml.

\subsection*{12.5.4 Constructor}
xml.new (callbacks [, separator])
The parser is created by a call to the function xml.new, which returns the created parser or raises a Lua error. It receives the callbacks table and optionally the parser separator character used in the namespace expanded element names.

\subsection*{12.5.5 Functions}
xml.close (parser)
Closes the parser, freeing all memory used by it. A call to close(parser) without a previous call to parse(parser) could result in an error.
xml.getbase (parser)
Returns the base for resolving relative URIs.

Returns the callbacks table.
```

xml.parse (parser, s)

```

Parse some more of the document. The string s contains part (or perhaps all) of the document. When called without arguments the document is closed (but the parser still has to be closed).

The function returns a non null value when the parser has been successful, and when the parser finds an error it returns five results: null, msg, line, col, and pos, which are the error message, the line number, column number and absolute position of the error in the XML document.
```

xml.pos (parser)

```

Returns three results: the current parsing line, column, and absolute position.
```

xml.setbase (parser, base)

```

Sets the base to be used for resolving relative URIs in system identifiers.
xml.setencoding (parser, encoding)
Sets the encoding to be used by the parser. There are four built-in encodings, passed as strings: 'US-ASCII', 'UTF-8', 'UTF-16', and 'ISO-8859-1'.

\subsection*{12.5.6 Callbacks}

The Agena callbacks define the handlers of the parser events. The use of a table in the parser constructor has some advantages over the registration of callbacks, since there is no need for the API to provide a way to manipulate callbacks.

Another difference lies in the behaviour of the callbacks during the parsing itself. The callback table contains references to the functions that can be redefined at will. The only restriction is that only the callbacks present in the table at creation time will be called.

The callbacks table indices are named after the equivalent Expat callbacks:
CharacterData, Comment, Default, DefaultExpand, EndCDataSection, EndElement, EndNamespaceDecl, ExternalEntityRef, NotStandalone, NotationDecl, Processinglnstruction, StartCDataSection, StartElement, StartNamespaceDecl, and UnparsedEntityDecl.

These indices can be references to functions with specific signatures, as seen below. The parser constructor also checks the presence of a field called _nonstrict in the callbacks table. If _nonstrict is absent, only valid callback names are accepted as indices in the table (Defaultexpanded would be considered an error for example). If _nonstrict is defined, any other fieldnames can be used (even if not called at all).

The callbacks can optionally be defined as false, acting thus as placeholders for future assignment of functions.

Every callback function receives as the first parameter the calling parser itself, thus allowing the same functions to be used for more than one parser for example.
```

callbacks.CharacterData = proc(parser, string)

```

Called when the parser recognises an XML CDATA string,
```

callbacks.Comment = proc(parser, string)

```

Called when the parser recognises an XML comment string.
```

callbacks.Default = proc(parser, string)

```

Called when the parser has a string corresponding to any characters in the document which wouldn't otherwise be handled. Using this handler has the side effect of turning off expansion of references to internally defined general entities. Instead these references are passed to the default handler.
```

callbacks.DefaultExpand = proc(parser, string)

```

Called when the parser has a string corresponding to any characters in the document which wouldn't otherwise be handled. Using this handler doesn't affect expansion of internal entity references.
```

callbacks.EndCdataSection = proc(parser)

```

Called when the parser detects the end of a CDATA section.
```

callbacks.EndElement = proc(parser, elementName)

```

Called when the parser detects the ending of an XML element with elementName.
```

callbacks.EndNamespaceDecl = proc(parser, namespaceName)

```

Called when the parser detects the ending of an XML namespace with namespaceName. The handling of the end namespace is done after the handling of the end tag for the element the namespace is associated with.
```

callbacks.ExternalEntityRef = proc(parser, subparser, base, systemId,
publicId)

```

Called when the parser detects an external entity reference.

The subparser is a XML/LuaExpat parser created with the same callbacks and Expat context as the parser and should be used to parse the external entity.

The base parameter is the base to use for relative system identifiers. It is set by setbase and may be null.

The systemld parameter is the system identifier specified in the entity declaration and is never null.

The publicld parameter is the public id given in the entity declaration and may be null.
```

callbacks.NotStandalone = proc(parser)

```

Called when the parser detects that the document is not `standalone`. This happens when there is an external subset or a reference to a parameter entity, but the document does not have standalone set to "yes" in an XML declaration.
```

callbacks.NotationDecl =
proc(parser, notationName, base, systemId, publicId)

```

Called when the parser detects XML notation declarations with notationName.
The base parameter is the base to use for relative system identifiers. It is set by setbase and may be null.

The systemld parameter is the system identifier specified in the entity declaration and is never null.

The publicld parameter is the public id given in the entity declaration and may be null.
```

callbacks.ProcessingInstruction = proc(parser, target, data)

```

Called when the parser detects XML processing instructions. The target is the first word in the processing instruction. The data is the rest of the characters in it after skipping all whitespace after the initial word.
```

callbacks.StartCdataSection = proc(parser)

```

Called when the parser detects the begining of an XML CDATA section.
```

callbacks.StartElement = proc(parser, elementName, attributes)

```

Called when the parser detects the begining of an XML element with elementName.

The attributes parameter is a table with all the element attribute names and values. The table contains an entry for every attribute in the element start tag and entries for the default attributes for that element.

The attributes are listed by name (including the inherited ones) and by position (inherited attributes are not considered in the position list).

As an example if the book element has attributes author, title and an optional format attribute (with `printed` as default value),
<book author=\"lerusalimschy, Roberto\" title=\"Programming in Lua\">
would be represented as
[1 ~ 'author',
2 ~ 'title',
author ~ 'Ierusalimschy, Roberto',
format ~ 'printed',
title ~ 'Programming in Lua']
callbacks.StartNamespaceDecl = proc (parser, namespaceName)
Called when the parser detects an XML namespace declaration with namespaceName. Namespace declarations occur inside start tags, but the StartNamespaceDecl handler is called before the StartElement handler for each namespace declared in that start tag.
```

callbacks.UnparsedEntityDecl =
proc(parser, entityName, base, systemId, publicId, notationName)

```

Called when the parser receives declarations of unparsed entities. These are entity declarations that have a notation (NDATA) field.

As an example, in the chunk
<!ENTITY logo SYSTEM "images/logo.gif" NDATA gif>
entityName would be "logo", systemld would be "images/logo.gif" and notationName would be "gif". For this example the publicld parameter would be null. The base parameter would be whatever has been set with setbase. If not set, it would be null.

\section*{The separator character:}

The optional separator character in the parser constructor defines the character used in the namespace expanded element names. The separator character is optional (if not defined the parser will not handle namespaces) but if defined it must be different from the character ' 10 '.

\section*{12.6 tar - UNIX tar}

As a plus package, the tar package is not part of the standard distribution and must be activated with the import statement, e.g. import tar.

\subsection*{12.6.1 Introduction}

This package lists, reads, and extracts individual files from a UNIX tar archive.
See also: gzip package.

\subsection*{12.6.2 Functions}
```

tar.close (fh)

```

Closes an archive archived file denoted by its file handle fh and returns true on success and false otherwise.

The function is written in Agena (see lib/tar.agn).
```

tar.extract (fn [, pattern])

```

Extracts files, directories, and symbolic links from the given tar archive fn , a file name of type string to the given current working directory. By default, all files are extracted. If a second argument pattern is given, then only the files matching the given pattern - a string - are copied. pattern may include wildcards, see strings.glob.

The return is a table of all the files extracted.
The function is written in Agena (see lib/tar.agn).
```

tar.lines (fh, length)

```

Creates an iterator function that with each call returns a new line of a file included in a tar file. The length (in bytes) of the archived file pointed to by fh must be given as the second argument.
fh is a numeric file handle returned by calling tar.open. Since tar.open also returns the length as a second return, it can be easily passed to tar.lines.

If the end of the archived file has been reached, the iterator function returns null. The iterator does not close the file connection, use tar.close to accomplish this.

The function is written in Agena (see lib/tar.agn).
```

tar.list (fn [, pattern])

```

Returns all files in the UNIX tar file fn (a file name), and returns a table of tables with the following information:
- file name (key ' name '),
- file mode (key 'mode'),
- start position (key 'start ', expressed as the offset to the beginning of the file),
- file length in bytes (key ' length'),
- file timestamp in UNIX time (key, ' timestamp ', decimal number of seconds since the start of a given epoch, use `os.date` to convert it into calendar date/time),
- ustar indicator ('ustar ' if set, else the empty string),
- numeric owner id (key 'ownerid', decimal),
- numeric group id (key 'groupid', decimal),
- and the decimal checksum (key 'checksum').

If a second argument pattern is given, then only the files matching the given pattern - a string - are returned. pattern may include wildcards, see strings.glob.

The function is written in Agena (see lib/tar.agn).
```

tar.open (tarfile, fn)

```

Opens an archived file fn (a file name) in the tar file given by tarfile (also a file name), sets the file pointer to the beginning of the actual contents of the archived file (i.e. not its tar header), and returns both a numeric file handle to the archived file and its size.

The function is written in Agena (see lib/tar.agn).

\section*{12.7 gzip - Library to Read and Write UNIX gzip Compressed Files}

As a plus package, in Solaris, Linux, Mac OS X, OS/2, DOS, and Windows, this library is not part of the standard distribution and must be activated with the import statement, e.g. import gzip. See also: tar package.

A typical session may look like this:
```

> import gzip;
> fd := gzip.open('primes.dat.gz', 'r'):
gzipfile(0096A9F8)
>for keys I in gzip.lines(fd) do print(i) od;
> gzip.close(f):
true
gzip.close (filehandle [, filehandle, ...])

```

Closes the files denoted by the given file handles.
```

gzip.deflate (str)

```

The function compresses the string str. The return is the compressed string and its size, in this order.

See also: gzip.inflate.
```

gzip.flush (filehandle)

```

This function takes a file handle and flushes all output to the working file.
```

gzip.inflate (str [, n])

```

The function decompresses a inflated string str. The size of the original uncompressed string is given as the second argument \(n\), which by default is size(str) +16383 )/16384. The return is the uncompressed string.

See also: gzip.deflate.
```

gzip.lines (filehandle)
gzip.lines (filename)

```

Returns an iterator function that, each time it is called, returns a new line from the file. Therefore, the construction
```

for keys line in gzip.lines(file) do ... od

```
will iterate over all lines of the file.

If a file name is given, the file is closed when the loop ends. If a file handle is given, the file is not closed.

\section*{gzip.open (filename [, mode])}

Opens a file name. If mode is not given, a default mode 'rb' will be used. mode can include special modes such as characters ' 1 ' to ' 9 ' that will be treated as the compression level when opening a file for writing.

It returns a new file handle, or, in case of errors, null plus an error message.
```

gzip.read (filehandle, format }\mp@subsup{}{1}{}, ...

```

Reads the file with the given file handle, according to the given formats, which specify what to read. For each format, the function returns a string with the characters read, or null if it cannot read data with the specified format. When called without formats, it uses a default format that reads the entire next line (see below).

The available formats are:
- '*a' reads the whole file, starting at the current position. On end of file, it returns the empty string.
- '*|' reads the next line (skipping the end of line), returning null on end of file. This is the default format.
- number reads a string with up to that number of characters, returning null on end of file. If number is zero, it reads nothing and returns an empty string, or null on end of file.

Unlike io.read, the '* \(n\) ' format is not available.

\section*{gzip.seek (filehandle [, whence] [, offset])}

Sets and gets the file position, measured from the beginning of the file, to the position given by offset plus a base specified by the string whence, as follows:
- 'set' base is position 0 (beginning of the file),
- 'cur' base is current position,
- 'end' is the end of the file.

In case of success, seek returns the final file position, measured in bytes from the beginning of the file. If this function fails, it returns null, plus a string describing the error.

The default value for whence is 'cur', and for offset is 0 . Therefore, the call gzip.seek(filehandle) returns the current file position, without changing it; the call gzip.seek(filehandle, 'set') sets the position to the beginning of the file (and returns 0); and the call gzip.seek(filehandle, 'end') sets the position to the end of the file, and returns its size.
```

gzip.write (filehandle, value., ...)

```

Writes the value of each of its arguments to the file specified by filehandle. The arguments must be strings or numbers. To write other values, use tostring or strings.format before write.

Chapter Thirteen

\section*{Communication}

\section*{13 Communication}

\section*{13.1 net - Network Library}

As a plus package, in Solaris, Linux, Mac OS X, and Windows, this library is not part of the standard distribution and must be activated with the import statement, e.g. import net.

\subsection*{13.1.1 Introduction and Examples}

This package provides basic functions to pass text from a client to a server using the IPv4 protocol. Thus it is suited to exchange information over the Internet and Local Area Networks.

\section*{Please remember that the package only supports unencrypted data transfer which might be insecure! There is no SSL support.}

If you do not use this package, no network functionality will be activated.
Please also note that when using net.accept, net.connect, net.receive, net.send, and net.survey, you will give access to your computer through LANs or the Internet, so please programme handshaking and blacklist/whitelist methods.

Limited white and blacklisting to allow or prohibit connections is supported through the net.whitelist and net.blacklist feature.

Communication is performed with `stream sockets` that ensure that data is sent and received in the original order and hopefully without errors. A socket is being created by a call to the net.open function.

In the following example, we will set up a one-way communication with the `client' sending and the `server` receiving data.

A typical session might begin by setting up the server. This is because a client cannot connect to a server until the latter is ready for it.
```

> import net alias
net v0.2.1 as of January 13, 2013
accept, address, bind, block, close, connect, listen, lookup, open,
opensockets, receive, remoteaddress, send, shutdown, survey

```

Create a socket: the net.open function returns a new socket handle:
```

> s := open():

```
932

Now associate this socket with a port on the server machine \({ }^{24}\) by running net.bind. In this example we expect data to be received on your own computer on port 1300.
```

> bind(s, '127.0.0.1', 1300):
127.0.0.1 1300

```

Now our socket must be converted to a server socket by calling
```

> listen(s):
true

```
and be told to get a pending connection by running net.accept.
net.accept waits until a client asks the server for a connection (see client example below). It returns a new socket handle which later on manages this specific connection, while the original socket is ready to wait for requests for other connection.
net.accept also returns the IP address of the client asking for a connection, and its port.
```

> t, ip, port := accept(s):
924 127.0.0.1 3230

```

If you do not want net.accept to wait indefinitely until something happens, call net.block with the original server socket and false as its second argument.

Please note that you should check the incoming connection against a white or black list so that only trusted clients can send you any data. To decline and terminate an incoming connection, either check the incoming caller and just call net.close with the handle returned by net.access, or use the built-in basic black and whitelist functionality described at the end of this subchapter.

It also a good idea to validate the incoming connection with a handshaking procedure which checks the incoming data for certain information and then automatically decides whether to go on or shut down the connection.

Data received from the client will be returned by calling net.receive with the new file handle returned by net.accept.
```

> receive(t):
Kuckuck ! 9

```

Finally, close both sockets (or just the handle returned by net.accept):
```

> close(t, s):
true

```

\footnotetext{
\({ }^{24}\) You may use the operating system commands ifconfig (UNIX, Mac) or ipconfig (Windows) to determine your own IP address.
}

To open a client session, start Agena in another shell:
```

> import net alias

```

To connect to a server, first issue:
```

> d := open()
932

```

Now connect to the server by passing the socket handle, the IP address and port number of the server. 'localhost' means that the server runs on the same machine as the client.
```

> connect(d, 'localhost', 1300):
true

```

Send some text once or more.
```

> send(d, 'Kuckuck !'):
9

```

The server immediately returns the text sent. To finish a client session, type:
```

> close(d):
true

```

Call net.opensockets to have a look at the state of all open sockets.
Following now is an extended but crude example for a one-way connection which sends one thousand hashes from the client to the server on the local host on port 1300.

Since with one single call, net.receive by default processes `only` 512 bytes in Windows and usually 8,192 bytes in UNIX, the server uses a while loop to receive all the data until the client closes the connection.

Since net.receive returns two results - the string and the number of characters received - its second return will be 0 if the client terminates a network session.
\begin{tabular}{|c|c|}
\hline Server & Client \\
\hline ```
> import net alias
> d := open():
132
> bind(d, 'localhost', 1300):
127.0.0.1 1300
> listen(d):
true
> e, f, g := accept(d);
> print(e,f, g);
352 127.0.0.1 49178
> x, y := receive(e);
> print(x, y);
##### (512 hashes) ##### 512
> while y <> 0 do
> x, y := receive(e);
> print(x, y);
> od;
##### (more hashes) #### 488
        0
> close(e, d):
true
``` & ```
> import net alias
> d := open():
352
> connect(d, 'localhost', 1300):
true
> send(d, strings.repeat('#', 1m)):
1000000
> close(d):
true
``` \\
\hline
\end{tabular}

A simple bi-directional connection:
\begin{tabular}{|c|c|}
\hline Server & Client \\
\hline ```
> import net alias
> d := open():
124
> bind(d, 'localhost', 1300):
127.0.0.1 1300
> listen(d):
true
> e, f, g := accept(d);
> print(e,f, g);
344 127.0.0.1 49183
> x, y := receive(e);
> print(x, y);
## etc. 512
> send(e, 'Got ' & y & ' bytes');
``` & ```
> import net alias
> d := open():
124
> connect(d, 'localhost', 1300):
true
> send(d, strings.repeat('#', 1k)):
1000
> receive(d):
Got }512\mathrm{ bytes 13
> receive(d):
Got 488 bytes 13
> close(d):
true
``` \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Server & & Client \\
\hline ```
> while y <> 0 do
> x, y := receive(e);
> print(x, y);
> send(e, 'Got '
bytes');
> od;
## etc.
488
    0
> close(e, d):
true
``` & \[
y \quad \& \quad '
\] & \\
\hline
\end{tabular}

Usage of black and whitelists: First initialise the net package.
> import net alias

Now put one or more a numeric (!) IPs to be blocked into the set net.blacklist to prohibit connections to these addresses (valid for both net.connect and net.accept).
```

> net.blacklist := {'127.0.0.1'}
> d := open():
3
> connect(d, '127.0.0.1', 1300):
Error in `net.connect`: partner in blacklist, closing socket 3.
Stack traceback: in `connect
stdin, at line 1 in main chunk

```

Socket d is now closed:
```

> opensockets():

```
[]

Now define a whitelist with all IPs to which a connection is allowed.
```

> net.whitelist := {'127.0.0.2'}
>d := open():
3
> return connect(d, '127.0.0.3', 1300)
Error in `net.connect`: partner not in whitelist, closing socket 3.
Stack traceback: in `connect
stdin, at line 1 in main chunk

```

The socket is closed, as well.
```

> opensockets():

```
[]

\subsection*{13.1.2 Functions}
net.accept (s)
Accepts a connection request from a client on the given server socket handle s. If the server socket has been set to blocking mode, it waits until there is an incoming connection.

The function returns a new socket handle (a number) for the data to be received later on, and the address (a string) and port (a number) of the client socket.

Please note that the new socket created by net.accept must be closed separately to avoid too many open sockets.

The function also checks the global sets net.blacklist and net.whitelist, in this order, and if they exist. If you are trying to accept a connect from an address that is included in net.blacklist, then net.accept refuses this connection, closes the new socket that it created (see above), and issues an error. If you are trying to accept a connection from an address that is not in net.whitelist, the function does not establish a connection, closes the freshly created socket, and issues an error, as well.

Please note that net.blacklist and net.whitelist must only contain numeric IPs, and not addresses like 'sunsite.abc.xyz'. However, net.accept tries to convert the incoming address to a numeric IP address and then checks both lists \({ }^{25}\). If an address could not be resolved, the function does not allow a connection, and closes the newly created socket, and finally issues an error.

You may use protect in order to intercept the errors described above, but you must take care yourself for allowing or prohibiting a connection.

You have to set up net.blacklist and/or net.whitelist yourself after initialising the net package.

The procedure is a binding to \(\mathrm{C}^{\prime}\) s accept function.
See also: net.accept, net.bind, net.block, net.listen, net.receive, net.survey.

\footnotetext{
\({ }^{25}\) Usually, the server that tries to connect sends its numeric IP address, but probably it does not. So this is just a precautionary action.
}

\section*{net.admin}

Table containing various operating system-specific administrative network settings:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline maxnsockets & \begin{tabular}{l} 
estimated maximum number of open sockets \\
allowed
\end{tabular} \\
\hline protocols & a table containing the supported protocols \\
\hline
\end{tabular}
```

net.address (s)

```

Returns two values: the IP address (a string) and port number (a number) to which socket s is bound.

See also: net.lookup, net.remoteaddress.
```

net.bind (s [, address [, port]])

```

Associates a socket s with an IP address and a port on the local machine and returns its IP address (a string) and the respective port on success or returns false and a string containing the error message otherwise.

If address is not given, localhost is bound to the socket (i.e. your own computer), otherwise the numeric IP address or host name is bound.

By default, port 1234 is connected, but you may specify another port (an integer) as a third argument. This might require administrative rights.

The procedure is a binding to C's bind function.
To determine your own IP address, open a shell and issue the command ipconfig in Windows, and ifconfig in Solaris, Linux, Mac, or other UNIX based platforms.

See also: net.accept, net.listen, net.receive, net.survey.
```

net.block (s, mode)

```

Sets a socket to blocking or non-blocking mode. The functions expects the socket handle (a number) s as its first argument and the mode (a Boolean) as its second argument. If the second argument is true, the socket is set to blocking mode, else to non-blocking mode. The return is true on success and false otherwise.

The procedure is a binding to C's fentl (UNIX) or ioctlsocket (Windows) function.
```

net.close (...)

```

Terminates all the given servers or clients denoted by their socket handles and returns true on success, or false and a string containing an error message otherwise.

The procedure is a binding to C's close or closesocket function.
net.closewinsock ([anything])
The function is available only in the Windows edition. It finally terminates the current network session and returns true on success, or issues an error otherwise if anything is not given. If any value anything is passed to the function, in case of an error it returns fail plus an error message of type string.

Please note that when you call this function, no further network communication will be possible. Call net.openwinsock to enable network communication again.

The procedure is a binding to C's wSACleanup function.
See also: net.openwinsock.
net.connect (s [, address [, port]])
Connects the client denoted by it socket handle s (first argument, a number) to a server at the specified IP address (second argument, a string) and its port (third argument) so that data can be sent later. If address is missing, the address is set to ' localhost', if port is missing, port 1234 will be used.

If the client socket is set to blocking mode, the function waits until the server responds; if the client socket is set to non-blocking mode, it immediately returns without waiting for a server response.

The return is either true in case of success or false and the error message (a string) at failure.

The function also checks the global sets net.blacklist and net.whitelist, in this order, and if they exist. If you are trying to connect to an address that is included in net.blacklist, then net.connect does not establish a connection, closes socket s, and issues an error. If you are trying to connect to a server that is not in net.whitelist, the function does not establish a connection, closes the socket, and issues an error, as well.

Please note that net.blacklist and net.whitelist must only contain numeric IPs, and not addresses like 'sunsite.abc.yz'. However, net.connect tries to convert address to a numeric \(\mathbb{I P}\) address and then checks both lists. If an address could not be resolved, the function does not establish a connection, closes socket s and issues an error.

You may use protect in order to intercept the errors described above, but you must take care yourself for allowing or prohibiting the connection.

You have to set up net.blacklist and/or net.whitelist yourself after initialising the net package.

The procedure is a binding to \(\mathrm{C}^{\prime}\) s connect function.
See also: net.send.
```

net.isconnected ()

```

In Windows, checks whether you are currently connected to the internet and returns true or false. The function is not available on other plafforms.
```

net.listen (s [, length])

```

Converts the given socket s to a server socket, enabling it to accept connections. You may optionally pass an integer in the range [1, 1024] determining the length of the queue for pending connections.

The return is either true, or false and a string with an error message if listening failed.
You must first run this function before calling net.accept and net.receive.
The procedure is a binding to C's listen function.
```

net.lookup ([x])

```

Determines the IP, an optional alias, the official name and the supported protocol of a given URL or numeric IP x of type string. If no argument is passed, the function will return the information on 'localhost'.

An example:
```

> lookup('www.zeit.de'):
[networkaddress ~ [0.0.0.1], alias ~ [zeit.de], official ~ Die Zeit, type ~
IPv4]
> lookup('10.137.0.1'):
[networkaddress ~ [10.137.0.1], alias ~ [anything.yz], official ~ Anything,
type ~ IPv4]

```

See also: net.address, net.remoteaddress.
```

net.open ([blocking])

```

Creates a (client) network socket. If the optional first argument blocking is set to false, the socket is set to non-blocking mode.

The return is the socket handle (a number), the default address 'localhost' and default port 1234, the protocol (a number) and a Boolean indicating whether the handle can be reused by the system after the socket has been closed. If a new socket could not be opened, an error is issued.
net.open does not connect the client to a server - use net.connect for this.

To create a server socket waiting for input, use net.bind, net.listen, and net.accept.

The procedure is a binding to C's socket function.
See also: net.close.
```

net.opensockets ()

```

Returns all open sockets along with their respective attributes.

The return is a table with its keys the open socket handles, and their entries tables containing information on whether the socket is a server or client (key 'server', true or false), their own address (key 'address', a string), their own port (key 'port', a number), the protocol being used (key 'protocol', a number), whether the socket works in blocking or non-blocking mode (key 'blocking', true or false), and whether the socket has been connected to a server ('connected', true or false).

The table key 'mode' holds information on the read and write status of the socket:
\begin{tabular}{|l|l|}
\hline Value & Meaning \\
\hline 'none' & the socket is not connected \\
\hline 'shutdown' & the socket no longer can receive or send data \\
\hline 'read' & the socket can only receive data, but cannot send any \\
\hline 'write' & the socket can only send data, but cannot receive any \\
\hline 'readwrite' & the socket can both send and receive data (the default) \\
\hline
\end{tabular}

Please note that modifying the contents of the table returned will not have any effect on the status of the sockets, so you cannot do any harm.

See also: net.shutdown.
```

net.openwinsock ([anything])

```

The function is available only in the Windows edition. It re-enables network communication and returns true on success, or issues an error otherwise if anything is not given. If any value anything is passed to the function, in case of an error it returns fail plus an error message of type string.

When initialising the net package by calling readlib or with, Agena automatically starts the Winsock daemon, so you do not have to call this function explicitly.

The procedure is a binding to C's wsAStartup function.
See also: net.closewinsock.
```

net.receive (s [, getall [, maxlength]])

```

Allows a server socket s to receive a string from a client. The function returns this string and its length (a number). s should be the socket handle returned by net.accept.

If the return is the empty string plus the value 0 (zero) for its length, the client has closed the connection - this is also a proper check on whether a client is still connected with a server socket. Please note that in this case, no further data can be received on this socket and you have to close s manually.

If true has been passed for the optional argument getall, the function reads in all data from the client until the latter closes the connection. If the client does not close the connection, net.receive waits infinitely.

The optional argument maxlength determines the maximum number of characters to be received. If a client tries to send more data than specified by maxlength, the function returns false and the string 'too many bytes received'.

The maximum number of bytes to be read by one stroke is determined by environ.kernel('buffersize') which value depends on the operating system and can also mbe changed.

If any error occurs during receipt of the data, net.receive does not close the socket \(s\), but returns false and a string containing either the message 'failure during receipt' or 'too many bytes received', the latter if maxlength and the number of bytes received exceeded it.

The procedure is an extended binding to C's recv function.
See also: net.accept, net.bind, net.block, net.listen, net.receive, net.send, net.survey.

\section*{net.remoteaddress (s)}

Returns two values: the IP address (a string) and port (a number) of the server that the client socket s is connected to.

See also: net.address, net.lookup.
```

net.send (s, str [, true])

```

Sends a string str (second argument) from the client denoted by its socket handle \(s\) (first argument, a number) to a server.

The return is the number of the characters actually sent. If the kernel decides not to send all the data in one chunk, the function might not send the complete string. If an optional third argument, the Boolean true, is given, net.send, however, tries to make sure that the complete string has been sent when it returns.

If \(s t r\) is the empty string, it will not be sent to the server.
The function returns fail and the string 'socket not connected' if the socket has not been connected before by either net.connect or net.accept. It also returns fail and 'socket not connected' if the connection has been disconnected.

If the number of bytes actually sent is not equal to the length of the string str, the function returns false, the string 'transfer size mismatch', and the number of bytes sent.

The procedure is an extended binding to C's send function.
See also: net.connect, net.receive.
```

net.shutdown (s, what)

```

The function stops further sends and receives on a socket s. If what is the string 'read', then the socket can no longer receive data; if what is the string 'write', it can lo longer send data; and if what is the string 'readwrite', it will not do both any longer.

Please note that socket s will still be active. Call net.close if you want to release the socket completely.

\section*{See also: net.opensockets.}
```

net.smallping (ip, port [, iters [, delay [, message [, noprint]]]])

```

Opens a socket, connects to a server given by the string ip (either a domain name or a numeric ip) on its port port, a number, optionally sends a string to the server, and then closes the connection again. It resembles the UNIX ping command, but works on a low-level network connection and does not use ICMP.

By default, only one connection attempt is conducted before the function returns. You can specify the number of connection attempts by the optional argument iters, a positive integer.

The function waits one second before connecting to the server again. You can change this by passing a different number of seconds for the argument delay, a positive integer.

If message is not given, the function does not send any data to the server. You can change this by passing a string as argument message, which might also be the empty string.

By default, the function prints the connection results at the console with each iteration. This can be suppressed by passing any non-null value as argument noprint. If you specify a value for noprint and if you do not want to send a string to the server, just pass a non-string value as argument message.

The following data is printed at the console if noprint is void: Date and time, round-trip time for the current connection in seconds, average round-trip time, a Boolean indicating whether the connection was successful (true) or not (false), and the number of the current iteration. Example:
```

> net.smallping('www.anything.foo', 80, 4, 2)
> \# four iterations, 2-second delay, no message
2014/01/01 13:54:30 0.296 0.296 true 1
2014/01/01 13:54:32 0.031 0.163 true 2
2014/01/01 13:54:34 0.047 0.125 true 3
2014/01/01 13:54:36 0.047 0.105 true 4

```

The function returns the date and time of the final iteration as a number indicating the number of seconds passed since a given `epoch`, the average round-trip time in seconds as a number, and a Boolean indicating whether the last connection attempt was successful (true) or not (false). Use skycrane.todate to convert the numeric date into a readable format.

The function is written in Agena and included in the lib/net.agn file.
net.survey ([0], [timeout [, mode [, throw]]])
The function looks for activity on all open sockets, or of specific sockets. If you want to scan only specific sockets, pass a sequence oof socket handles as the first argument.

The returns are three sequences and a Boolean: the first sequence with descriptors of sockets ready for reading, the second sequence containing all descriptors of sockets ready for writing, and the third sequence with the descriptors of sockets which encountered exceptional conditions. (Exceptional conditions are not failures.) If the Boolean is true then input is available, if it is false it indicates a timeout.

By default, net.survey waits endlessly and only returns if a network action has been detected (so-called `blocking mode`).

If the positive number timeout is passed to the function, the functions will always return after timeout seconds even if there was no activity, if timeout is infinity, it waits endlessly for a connection.

If mode is the string 'read', then the function only scans sockets ready for reading. If mode is the string 'write', then the function only scans sockets ready for writing. If mode is the string 'except', then the function only scans sockets where exceptions occurred. In all three cases, the returns are a sequence of the respective sockets handles and the Boolean true if input is available, or false at timeout.

If throw is set to false, then the function does not quit with an error in case the socket status could not be determined.

A socket handle returned can be passed to the net.accept function so that an incoming connection can be further processed.

The function is a binding to \(C^{\prime}\) s select function.
See also: net.accept, net.bind, net.listen, net.receive.
net.wget (domain, [path [, port]]])
The function downloads an HTML file from a web server.
domain, a string, specifies the domain. path, also of type string, indicates the absolute path including the HTML file name on the web server. If port, a non-negative integer less than 65,535 is given, then the function tries to query this port instead of the standard HTML port 80.

If only domain is given, then it may include the absolute path. If you want to download data from a different port than 80, however, you must pass the absolute path as the second argument.

The function uses the HTTP 1.0 protocol along with the GET method.
The function returns the retrieved web page as a string, including its HTTP protocol header.

Examples:
```

> import net
> net.wget('www.lua.org', 'about.html'):
HTTP/1.1 200 OK
Server: Zeus/4.3

```
> net. wget('www.lua.org/about.html'):

The function is written in Agena and included in the lib/net.agn file.

\section*{13.2 usb - libusb Binding}

As a plus package, this library is not part of the standard distribution and must be activated with the import statement, e.g. import usb.

The package provides 1:1 access to libusb functions. Please have a look at the libusb man pages and is available in the Windows version of Agena, only.

The functions provided by this binding are:

\subsection*{13.2.1 CTX Functions}
\begin{tabular}{|l|l|}
\hline Package function name & Corresponding libusb function \\
\hline usb.event_handler_active & libusb_event_handler_active \\
\hline usb.event_handling_ok & libusb_event_handling_ok \\
\hline usb.get_device_list & libusb_get_device_list \\
\hline usb.get_next_timeout & libusb_get_next_timeout \\
\hline usb.get_pollfds & libusb_get_pollfds \\
\hline usb.handle_events & libusb_handle_events \\
\hline usb.handle_events_locked & libusb_handle_events_locked \\
\hline usb.handle_events_timeout & libusb_handle_events_timeout \\
\hline usb.lock_event_waiters & libusb_lock_event_waiters \\
\hline usb.lock_events & libusb_loc__events \\
\hline usb.pollffs__handle_timeouts & libusb_pollfds_handle_timeouts \\
\hline usb.set_debug & libusb_set_debug \\
\hline usb.set_pollfd_notifiers & libusb_set_pollfd_notifiers \\
\hline usb.try_lock_events & libusb_tr_lock_events \\
\hline usb.unlock_event_waiters & libusb_unlock_event_waiters \\
\hline usb.unlock_events & libusb_unlock_events \\
\hline usb.wait_for_event & libusb_wait_for_event \\
\hline
\end{tabular}

\subsection*{13.2.2 DEV Functions}
\begin{tabular}{|l|l|}
\hline Package function name & Corresponding libusb function \\
\hline usb.get_active_config_descriptor & libusb_get_active_config_descriptor \\
\hline usb.get_bus_number & libusb_get_bus_number \\
\hline usb.get_config_descriptor & libusb_get_config_descriptor \\
\hline usb.get_config_descriptor_by_value & libusb_get_config_descriptor_by_value \\
\hline usb.get_device_address & libusb_get_device_address \\
\hline usb.get_device_descriptor & libusb_get_device_descriptor \\
\hline usb.get_max_iso_packet_size & libusb_get_max_iso_packet_size \\
\hline usb.get_max_packet_size & libusb_get_max_packet_size \\
\hline usb.open & libusb_open \\
\hline
\end{tabular}

\subsection*{13.2.3 Handles}
\begin{tabular}{|l|l|}
\hline Package function name & Corresponding libusb function \\
\hline usb.attach_kernel_driver & libusb_attach_kernel_driver \\
\hline usb.bulk_transfer & libusb_bulk_transfer \\
\hline usb.claim_interface & libusb_claim_interface \\
\hline usb.clear_halt & libusb_clear_halt \\
\hline usb.close & closehandle \\
\hline usb.control_transfer & libusb_control_transfer \\
\hline usb.detach_kernel_driver & libusb_detach_kernel_driver \\
\hline usb.get_configuration & libusb_get_configuration \\
\hline usb.get_descriptor & libusb_get_descriptor \\
\hline usb.get_device & libusb_get_device \\
\hline usb.get_string_descriptor & libusb_get_string_descriptor \\
\hline usb.get_string_descriptor_ascii & libusb_get_string_descriptor_ascii \\
\hline usb.get_string_descriptor_utf8 & libusb_get_string_descriptor_utf8 \\
\hline usb.interrupt_transfer & libusb_interrupt_transfer \\
\hline usb.kernel_driver_active & libusb_kernel_driver_active \\
\hline usb.release_interface & libusb_release_interface \\
\hline usb.reset_device & libusb_reset_device \\
\hline usb.set_configuration & libusb_set_configuration \\
\hline usb.set_interface_alt_setting & libusb_set_interface_alt_setting \\
\hline
\end{tabular}

\subsection*{13.2.4 Transfer Functions}
\begin{tabular}{|l|l|}
\hline Package function_name & Corresponding libusb function \\
\hline usb.cancel_transfer & libusb_cancel_transfer \\
\hline usb.control_transfer_get_data & libusb_control_transfer_get_data \\
\hline usb.contro__transfer_get_setup & libusb_control_transfe__get_setup \\
\hline usb.fill_bulk_transfer & libusb_fill_bulk_transfer \\
\hline usb.fill_control_setup & libusb_fill_control_setup \\
\hline usb.fill_control_transfer & libusb_fill_control_transfer \\
\hline usb.fill_interrupt_transfer & libusb_fill__interrupt_transfer \\
\hline usb.fill_iso_transfer & libusb_fill_iso_transfer \\
\hline usb.get__so_packet_buffer & libusb_get__so_packet_buffer \\
\hline usb.set_iso_packet_buffer & libusb_set_iso_packet_buffer \\
\hline usb.set_iso_packet_lengths & libusb_set_iso_packet_lengths \\
\hline usb.submit_transfer & libusb_submit_transfer \\
\hline usb.transfer_get_data & libusb_transfer_get_data \\
\hline
\end{tabular}

\subsection*{13.2.5 Miscellaneous Functions}
\begin{tabular}{|l|l|}
\hline Package function name & Corresponding libusb function \\
\hline usb.init & libusb_init \\
\hline usb.open_device_with_vid_pid & libusb_open_device_with_vid_pid \\
\hline usb.transfer & libusb_transfer \\
\hline
\end{tabular}

\section*{13.3 com - Serial RS-232 Communication through COM Ports}

As a plus package, the com package is not part of the standard distribution and must be activated with the import statement, i.e. import com.

The com library allows to send and receive data through physical and virtual COM ports. It is currently in an experimental state.

Typical usage for sending data to another com port:
```

> import com
> fd := com.open('COM4');
> com.init(fd, 9600, "sb1"):
> com.attrib(fd):
> com.write(fd, 'hallo !');
> com.close(fd);

```
Reading data from a com port:
> fd := com.open('COM4');
> com.init(fd, 9600, "sb1"):
> do \# if nothing has been read, com.read ...
> str := com.read(fd, 80); \# returns null ...
\(>\) if str : : string then print(str) fi \# and a string otherwise
> od;

The functions included are:

\section*{com.open (port)}

Creates a handle to the given COM port str, a string, and returns the handle, of type userdata.

In Windows, a COM port may be denoted by the strings ' сом1 ', ' сом2 ', etc.
The function does not configure the port, see com.init.
See also: com.close.
```

com.close (hdl)

```

Closes the given port denoted by its handle hdı of type userdata.
See also: com.open.
```

com.write (hdl, str)

```

Sends the entire string str to the port denoted by hdl. The number of bytes actually sent will be returned.

See also: com.read.
```

com.read (hdl [, bufsize])

```

Reads data from the port denoted by hal and returns it as a string. If nothing could be read, the return is null.

The (maximum) number of bytes to be read is given by bufsize. If not given, the function tries to read the entire in-queue. You should prefer to pass a value for bufsize.

See also: com.write.
```

com.attrib (hdl)

```

Returns the settings of the given COM port, denoted by its handle hdl. The function is available in Windows only.
```

com.init (hdl, option1, options, (, ..)

```

Configures the COM port denoted by its handle hdı. The function re-initialises all hardware and control settings, but it does not empty output or input queues.

Supported settings are:
- 'reset' - reset
- baud rate, a number,
- 'cs5' to 'cs8', - character size,
- 'parno', 'parodd', 'pareven' - parity
- 'sb1', 'sb2' - stop bits,
- 'foff','frtscts','fxio' - flow Controls.

\section*{Example:}
```

> com.init(fd, 9600, "sb1");

```

In DOS, you (obviously ?) can only use baud rates 9600, 19200 and 38400. At least in UNIX, supported baud rates are:

9600, 19200, 38400, 57600, 115200, 230400, 460800, 500000, 576000, 921600, \(1000000,1152000,1500000,2000000,2500000,3000000,3500000,4000000\)
com.control (hdl, option1, ...)
Sets DTR/DSR or RTS/CTS hardware flow controls to the COM port denoted by its handle hdl. Options are:
- 'dtr' - Data Terminal Ready
- 'dsr' - Data Set Ready
- 'rts' - Request To Send
- 'cts' - Clear To Send

The function does not empty output or input queues.
```

com.timeout (hdl, msecs)

```

Sets the time-out parameters for all read and write operations on the specified COM port, denoted by its handle hdl. msecs is in milliseconds.
```

com.queues (hdl, in_buffersize, out_buffersize)

```

Sets buffer sizes for in and out queues for the COM port denoted by its hal handle. *buffersizeS are integers.
```

com.purge (hdl, mode)

```

Discards all characters from the output or input buffer of the given COM port, denoted by it handle hal. It can also terminate pending read or write operations on the resource.
mode may be the string: 'rw', 'r' or 'w'.
```

com.wait (hdl, event1, ...)

```

Waits for an event to occur for the COM port denoted by its handle hdl. The set of events that are monitored by this function are the strings: 'car', 'cts', 'dsr', 'ring'.

The function returns a Boolean.

Chapter Fourteen
System \& Environment

\section*{14 System \& Environment}

\section*{14.1 os - Access to the Operating System}

This library is implemented through table os.
To determine the operating system and CPU in use by Agena, see the environ.os and environ.cpu environment variables explained in Appendix A3.

Summary of functions:
File and directory handling:
os.chdir, os.chmod, os.chown, os.curdrive, os.curdir, os.dirname, os.exists, os.fattrib, os.fcopy, os.filename, os.fstat, os.ftok, os.gettemppath, os.inode, os.isdir, os.isfile, os.islink, os.iterate, os.list, os.listcore, os.mkdir, os.move, os.prefix, os.readlink, os.realpath, os.remove, os.rmdir, os.suffix, os.symlink, os.tmpdir, os.tmpname, os.whereis.

Hardware access:
os.battery, os.beep, os.cdrom, os.endian, os.freemem, os.hasnetwork, os.isdocked, os.ismounted, os.isremovable, os.isvaliddrive, os.meminfo, os.screensize.

\section*{Operating System Access:}
os.codepage, os.computername, os.cpuinfo, os.cpuload, os.drives, os.drivestat, os.environ, os.execute, os.exit, os.getenv, os.getlanguage, os.getlocale, os.getmodulefilename, os.groupinfo, os.isansi, os.isarm, os.isdos, os.islinux, os.islocale, os.isos2, os.isppc, os.isunix, os.iswindows, os.isx86, os.login, os.netdomain, os.netsend, os.netuse, os.os2info, os.pause, os.pid, os.setenv, os.settime, os.setlocale, os.system, os.terminate, os.userinfo, os.wait, os.winver.

Date and Time:
os.clock, os.date, os.datetosecs, os.difftime, os.esd, os.isdst, os.Isd, os.now, os.secstodate, os.speed, os.time, os.tzdiff, os.uptime, os.usd.
os.battery ()
On Windows 2000 and later, the function returns the current battery status of your system (usually laptops) as a table with the following information:
\begin{tabular}{l|l|}
\hline Key & Meaning \\
\hline 'acline' & 'on', 'off', or 'unknown' \\
\hline 'installed' & true if a battery is present, and false otherwise \\
\hline 'life' & \begin{tabular}{l} 
battery life in percent; a value > 100 indicates that a battery is \\
not installed (see 'status' entry)
\end{tabular} \\
\hline 'status' & \begin{tabular}{l} 
either 'low' (capacity \(<33 \%), ~ ' m e d i u m ' ~(c a p a c i t y ~>~ 32 \% ~ a n d ~\) \\
\(<67 ~ \%), ~ ' h i g h ' ~(c a p a c i t y ~>~ 66 \%), ~ ' c r i t i c a l ' ~(c a p a c i t y ~<~ 5 \%), ~\)
\end{tabular} \\
'charging', 'no battery', 'unknown'
\end{tabular}

On OS/2 Warp 4 and higher, with APM running, the functions returns the status of the battery as a table with the following information:
\begin{tabular}{l|l|}
\hline Key & Meaning \\
\hline 'acline ' & 'on', 'off', 'unknown', or 'invalid' \\
\hline 'life' & battery life in percent, or 'undefined' if not available \\
\hline 'status' & either 'high',' 'low', 'critical', 'charging', 'unknown', or 'invalid' \\
\hline \begin{tabular}{l} 
'flags'
\end{tabular} & OS/2 power flags \\
\begin{tabular}{l} 
'power- \\
management'
\end{tabular} & true if power management is switched on, or false if not. \\
\hline
\end{tabular}

On other operating systems, the function returns fail.
```

os.beep ()
os.beep (freq, dur)

```

In the first form, the functions sounds the loudspeaker with a short `beep` and returns null.

The second form sounds the loudspeaker with frequency freq Hz (a positive integer in the range 37 .. 32767) for dur seconds (a positive float) in Windows, DOS and OS/2. In UNIX, the loudspeaker beeps dur times, and the frequency is ignored (just pass any number to freq). Returns null if a sound could be created successfully, or fail if non-positive arguments were passed.
```

os.cdrom (d, action)

```

Opens and closes the tray of an optical disk drive d. It can also eject any other removable drive d. If action is 'open' or 'eject', the tray is opened or the media is ejected. If action is 'close', the tray is closed. The function is available in the OS/2, Linux, and Windows edition of Agena only.

\section*{See also: os.unmount.}
```

os.chdir ([str [, any]])

```

Changes into the directory given by string str on the file system. Returns true on success and issues an error on failure otherwise if any has not been given. If you pass any second argument, the function will not issue an error and will return false if the given path does not exist, or fail if you have no permission to enter the directory.

If no argument is given or null is passed for str, the name of the current working directory will be returned as a string. Otherwise, the function will commit the change of directory and return true.

See also: os.curdir, os.dirname, os.isdir, os.iterate, os.list.
```

os.chmod (fn, m)

```

Takes a file path fn (a filename, thus a string) and a mode m (an integer) denoting a three-digit octal number and changes the file permissions accordingly. Contrary to os.fattrib, mode m must not be preceded by the `Oo` token. The function returns true on success and issues an error otherwise. It is available in the UNIX versions of Agena, only.

See also: os.chown, os.fattrib.
```

os.chown (fn, o [, g])

```

The function changes the owner of the file fn (a filename, thus a string) to owner \(\circ\), and optionally to group \(g\).
- and g may be numbers or strings. If a number is passed for \(\circ\) or g , it denotes a user id (uid) or group id (gid), respectively. If a string is passed, it denotes a user or group name. If \(g\) is not given, the default group of user \(\circ\) is set.

The function returns true on success and issues an error message otherwise. It is available in the UNIX versions of Agena, only.

See also: os.chmod, os.fattrib.
```

os.clock ()

```

Returns the processor time used by Agena. Divide the return by environ.kernel().clockspersecond to get the number of seconds.

See also: time, os.time.
```

os.codepage ()
os.codepage (p)

```

In Windows, in the first form, returns - in the following order: input code page, output code page, the input code page name and the output code page name.

In OS/2, in the first form, returns - in the following order: input code page and output code page. In DOS, in the first form, returns the output code page.

In OS/2 and Windows only, in the second form, sets the input and output code page. To change the input code page, pass the pair 'input': <code page number>. To change the output code page, pass the pair 'ouput': <code page number>.

In all other operating systems, the function is not available.
See also: os.getlocale, os.setlocale.
os.computername ([option])
Returns the name of the computer in Windows, OS/2, DOS, Mac OS X and UNIX. The return is a string. On other architectures, the function returns fail.

If called with any option, returns detailed information on the NetBIOS or DNS name associated with the local computer in a table.

See also: os.netdomain.
```

os.cpuinfo ()

```

Returns various information on the CPU in use: its type, frequency, and number of cores. It is available in Windows 2000 and later, OS/2, DOS, Solaris, Linux, and Mac OS \(X\) only \({ }^{26}\). The return is a table with the following fields:

\footnotetext{
\({ }^{26}\) In Solaris, you may issue io.pcall('kstat') and parse its return.
}
\begin{tabular}{|c|c|c|c|c|c|}
\hline Field & Meaning & OS/2 & Windows & Mac & Linux \\
\hline 'bigendian' & endianness: true means Big Endian, false Little Endian, and fail undetermined. & X & X & X & X \\
\hline 'bogomips' & crude measurement of CPU speed & & & & X \\
\hline 'brand' & processor name, a string \({ }^{27}\) & & X & X & X \\
\hline 'cpuid' & detailed information on the underlying CPU hardware returned by the C function _cpuid. & & X & & \\
\hline 'cputype' & detailed information on the CPU & & X & & \\
\hline 'frequency' & clock rate in MHz , a posint & & X & X & X \\
\hline 'level' & processor level, a posint & & X & X & \\
\hline 'model' & processor model, a posint & & & X & X \\
\hline 'ncpu' & number of cores, a posint & X & X & X & \\
\hline 'revision' & processor revision, a posint & & X & & \\
\hline 'stepping' & processor stepping, a posint & & & X & X \\
\hline 'support' & supported instruction sets & & X & & \\
\hline 'type' & architecture: in Windows the string: 'x86', 'x64', 'ARM', 'Itanium', or 'unknown'; on a Mac: 'x86', 'x64', 'ppc', 'ppc64', 'MC680x0', 'MC88000', MC98000', HPPA', 'ARM', 'sparc', 'i860', or 'unknown'. In Linux: a posint. & X & X & X & X \\
\hline 'vendor' & vendor ID, e.g. 'GenuineAMD', 'Genuinelntel'. & & X & X & X \\
\hline
\end{tabular}

On all supported operating systems, all data is determined by querying the first processor on the platform, assuming that all other cores have the same features. The returns may be platform-dependent - especially, the return regarding 'level' may have a different meaning.

On other platforms, the function returns fail.
The Linux version has been written in Agena, see the lib/library.agn file; the other OS versions have been implemented in C .

See also: os.cpuload, os.endian.

\section*{os.cpuload ()}

In OS/2, Linux and Mac OS X, returns the 1,5 and 15 minute load averages of the computer as a sequence of three numbers in the range [0, 1]. In Windows Vista and later, it just returns a sequence containing the current average load, the load caused by the kernel and the load caused by user programmes - all three in the range [ 0,1 ] - plus the number of elements in the CPU queue, the number of

\footnotetext{
\({ }^{27}\) The return may include leading or trailing blanks.
}
context switches per second and the number of interrupts per second - in this order. If the load could not be returned, the function just returns fail.

On all other platforms, the function returns fail.

\section*{See also: os.cpuinfo, os.speed.}
os.curdir ()
Determines the current working directory and returns its absolute path.
See also: os.chdir.
os.curdrive ()
In OS/2, DOS, and Windows returns the letter of the current drive, a one-character string with an appending colon.
```

os.date ([format [, time]])
os.date ([format [, obj]])
os.date (format, year, month, day [, hour [, minute [, second]]])

```

Returns a string or a table containing date and time, formatted according to the given string format.

If the time argument is present, i.e. the number of seconds elapsed since a given epoch (usually January 01, 1970, or try os. now (0) ), this is the time to be formatted. Otherwise, date formats the current time. To convert a date and time to seconds, see os.datetosecs.

In the second form, receives a format and a date and optionally time of the form year, month, date [, hour [, minute [, second]]], with all values in table, sequence or register obj. Alternatively in the third form, year. month, day and optionally hour, minute, and second can be passed directly.

If format starts with '!', then the date is formatted in Co-ordinated Universal Time. After this optional character, if format is *t, then date returns a table with the following fields: year (four digits), month (1..12), day (1..31), hour (0..23), min (0..59), sec (0..59), msec (0..999) - if milliseconds could be determined, wday (weekday, Monday is 1 , Sunday is 7), yday (day of the year, where 1 is January 01 , and December 31 either 365 or 366), and isdst (daylight saving flag, a boolean). By setting environ.kernel(iso8601 = false), the weekday return 1 means Sunday and 7 Saturday.

If the format is \({ }^{j}\), the Julian date, a number, will be returned. If the format is \(* 1\), the Lotus 1-2-3 Serial Date, a number, will be returned. For more information on the Lotus Serial Date value returned, see os.Isd. If the format is *e, the Excel Serial Date,
a number, will be returned, see os.esd. *sdn computes the Julian date in the Julian calendar (whereas *j, *ı, *e , *t compute it in the Gregorian calendar).

If format is not *t, *e, *l, *j, or *sdn, then date returns the date as a string, formatted according to the same rules as the \(C\) function strftime.

When called without arguments, os.date on all supported platforms returns a string of the format 'YYY/MM/DD mm:hh:ss.xxx', where .xxx denotes milliseconds, if they could be determined; otherwise the return would simply be in the format "YYY/MM/DD mm:hh:ss'.

Examples:
```

> os.date('%a, %d %b %Y %H:%M:%S, %z'):
Mon, 02 Nov 2015 17:22:09, W. Europe Standard Time
> os.date('%A, %d %B %Y %H:%M:%S, %z'):
Monday, 02 November 2015 01:02:28, W. Europe Standard Time

```

The following date specifiers always refer to the current locale, and may not be fully supported by your operating system, if not, an empty string will be returned:
\begin{tabular}{|l|l|l|}
\hline Spec & Meaning & Example (w/o the quotes) \\
\hline \%a & abbreviated weekday name & 'Fri' for Friday \\
\hline \%A & full weekday name & 'Friday' \\
\hline \%b & abbreviated month name & 'Apr' for April \\
\hline \%B & full month name & 'Apri' \\
\hline \%c & preferred calendar time representation & 'O5/19/17 20:33:13' for UK \\
\hline \%C & \begin{tabular}{l} 
century of the year, greatest integer not \\
greater than year divided by 100.
\end{tabular} & does not work on Windows \\
\hline \%d & day of the month as two-digit integer & 'O3' \\
\hline \%D & date of the format \%m/\%d/\%y & does not work on Windows \\
\hline \%e & \begin{tabular}{l} 
day of the month like with \%d, but \\
padded with blank instead of a zero
\end{tabular} & does not work on Windows \\
\hline \%F & date of the format \%Y-\%m-\%d & does not work on Windows \\
\hline \%g, & \begin{tabular}{l} 
year corresponding to the ISO week \\
\%umber, but without the century
\end{tabular} & do not work on Windows \\
\hline \%h & abbreviated name of month & does not work on Windows \\
\hline \%H & two-digit hour in the range 00 .. 23 & 'O1' \\
\hline \%l & two-digit hour in the range 00 .. 12 & 'O1' \\
\hline \%j & \begin{tabular}{l} 
three-digit day of year in the range 001 .. \\
366
\end{tabular} & 'O01' \\
\hline \%k & \begin{tabular}{l} 
hour in the range 0 .. 23, like \%H, padded \\
with a blank
\end{tabular} & does not work on Windows \\
\hline \%l & \begin{tabular}{l} 
hour in the range 0 .. 12, like \%H, padded \\
with a blank
\end{tabular} & does not work on Windows \\
\hline \%m & month in the range 01 .. 12 & 'O5' \\
\hline \%M & minute in the range 00 .. 59 & 'O1' \\
\hline \%n & newline & does not work on Windows \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Spec & Meaning & Example (w/o the quotes) \\
\hline \%p & AM or PM & 'PM' \\
\hline \%P & am or pm & does not work on Windows \\
\hline \%R & hour and minute, like\%H:\%M & does not work on Windows \\
\hline \%s & number of seconds since the epoch & does not work on Windows \\
\hline \%S & seconds in the range \(00 . .60\) & '01 \\
\hline \%T & time of day of format \%H:\%M:\%S & does not work on Windows \\
\hline \%u & day of week as a decimal number range 1 (Monday) to through 7 & does not work on Windows \\
\hline \[
\begin{aligned}
& \text { \%U, } \\
& \text { \%V }
\end{aligned}
\] & week number in the range 00 ..53, starting with the first Sunday as the first day of the first week & '18' \\
\hline \%w & day of week in the range 0 (Sunday) to 6 & '1' \\
\hline \%W & week number of current year in the range 00 .. 53, starting with the first Monday as the first day of the first week & '18' \\
\hline \%x & preferred date representation & '05/03/17' for UK \\
\hline \%X & preferred time of day representation & '21:09:02' for UK \\
\hline \%y & year in the range \(00 . .99\) & \({ }^{1} 17\) \\
\hline \%Y & full year number & '1949' \\
\hline \%z & numeric time zone & Windows returns time zone as words \\
\hline \%Z & abbreviation of time zone & Windows returns time zone as words \\
\hline \%\% & character '\%' & '\%' \\
\hline
\end{tabular}

Please note that the behaviour is undefined if the date passed is earlier than the epoch.

See also: astro.cweek, astro.hdate, os.now, os.time, utils.checkdate.
os.datetosecs ([obj])
os.datetosecs (year, month, day [, hour [, minute [, second]]])
In the first form, receives a date and optionally time of the form year, month, date [, hour [, minute [, second]]], with all values in table, sequence or register obj being integers, and transforms it to the number of seconds elapsed since the start of an `epoch` (usually January 01, 1970, try os.now(0)). By default, hour, minute, and second are 0 . and If no argument is given, returns the number of seconds elapsed from the epoch till the current date and time.

In the second form, receives the given integers, and conducts the same operation.
The time zone acknowledged may depend on your operating system.
The function returns -1 if the date is older than the start of the epoch.

\section*{See also: os.time, os.secstodate, utils.checkdate.}
```

os.difftime (t2, t1)

```

Returns the number of seconds from time t1 to time t2. In POSIX, Windows, and some other systems, this value is exactly \(\mathrm{t} 2-\mathrm{t} 1\).

See also: time, os.time.

\section*{os.dirname (path)}

Returns the directory name of the given path, a string. If path has no separator, then the function returns '. '. If you would like to test relative paths, apply os.realpath to path before calling this function.

See also: os.filename, os.isdir, os.prefix, os.suffix.

\section*{os.drives ()}

In Windows, OS/2 and DOS, the function returns all the logical drives available at the local computer. The return is a sequence of drive letters. In DOS, floppy drives are not checked to avoid "Insert floppy disk" messages. In other systems, the return is fail.
```

os.drivestat (drive)

```

In Sun Solaris, Linux, OS/2, DOS and Windows, the function returns information of the given logical drive in a table. In DOS-based systems, pass the drive letter followed by a colon. In UNIX, pass just ' . '. The following data will be returned:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline 'label' & the drive label \\
\hline 'filesystem' & the file system (e.g. NTFS, FAT32, JFS, HPFS, etc.) \\
\hline 'drivetype' & \begin{tabular}{l} 
the type of the drive, i.e. 'Removable', 'Fixed', 'Remote', \\
'CD-ROM', or 'RAMDISK'
\end{tabular} \\
\hline 'freesize' & the number of free space in bytes \\
\hline 'totalsize' & the total number of physical bytes \\
\hline 'totalclusters' & total number of clusters (OS/2: allocation units) \\
\hline 'freeclusters' & number of free clusters (OS/2: allocation units) \\
\hline 'freeuserclusters' & number of free clusters to non-superusers (UNIX only) \\
\hline \begin{tabular}{l} 
'sectorsper \\
cluster'
\end{tabular} & number of sectors per cluster \\
\hline 'bytespersector' & number of bytes per sector \\
\hline 'maxnamelength' & maximum number of characters in a filename (Linux only) \\
\hline 'totalnodes' & total number of nodes (UNIX only) \\
\hline 'freenodes' & number of free file nodes (UNIX only) \\
\hline 'trim' & solid-state disk indicator (Windows only) \\
\hline 'dosdevice' & DOS device name (Windows only) \\
\hline 'fatsize' & number of bits used by the FAT (12, 16 or 32, DOS only) \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Key & Meaning \\
\hline 'isfat32' & FAT32-formatted drive (DOS only) & \\
\hline 'driveletter' & drive letter of device, including colon (OS/2 only) & \\
\hline ' itype' & \begin{tabular}{l} 
unknown meaning, PFSQBUFFER2 data type item `iType` \\
(OS/2 only)
\end{tabular} \\
\hline 'idFileSystem' & \begin{tabular}{l} 
unknown meaning, FSALLOCATE data type item \\
'idFileSystem`(OS/2 only)
\end{tabular} \\
\hline
\end{tabular}

In other systems, the return is fail.

\section*{Example:}
```

> os.drivestat('c:'): \# get information on drive C:\
[bytespersector ~ 512, drivetype ~ Fixed, filesystem ~ NTFS, freeclusters ~
62051077, freesize ~ 254161211392, label ~ <none>, sectorspercluster ~ 8,
totalclusters ~ 122070527, totalsize ~ 500000878592]

```

See also: os.ismounted, os.isremovable.
```

os.endian ()

```

Determines the endianness of your system. Returns 0 for Little Endian, 1 for Big Endian, and fail if the endianness could not be determined.

See also: os.cpuinfo.
os.environ ()
Returns all environment variables of the underlying operating system and their current settings as a table of key ~ value pairs of type string.

See also: os.getenv, os.setenv.
os.esd ([year, month, day [, hour [, minute [, second]]]])
os.esd (x)
The function computes the Excel Serial date for the given date or - if no argument is given - the current date and time. The Excel Serial represents the number of days that have elapsed since 31 st December 1899, 00:00h, where midnight January 01, 1900 is day 1 .

If no argument is given, the current Lotus Serial Date is computed. Otherwise, at least year, month, and day - all numbers - must be given. Optionally, you may add an hour, minute, or second, where all three default to 0 . The arguments can also be passed in a table or sequence.

The returns is a number, where the fractional portion represents the decimal time.

In the second form, if the Excel Serial Date x - a number - is given, the function returns the corresponding Gregorian year, month, day, the decimal fraction of the day - in the range \([0,1)\)-, the hour, minute, and second, all numbers. x may be 60, returning February 29, 1900.

The function implemented here takes no account of daylight saving time (which os.Isd does): at Winter time change, it returns the same values for (as an example) 02:00 a.m. before and after time change. Also, there is a `gap` in the values returned at Summer time change between 02:00 a.m. and 03:00 a.m.

In case of a non-existing date or if the date is older than the start of the epoch, the function issues an error. Thus, the function never returns 60 for February 29, 1900, the bug in the original Lotus 1-2-3 formula.

See also: os.Isd, os.now, os.usd, utils.checkdate.

\section*{os.execute ([command [, option]])}

This function is equivalent to the C function system. It passes the string command to be executed by an operating system shell. It returns a status code, which is system-dependent. If command is absent, then it returns non-zero if a shell is available and zero otherwise.

If any option is given, the function runs command and returns the entire output of the command as one string. Any carriage returns ('\r') are removed from the result, but keeps newlines (' \(\backslash \mathrm{n}\) ') untouched.

See also: io.pcall.

\section*{os.exists (filename)}

Checks whether the given file or directory (filename is of type string) exists and the user has at least read permissions for it. It returns true or false.

See also: os.exists.
```

os.exit ([code])
os.exit (code [, false])

```

In the first form, calls the C function exit, with an optional code to be passed to the environment in which Agena has been started, to terminate the host programme. The default value for code is the success code, usually 0 . (In Windows, query ERRORCODE in the shell for the exit status.)

The function by default also closes the interpreter state - this can be prevented by passing the optional Boolean value false.
```

os.faccess (path [, mode])
os.faccess (path [, flags])

```

Checks whether a directory or file can be accessed. path represents the path to the file, directory or symbolic link.

In the first form, mode specifies the accessibility through the integer constants:
- os.f_ok = check for existence
- os.x_ok = file is executable
- os.w_ok = write access is granted
- os.r_ok = read access is permitted (the default)

You can either specify the constant os.f_ok for mode, or a bitwise-OR mask of the constants os.r_ok, os.w_ok and/or os.x_ok created by calling the || operator, see example below.

Please note that the integer values these constants represent vary across platforms, so it is recommended to always use the constant names in the calls to the function.

In the second form, a string flags of one or more unique characters, in any order, specifies the permissions to be queried:
- 'f' = check for existence
- ' x ' = file is executable
- ' w ' = write access is granted
- 'r' = read access is permitted (the default)

You cannot mix the ' f ' flag with the other flags.
In both forms, if at least one bit in the mask asked for a permission is denied, the function returns false, and true otherwise. If the specified access is not granted, a string describing the kind of error will be returned, too.

\section*{Example:}
```

> \# check for read access to a non-existent folder
> os.faccess('nofolder'):
false file or directory does not exist
> \# check for both read and write access to an existing file
> os.faccess('myfile.txt', os.r_ok || os.w_ok):
true
> \# dito
> os.faccess('myfile.txt', 'rw'):
true

```

See also: os.fattrib, os.fstat, os.exists.
```

os.fattrib (fn, mode)
os.fattrib (fn, oct)
os.fattrib (fn, time)

```

In the first form, sets or deletes file permission flags given by the mode string to the file denoted by the filename fn .

The mode argument must consist of at least three characters and have the following form:
\begin{tabular}{|c|c|c|}
\hline Character 1 & Character 2 & Character 3, etc. \\
\hline ' u' - user & ' + ' - add permission & 'r' - read permission \\
\hline 'g'-group & ' - ' - remove permission & 'w' - write permission \\
\hline 'o'- other & & 'x' - execute permission \\
\hline 'a'- user, group, and other & & \\
\hline
\end{tabular}

The first character in mode denotes the owner of the file, the second character indicates whether to set or delete a permission, and the following characters indicate which permissions to set or remove.

In Windows and OS/2 the following permission flags are additionally supported:
\begin{tabular}{|l|}
\hline Character 3, etc. \\
\hline ' \(\mathrm{a}^{\prime}\) - archive flag \\
\hline ' s ' - system flag \\
\hline ' h ' - hidden flag \\
\hline ' r ' - read-only flag \\
\hline
\end{tabular}

In the second form, the file mode is set according to the octal number oct. This number is the same as the numeric argument to the UNIX chmod command, so for example - pass \(\underline{00444}\) (instead of 444) to the function to set a file to read-only mode for all users.

In the third form, the function changes the modification and access time of the file denoted by its name \(\mathrm{fn}_{\mathrm{n}}\) to the date and time given in table time. The table must include at least integers representing a year, month, and day. It may optionally include an hour, a minute, and a second. If they are missing, they default to zero.

File timestamps can only be changed in UNIX, Windows, Mac OS X, and DOS.
The function returns true on success, and fail otherwise.
Examples:
```

> os.fattrib('file.txt', 'a-wx'); \# deletes write and execute permissions
> os.fattrib('file.txt', 0o444); \# sets read-only for all users

```
```

> os.fattrib('file.txt', [2012, 05, 23, 12, 30, 0]); \# sets timestamp

```

See also: os.fstat, os.now.
os.fcopy (infile, outfile [, overwrite])
os.fcopy (infile, dir [, overwrite])
In the first form, copies the file and its permissions denoted by the filename infile to the new file called outfile. If outfile already exists, an error will be issued, but you may overrule this by passing true for overwrite. The function internally uses environ.kernel['buffersize'] for the number of bytes to be copied at the same time, which you may change to another positive integer.

In the second form, the function copies the file infile to the existing directory dir.
The function returns true on success, and fail and infile otherwise. It also returns fail and infile if the file could be copied, but the file permissions could not be set. The function issues errors if a file could not be read or created, or if the source and target file are identical.

Use skycrane.fcopy if you want to use wildcards/file globbing.
```

os.filename (path [, option])

```

Returns the filename of the given path, a string. This is equivalent to the C basename function. If you would like to test relative paths, apply os.realpath to path before calling this function.

If any option is given in Windows, then the 8.3 DOS filename is also returned if the file exists, otherwise null will be returned as the second result.

\section*{See also: os.dirname, os.isfile, os.prefix, os.suffix.}

\section*{os.freemem ([unit])}

Returns the amount of free physical RAM available on Windows and Mac OS X and UNIX machines. In OS/2, the function returns the amount of free virtual RAM.

If no argument is given, the return is in bytes. If unit is the string 'kbytes', the return is in kBytes; if unit is 'mbytes', the return is in Mbytes; if unit is 'gbytes', the return is in Gigabytes; if unit is 'tbytes', the return is in TeraBytes. On other architectures, the function returns fail.

See also: environ.used, os.meminfo.

\section*{os.fstat (fn)}

Returns information on the file, symbolic link (UNIX and Windows only), or directory given by the string fn in a table.

The table includes the following information:
\begin{tabular}{|c|c|}
\hline Key & Meaning \\
\hline 'mode' & 'File' if fn is a regular file, 'link' if fn is a symbolic link (UNIX and Windows only), 'DIR' if \(f n\) is a directory, 'ChARSPECFILE' if \(\mathrm{fn}_{\mathrm{n}}\) is a character special file (a device like a terminal), 'blockspecfile ' if fn is a block special file (a device like a disk), or 'оTHER' Otherwise \\
\hline 'length' & the size of the file in bytes \\
\hline 'compressed' & the compressed size of the file in bytes (Windows only) \\
\hline 'date' & last modification date in the form yyy, mm, dd, hh, mm, ss \\
\hline 'lastaccess' & last file access date in the form yyy, mm, dd, hh, mm, ss \\
\hline 'attribchange' & last file attribute change date in the form yyy, mm, dd, hh, mm, ss \\
\hline 'perms' & file attributes coded in a decimal integer, use math.convertbase to convert the integer \(x\) into its octal representation (from base 10 to base 8). \\
\hline 'bits' & \begin{tabular}{l}
The permission bits, a string similar to that in UNIX and DOS, e.g. '-rw-rw-r--:------' or '----------:-drhas' where the bits to the left of the colon are set in the UNIX and DOS versions of Agena, while in Windows and OS/2, the bits to the right of the colon are set. The letters indicate: \\
'r' - read permission granted (UNIX \& DOS) \\
'w' - write permission granted (UNIX \& DOS) \\
'x' - execute permission granted (UNIX \& DOS) \\
'd' - indicates directory (OS/2 only) \\
'r' - readonly file (OS/2 and Windows) \\
' h ' - hidden file (OS/2 and Windows) \\
'a' - archived file (OS/2 and Windows) \\
's' - system file (OS/2 and Windows)
\end{tabular} \\
\hline \begin{tabular}{l}
'owner' \\
'group', \\
other
\end{tabular} & \begin{tabular}{l}
Access permissions to the file or directory are returned with the owner, group (UNIX only), and other (UNIX only) keys which each reference tables with information on read, write, and execute permissions. These tables have the following form: ['read' <boolean>, 'write' ~ <boolean>, 'execute' ~ <boolean> ], where <boolean> is either true or false. \\
In OS/2 and Windows, the file attributes 'hidden', 'readonly', 'archived', and 'system' are also returned in the subtable with key 'owner'.
\end{tabular} \\
\hline 'blocks' & (UNIX only) Disk space occupied by the file, measured in units of 512 -byte blocks. \\
\hline
\end{tabular}
\begin{tabular}{l|l|}
\hline Key & Meaning \\
\hline 'blocksize' & \begin{tabular}{l} 
(UNIX only) Optimal block size for reading or writing this file, in \\
bytes.
\end{tabular} \\
\hline 'device' & (Windows \& UNIX-like OSs only) Volume serial number \\
\hline 'inode' & \begin{tabular}{l} 
(OS/2, Windows \& UNIX-like OSs only) Unique file serial \\
number/index node. In OS/2 \& Windows, a pair of two 32-bit \\
integers representing the higher and lower parts is returned. On \\
all other systems it is a pair, where the left-hand side is always 0, \\
and the right-hand side a 32-bit integer depicting the actual \\
inode.
\end{tabular} \\
\hline 'dosname' & (Windows only) 8.3 DOS name of the file \\
\hline 'binarytype' & \begin{tabular}{l} 
binary type of an executable: "Win16", "Win32", "Win64", "DOS", \\
"OS2/1 6", "PIF", "POSIX" or "unknown"
\end{tabular} \\
\hline 'uid' & (UNIX only) user ID \\
\hline 'gid' & (UNIX only) group ID \\
\hline
\end{tabular}

See also: os.fattrib.
os.ftok (path, id)
The function uses the identity of the file, i.e. its index node (inode, see os.fstat) named by the given path name, a string, and the least significant 8 bits of id (which must be non-zero) to generate a signed 4-byte integral System V IPC (Inter Process Communications) key.

On UNIX platforms, the return is one integer, and on OS/2 \& Windows two integers, the first for the higher part of the file index and the second for its lower part. On all other systems, the function issues an error.

The result is the same for all pathnames that name the same file, when the same value of id is used.

The value returned should be different when the (simultaneously existing) files or the given ids differ.

See also: hashes.ftok.

\section*{os.getenv (varname)}

Returns the value of the system environment variable varname, or null if the variable is not defined.

See also: os.setenv, os.environ.

\section*{os.getextlibpath ()}

In OS/2, returns the current paths to be searched before and after system LIBPATH, when trying to locate DLLs.

The first return is the path to be searched before the LIBPATH, the second one after the LIBPATH.

The function is not available in other operating systems.
See also: os.setextlibpath.

\section*{os.getlanguage (id)}

Returns the name of the language by number id. The return is a string. Available in Windows only. See also: os.getlocale.
```

os.getlocale ()

```

Returns various information on the current locale including decimal point and thousands separators, currency, and monetary formatting suggestions. The return is a table of the key~value pairs listed below. A value of " (the empty string) means `unspecified`.
\begin{tabular}{|l|l|c|}
\hline Key & Value & Value type \\
\hline 'locale' & current locale of your system & string \\
\hline 'charset' & \begin{tabular}{l} 
current character classification category of \\
the C locale
\end{tabular} & string \\
\hline 'decimal_point' & decimal-point separator & string \\
\hline 'thousands_sep' & thousands separator & string \\
\hline 'int_curr_symbol' & \begin{tabular}{l} 
international currency symbol according to \\
international standard ISO 4217 "Codes for \\
the Representation of Currency and Funds"
\end{tabular} & string \\
\hline 'currency_symbol' & \begin{tabular}{l} 
local currency symbol like XXX
\end{tabular} & string \\
\hline 'mon_decimal_point'' & \begin{tabular}{l} 
decimal point separator for monetary \\
amounts
\end{tabular} & string \\
\hline 'mon_thousands_sep' & thousands separator for monetary amounts & string \\
\hline 'positive_sign' & \begin{tabular}{l} 
symbol for positive values
\end{tabular} & string \\
\hline 'negative_sign' & \begin{tabular}{l} 
symbol for negative values
\end{tabular} \\
\hline 'int_frac_digits' & \begin{tabular}{l} 
recommended number of decimal places \\
of monetary amounts according to \\
international standard
\end{tabular} & number \\
\hline 'frac_digits' & \begin{tabular}{l} 
recommended number of decimal places \\
of monetary amounts according to local \\
standard
\end{tabular} & number \\
\hline 'p_cs_precedes' & \begin{tabular}{l} 
recommendation whether currency symbol \\
precedes positive monetary amount
\end{tabular} & boolean \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Key & Value & Value type \\
\hline 'n_cs_precedes' & recommendation whether currency symbol precedes negative monetary amount & boolean \\
\hline 'p_sep_by_space' & recommendation whether currency symbol and non-negative monetary amount are separated by a blank & boolean \\
\hline 'n_sep_by_space' & recommendation whether currency symbol and negative monetary amount are separated by a blank & boolean \\
\hline \begin{tabular}{l}
'p_sign_posn', \\
'n_sign_posn'
\end{tabular} & \begin{tabular}{l}
indicator how to position the sign for non-negative and negative monetary quantities: \\
0 : currency symbol and quantity to be enclosed in parentheses \\
1: print sign before quantity and currency \\
2: print sign after quantity and currency \\
3: print sign right before currency symbol \\
4: print sign right after currency symbol any other number: unspecified
\end{tabular} & number \\
\hline 'grouping' & unknown meaning *) & string \\
\hline 'mon_grouping' & ditto & string \\
\hline 'keyboard' & \begin{tabular}{l}
(Windows only) for an attached keyboard, the return has the following fields: 'hex' depicts the language ID as a hexadecimal string; and 'name' contains the associated language name as a string; 'langid' is the language ID, an integer. \\
'primarylangid' includes the primary language ID as an integer; 'sublangid' represents the sublanguage ID as an integer; and 'SystemDefaultuILangID' are integers. 'UserDefaultLangName' and 'SystemDefaultuILangName' are strings and represent the respective Windows settings. Warning: On mixed systems (e.g. default language UK and German keyboard) the information returned may be wrong.
\end{tabular} & table \\
\hline
\end{tabular}
*) See description of the \(C\) function localeconv on the web.
See also: environ.decpoint, os.codepage, os.getlanguage, os.setlocale.
os.getmodulefilename ()
In Linux and Windows, returns the absolute path to the currently executing programme as a string. In case of error, returns null.

\section*{os.gettemppath ()}

Retrieves the path of the directory designated for temporary files, of type string. Note that on non-Windows systems, the function issues an error if the environment variables TEMP, TMP and TMPDIR are all unassigned.

\section*{See also: os.tmpdir, os.tmpname.}
```

os.groupname (groupname)
os.groupname (gid)

```

The function receives a group name (a string) or a group id (an integer) and returns a table with keys 'groupname' denoting the group name (a string) and 'gid' denoting the group id (a number). It is available in the UNIX versions of Agena, only.

On all other systems, the function just returns fail.
See also: os.login, os.userinfo.

\section*{os.hasnetwork ()}

The function returns true if the system is connected to any network, and false otherwise. The function is available in Windows, only. The result is usually true. On all other architectures, the function returns fail.
```

os.inode (path)

```

On UNIX-like systems and DOS, for the given path, a string, the function returns the device ID and the index node (inode), i.e. two unsigned 4-byte integers.

On OS/2 and Windows, the function returns the volume serial number, an unsigned 4-byte integer, along with two additional unsigned 4-byte integers representing the higher and lower parts of the file index.

On all other platforms, the function issues an error.
```

os.isansi ()

```

Returns true on Agena editions compiled with the LUA_ANSI (strict ANSI C) option, and false otherwise.

See also: os.isdos, os.islinux, os.isos2, os.isppc, os.isunix, os.iswindows, os.isx86.

\section*{os.isarm ()}

Returns true if Agena is run on an ARM CPU, 32- or 64-bit, and false otherwise.
```

os.isdos ([any])

```

Checks whether Agena is run in the DOS environment and returns true or false.
The procedure is quite dumb: if you are running the DOS version of Agena, it will always return true regardless whether it is actually being run in DOS, OS/2 or Windows.

If you pass any argument, the function returns additional information in the following order: the name of the DOS edition, the official major and minor version if available, and the internal major and minor version from which you may deduce the actual DOS version. Furthermore, the internal OEM version number if returned. In FreeDOS, the kernel version number will also be given as the last return.

See also: environ.os, os.isansi, os.islinux, os.isos2, os.isunix, os.iswindows.

\section*{os.isdocked ()}

The function returns true if the computer is in docking mode, and false otherwise. The function is available in Windows, only. On all other architectures, the function returns fail.
```

os.isdir (path)

```

Checks whether the given path refers to a directory and returns true or false.
See also: os.chmod, os.chown, os.dirname, os.isfile, os.islink.
```

os.isdst ([year, month, day [, hour [, minute [, second]]]])

```

Receives a date and optionally time of the form year, month, date [, hour [, minute [, second]]], with all values being integers, checks whether Daylight Saving Time is active for a given date. Alternatively, you may pass the date and time in a table, sequence or register.

The function returns true or false. By default, hour, minute, and second are 0.
If no argument is given, returns the number of seconds elapsed from the epoch till the current date and time.

The function issues an error if a non-existing date has been passed.
See also: os.date, os.tzdiff, utils.checkdate.
```

os.isfile (path)

```

Checks whether the given path refers to a file and returns true or false.

See also: os.chmod, os.chown, os.filename.
```

os.islink (path)

```

Checks whether the given path refers to a link and returns true or false.

See also: os.chmod, os.chown, os.filename.
os.islinux()
The function determines whether Agena runs on Linux and returns true or false.

The function is written in Agena and included in the libary. agn file.

See also: environ.os, os.isansi, os.isdos, os.isos2, os.isunix, os.iswindows.
```

os.islocale(l)

```

The function checks whether the given locale 1 - represented as a string - is supported by the operating system and returns true or false. If the locale is supported, a description (of type string) will be returned as a second result.

The function - contrary to os.setlocale - never changes the current locale.

Examples for locales are 'uk' for the United Kingdom (at least in Windows localised to the United Kingdom), 'he_il' for Hebrew (Israel), 'de_AT' for Austrian and 'zh_Hans_SG' for Simplified Chinese (Singapore).
os.ismounted (d)
Checks whether the given drive a has been mounted. It is available in the Windows edition of Agena only.

See also: os.cdrom, os.drivestat, os.isremovable, os.isvaliddrive.
os.isos2()
The function determines whether Agena runs on \(O S / 2\) and returns true or false.

See also: environ.os, os.isansi, os.isdos, os.islinux, os.isunix, os.iswindows.
os.isppc ()
Returns true if Agena is run on a PowerPC CPU, 32- or 64-bit, and false otherwise.

See also: os.isarm, os.isdos, os.islinux, os.isos2, os.isunix, os.iswindows, os.isx86.

\section*{os.isremovable (d)}

Checks whether the given drive d is removable. It is available in the Windows edition of Agena only.

See also: os.cdrom, os.drivestat, os.ismounted, os.isvaliddrive.
os.isunix ()
Returns true if Agena is being run in a UNIX environment (i.e. Solaris, Linux, and OpenSolaris), and false otherwise.

The function is written in Agena and included in the libary . agn file.
See also: environ.os, os.isansi, os.isdos, os.islinux, os.isos2, os.iswindows.
os.isvaliddrive (d)
Checks whether the given drive a is part of the file system. It is available in the Windows edition of Agena only.

See also: os.cdrom, os.drivestat, os.ismounted, os.isremovable.
os.iswindows ()
Checks whether the Agena version for Windows is being run and returns true or false.

See also: environ.os, os.isansi, os.isdos, os.islinux, os.isos2, os.isunix.
```

os.isx86 ()

```

Returns true if Agena is run on an x86-compatible CPU, 32- or 64-bit, and false otherwise.

See also: os.isarm, os.isdos, os.islinux, os.isos2, os.isppc, os.isunix, os.iswindows.
```

os.iterate (path [, option])

```

Creates a factory that when called traverses a directory path and optionally also returns the type (file, directory, link, etc.). The first argument must be the path to the (sub)directory to be iterated - you can also use the ' . ' , '*' or '*.*' abbreviations instead. The iterator returns the name of the file, link, directory, etc.

The optional boolean second argument true causes the iterator to additionally return the type, i.e. 'FILe', 'DIR', 'Link', 'ChARSPECFILE', 'blockspecfile' or 'отнеR'. After the directory has been completely traversed, the function returns null.

The iterator cannot recurse into a subdirectory, just create another factory instead.
See also: os.chdir, os.list, os.listcore.
os.list (d [, options])
Lists the contents of a directory a (given as a string) by returning a table of strings denoting the files, subdirectories, and links. The second return is a string with the absolute path to the main directory scanned. If a is null or the empty string, the current working directory is evaluated. If the return is null and a warning text, then a does not exist.
a may include the ? and * jokers known from UNIX, OS/2, DOS or Windows to select a subset of files, e.g. os.list ('*.c') to return all files with suffix .c. Jokers can only be used to select files, but not to parse subdirectories if they exist.

If no option is given, files, links, and directories are returned. If the optional argument 'files' or 'file' is given, only files are returned. If the optional argument 'dirs' or 'dir' is given, directories are returned exclusively. If the optional argument 'links' or 'link' is given, links are returned (UNIX only). The ' \(r\) ' option forces a recursive descent into all subfolders of \(d\). Multiple options can be given.

If \(d\) is '.', then the current working directory is examined. If \(d\) is '..', then the directory one level higher than the current one is searched.

If the string ' \(r\) ' is passed as an option, the function traverses all subfolders in d .
The function is written in Agena and included in the lib/library.agn file.
See also: os.iterate.
```

os.listcore (d)
os.listcore (d [, options] [, pattern])

```

In the first form, returns a table with all the files, links and directories in the given path d. If \(a\) is void or the string ' . ', the current working directory is evaluated. It is the core function used by os.list.

In the second form, by giving at least one of the options 'files' or 'file', 'dirs' or 'dir', or 'links' or 'link', the file, directory name, or link names are returned, respectively. These three options can be mixed.

Another option may be a pattern of type string which can include the wildcards ? or *. If given, the function will only return those entries which match this pattern.

\section*{os.login ()}

Returns the login name of the current user as a string. The return is a string. In DOS, the function returns fail. See also: os.username, os.groupname.
os.lsd ([year, month, day [, hour [, minute [, second]]]] [, option])
os.lsd (x)
The function computes the Lotus 1-2-3 Serial Date, which is also used in Excel (known there as `Excel Serial Date`). It represents the number of days that have elapsed since 31st December 1899, 00:00h, where midnight January 01, 1900 is day 1.

The function always returns a Standard Time value even if Daylight Saving Time is active for the given date. By passing the option false, the function takes into account Daylight Saving Time, however.

In the first form, if no argument is given, the current Lotus Serial Date is computed. Otherwise, at least year, month, and day - all numbers - must be given. Optionally, you may add an hour, minute, or second, where all three default to 0 .

The first return is a number, where the fractional portion represents the decimal time. Also, the second return true or false indicates whether Daylight Saving Time has been active for the current or given date (if no option has been passed) so that you may add \(1 / 24\) to the first result to receive a value Microsoft Excel would return in DST situations. In case of a non-existing date, the function issues an error. Thus, the function never returns 60 for February 29, 1900, the bug in the original Lotus 1-2-3 formula.

In the second form, if the Lotus Serial Date x - a number - is given, the function returns the corresponding Gregorian year, month, day, the decimal fraction of the day - in the range \([0,1)\)-, the hour, minute, and second, all numbers. x may be 60, returning February 29, 1900.

To compute the Julian date from the Lotus Serial Date, add 2415018.5 .
See also: os.esd, os.now, os.usd, utils.checkdate.
```

os.meminfo ([unit])

```
os.memstate([unit])
(Windows, UNIX, Mac OS X, DOS and OS/2 only.) Returns a table with information on current memory usage. With no arguments, the return is the respective number of bytes (integers). If unit is the string 'kbytes', the return is in kBytes; if unit is 'mbytes ', the return is in Mbytes; if unit is 'gbytes ', the return is in Gigabytes, if unit is 'tbytes', the return is in Terabytes.

The resulting table will contain the following values, an 'x' indicates which values are returned on your system.
\begin{tabular}{|c|c|c|c|c|c|}
\hline Key & Description & OS/2 & Windows & UNIX & Mac \\
\hline 'freephysical' & free physical RAM & & X & X & X \\
\hline 'totalphysical' & installed physical RAM & X & X & X & X \\
\hline 'freevirtual' & free virtual memory & X & X & & \\
\hline 'totalvirtual' & total virtual memory & & X & & \\
\hline 'pagesize' & page size in bytes & X & X & X & X \\
\hline 'resident' & occupied resident pages & X & & & \\
\hline 'maxprmem' & maximum number of bytes available for the active process & X & & & \\
\hline 'maxshmem' & maximum number of shareable bytes available & X & & & \\
\hline 'active' & active memory & & & & X \\
\hline 'freepagefile' & current committed memory limit for the current process & & X & & \\
\hline 'totalpagefile' & maximum commitable amount of memory for the current process & & X & & \\
\hline 'inactive' & inactive memory & & & & X \\
\hline 'speculative' & unknown meaning, see vm_stat.c source code. & & & & X \\
\hline 'wireddown' & memory that cannot be paged out & & & & X \\
\hline 'reactivated' & memory reactivated & & & & X \\
\hline
\end{tabular}

On Mac, the function returns Mach virtual memory statistics. Type man vm_stat in a shell to get more information on the meaning of the above mentioned Mac-specific values.

The values returned in DOS should be self-explanatory. 'ems_major' and 'ems_minor' are memory manager version numbers.

On other architectures, the function returns fail.
See also: environ.used, os.freemem.

\section*{OS.mkdir (str)}

Creates a directory given by string str on the file system. Returns true on success, and issues an error on failure otherwise.

The function is available on OS/2, DOS, UNIX, Mac OS X, and Windows based systems only.

\section*{os.monitor (action)}

The function switches the monitor on and off (Windows and Linux), and can also put it on stand-by if the monitor supports this feature (Windows only).

Pass the string 'off' as the only argument to switch off the monitor; pass 'on' to switch it on, and 'standby' to put it into stand-by mode. If no argument is given, the Monitor is switched on (which has no effect, if the screen is already active).

On success, the function returns true, and false and a string containing the error analysis otherwise.
os.mouse ([mhd])
In OS/2, DOS and Windows, the function returns various information on the attached mouse by returning a table with the following entries:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline 'mousebuttons' & \begin{tabular}{l} 
number of mouse buttons; if more than one mouse is \\
attached, the sum of all mouse buttons is computed
\end{tabular} \\
\hline 'hmousewheel' & \begin{tabular}{l} 
Windows only: true if the mouse features a horizontal mouse \\
wheel, and false if not
\end{tabular} \\
\hline 'mousewheel' & \begin{tabular}{l} 
Windows only: true if the mouse features a vertical mouse \\
wheel, and false if not
\end{tabular} \\
\hline 'swapbutton' & \begin{tabular}{l} 
Windows only: true if the left and right mouse buttons have \\
been swapped
\end{tabular} \\
\hline 'speed' & \begin{tabular}{l} 
Windows only: an integer between 1 (slowest) and 20 \\
(fastest)
\end{tabular} \\
\hline 'threshold' & \begin{tabular}{l} 
OS/2 \& Windows only: the two mouse threshold values, x and \\
y co-ordinates, as a pair of two numbers
\end{tabular} \\
\hline 'mickeys' & \begin{tabular}{l} 
OS/2 only: number of mickeys per centimeter; a mickey is \\
the amount that a mouse has to move for it to report that it \\
has moved
\end{tabular} \\
\hline 'inmickeys' & OS/2 only: mouse data in mickeys, not "pels" \\
\hline 'rowscale' & OS/2 only: row scaling factor \\
\hline 'columnscale' & OS/2 only: column scaling factor \\
\hline
\end{tabular}

In OS/2 you have to supply a mouse handle mhd, see os.mouseopen.
On all other platforms, the function returns fail.

\section*{os.mouseflush (mhd)}

In OS/2, flushes the queue of the mouse denoted by mhd and returns true on success and false otherwise. The function is not available in all other operating systems. See also: os.mouseopen.

\section*{os.mouseopen ()}

In OS/2 only, returns a mouse handle - an integer - that is needed with other os.mouse* functions.

\section*{os.mouseclose (mhd)}

In OS/2 closes the connection to the mouse denoted by mhd. See os.mouseopen.
```

os.mousestate ([mhd, ] [mask [, threshold]])

```

In OS/2 and Windows, returns information on the position of the attached mouse and on button clicks plus some operating system-dependent data. In OS/2 you have to supply a mouse handle mhd, see os.mouseopen.

If the bit-mask is 0 bO (equals 0 decimal, the default), the function does not check whether the mouse is being moved at invocation. If mask is \(0 \mathrm{bl} 1=1\) decimal), movement is being checked. If mask is 0 blO ( \(=2\) decimal), the function in Windows tries to transform absolute to window coordinates (default: false, may not work on every Windows version), and if mask is 0bll ( \(=3\) decimal) both coordinates are converted and motion is being tracked.

In Windows, the threshold to detect mouse movement is 0.001 seconds. You can choose other values by passing a number to optional threshold. In OS/2, the setting is ignored.

The function is not available in all other operating systems.
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline 'row' & horizontal position of the mouse \\
\hline 'column' & \begin{tabular}{l} 
vertical position of the mouse \\
\hline 'button' \\
\begin{tabular}{l} 
table of three Booleans: the first for the left mouse button, \\
the second for the middle button, and the third for the right \\
button, where true depicts 'button clicked' and false \\
otherwise (experimental in OS/2)
\end{tabular} \\
\hline 'motion' \\
\hline mouse is being moved (true) or not moved (false) \\
\hline 'eventmask' \\
\hline 'flush'
\end{tabular} \begin{tabular}{l} 
OS/2 only: check EDM/2 Website on the MouGetEventMask \\
API function for a description
\end{tabular} \\
\hline 'blockread' & OS/2 only: mouse flush is in progress (true, false otherwise) \\
\hline \begin{tabular}{l} 
'eventqueuebusy \\
withio'
\end{tabular} & OS/2 only: block read is in progress (true, false otherwise) \\
\hline
\end{tabular}
os.move (oldname, newname [, option])
Renames or moves a file or directory named oldname to newname. The function returns true on success, and issues an error on failure otherwise.

If you pass the option true, then the function does not issue an error if oldname does not exist or if newfile already exists. Instead, the function just returns fail.

See also: skycrane.move.

\section*{os.netdomain (servername)}

On Windows, returns the domain name and the name of the primary domain controller (PDC). If servername is null or not given, the local computer is used.

See also: os.computername.
os.netsend (server, user, message)
On older Windows flavours, sends a message (a string) to a user (a string) on a given server (a string). If server is null or not given, the local computer is used.
```

os.netuse (letter [, path])

```

On Windows, connects or disconnects a drive letter to a network path. The drive letter must be followed by a colon. For drive letters already in use, see os.drives.

Example:
```

>\# connect drive with label 'drive_c' on computer TITANIA
>\# to drive letter Z:
> os.netuse('z:', '<br><br>TITANIA<br>drive_c');
> os.netuse('z:'); \# disconnect

```

The function returns true on success and issues an error otherwise.
```

os.now ([secs])
os.now (year, month, day [, hour [, minute [, second]]])

```

Returns rather low-level information on the current or given date and time in form of a dictionary.

If no argument is passed, the function returns information on the current date and time. If a non-negative number is given which represents the amount of seconds elapsed since the start of the epoch (try os.now(0)), information on this date and time are determined (see os.datetosecs to convert a date to seconds).

In the second form, the given date year, month, date and optionally time hour, minute, second, where all the optional values default to 0 , is used. Alternatively, you may pass the date and time in a table, sequence or register.

The `gmt' table in the return of the function represents the current date and time in GMT/UTC. The `localtime` table includes the same information for your local time zone.

The `tz` entry represents the difference between your local time zone and GMT in minutes with daylight saving time cancelled out, and east of Greenwich. The `td` entry represents the difference between your local time zone and GMT in minutes including daylight saving time, and east of Greenwich. `East of Greenwich` means: A positive integer indicates that your computer is located east of Greenwich, a negative value means that you are in a time zone to the west of Greenwich, and 0 means your computer is using GMT. The `jd` entry features the Julian date and time, the `Isd` key represents the Lotus 1-2-3 Serial Date, also known as Excel Serial Date.

The `seconds` entry is the number of seconds elapsed since some given start time (the `epoch `), which on most operating systems is January 01, 1970, 00:00:00. The `mseconds` entry represents milliseconds; it may be missing if milliseconds could not be determined on your platform. The 'dst` entry indicates whether daylight saving time is in effect.

The `gmt` and `localtime` entries have the same structure: it is a table of data of the following order: year, month, day, hour, minute, second, number of weekday (where 0 means Sunday, 1 is Monday, and so forth), the number of full days since the beginning of the year (in the range 0:365), whether daylight saving time is in effect at the time given (0: no, 1: yes), the strings 'AM' or 'PM', the month in English (a string), and the weekday in English (a string).

If the date and time could not be determined, fails are returned.
See also: utils.calendar, utils.checkdate, os.datetosecs, os.Isd, os.secstodate, os.time, os.tzdiff.
```

os.os2info ()

```
os.os2info (...)

In the first form, returns all 31 OS/2 settings that can be queried via the C API function DosQuerySysInfo, in a table.

In the second form, you can pass any of the following options, to individually query the current settings, either in upper or lower case:
\begin{tabular}{|l|l|}
\hline "QSV_MAX_PATH_LENGTH" & "QSV_TOTPHYSMEM" \\
\hline "QSV_MAX_TEXT_SESSIONS" & "QSV_TOTRESMEM" \\
\hline "QSV_MAX_PM_SESSIONS" & "QSV_TOTAVAILMEM" \\
\hline "QSV_MAX_VDM_SESSIONS" & "QSV_MAXPRMEM" \\
\hline "QSV_BOOT_DRIVE" & "QSV_MAXSHMEM" \\
\hline "QSV_DYN_PRI_VARIATION" & "QSV_TIMER_INTERVAL" \\
\hline "QSV_MAX_WAIT" & "QSV_MAX_COMP_LENGTH" \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline "QSV_MIN_SLICE" & "QSV_FOREGROUND_FS_SESSION" \\
\hline "QSV_MAX_SLICE" & "QSV_FOREGROUND_PROCESS" \\
\hline "QSV_PAGE_SIZE" & "QSV_NUMPROCESSORS" \\
\hline "QSV_VERSION_MAJOR" & "QSV_MAXHPRMEM" \\
\hline "QSV_VERSION_MINOR" & "QSV_MAXHSHMEM" \\
\hline "QSV_VERSION_REVISION" & "QSV_MAXPROCESSES" \\
\hline "QSV_MS_COUNT" & "QSV_VIRTUALADDRESSLIMIT" \\
\hline "QSV_TIME_LOW" & "QSV_INTIOENABLED" \\
\hline "QSV_TIME_HIGH" & \\
\hline
\end{tabular}

See: http://www.edm2.com/os2api/Dos/DosQuerySysinfo.html.
```

os.pause ([n [, msg]])

```

Waits for an amount of time or any user input and emulates the ZX Spectrum command PAUSE: if no argument is given or \(n=0\), the function waits forever until the user presses any key.

If n is a positive number, then the function waits for n seconds -n may be a fraction - unless the user presses any key - in the latter case, the function quits waiting immediately and exits. If an optional string msg is given, the function prints it on screen - you may terminate the string with a newline ('In') to force a linefeed. The function returns the number of seconds the function waited.

See also: os.wait.
os.pid ()
Returns Agena's process ID as a number.

\section*{os.prefix (filename)}

Returns filename, a string, without suffix if there is one. If filename includes a path, it is included in the return.

The function is written in the Agena language and part of the lib/library.agn file.
See also: os.dirname, os.filename, os.suffix, strings.chomp.

\section*{os.readlink (linkname)}

Returns the target of the symbolic link linkname as a string. If the link does not exist or if an error occurred, it returns fail and optionally a string indicating the type of error.

In Windows, the function only recognises classical Windows shortcut files, it cannot resolve NTFS symbolic links or junctions.

The function is available in UNIX including Mac OS X, and Windows.
See also: os.symlink.
os.realpath (pathname [, option])
Converts the pathname argument of type string to an absolute pathname, with symbolic links resolved to their actual targets and no . or .. directory entries. The return is a string. This only works satisfactorily if you are in the current working directory of the file to be scrutinised when calling the function.

In Windows, OS/2 and DOS, the function returns the path with slashes instead of backslashes by default. You can override this by passing an optional false.
os.remove (filename [, option])
Deletes the file or directory with the given name. Directories must be empty to be removed. Returns true on success, and issues an error on failure otherwise.

If you pass the option true, then the function does not issue an error if the file to be deleted does not exist. Instead, the function returns fail.
os.rmdir (dirname [, option])
Deletes a directory denoted by the string dirname on the file system. Returns true on success, and issues an error on failure otherwise.

If you pass the option true, then the function does not issue an error if the directory to be deleted does not exist. Instead, the function returns fail.

\section*{os.screensize ()}

In OS/2 and Windows, returns the current horizontal and vertical resolution of the display as a pair of width:height. On all other platforms, the function issues fail.
os.secstodate (secs)
Takes the number of seconds secs elapsed since the start of an epoch, in your local time zone, and returns a table of integers in the order: year, month, day, hour, minute, second. In case of an error, fail will be returned.

See also: os.datetosec.
os.setenv (var, setting)
Sets the environment variable in the underlying operating system. var must be a string. If setting is a string or number, the environment variable var is set to setting. If var has already been assigned before, its value is overwritten.

If setting is null, then the environment variable var is deleted (not supported in DOS).

See also: os.getenv, os.environ.
os.setextlibpath (path [, option])
In OS/2, sets the path to be searched before and after system LIBPATH, when trying to locate DLLs. If option is 0 , then the path is set to the beginning of LIBPATH; if it is non-zero, the path is set to its end.

The function returns true on success and false otherwise.
The function is not available in other operating systems.
See also: os.getextlibpath.
os.setlocale (locale [, category])
Sets the current locale of the programme. locale is a string specifying a locale, the empty string returns the locale of your operating system (and not the locale you have set in Agena); category is an optional string describing which category to change: 'all', 'collate', 'ctype', 'monetary', 'numeric', or 'time'; the default category is 'all'.

The function returns the name of the new locale, or null if the request cannot be honoured.

When called with null as the first argument or no argument at all, this function only returns the name of the current locale for the given category.

See also: os.codepage, os.islocale, skycrane.getlocales.
```

os.settime (secs)
os.settime (year, month, day [, hour [, minute [, second]]])

```

In the first form, takes the number of seconds secs elapsed since the start of an epoch, in your local time zone, and sets the system clock accordingly. In the second form, the given date year, month, date and optionally time hour, minute, second, where all the optional values default to 0 , is used. Alternatively, you may pass the date and time in a table, sequence or register.

Agena must be run in root mode in order to change the system time. In case of an error, fail will be returned. The function is available only in the Windows, Solaris, OS/2, and Linux versions of Agena.

\section*{See also: os.datetosecs, utils.checkdate.}
```

os.strerror ([n])

```

Returns the text message for the given integral error code \(n\), or the latest error issued by the underlying operating system if no argument is given. The result varies across platforms.

\section*{os.suffix (filename)}

Returns the last suffix in filename (a string) and also the position (an integer) of the last suffix in filename.

If there is no suffix in filename, the function returns the empty string and 0 (zero).
The function is written in the Agena language and part of the lib/library.agn file.
See also: os.dirname, os.filename, os.prefix, strings.chomp.
```

os.symlink (target, linkname)

```

In UNIX, the function creates a symbolic link named linkname to the file called target. In Windows, the function creates a classical regular Windows shortcut file that points to a real file. It does not create NTFS junctions or NTFS symbolic links.

Both arguments must be strings. The function is not available in DOS.

\section*{See also: os.readlink.}

\section*{os.system ()}

Returns information on the platform on which Agena is running.
Under Windows, it returns a table containing the string 'Windows', the major version (e.g. 'NT 4.0', '2000', etc.) as a string, the Build (dwBuildNumber) as a number, the platform ID (dwPlatform/d) as a number, the major version (dwMajorVersion) as a number, the minor version (dwMinorVersion) as a number, the product type (wProductType) as a number, maintainence information (szCSDVersion) usually depicting an installed service pack as a string, and a summary string combining all the previously mentioned data in a human-readable fashion, all in this order. For an alternative, see: os.winver.

In UNIX, Mac OS X, OS/2, and DOS, it returns a table of strings with the name of the operating system (e.g. 'SunOS', 'OS/2' or 'MS-DOS'), the release, the version, and the
machine, in this order. Note that Mac OS \(X\) is recognised as 'Darwin'. In OS/2, the major and minor revision, along with the revision, are returned as numbers, as well.

In Linux and Windows, the function also checks whether the underlying plafform runs in 32 or 64-bit mode, and returns the result with key 'bits'.

If the function could not determine the platform properly, it returns fail.
See also: environ.os.

\section*{os.terminate (action)}

The function halts, reboots, sleeps, or log-offs Windows, OS/2 or Mac OS X. In Windows, it can also lock the current user session or hibernate the system.

The function makes sure that no data loss occurs: if there is any unsaved data, the function does not start termination and just quits.

To put the system into energy-saving sleep mode, pass the string 'sleep' as the only argument. To hibernate (save the whole system state and then shut off the PC), pass 'hibernate' (Windows only); to shut down the computer completely, pass 'halt'; to reboot the system, pass 'reboot '; to lock the current user session without logging the user off, pass 'lock ' (Windows only); to log-off the open session of the current user, pass 'logoff'.

The OS/2 version solely supports system halt ('halt' argument, without power-off) and reboot.

By default, the function waits for 60 seconds before initiating the termination process. You can change this time-out period to another number of seconds by setting the optional second argument to any non-negative integer.

On all other platforms, the function returns fail and does nothing.

\section*{os.time ([obj])}

Returns the current time when called without arguments, or a value representing the date and time specified by the given table or sequence obj.

If a table is given, it must either:
- have fields year, month, and day, and may have fields hour, min, sec, and isdst, see example below,
- or at least three integers representing year, month, day, and optionally also hour, minute, second.

If obj is a sequence, it must contain a four-digits year, the month, and the day, all integers, in this order. It may additionally include the hour, the minute, and the
second, all integers, too, in this order. The optional seventh entry must either be the Boolean true or false and indicates whether daylight saving time is in effect (default is false). See example below.

The returned value is a number, whose meaning depends on your system. In POSIX, Windows, and some other systems, this number counts the number of seconds since some given start time (the `epoch '). In other systems, the meaning is not specified, and the number returned by os.time can be used only as an argument to os.date and os.difftime.

If the return is null, then the given date lies before the start of the epoch (check os.now (0)). The function process dates between the start of 1900 and the end of 2099, only.

If a second number is returned, it will denote the millisecond portion of the current time in the range [0, 999].

Examples:
```

> os.time(['year' ~ 2013, 'month' ~ 5, 'day' ~ 23,
> 'hour' ~ 1, 'min' ~ 2, 'sec' ~ 3]):
1369263723 791
> os.time(seq(2013, 5, 23, 1, 2, 3, false)):
1369267323 791

```

See also: time, os.clock, os.date, os.datetosecs, os.difftime, os.now, utils.checkdate.
```

os.tmpdir ([p])

```

Creates a unique temporary directory from pattern \(p\) which ends in six ' \(X^{\prime}\) ' characters and returns its name. By default, the function uses the pattern 'agn_XXXXXX' (non-DOS) or 'agXXXXXX' (DOS).

In case of an error, the function returns null and an error message. You have to manually remove the directory if it is not needed any longer.

See also: os.gettemppath, os.tmpname.
os.tmpname ()
Returns a string with a file name that can be used for a temporary file or directory. The file must be explicitly opened before its use and explicitly removed when no longer needed. The same applies to directories: you have to manually create and remove it. Depending on the platform, the name might denote an absolute or relative path.

See also: os.gettemppath, io.tmpfile, io.mkstemp, os.tmpdir.
```

os.tzdiff ([secs])
os.tzdiff (year, month, day [, hour [, minute [, second]]])

```

Computes the difference between the system's local time zone and UTC in minutes, taking into account whether Daylight Saving Time is active, plus a Boolean indicating whether Daylight Saving Time is active.

If no argument is passed, the function uses the current date and time. If a non-negative number secs is given - representing the amount of seconds elapsed since the start of the epoch -, this date and time is used to compute the result.

In the second form, the given date year, month, date and optionally time hour, minute, second, where all the optional values default to 0 , is used. You may also pass these date and time data as a table, sequence or register.

\section*{See also: os.isdst, os.now.}
```

os.unmount (fs [, force])

```

The function unmounts the filesystem fs , which has to be passed as a string. If the option true is given for the second argument force, the function forces a disconnection even if the filesystem is in use by another process. The default is false. If your system cannot force a `umount`, this flag is simply ignored.

The function works only if Agena is run with superuser rights. Depending on the operating system, it may only unmount filesystems that the UNIX kernel directly supports (in Linux, look into /proc/filesystems folder), e.g. ntfs-3g filesystems using the FUSE driver may not be unmounted.

On success, os.unmount returns true, and false plus a string indicating the error reason, otherwise.

See also: os.cdrom, os.execute.
```

os.uptime ()

```

Returns the number of seconds a system has been running. It is available in OS/2, Windows, Solaris, and Linux. In Windows, there may be an overflow if the system has been up for more than 49.7 days.
```

os.usd ([year, month, day [, hour [, minute [, second]]]])

```
os.usd (x)

The function computes the UTC Serial date, a number, for the given date or - if no argument is given - the current date and time, where the time zone is assumed to be UTC.

The UTC Serial represents the number of days that have elapsed since 31st December 1899, 00:00h, where midnight January 01, 1900 is day 1.

If no argument is given, the UTC Serial Date for the current date and time is computed. Otherwise, at least year, month, and day - all numbers - must be given. Optionally, you may add an hour, minute, or second, where all three default to 0 .

In the second form, if the UTC Serial Date x - a number - is given, the function returns the corresponding Gregorian year, month, day, the decimal fraction of the day - in the range \([0,1)\)-, the hour, minute, and second, all numbers. x may be 60, returning February 29, 1900.

Since the date and time is considered to be UTC, the function implemented here takes no account of daylight saving time: at Winter time change, it returns the same values for (as an example) 02:00 a.m. before and after time change.

Also, there is a `gap` in the values returned at Summer time change between 02:00 a.m. and 03:00 a.m.

In case of a non-existing date or if the date is older than the start of the epoch, the function issues an error.

See also: os.esd, os.Isd, os.now, utils.checkdate.
```

os.username ([groupname])

```
os.username ([uid])

The function receives a user name (a string) or a user id (an integer) and returns a table with the following key ~ value pairs:
\begin{tabular}{|l|l|}
\hline Key & Value \\
\hline 'username' & user's login name \\
\hline 'uid' & user ID number \\
\hline 'gid' & user's default group ID number \\
\hline 'realname' & user's real name, etc. \\
\hline 'homedir' & \begin{tabular}{l} 
user's home directory, or initial working directory (undefined means \\
system default)
\end{tabular} \\
\hline 'shell' & user's default shell (undefined means system default) \\
\hline
\end{tabular}

If no argument is given, data for the current user is being determined.
The function is available in the UNIX versions of Agena, only. On all other systems, the function just returns fail.

See also: os.login, os.groupinfo.
os.vga ()
In OS/2, DOS and Windows, the function returns a table with the following information on the display:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline 'resolution' & \begin{tabular}{l} 
a pair with the horizontal and vertical number of pixels (OS/2 and \\
Windows)
\end{tabular} \\
\hline 'dimension' & a pair with the number of rows and columns \\
\hline 'depth' & an integer indicating the colour depth in bits \\
\hline 'monitors ' & the number of monitors attached to the system (Windows only) \\
\hline 'vrefresh' & the vertical refresh rate in Hertz (Windows only) \\
\hline 'mode' & screen mode, an integer (unknown meaning, DOS only) \\
\hline 'colours ' & number of colours (OS/2 only) \\
\hline
\end{tabular}

See also: os.monitor, os.screensize.
os.wait (x)
Waits for x seconds and returns null. x may be an integer or a float. This function does not strain the CPU, but execution cannot be interrupted. The function is available on OS/2, DOS, UNIX, Mac OS X, and Windows based systems only.

On other architectures, the function returns fail.
See also: os.pause.
os.whereis (file, dir [, options])
Searches case-insensitively for the given file, link or directory in directory dir and returns a table of all the hits.

If dir is not given, it defaults to the current working directory. If option is ' \(r\) ', the subfolders in dir are also scanned, returning the files found with their relative paths. If option is ' \(s\) ', the search is case-sensitive. You can mix both options.
file may include the wildcards ? and *, where ? represents exactly one unknown character, and * represents zero or more unknown characters.

Example:
```

> os.whereis('agena*', '..', 'r'):

```

See also: os.chdir, os.list, strings.glob.

\section*{os.winver ([argument])}

This function is an alternative to os.system and returns the internal Windows release number (a float). If any argument is given, it also returns the service pack major (an
integer) and minor version (an integer), whether the operating system is workstation (true) or server (false) and the build number (an integer), in this order.

On all other platforms other than Windows, the function returns undefined, which, if used in a relation, always evaluates to false.
\begin{tabular}{|l|l|}
\hline Internal Version Number & Official Release \\
\hline 5.0 & Windows 2000 \\
\hline 5.1 & Windows XP \\
\hline 5.2 & \begin{tabular}{l} 
Windows XP 64-Bit Edition, Windows Server 2003, \\
Server 2003 R2
\end{tabular} \\
\hline 6.0 & Windows Vista, Windows Server 2008 \\
\hline 6.1 & Windows Server 2008 R2, Windows 7 \\
\hline 6.2 & Windows Server 2012, Windows 8 \\
\hline 6.3 & Windows Server 2012 R2, Windows 8.1 \\
\hline 10.0 & Windows Server 2016 \& 2019, Windows 10 \\
\hline
\end{tabular}

\section*{14.2 environ - Access to the Agena Environment}

This package comprises functions to access the Agena environment, explore the internals of data, read settings, and set defaults.
```

environ.anames ([option])

```

Returns all global names that are assigned values in the environment. If called without arguments, all global names are returned. If option is given and option is a string denoting a basic or user-defined type (e.g. 'boolean', 'table', etc.), then all variables of that type are returned.

The function is written in Agena and included in the lib/library.agn file.
```

environ.arithstate ()

```

The function returns information encoded in a bit field on the kind of numerical exception encountered by the inc, dec, mul, div, intdiv and mod operators:

\section*{add, sub:}

0b0000: no exception
0b0010: very large value to be added to (subtracted from) value close to zero
0b0100: very large values to be added (or subtracted)
0b1000: both operands are close to zero:

\section*{mul:}

0b0000: no exception
0b0010: very large value to be multiplied by value close to zero
0b0100: very large values to be multiplied
0b1000: both operands are close to zero

\section*{div, intdiv, mod:}

0b0000: no exception
0b0001: denominator is zero
0b0010: very large value to be divided by value close to zero
0b1000: indicates both operands are close to zero
See also: environ.kernel/closetozero setting.
```

environ.arity (f)

```

The function returns the number of parameters of a function \(f\) and additionally a Boolean indicating whether its parameter list includes a `?` (varargs) token or not, plus the number of upvalues used in functions created by factories. The first return does not count a varargs token.

See also: debug.getinfo.

\section*{environ.attrib (obj)}

The function returns various internal status information on structures and procedures.
With the table obj, returns a new table with
- the current maximum number of key~value pairs allocable to the array and hash parts of obj; in the resulting table, these values are indexed with keys 'array_allocated' and 'hash_allocated', respectively,
- the number of key~value pairs actually assigned to the respective array and hash sections of obj; in the resulting table, these values are indexed with keys 'array_assigned' and 'hash_assigned',
- an indicator 'array_hasholes' stating whether the array part contains at least one hole,
- an indicator 'bytes' stating the estimated number of bytes reserved for the structure,
- an indicator 'metatable' denoting whether a metatable has been attached to the structure,
- if present, a user-defined type is indexed by the 'utype ' key, otherwise fail,
- if present, a weak table is indexed by the 'weak ' key, otherwise fail,
- the 'length' entry contains the estimated number of elements in a table (see tables.getsize \& tables.getsizes),
- the 'lowest' and 'keys' represent the lowest and highest index positions in the array part; they are set to zero if there is no array part in the table;
- the 'dummynode ' entry indicates whether a table has no allocated hash part.
- See also: tables.borders, tables.indices, tables.maxn.

With the set obj, returns a new table with
- the current maximum number of items allocable to the set; in the resulting table, this value is indexed with the key 'hash_allocated'.
- the number of items actually assigned to obj; in the resulting table, this value is indexed with the key 'hash_assigned',
- an indicator 'bytes' stating the estimated number of bytes reserved for the structure,
- an indicator 'metatable' betoking whether a metatable has been attached to the structure,
- if present, a user-defined type is indexed by the 'utype ' key, otherwise fail.

With the sequence obj, returns a new table with
- the maximum number of items assignable; in the resulting table, this value is indexed with the key 'maxsize'. If the number of entries is not restricted, 'maxsize' is infinity.
- the current number of items actually assigned to obj; in the resulting table, this value is indexed with the key 'size',
- an indicator 'bytes' stating the estimated number of bytes reserved for the structure,
- an indicator 'metatable' betoking whether a metatable has been attached to the structure,
- if present, a user-defined type is indexed by the 'utype ' key, otherwise fail,
- if present, a weak table is indexed by the 'weak ' key, otherwise fail.

With the register obj, returns a new table with
- the total number of items assigned; in the resulting table, this value is indexed with the key 'size'.
- the current top indexed by the key 'top',
- an indicator 'bytes' stating the estimated number of bytes reserved for the structure,
- an indicator 'metatable' indicating whether a metatable has been attached to the structure,
- if present, a user-defined type is indexed by the 'utype ' key, otherwise fail,
- if present, a weak table is indexed by the 'weak ' key, otherwise fail.

With the pair obj, returns a new table with
- an indicator 'bytes ' stating the estimated number of bytes reserved,
- an indicator 'metatable' betoking whether a metatable has been attached to the structure,
- if present, a user-defined type is indexed by the 'utype ' key, otherwise fail,
- if present, a weak table is indexed by the 'weak ' key, otherwise fail.

With function obj returns a new table with
- the information whether the function is a C or an Agena function. In the resulting table, this value is indexed with the key ' \(\mathrm{c}^{\prime}\) ';
- the information whether a function contains a remember table, indicated by the key 'rtableWritemode', where the entry true indicates that it is an rtable (which is updated by the return statement), where false indicates that it is an rotable (which cannot be updated by the return statement), and where fail indicates that the function has no remember table at all,
- the information whether an internal storage table is present, in the 'storage' field, see Chapter 6.2.5,
- an indicator 'bytes ' stating the estimated number of bytes reserved,
- if present, a user-defined type is indexed by the 'utype' key, otherwise fail,
- the number of parameters excluding varargs (?) in the 'arity' field (with OOP methods, the result includes the self variable),
- a Boolean indicating whether the varargs tokern (?) is part of the parameter list, in the 'varargs' field,
- the number of upvalues in the ' nupvals' field.
environ. decpoint ()
Returns the decimal point separator used in the current locale. It is an alternative to the expression os.getlocale.decimal_point, but is faster.
```

environ.gc ([opt [, arg]])

```

This function is a generic interface to the garbage collector. It performs different functions according to its first argument, opt:
- 'stop': stops the garbage collector.
- 'restart': restarts the garbage collector.
- 'collect': performs a full garbage-collection cycle (if no option is given, this is the default action).
- 'count': returns the total memory in use by Agena (in Kbytes).
- 'step': performs a garbage-collection step. The step 'size' is controlled by arg (larger values mean more steps) in a non-specified way. If you want to control the step size you must experimentally tune the value of arg. Returns true if the step finished a collection cycle.
- 'setpause': sets arg/100 as the new value for the pause of the collector.
- 'setstepmul': sets arg/l00 as the new value for the step multiplier of the collector.
- 'status': determines whether the garbage collector is running or has been stopped, and returns true - i.e. collection has been activated - or false.
```

environ.getfenv (f)

```

Returns the current environment in use by the function. f can be an Agena function or a number that specifies the function at that stack level: Level 1 is the function calling getfenv. If the given function is not an Agena function, or if \(f\) is 0 , getfenv returns the global environment. The default for f is 1 .
```

environ.getopt (args, format)

```

The function parses command-line options passed from the underlying operating system to an Agena script.

Each option (switch) may consist of exactly one letter, preceded by a dash or slash, multi-letter switches are not supported and will be incorrectly processed.

\section*{Examples:}

Valid: agena script.agn -h
Valid: agena script.agn /h
Valid: agena script.agn -apx (expanded to -a -p-x)
Valid: agena script.agn /apx (expanded to /a /p/x)
Valid: agena script.agn -val 3.141592654
Valid: agena script.agn -val=3.141592654

Invalid: agena script.agn -help (would be split into the switches -h, -e, -l and -p.
The function takes the args system table and a format string denoting the switches to detect and - if found - returns the switch name without a preceding dash or slash, an optional value if given, and the index of the next args entry to be processed in a subsequent call. If args is null, the function simply returns.

Depending on their position in the call from the operating system, unknown options might be ignored.

\section*{Example:}
```

> for switch, optarg, nextidx in environ.getopt(args, 'ab:c::d') do
> print(switch, optarg, nextidx)
> end

```

In this example, the format string 'ab:c:p' has the following meaning, and you can use combinations in any order:
- 'a' - check for just the /a or -a switch.
- 'b:' - check for the /b or -b switch succeeded by a mandatory value; the switch and the value may be separated by a blank or an equals sign ('=');
- 'c::' - check for the /c or -c switch optionally succeeded by a value, both separated by a blank or an equals sign ('=');
- 'd' - check for just the /d or -d switch.

For an example script, check file getopt.agn in the share/scripting folder of your Agena installation.

The function is a port to a modified version of the C library function getopt.
```

environ.globals (f)

```

Determines \({ }^{28}\) whether function f includes global variables (names which have not been defined local). The return is a sequence of pairs: their left-hand side the variable name of type string, the right-hand side the respective line number (of type number). If no global variables could be found, the function returns null.
```

environ.isequal (obj1, obj2)

```

Compares two objects obj1, obj2 for equality and returns true or false. Note that the function considers two structures (tables, sequences, registers and pairs) a and \(b\) of the same type to be different if they do not reference one another. Thus, for example, with \(a:=[1]\) and \(b:=[1]\), the function returns false, whereas \(a\) and \(b\) with \(a:=[1]\) and \(b:=a\) are equal.

See also: =, = o operators.

\footnotetext{
\({ }^{28}\) Note that the function not always returns all global names.
}
environ.isselfref (obj)
Checks whether a structure obj (table, set, sequence, or pair) references to itself. It returns true if it is self-referencing, and false otherwise.

The function is written in Agena and included in the lib/library.agn file.
```

environ.kernel ([setting])
environ.kernel (setting:value)

```

Queries or defines kernel settings that cannot be changed or deleted automatically by the restart statement.

In the first form, by passing the given setting as a string, the current configuration will be returned. If no argument is given, then all current settings are returned in a table.

In the second form, by passing a pair of the form setting: value, where setting is a string and value the respective setting given in the table below, the kernel is set to the given configuration.

The return is the new configuration.
Settings are:
\begin{tabular}{l|l|l|}
\hline Setting & Value & Description \\
\hline 'alignable' & true or false & \begin{tabular}{l} 
Indicates whether your system aligns data \\
along the 4- or 8-byte word boundary. The \\
check is done at runtime, the setting is not \\
compiled into the interpreter.
\end{tabular} \\
\hline 'bitsint' & a number & \begin{tabular}{l} 
Number of bits in a C int, should mostly be \\
32.
\end{tabular} \\
\hline 'buffersize' & a number & \begin{tabular}{l} 
The default buffer size for file operations for \\
the os.fcopy, net.receive, and \\
binio.readlines functions. Must be set to \\
{\(\left[512 . .1024^{3}\right]\) It is equal to the C constant } \\
BUFSIZ in stdio.h. Grep LUAL_BUFFERSIZE in \\
the C sources.
\end{tabular} \\
\hline 'builtoncpu' & a string & \begin{tabular}{l} 
Denotes the CPU architecture Agena has \\
been built on.
\end{tabular} \\
\hline 'clockspersec' & an integer & \begin{tabular}{l} 
licks per second measured by the os.clock \\
function, read-only.
\end{tabular} \\
\hline 'closetozero' & a number & \begin{tabular}{l} 
threshold so that the binary inc, dec, mul, \\
div, intdiv and mod operators can \\
recognise operators close to zero. Default is \\
DoubleEps.
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Setting & Value & Description \\
\hline 'constants' & true or false & Turn constants feature on or off. Default: on. \\
\hline 'debug' & true or false & Prints further debugging information if the initialisation of a C dynamic library failed \\
\hline 'digits' & an integer in
\[
[1,17]
\] & Sets the number of digits used in the output of numbers. Note that this setting does not affect the precision of arithmetic operations. The default is 14 . \\
\hline 'duplicates' & true or false & Turns duplicate declarations (shadowing) warnings on (true) and off. Default: true. \\
\hline 'emptyline' & true or false & If set true (the default), two input regions are always separated by an empty line. If set false, no empty line is inserted. \\
\hline 'errmlinebreak' & a positive integer & Stores the maximum number of characters to be displayed per line in syntax error messages. Default is 70 . \\
\hline 'eps' & a number & Stores the accuracy threshold epsilon used by the \(\sim=\) operator and the approx function. \\
\hline 'doubleeps' & a number & Gets and sets DoubleEps variable; default is \(2.2204460492503131 \mathrm{e}-16\). \\
\hline 'foradjust' & true or false & Controls auto-correction of iteration values \(x\) close to zero in numeric for loops with fractional step sizes. Default is true, i.e. \(x\) will be set to zero if \(\mathrm{x}<\mathrm{hEps}\). \\
\hline 'glibc' & a number & When Agena has been compiled with GCC, denotes the major GLIBC version linked during compilation. Otherwise is null. \\
\hline 'glibcminor' & a number & Dito, but with respect to the minor GLIBC version. \\
\hline 'gui' & true or false & If set true, tells the interpreter that it has been invoked by AgenaEdit. Default is false. \\
\hline 'hEps' & a number & Gets and sets hEps variable; default is \(1.4901161193847656 \mathrm{e}-12\). Also controls auto-correction features in numerical for loops, see Chapter 5.2.2. \\
\hline 'iso8601' & true or false & If set to true, os.date determines weekdays according to the ISO 8601 norm. Default is true. \\
\hline 'is32bit' & true or false & If set to true, then Agena has been compiled in 32-bit mode. \\
\hline 'is64bit' & true or false & If set to true, then Agena has been compiled in 64-bit mode. \\
\hline 'isARM' & true or false & If set to true, then Agena is running on an ARM CPU. \\
\hline 'isIntel' & true or false & If set to true, then Agena is running on an Intel-compatible CPU. \\
\hline
\end{tabular}
\begin{tabular}{l|l|l|}
\hline Setting & Value & Description \\
\hline 'isDos' & true or false & If set to true, then Agena is running in DOS. \\
\hline 'isLinux' & true or false & If set to true, then Agena is running in Linux. \\
\hline 'isMac' & true or false & \begin{tabular}{l} 
If set to true, then Agena is running in Mac \\
OS X.
\end{tabular} \\
\hline 'isos/2' & true or false & \begin{tabular}{l} 
If set to true, then Agena is running in OS/2 \\
and successors.
\end{tabular} \\
\hline 'issolaris' & true or false & \begin{tabular}{l} 
If set to true, then Agena is running in \\
Solaris.
\end{tabular} \\
\hline 'isWindows' & true or false & \begin{tabular}{l} 
If set to true, then Agena is running in \\
Windows.
\end{tabular} \\
\hline 'kahanbabuska' & true or false & \begin{tabular}{l} 
If set to true, Kahan-Babuška round-off error \\
prevention in numeric for loops instead of \\
the original Kahan algorithm. Default is \\
false.
\end{tabular} \\
\hline 'kahanozawa' & true or false & \begin{tabular}{l} 
If set to true, Kahan-Ozawa round-off error \\
prevention in numeric for loops instead of \\
the original Kahan algorithm. Default is \\
false.
\end{tabular} \\
\hline 'lastcontint' & a number & \begin{tabular}{l} 
Largest accurately representable integer \\
(usually 253.
\end{tabular} \\
\hline 'libnamereset' & true or false & \begin{tabular}{l} 
If set true, the restart statement resets \\
libname and mainlibname to their original \\
values. Default is false.
\end{tabular} \\
\hline 'pathmax' & a string & \begin{tabular}{l} 
If set to true, the interpreter has been \\
started with the -a option, ignoring the \\
setting of the AGENAPATH environment \\
variable. Default is false.
\end{tabular} \\
\hline 'pathsep' & a string & \begin{tabular}{l} 
Returns the names of all basic libraries \\
initialised at start-up of the interpreter. \\
accepted by the operating system, an \\
integer.
\end{tabular} \\
\hline The token that separates paths in libname;
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Setting & Value & Description \\
\hline & & by default is 'i,', cannot be changed. Grep LUA PATHSEP in the C sources. \\
\hline 'promptnewline' & true or false & If set to true, prints an empty line between the input and output regions. Default is false. \\
\hline 'readlibbed' & a set & Returns the names of all libraries manually imported in a session by import, readlib, initialise. \\
\hline 'regsize' & a number & Sets the default size of registers, the number must be a non-negative integer. \\
\hline 'rounding' & a string & Returns or sets the current rounding method (beware, this may cause unwanted results; see also math.rint): 'downward' rounds down to the next lower integer, 'upward' rounds up to the next greater integer, 'nearest' rounds up or down toward whichever integer is nearest (default on most systems), 'zero' rounds toward zero. \\
\hline 'seqautoshrink' & true or false & If set to false, Agena does not free memory when you remove sequence values; default is true. \\
\hline 'signedbits' & true or false & If set to true, the bitwise operators \(\& \&, \sim \sim\), ||, ^ ^, <<<<, >>>, <<<< and >>>> internally use signed integers (the default), otherwise they use unsigned integers. \\
\hline 'skipinis' & true or false & If set to true, does not read the Agena initialisation files agena.ini / .aganea.init at restart. Default is false. \\
\hline 'skipmainlib' & true or false & If set to true, does not read the main library file lib/library at restart. Default is false. \\
\hline 'smallestnormal' & a number & Smallest normal number (usually \(2^{-1022}\) ). \\
\hline 'warnings' & an integer or Boolean & \begin{tabular}{l}
When just reading this setting, returns a number: 0 - warning system is off; 1 -ready to start a new message; 2 - previous message is to be continued. \\
Setting the warning mode requires a Boolean: true - switch on warnings, false switch them off.
\end{tabular} \\
\hline 'zeroedcomplex' & true or false & When set to true, real and imaginary parts of complex values close to zero are rounded to zero on output. (Note that internally, complex values are not rounded.) Default is false. \\
\hline
\end{tabular}

Examples:
```

> environ.kernel('signedbits'):
false
> environ.kernel(signedbits = true):
true

```

See also: environ.system.
```

environ.onexit ()

```

If assigned a function to the name environ.onexit, this function is automatically called when quitting or restarting Agena. For more information, see bye.
```

environ.pointer (obj)

```

Converts obj to a generic C pointer (void*) and returns the result as a string. obj may be userdata, a table, set, sequence, register, pair, thread or function; otherwise, pointer returns fail. Different objects will give different pointers, which gives a unique string identifier.
```

environ.ref (tbl, obj [, option])

```

Creates a unique integer reference for any argument obj and inserts obj into table tbl at position ref (i.e. tbi[ref] :=obj).

The function returns ref. Do not manually put any integer keys into tbl or delete them, always use environ.ref and environ.unref to modify tbl.

By default, obj is always inserted into tbl, even if it is already stored there.
If the optional third argument is 'reference' or 'full', then a check is performed to ensure that obj has not already been included in tbl. If obj is already in tbr, it is not inserted again and the integer index of obj in tbl is simply returned.

If option is 'reference', the function uses environ.isequal for the check, whereas with the option 'full', the standard = equality operator is being used.

See also: environ.unref, sema.open, utils.uuid.
```

environ.setfenv (f, table)

```

Sets the environment to be used by the given function. f can be an Agena function or a number that specifies the function at that stack level: Level 1 is the function calling setfenv. setfenv returns the given function.

As a special case, when f is 0 setfenv changes the environment of the running thread. In this case, setfenv returns no values.

\section*{environ.system ()}

Returns a table with the following system information: The size of various C types (char, int, long, long long, float, double, long double, uint16_t, int32_t, int64_t), the smallest and largest numeric values for C doubles (fields 'mindouble', 'maxdouble'), C unsigned short int (16-bit, 'maxushort'), C long ints (32-bit, fields 'minlong', 'maxlong'), C long long ints (fields 'minlonglong', 'maxlonglong'), and C unsigned long ints (field 'maxulong') (all compiled into the Agena binary), the number of bits in an C unsigned char ('bitschar') and a 32-bit integer (field 'bitsint'), the endianness of your platform (field 'endianess'), the hardware (field 'hardware') and the operating system (field 'OS') for which the Agena executable has been compiled. The 'floatradix' key represents the GNU C FLT_RADIX environment variable, with usually is 2.

\section*{See also: environ.kernel.}
```

environ.unref (tbl, ref)

```

With tbi a table and ref an integer, deletes value tbı[ref] and returns it. See also: environ.ref.
```

environ.used ( [opt] )

```

By default, returns the total memory in use by Agena in Kbytes. If opt is the string 'bytes', 'kbytes', 'mbytes', 'gbytes' or 'tbytes', the number will be refurned in the given unit.

See also: os.freemem, os.memstate.
environ.userinfo (f, level [, ...])
Writes information to the user of a procedure f depending on the given level, an integer. The information to be printed is passed as the third, etc. arguments and may be either numbers or strings.

At first the procedure should be registered in the environ.infolevel table along with a level (an integer) indicating the infolevel setting at which information will be printed, e.g. environ.infolevel[myfunc] :=1.

If you do not enter an entry for the function to the environ.infolevel table, then nothing is printed.
```

f := proc(x) is
environ.userinfo(f, 1, 'primary info to the user: ', x, '\n');
environ.userinfo(f, 2, 'additional info to the user: ', x, '\n')
end;

```

If the level argument to userinfo is equal or less than the environ.infolevel table setting, then the information is printed, otherwise nothing is printed.
```

> environ.infolevel[f] := 2;
> f('hello !');
primary info to the user: hello !
additional info to the user: hello !

```

Now the infolevel is decreased such that less information will be output.
```

> environ.infolevel[f] := 1;
> f('hello !');
primary info to the user: hello !

```

See also: environ.warn.
```

environ.warn (str [, ...])

```

Emits a warning with a message composed by the concatenation of all its arguments (which should be strings or numbers).

By convention, a one-piece message starting with '@' is intended to be a control message, which is a message to the warning system itself. In particular, the standard warning function in Lua recognizes the control messages "@off", to stop the emission of warnings, and "@on", to (re)start the emission; it ignores unknown control messages.

If called without arguments, returns a Boolean indicating whether the warning system is on or off, and the current warning state as an integer:
- 0 - warning system is off;
- 1 - ready to start a new message;
- 2 - previous message is to be continued.

See also: environ.infolevel, environ.userinfo.

\section*{14.3 package - Modules}

The package library provides a basic facility to inspect which packages have been loaded in a session.
```

package.checkclib (pkg)

```

Checks whether the package denoted by the string pkg and stored to a C dynamic library has already been initialised. If not, it returns a warning printed on screen and creates an empty package table. Otherwise it does nothing.
```

package.loadclib (packagename, path)

```

Loads the C library packagename (with extension .so in UNIX and Mac, or .dll in Windows) residing in the folder denoted by path. path must be the name of the folder where the C library is stored, and not the absolute path name of the file. The function returns true in case of success and false otherwise. On successful initialisation, the name of the package is entered into the package.readlibbed set.

See also: readlib, with.

\section*{package.loaded}

A table containing all the names of the packages that have been initialised, either at start-up or later on in a session.
package.packages ()
Returns a set with all the names of Agena's standard libraries that are initialised at start-up. The set does not include packages that have been loaded manually later on in a session, for example by the import statement or the readlib or with functions.

\section*{package.readlibbed}

A set with all the names of the packages that have been initialised with the readlib and with functions, and the import statement. This set may be deprecated in future versions of Agena.

\section*{14.4 rtable - Remember Tables}

This package comprises functions to administer remember tables.
```

rtable.defaults (f)
rtable.defaults (f, tab)
rtable.defaults (f, null)

```

Administrates read-only remember tables of functions. As it works exactly like the remember function, except that it creates remember tables that cannot be updated by the return statement, please refer to the description of the rtable.remember function for further details.
```

rtable.remember (f)
rtable.remember (f, tab)
rtable.remember (f, null)

```

Administers remember tables.

In the first form, the remember table stored to procedure \(£\) will be returned. See rtable.get for more information.

In the second form, remember adds the arguments and returns contained in table tab to the remember table of function \(f\). If the remember table of f has not been initialised before, remember creates it. If there are already values in the remember table, they are kept and not deleted.

If f has only one argument and one return, the function arguments and returns are passed as key~value pairs in table tab.

If \(£\) has more than one argument, the arguments are passed in a table. If \(£\) has more than one return, the returns are passed in a table, as well.

Valid calls are:
import rtable alias remember;
```

remember(f, [0 ~ 1]); \# one argument 0 \& one return 1
remember(f, [[1, 2] ~ [3, 4]); \# two arguments 1, 2 \& two returns 3, 4
remember(f, [1 ~ [3, 4]]); \# one argument 1 \& two returns 3, 4
remember(f, [[1, 2] ~ 3]]; \# two arguments 1, 2 \& one return 3

```

In the third form, by explicitly passing null as the second argument, the remember table of f is destroyed and a garbage collection run to free up space occupied by the former rtable.
remember always returns null. It is written in Agena and included in the lib/library.agn file.

\section*{See Chapter 6.18 for examples. See also: rtable.defaults.}
```

rtable.forget (f)

```

Empties the remember table or read-only remember table of procedure f entirely, giving back the space formerly occupied to the interpreter. It also enforces an immediate garbage collection. The function returns null.
```

rtable.get (f [, option])

```

Returns the contents of the current remember table or read-only remember table of procedure \(£\). If any value for option is given, the internal remember table including all the hash values are returned.
```

> fib := proc(n) is
> assume(n >= 0);
> return fib(n - 2) + fib(n - 1)
> end;
> rtable.remember(fib, [0 ~ 0, 1 ~ 1]);
> rget(fib):
[[0] ~ [0], [1] ~ [1]]

```

You cannot destroy the internal remember table by changing the table returned by rtable.get.

\section*{rtable.init (f)}

Creates a remember table (an empty table) for procedure \(£\). The procedure must have been written in Agena; reminisce that rtables for C API functions are not supported and that in these cases the function quits with an error.

If there is already a remember function for \(£\), it is overwritten. init returns null.
```

rtable.mode (f)

```

Returns the string 'rtable' if function \(f\) has a remember table, 'rotable' if \(f\) has a read-only remember table (that cannot be updated by the return statement), and the string ' none' otherwise.
```

rtable.purge (f)

```

Deletes the remember table or read-only remember table of procedure f entirely. It also enforces an immediate garbage collection. The function returns null.
rtable.roinit (f)
Creates a read-only remember table (an empty table) for procedure \(£\), which may be either a C function or an Agena procedure.

If there is already a remember function for f , it is overwritten. roinit returns null.
rtable.put (f, arguments, returns)
The function adds one (and only one) function-argument-and-returns `pair` to the already existing remember table or read-only remember table of procedure \(£\).
arguments must be a table array, returns must also be a table array. If the argument(s) already exist(s) in the remember table, then the corresponding result(s) are replaced with returns.

Given a function \(\mathrm{f}:=\langle<\mathrm{x}\)-> x >> for example, valid calls are:
rtable.put(f, [1], [2]); rtable.put(f, [1, 2], [2]);
rtable.put(f, [1], [1, 2]).

\section*{14.5 registry - Access to the Registry}

This package provides limited access to the registry (see Chapter 6.31). It should be used carefully.

Its library functions are:
registry.anchor (key, value)
Inserts a new key ~ value pair into the registry, where the key is a unique string, and the value the corresponding data. To delete entries in the registry, pass null for value.

The function returns nothing.
See also: registry.get.
```

registry.anyid (key)

```

The function has become obsolete and just returns the string key given.
See also: registry.get, utils.uuid.
```

registry.get (key)

```

The function returns the registry value indexed by key, which may be any type. If the registry entry is occupied by userdata, refers to loaded libraries or open files, the function just returns null. Otherwise, the entry is simply returned.

If a C library metatable contains the \(\qquad\) metatable read-only `metamethod`, null will be returned, as well.

With metatables defined by C libraries, it is still possible to delete or change metamethods, so extreme care should be taken when referencing to metatables returned. Especially, the \(\qquad\) gc metamethod must not be deleted or changed.

See also: registry.anchor.

\section*{14.6 stack - Built-In Number and Character Stacks}

The functions and operators in this package work with one of the six built-in numerical and character stacks, internal last-in-first-out data structures that can either store numbers or characters only. The stacks are addressed by their stack number and not variable names.

Stacks 1 to 3 are number stacks, stacks 4 to 6 are character stacks. The default stack is stack 1, i.e. a number stack.

Never use or change numeric stack 0 which is used by Agena internally as some sort of fixed-sized register array for numeric and other operations.

You may switch between the stacks by calling switchd(1) for the first stack, switchd(2) which is the second stack, etc.

While any element in - for example - a sequence occupies 24 bytes of memory, a number in a numeric stack takes only eight bytes, and a character in a character stack only one byte.

You can push a theoretically unlimited amount of numbers or characters onto the currently selected stack, with 128 pre-allocated slots after Agena initialisation.

If more numbers or characters are added, Agena automatically enlarges the current stack. However, if values are removed, Agena itself does not shrink the allocated memory. Call stack.shrinkd to accomplish this if required, and stack.sized to query the amount of used and internally allocated space.

Example: to convert a decimal number into the binary system, you might use a numerical stack:
```

tobinary := proc(x :: number) is \# for positive numbers only
local base := 2; \# new base
local r := '';
stack.resetd(); \# always clear stack before usage, destructive !
while x > 0 do
pushd(x % base); \# push the remnant onto the stack (0 or 1)
x := x \ base
od;
while allotted() do \# now traverse the stack from top to bottom
r := r \& popd() \# and also remove the remnants one after another
od;
return r \# return result as a string
end;
> switchd(1): \# select a numeric stack
> tobinary(6):
110

```

The names of functions and operators usually end in a final ` \(d\) ’.

The basic library functions and operators are:
```

allotted ([n])

```

If given no argument and if the stack contains one or more elements, the function returns the number of values in the stack, else it returns null. It can be easily used in while loops to traverse a stack, see example above.

If given a stack number \(n\), it either returns the number of elements currently in the given stack or null if no values are in this stack.

See also: stack.sized.

\section*{cell (idx)}

The operator returns the element stored at the absolute or relative position idx of the current stack. While -1 refers to the top of the stack, -2 , to the element just below the top, etc., 0 refers to the first element at the bottom of the stack, 1 one step `above`, etc. If the stack is empty or idx is out-of-bounds, null will be returned.

\section*{popd ([n [, anyoption]])}

The function pops n numbers or characters from the top of the current stack, or if \(n\) is not given, the element at the current top of the stack. If the stack is empty, null will be returned.

By default, the function returns the last value popped. This can be suppressed if any second argument is given.

See also: pushd.
```

pushd (x [, ...])

```
pushd (s)
In the first form, the statement pushes one or more numbers, strings or single characters \(x\) onto the current stack. In the second form, the command pushes all the numbers, strings or single characters in the sequence s. With strings, all the characters in the string are pushed, with the last character put at the stack top, and all the preceding characters below.

The function returns nothing.
You may or may not enclose the arguments in brackets.
If the current stack is a character stack and x or an element in s is an integer in the range 0 to 9 , both inclusive, the operator converts \(x\) to a character and inserts this character into the stack. If you insert an empty string and dump the string using - for
example - stack.dumpd later, the resulting string is terminated at the position you inserted the empty string.

Hint: If the very last argument is the pair 'stack':<stacknumber>, with <stacknumber> an integer, the values are pushed onto the given stack <stacknumber>. Using this option, however, may slow down the operation since processing an option takes quite some computation time.

See also: stack.pushstringd.

\section*{switchd ( n )}

The statement switches to stack \(n\) with \(n\) an integer.
You may not or may not enclose the argument in brackets.
See also: stack.selected, stack.switchto.

The stack library features the following auxiliary procedures:
```

stack.attribd ()

```

Returns various status information on the current stack in a table with the keys: 'currentstack' (number of the current stack), 'defaultsize' (number of default slots), 'isnumstack' (true if the stack stores Agena numbers, false if the stack stores ASCll character codes), 'stackmax' (maximum number of allocated slots), 'stacktop' (current stack top, counting from 0).

\section*{stack.choosed ()}

Returns the ID of both the number and character stack with the least number of values in them. The first return is the ID of the smallest number stack, the second return the one of the smallest character stack.

See also: switchd, stack.selected.
stack. dequeued ()
Removes the value at the bottom of the current stack, returns it, and moves all elements to close the space. It is equivalent to stack.removed(0).

See also: stack.enqueued.
```

stack.dumpd ([n] [, option])

```

With a numeric stack, returns all values in the current stack in a new sequence if given no argument, or the last n values pushed onto the stack, and pops them all from the stack. The number of pre-allocated slots is not changed, see stats.shrinkd.

With a character stack, when given no argument, all characters are returned as exactly one string, first-in first-out style. If \(n\) is given, the last \(n\) characters inserted are returned in exactly one string.
If passed true as the very last argument, the selected numbers or characters are returned in reverse order. This saves an expensive call to stack.reversed.

If the stack is empty, the function just returns null.
See also: stack.explored.
stack.enqueued ( \(x\) )
Inserts the number or character x at the bottom of the current stack, shifting up other elements to open space. The function returns nothing. It works like stack.insertd(0, x).

See also: stack.dequeued.

\section*{stack.explored ()}

Returns the entire contents of the current stack without modifying it. If the current stack is numeric, the return is a sequence of numbers, otherwise a string will be returned.

If the stack is empty, the function just returns null.
See also: stack.dumpd.
```

stack.insertd (idx, x)

```

Inserts the number or character x at the given relative stack position idx, shifting up other elements to open space. The function returns nothing.

If \(i d x\) is a non-negative integer, 0 represents the bottom of the stack, 1 the position just above the bottom, etc. If idx is negative, -1 represents the stack top, -2 the element just below the top, etc. If no argument is given, idx is set to -1 by default, i.e. the top element.

See also: stack.dequeued, stack.enqueued, stack.removed.
```

stack.mapd ([idx, ] f, [...] [, true])
stack.mapd (true, f, [, true])

```

In the first form, if \(i d x\) is not given or if \(i d x=-1\), the default, maps function \(f\) on the top element of the current character or numeric stack. With a character stack, the result of the call to f must be a character, and with a number stack the result must be a number, otherwise the function issues an error.

If \(i d x\) is a negative integer, the stack.mapd applies \(f\) on the \(\mid\) idx \(\mid\)-th value in the stack.

If f is a multivariate function, its second, third, etc. argument must be passed right after f .

In the second form, by passing the Boolean true and a univariate or multivariate function f of n parameters, stack.mapd takes the n top stack values, passes them as arguments to \(f\), with the value at the top of the stack the last argument, and returns the result. If the parameter list of f contains a ?-varargs token, then all stack elements are passed to f . Example:

We have a function of three parameters \(x, y, z\) that returns \(x^{*} y+z\). The call puts the top three argumements 3, 2, 4
```

> pushd 3, 2, 4

```
into the argument list, pops them from the stack, pushes the result of the function call onto the stack and returns it:
```

> stack.mapd(true, << x, y, z -> fma(x, y, z) >>):
1 0

```

In both the first and the second form, the stack element(s) is (are) replaced by the result of the function call if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the stack element(s) is (are) not replaced and the result is just put onto the stack top.
```

stack.pushstringd (str)

```

Pushes all the characters in string str onto a character stack. After the operation, str [-1] resides at the top of the stack, str[-2] just below, etc. The return is the size of str, i.e. size str.

See also: pushd.
stack.pushvalued (idx)
Pushes the value residing at the given relative stack position idx to the top of the stack. The original value also remains at position idx.

If \(i d x\) is a non-negative integer, 0 represents the bottom of the stack, 1 the position just above the bottom, etc. If idx is negative, -1 represents the stack top, -2 the element just below the top, etc. If no argument is given, idx is set to -1 by default, i.e. the top element.
stack. removed (idx)
Removes the value residing at the given relative stack position idx, returns it, and moves all elements to close the space.

If \(i d x\) is a non-negative integer, 0 represents the bottom of the stack, 1 the position just above the bottom, etc. If idx is negative, -1 represents the stack top, -2 the element just below the top, etc. If no argument is given, idx is set to -1 by default, i.e. the top element.

See also: stack.insertd, stack.dequeued, stack.enqueued.
stack.readbytes (filehandle [, bytes] [, options])
By default, the function reads environ.kernel('buffersize') bytes from the file denoted by filehandle and writes them to the current stack.

Open the file with binio.open before the first call and when you are finished, call binio.close to release the file.

The function increments the file position thereafter so that the next bytes in the file can be read with a new call to various stack.readbytes.

You may change the kernel buffer size value to any other values in order to read less or more bytes.

If bytes is given, the function writes bytes bytes from the file denoted by filehandle to the current stack.

To write the file contents to another than the current stack, pass the optional stack option with the preferred stack number, e.g.:
> stack.readbytes(fh, stack=6);
By default, the function ignores any newlines (ASCII 10) or carriage returns (ASCII 13) in the file. You can change this by setting the ignore option and passing a string of explicit characters that shall be skipped, e.g.:
```

> stack.readbytes(fh, ignore=" .\n"); \# skip white space, dot \& newline

```

By default the function reads in embedded zeros and treats them as every other byte. If you pass the eof option and set it to true, then the function quits if it
encounters an embedded zero in the file. The file pointer is automatically reset to the position of the embedded zero. The default is false, i.e. the whole file is read in.

The function returns both the number of bytes read from the file and the number of bytes written to the stack. If the end of the file has been reached, null will be returned. In case of an error, it quits with the respective error.

See also: binio.readbytes.
stack.replaced (idx, x)
Replaces the value at stack position idx with the number or one-character string x . The value replaced will be returned.

If idx is a non-negative integer, 0 represents the bottom of the stack, 1 the position just above the bottom, etc. If idx is negative, -1 represents the stack top, -2 the element just below the top, etc. If no argument is given, idx is set to -1 by default, i.e. the top element.

Note that with character stacks, if \(x\) should be the empty string, the string returned by strings.dumpd will be terminated at position idx.
stack.resetd ([..] )
If given no arguments, clears the entire stack so that it becomes empty. The functions does not return anything and should be used cautiously as another function might still need elements in the stack.

If passed one or more valid stack numbers (integers), the function conducts the same for the given stack(s).

The number of pre-allocated slots is not reset, however, see stack.shrinkd.

\section*{stack.reversed ([n])}

If \(n\) is not given, reverses the positions of all the elements in the current stack. If \(n\) is given, only the last \(n\) elements pushed onto the stack are reversed. The function returns nothing.

See also: strings.reverse.
```

stack.rotated ([n])

```

Moves all the elements in the current stack \(n\) places from the bottom to the top if \(n\) is positive, and \(n\) places from the top to the bottom if \(n\) is negative. The default is \(n\) \(=+1\). The function returns nothing.
```

stack.selected ()

```

Returns the number of the currently selected stack, i.e. an integer.

\section*{See also: switchd, stack.choosed.}
```

stack.shrinkd ([any])

```

With no argument, shrinks the number of pre-allocated but not assigned slots in the current stack if possible. If any argument is given, all stacks are shrunk.

The function returns the new number(s) of pre-allocated slots but does not pop any elements. The function is useful to reduce memory consumption if a lot of values have been removed from the stack.

See also: stack.resetd.

\section*{stack.sized ()}

Returns the current number of elements in the current stack along with the current maximum number of slots internally allocated by the system. See also: allotted.
```

stack.sorted ([n])

```

Sorts all or the last n values pushed onto the current stack in ascending order using the fast Introsort algorithm. If no argument is passed, all elements in the current stack are processed. The function returns nothing.

The function works with numeric stacks only.
stack.swapd (i, j)
Swaps the values stored at position \(i\) and \(j\) of the current stack.
```

stack.switchto ([x])

```

Determines the current stack number p , and then switches to the number stack q with the least number of elements if any number x or no argument is given, or to the character stack \(q\) with the least number of elements if any string x is given.

The function returns \(p\) and \(q\), in this order.
You can use p later to switch back to the former stack with the switchd statement.

The following functions perform real arithmetic on a numeric stack:
stack.addtod (x [, true])
Adds its argument \(x\), a number, to the top element of the current numeric stack.

The top stack element is replaced by the resulting sum if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the sum computed. It uses the Kahan-Babuška algorithm to prevent round-off errors.

See also: stack.mulby, stack.powd, stack.sumupd.
stack.mulbyd (x [, true])
Multiplies its argument \(x\), a number, by the top element of the current numeric stack.

The top stack element is replaced by the resulting product if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns computed product.
See also: stack.addto, stack.mulupd, stack.powd, stack.recipd.
stack.absd ([true])
Computes the absolute value of the top element of the current numeric stack.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
```

stack.negated ([true])

```

Multiplies the top numeric stack element by -1 .

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
stack.recipd ([true])
Computes the reciprocal of the top element of the current numeric stack.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
stack.intd ([true])
Rounds the number on the top of a numeric stack to the nearest integer towards 0 .
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.

\section*{stack.fracd ([true])}

Converts the number on the stack top to its fractional part.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
stack.intdivd (x [, true])
Integer division of the top element of the current numeric stack and the given number x; works like the \operator.

The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
See also: stack.modd.
```

stack.modd (x [, true])

```

Modulus of the top element of the current numeric stack and the given number x; works like the \% operator.

The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.

See also: stack.intdivd.
stack.powd (power [, true])
Raises the top element of the current numeric stack to the given power, a number.
The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

The function also returns the result.
See also: stack.antilogd, stack.rootd.
stack.pythad ([true])
Computes the hypotenuse or inverse hypotenuse of the number below the stack top and the number on the top and returns the computed result. The function avoids over- and underflows and treats subnormal numbers accordingly.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.hypotd, stack.invhypotd.
stack.squared ([true])
Raises the top element of the current numeric stack to the power of 2 .
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
The function also returns the result.

See also: stack.antilogd, stack.powd, stack.rootd.
```

stack.rootd (n [, true])

```

Computes the non-principal \(n\)-th root of the top element of the current numeric stack. n must be an integer and is 2 by default.

The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.cbrtd, stack.powd, stack.sqrtd.
stack.cbrtd ([true])
Computes the cubic root of the top element of the current numeric stack.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.powd, stack.rootd, stack.sqrtd.
```

stack.sqrtd ([true])

```

Computes the square root of the top element of the current numeric stack.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.cbrtd, stack.powd, stack.rootd.
stack.fmad ([true])
Computes \(x^{\star} y+z\), where \(x\) represents the second number below the stack top, \(y\) the number below the stack top and \(z\) the number on the top and returns the computed result. The function avoids over- and underflows and treats subnormal numbers accordingly.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
stack.hypotd ([true])
stack.invhypotd ([true])
Computes the hypotenuse or inverse hypotenuse of the number below the stack top and the number on the top and returns the computed result. The function avoids over- and underflows and treats subnormal numbers accordingly.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.pythad, stack.hypot4d.
stack.hypot4d ([true])
Computes \(\sqrt{x^{2}-y^{2}}\), where \(x\) represents the number below the stack top and \(y\) the number on the top and returns the computed result. The function avoids over- and underflows and treats subnormal numbers accordingly.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.hypotd.
stack.lnd ([true])
Returns the natural logarithm of the top element of the current numeric stack.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.antilogd, stack.expd, stack.logd.

\section*{stack.logd (base [, true])}

Returns the logarithm of the top element of the current numeric stack to the given base, with base a number. For the natural logarithm, pass Efor base.

The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.antilogd, stack.Ind.
```

stack.antilogd (base [, true])

```

Raises the given base, a number, to the power of the top element of the current numeric stack.

To compute the exponential function \(e^{x}, x\) should be the top stack element and pass E as function argument base.

The top stack element is replaced by the result if true is not given as the last argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.expd, stack.exp2d, stack.exp10d.
stack.expd ([true])
Raises \(\mathrm{E}=\exp (1)\) to the power of the number at the stack top and returns it.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.exp2d, stack.exp10d.
```

stack.exp2d ([true])

```

Raises 2 to the power of the number at the stack top and returns it.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.expd, stack.exp10d.
stack. exp10d ([true])
Raises 10 to the power of the number at the stack top and returns it.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

See also: stack.expd, stack.exp2d.
```

stack.sind ([true])
stack.cosd ([true])
stack.tand ([true])

```

Returns the sine, cosine or tangent of the top element of the current numeric stack, in radians.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
```

stack.sinhd ([true])
stack.coshd ([true])
stack.tanhd ([true])

```

Returns the hyperbolic sine, hyperbolic cosine or hyperbolic tangent of the top element of the current numeric stack, in radians.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
```

stack.arcsind ([true])
stack.arccosd ([true])
stack.arctand ([true])

```

Returns the arcus sine, arcus cosine or arcus tangent of the top element of the current numeric stack, in radians.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
```

stack.arcsinhd ([true])
stack.arccoshd ([true])
stack.arctanhd ([true])

```

Returns the inverse hyperbolic sine, inverse hyperbolic cosine or inverse hyperbolic tangent of the top element of the current numeric stack, in radians.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
stack.arctan2d ([true])
Computes the arc tangent of \(\mathrm{y} / \mathrm{x}\) of the two top elements of the current numeric stack, in radians, where \(x\) represents the value just below the top and \(y\) the value at the top of the stack.

The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
stack.meand ([n] [, true])
Computes the arithmetic mean of all or a given number \(n\) of values in the current numeric stack and either pushes the result onto the top of the stack if true has been passed as the last argument; or pops all the values processed and pushes the result on top of the stack if only n or no argument has been given.

The function in general also returns the arithmetic mean.
By dividing each element before summation, the function avoids arithmetic overflows and also uses the Kahan-Babuška algorithm to prevent round-off errors during summation. Computation is done from top to bottom.
stack.sumupd ([n] [, true])
Sums up all or a given n number of values in the built-in numeric stack and either pushes the result onto the top of the stack if true has been passed as the last argument; or pops all the values summed-up and pushes the sum on top of the stack if only n or no argument has been given.

Summation is done from top to bottom. The function uses the Kahan-Babuška algorithm to prevent round-off errors during summation and also returns the sum.
stack.mulupd ([n] [, true])
Multiplies all or a given n number of values in the built-in numeric stack and either pushes the result onto the top of the stack if true has been passed as the last argument; or pops all the values multiplied and pushes the product on top of the stack if only n or no argument has been given.

Multiplication is done from top to bottom. The function in general also returns the product.

The following functions perform operations on the two values at the top of the stack, i.e. the value at the top and the value just below it. They have been deliberately kept lean for maximum performance:

\section*{stack.addtwod ()}

Adds up the two numbers on top of the current stack and replaces them with the result; also returns the sum.
```

stack.subtwod ()

```

Subtracts the number on top of the current stack from the number below it and replaces them with the result; also returns the difference.

\section*{stack.multwod ()}

Multiplies the number on top of the current stack by the number below it and replaces them with the result; also returns the product.
```

stack.divtwod ()

```

Divides the number below the stack top by the number on the top and replaces them with the result; also returns the quotient.
stack.intdivtwod ()
Performs an integer division of the number below the stack top by the number on the top and replaces them with the result; also returns the integer quotient.
stack.modtwod ()
Like stack.intdivtwod but computes the modulus.

\section*{stack.powtwod ()}

Raises the number below the stack top to the power on the top and replaces both numbers with the result; also returns the power.

The following functions perform operations on a character stack:
stack.absd ()
Returns the ASCII value of the top element of the current numeric stack.

The function does not modify the stack.
stack.lowerd ([true])
Converts the character at the stack top to lower-case and returns it.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.
stack. upperd ([true])
Converts the character at the stack top to upper-case and returns it.
The top stack element is replaced by the result if true is not given as an argument, but the rest of the stack is left unchanged. Otherwise, if you pass true, the top stack element is not replaced and the result is just put onto the stack top.

\section*{14.7 sema - Unique Identifiers}

As a plus package, the sema package is not part of the standard distribution and must be activated with the import statement, i.e. import sema.

The package provides functions to create and administer unique, non-negative integer identifiers, called `semaphore ids` in this context, in a memory-saving fashion (see sema.state and sema.open for details).

There are two types of `semaphores`: a global built-in one, and one or more instances represented by userdata objects:
```

> import sema;
> sema.open(): \# create a new global semaphore id
0
> s := sema.new(): \# create a semaphore instance s
sema(01CCD3B8)
> sema.open(s): \# create a new semaphore id for semaphore s
0
> sema.open(s):
1
> sema.open(s):
2
> t := sema.new(): \# create another semaphore instance t
sema(01CCD298)
> sema.open(t): \# create a new semaphore id for semaphore t
0
sema.close (id, [...])
sema.close (s, id, [...])

```

In the first form, closes the given global semaphore id, and optionally other semaphores, as well. If sema.open is called thereafter, it will return id. The function returns nothing. Note that if id is not the last semaphore id opened before, then Agena automatically switches to dynamic memory management consuming "O(n)" of memory space instead of using just one 8 -byte integer for the internal counter.

In the second form, the id of semaphore s is closed.
See also: sema.open, sema.shrink.
sema.isopen ([s, ] id)
Checks whether the given global semaphore id or the id of the semaphore \(s\) is open and returns true or false.
```

sema.open ([s, ] [id])

```

Without any argument, creates a new global semaphore id, a non-negative integer. With the very first call, returns 0 , counting up by 1 subsequently as along as sema.close or sema.reset are not executed.

If the non-negative global integer id id is passed and id has not yet been created by sema.open, the function creates it. If \(s\) is being passed, then semaphore s returns the next free id or the given id.

This feature also allows you to write functions dumping the current semaphore state to a file and re-load it later, see binio.writechar, binio.readchar, bytes.tobytes.

If the current internal administrative memory is exceeded, the function automatically expands it. Note that if id is not the next semaphore id opened just before, then Agena automatically switches to dynamic memory management consuming " \(\mathrm{O}(\mathrm{n})\) " of memory space instead of using just one 8 -byte integer for the internal counter.

See also: environ.ref, factory.count, utils.uuid.
```

sema.reset ([s])

```

Closes all allocated semaphores ids and also shrinks the internal memory used to administer the semaphores to the default size, if possible. If semaphore s is given, then all ids of this semaphore are reset.

The function returns nothing. See also: sema.shrink.
```

sema.shrink ([s])

```

Without any argument, shrinks the internal memory used to administer all global semaphores ids so that it consumes the least necessary space. The same applies to semaphore s if given. If internal memory size could be reduced, it returns true and false otherwise. Note that due to performance reasons, sema.close does not try to reduce memory consumption.

See also: sema.reset.
```

sema.state ([s])

```

Returns administrative information on the current global semaphore state if not argument is given or on semaphore instance s, in a table.

The semaphores are internally stored using an 8 * 32 bits array by default. Each 32-bit chunk is called a `slot`.

The 'firstfreeslot' field contains the number of the first slot that might harbour a new semaphore. Note that once you have used sema.close, this may just be an estimate.

The 'slot' sequence returns the bits set in all slots, as decimal non-negative integers.

Field ' current' is an estimate of the last allocated semaphore id.
Key 'minopen' denotes the semaphore id with the smallest ID, 'maxopen' the one with the largest ID.
'nextfree' denotes the number of the semaphore id if sema.open would be called next.
'simplecounter_active' indicates whether the memory-efficient counting is active (true) or dynamic memory management of the semaphore ids is in use (false).
'simplecounter ' depicts the current semaphore id.

\subsection*{14.8 Coroutines}

The operations related to coroutines comprise a sub-library of the basic library and come inside the table coroutine. To find out what coroutines are, please have a look at the website of the Lua programming language.
```

coroutine.resume (co [, val1, ...])

```

Starts or continues the execution of coroutine co. The first time you resume a coroutine, it starts running its body. The values vall, \(\cdots\) are passed as the arguments to the body function. If the coroutine has yielded, resume restarts it; the values val1, ... are passed as the results from the yield.

If the coroutine runs without any errors, resume returns true plus any values passed to yield (if the coroutine yields) or any values returned by the body function (if the coroutine terminates). If there is any error, resume returns false plus the error message.
```

coroutine.running ()

```

Returns the running coroutine, or null when called by the main thread.
coroutine.setup (f)
Creates a new coroutine, with body \(f\). f must be an Agena function. Returns this new coroutine, an object with type 'thread'.
```

coroutine.status (co)

```

Returns the status of coroutine co, as a string: 'running', if the coroutine is running (that is, it called status); 'suspended', if the coroutine is suspended in a call to yield, or if it has not started running yet; 'normal' if the coroutine is active but not running (that is, it has resumed another coroutine); and 'dead' if the coroutine has finished its body function, or if it has stopped with an error.
coroutine.wrap (f)
Creates a new coroutine, with body f. f must be an Agena function. Returns a function that resumes the coroutine each time it is called. Any arguments passed to the function behave as the extra arguments to resume. Returns the same values returned by resume, except the first boolean. In case of error, propagates the error.
```

coroutine.yield (...)

```

Suspends the execution of the calling coroutine. The coroutine cannot be running a C function, a metamethod, or an iterator. Any arguments to yield are passed as extra results to resume.

\section*{14.9 debug - Debugging}

This library provides the functionality of the debug interface to Agena programmes. You should exert care when using this library. The functions provided here should be used exclusively for debugging and similar tasks, such as profiling. Please resist the temptation to use them as a usual programming tool: they can be very slow. Moreover, several of its functions violate some assumptions about Agena code (e.g., that variables local to a function cannot be accessed from outside or that userdata metatables cannot be changed by Agena code) and therefore can compromise otherwise secure code.

All functions in this library are provided inside the debug table. All functions that operate over a thread have an optional first argument which is the thread to operate over. The default is always the current thread.

\section*{debug. debug ()}

Enters an interactive mode with the user, running each string that the user enters. Using simple commands and other debug facilities, the user can inspect global and local variables, change their values, evaluate expressions, and so on. A line containing only the word cont finishes this function, so that the caller continues its execution.

Note that commands for debug.debug are not lexically nested within any function, and so have no direct access to local variables.

\section*{debug.funcname (level)}

Returns the name of the function in which it (i.e. debug.funcname) has been called. The return is a string. It is a wrapper for "debug.getinfo(level, "n").name". By default, level 1 is used, but you may pass another level. If level is out of range, then fail will be returned. If the function name could not be determined, null will be returned. The function may be useful to create more flexible error messages.
debug.getconstants ()
Returns the internal set that stores global constants.
debug.getfenv (obj)
Returns the environment of object obj.
See also: debug.setfenv.

\section*{debug.gethook ([thread])}

Returns the current hook settings of the thread, as three values: the current hook function, the current hook mask, and the current hook count (as set by the debug.sethook function).
debug.getinfo ([thread,] function [, what])
Returns a table with information about a function. You can give the function directly, or you can give a number as the value of function, which means the function running at level function of the call stack of the given thread: level 0 is the current function (getinfo itself); level 1 is the function that called getinfo; and so on. If function is a number larger than the number of active functions, then getinfo returns null.

The returned table may contain all the fields returned by lua_getinfo, with the string what describing which fields to fill in. The default for what is to get all information available, except the table of valid lines. If present, the option 'f' adds a field named func with the function itself. If present, the option ' L' adds a field named activelines with the table of valid lines. If present, the option ' \(g\) ' adds a field named globals with a table of variables that have been globally assigned. The 'a' option adds a field called arity that includes the number of arguments - excluding possible varargs - expected by function. When given the 'v' formatter, the 'varargs' entry indicates whether varargs can be passed to the function (? in its parameter list). 'v' returns a table of all parameters and locally declared variables along with their current values. ' c ' returns activation record ar->i_ci setting.

For instance, the expression debug.getinfo(1, 'n').name returns a name of the current function, if a reasonable name can be found, and debug.getinfo(print) returns a table with all available information about the print function.

See also: debug.funcname.
debug.getlocal ([thread,] level, local)
This function returns the name and the value of the local variable with index local of the function at level level of the stack. (The first parameter or local variable has index 1 , and so on, until the last active local variable.) The function returns null if there is no local variable with the given index, and raises an error when called with a level out of range. (You can call debug.getinfo to check whether the level is valid.)

Variable names starting with '(' (open parentheses) represent internal variables (loop control variables, temporaries, and C function locals).

See also: debug.getlocals, debug.setlocal.
```

debug.getlocals (level [, option])

```

Like debug.getlocal, but returns a table of all local variables of a function running at level level of the stack. The array part of the table includes the variable names, the hash part the variables and their current values as key ~ value pairs. The other returns, in the following order are: number of local variables including procedure parameters, number of procedure parameters, a boolean indicating whether ? (varargs) is part of the parameter list, a table with all unassigned local variables.

By passing any option, only an array of parameter and local variable names plus the number of parameters (first entries in the array) will be returned.
```

debug.getmetatable (object)

```

Returns the metatable of the given object or null if it does not have a metatable.
See also: debug.setmetatable.
```

debug.getregistry ()

```

Returns the registry table, see Chapter 6.31. Do not change values with integer keys - this would destroy occupied by userdata and could lead to undefined behaviour of the interpreter.
```

debug.getrtable (f)

```

Returns a reference to the internal remember table of procedure \(£\). Opposed to rtable.rget, the function gives you direct read and write access to the remember table, so use it with care.
```

debug.getstore (f)

```

Returns a reference to the internal storage table of procedure f. You can both inspect this table as well as inject values into it. See debug.setstore or source file lib/mapm.agn or Chapter 6.25 for an example of how to store precomputed values, here Chebyshev coefficients, in a function, to be used later at function invocation.
```

debug.getupvalue (f, up)

```

This function returns the name and the value of the upvalue with index up of the function \(f\). The function returns null if there is no upvalue with the given index.

See also: debug.getupvalues, debug.nupvalues, debug.setupvalue.

\section*{debug.getupvalues (f)}

Returns all upvalues of an Agena closure f in a table, plus the number of upvalues. The first entry in the table depicts the first upvalue, and so on. If there are no upvalues, the return is null plus zero. The function does not accept closures written in \(C\).

\section*{See also: debug.getupvalue, debug.nupvalues, debug.setupvalue.}
```

debug.nupvalues (f)

```

Returns the number of upvalues in an Agena closure. The function does not accept closures written in C .

\section*{See also: debug.getupvalue, debug.getupvalues.}
debug.setfenv (object, \(t\) )
Sets the environment of the given object to the given table \(t\). Returns object.
See also: debug.getfenv.
debug.sethook ([thread,] hook, mask [, count])
Sets the given function as a hook. The string mask and the number count describe when the hook will be called. The string mask may have the following characters, with the given meaning:
- ' c ': The hook is called every time Agena calls a function;
- ' \(r\) ': The hook is called every time Agena returns from a function;
- ' 1 ': The hook is called every time Agena enters a new line of code.

With a count different from zero, the hook is called after every count instructions.
When called without arguments, debug.sethook turns off the hook.
When the hook is called, its first parameter is a string describing the event that has triggered its call: 'call', 'return' (or 'tail return'), 'line', and 'count'. For line events, the hook also gets the new line number as its second parameter. Inside a hook, you can call getinfo with level 2 to get more information about the running function (level 0 is the getinfo function, and level 1 is the hook function), unless the event is 'tail return'. In this case, Agena is only simulating the return, and a call to getinfo will return invalid data.
```

debug.setlocal ([thread,] level, local, value)

```

This function assigns the value value to the local variable with index local of the function at level level of the stack. The function returns null if there is no local variable with the given index, and raises an error when called with a level out of range. (You can call getinfo to check whether the level is valid.) Otherwise, it returns the name of the local variable.

See also: debug.getlocal.
debug.setmetatable (object, \(t\) )
Sets the metatable for the given object to the given table \(t\) (which can be null).
See also: debug.getmetatable.
```

debug.setstore (f, t)

```

Sets all the key~value pairs in table t into the internal store of procedure f .
See also: debug.getstore.
```

debug.setupvalue (f, up, value)

```

This function assigns the value value to the upvalue with index up of the function \(£\). The function returns null if there is no upvalue with the given index. Otherwise, it returns the name of the upvalue.

See also: debug.getupvalue.

\section*{debug.system ()}

Returns a table with the following system information: The size of various C types (char, int, long, long long, float, double, int32_t, int64_t), the smallest and largest numeric values for C doubles, C long ints, C long long ints, and C unsigned long ints (all compiled into the Agena binary), the endianness of your platform, the hardware and the operating system for which the Agena executable has been compiled.

See also: environ.kernel.
```

debug.traceback ([thread,] [message])

```

Returns a string with a traceback of the call stack. An optional message string is appended at the beginning of the traceback. This function is typically used with xpcall to produce better error messages.

Chapter Fifteen

\section*{Graphics}

\section*{15 Graphics}

\section*{15.1 gdi - Graphic Device Interface package}

As a plus package, this graphics interface is not part of the standard distribution and must be activated with the import statement, e.g. import gdi.

The gdi package provides functions to plot graphics either to a window or a PNG, GIF, JPEG, FIG, or PostScript file. It is available for the Solaris, Linux, Mac OS X for Intel CPUs, and Windows editions of Agena. There is an experimental OS/2 - ArcaOS version that is still experimental and it can create FIG and PostScript files only. The package is not available in the 64-bit editions.

The gdi package provides procedures to plot basic geometric objects such as points, lines, circles, ellipses, rectangles, etc.

It also provides means to easily plot graphs of univariate functions and geometric objects where the user does not need pay attention for proper axis ranges, mapping to the internal coordinate systems, etc.

\subsection*{15.1.1 Opening a File or Window}

Operation starts by opening a device - window or file - with the gdi.open function. The function returns a device handle for later reference. Almost all functions provided by the package request this device handle.
```

> import gdi;
> d := gdi.open(640, 480);

```

\subsection*{15.1.2 Plotting Functions}

Plot a point to the window at \(x=200\) and \(y=100\) :
```

> gdi.point(d, 200, 100);

```

Plot a line between two points [200, 150] and [300, 200]:
```

> gdi.line(d, 200, 150, 300, 200);

```

Draw a circle and a filled circle. Besides giving the device number, pass a centre ( \(x\) and y co-ordinates) and a radius.
```

> gdi.circle(d, 320, 240, 50);
> gdi.circlefilled(d, 400, 240, 50);

```

\subsection*{15.1.3 Colours, Part 1}

All functions accept a colour option passed as an additional - the last - argument.
The colour must be given as an integer that must be determined by a call to the gdi.ink function. gdi.ink requires the device number, and three RGB colour values in the range \(\left[\begin{array}{ll}0 & . \\ 1\end{array}\right]\). Each colour should be determined only once.

There are 26 predefined colours with numbers 0 to 25 , automatically set at each invocation of a new device (call to the gdi.open function). Thus, these 26 basic colours do not need to be explicitly set with gdi.ink.

The default colours are:
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline 0 & white & 7 & light green & 14 & grey & 21 & purple \\
\hline 1 & black & 8 & greenish & 15 & grey-blue & 22 & dark orange \\
\hline 2 & blue & 9 & light sky-blue & 16 & bright green & 23 & purple \\
\hline 3 & light blue & 10 & bordeaux & 17 & light greenish & 24 & light lilac \\
\hline 4 & greenish & 11 & lilac & 18 & light sky-blue & 25 & yellow \\
\hline 5 & cyan & 12 & light lilac & 19 & red & & \\
\hline 6 & sky-blue & 13 & khaki & 20 & purple & & \\
\hline
\end{tabular}

If you want to set a default colour for all subsequent drawings, use gdi.useink.

\subsection*{15.1.4 Closing a File or Window}

To finally close the window, use gdi.close.
> gdi.close(d);

\subsection*{15.1.5 Supported File Types}

To create image files, simply pass the name of the file as the third argument to gdi.open. Agena determines the type of the image file from its suffix.

If a file name ends in .png, it creates a PNG file. If a file name ends in .gif, it creates a GIF file. If a file name ends in . jpg, it creates a JPEG file. Likewise, the suffix . fig creates a FIG, and .ps generates a PostScript file.

\subsection*{15.1.6 Plotting Graphs of Univariate Functions}

The gdi.plotfn function plots graphs of functions in one real to a window or file. It accepts various options for colour, line thickness, line style, sizing, axis type, etc. The function takes care for opening a device, plotting the graph and axes, so that the user does not need to draw them manually. The function requires a function and the left and right border on the \(x\)-axis.
```

> import gdi alias
> plotfn(<< x -> x*sin(x) >>, -10, 10);

```

For further details and examples see gdi.plotn. For available plot options, see gdi.options. See calc.nokspline which along with gdi.plotfn generates a smoothed graph through a given list of interpolation points.

\subsection*{15.1.7 Plotting Geometric Objects Easily}

Like gdi.plotfn, the gdi function plot outputs geometric objects in the Cartesian co-ordinate system with the point \([0,0]\) its centre. It accepts options for user-defined colours, window sizes, axis types, etc. The function opens a device automatically, plots all the objects that are stored in a PLOT data structure optionally along with axes, a user-defined background colour, etc.

The function requires the PLOT structure as the first argument, and any options as additional arguments. Contrary to gdi.plotfn, it does not accept left, right, lower or upper borders, for it determines the borders automatically.

A PLOT data structure is a sequence of the user-defined type 'PLOT', and contains the geometric objects with their positions and respective colours.

The following geometric objects can be drawn with gdi.plot:
\begin{tabular}{|l|l|l|l|}
\hline Object & Name & Object & Name \\
\hline arc & ARC & line & LINE \\
\hline filled arc & ARCFILLED & point & POINT \\
\hline circle & CIRCLE & rectangle & RECTANGLE \\
\hline filled circle & CIRCLEFILLED & filled rectangle & RECTANGLEFILLED \\
\hline ellipse & ELLIPSE & triangle & TRIANGLE \\
\hline filled ellipse & ELLIPSEFILLED & filled triangle & TRIANGLEFILLED \\
\hline
\end{tabular}

A line stretching from \([0,0\) ] to \([1,1]\) in grey colour (RGB values \(0.5,0.5,0.5\) ) for example is represented as follows:
\(\operatorname{LINE}(0,0,1,1,[0.5,0.5,0.5])\)
A PLOT structure can be created with the gdi.structure function that optionally accepts the minimum number of entries (for speed).
```

> import gdi alias;
> s := structure();

```

Any geometric objects is inserted into the structure with its respective gdi.set* function. The line \(\operatorname{LINE}(0,0,1,1,[0.5,0.5,0.5])\) for example is added with the gdi.setline function:
```

> setline(s, 0, 0, 1, 1, [0.5, 0.5, 0.5]);

```

A PLOT structure can include any number of objects:
```

> setcircle(s, 0, 0, 0.5, [1, 0, 0]);

```

Finally, the plot statement puts them onto the screen:
```

> plot(s);

```

The following table shows the various functions to create objects:
\begin{tabular}{|l|l|l|l|l|l|}
\hline Object & Function & Object & Function & Object & Function \\
\hline arc & setarc & ellipse & setellipse & rectangle & setrectangle \\
\hline \begin{tabular}{l} 
filled \\
arc
\end{tabular} & setarcfilled & \begin{tabular}{l} 
filled \\
ellipse
\end{tabular} & \begin{tabular}{l} 
setellipse- \\
filled
\end{tabular} & \begin{tabular}{l} 
filled \\
rectangle
\end{tabular} & \begin{tabular}{l} 
setrectangle- \\
filled
\end{tabular} \\
\hline circle & setcircle & line & setline & triangle & settriangle \\
\hline \begin{tabular}{l} 
filled \\
circle
\end{tabular} & \begin{tabular}{l} 
setcircle- \\
filled
\end{tabular} & point & setpoint & \begin{tabular}{l} 
filled \\
triangle
\end{tabular} & \begin{tabular}{l} 
settriangle- \\
filled
\end{tabular} \\
\hline
\end{tabular}

\subsection*{15.1.8 Colours, Part 2}

The following colour names (of type string) are built in and are accepted by the gdi.plot and gdi.plotfn functions only, so that you must not define colours with gdi.useink or gdi.ink when plotting sets of points or graphs of functions:
```

'aquamarine', 'black', 'blue', 'bordeaux', 'brown', 'coral', 'cyan',
'darkblue', 'darkcyan', 'darkgrey', 'gold', 'green', 'grey', 'khaki',
'lightgrey','magenta', 'maroon', 'navy', 'orange', 'pink', 'plum', 'red',
'sienna', 'skyblue', 'tan', 'turquoise', 'violet', 'wheat', 'white',
'yellow', 'yellow2'.

```

\subsection*{15.1.9 GDI Functions}
gdi.arc (d, x, y, r1, r2, a1, a2 [, colour])
Draws an arc around the centre \([\mathrm{x}, \mathrm{y}\) ] with x radius \(\mathrm{r} 1, \mathrm{y}\) radius r 2 , and the starting and ending angles a1, a2, given in degrees [0 .. 360], on device d. A colour (an integer, see Chapter 15.1.3), may be given optionally.
```

gdi.arcfilled (d, x, y, r1, r2, a1, a2 [, colour])

```

Draws a filled arc around the centre [ \(\mathrm{x}, \mathrm{y}\) ] with X radius \(\mathrm{r} 1, \mathrm{y}\) radius r 2 , and the starting and ending angles a1, a2, given in degrees [0..360], on device d. The arc is filled with either the default colour, or the one given by colour (an integer, see Chapter 15.1.3).
```

gdi.autoflush (d, state)

```

Sets the auto flush mode for device a to either true or false (second argument). If state is true (the default), then after each graphical operation the output is flushed so that it is immediately displayed.

This may decrease performance significantly with a large number of graphical operations - Sun Sparcs seem to be the only exceptions -, so it is advised to
1. set state to false right after opening device a before calling any other function that plots something,
2. call gdi.flush after the graphical operations have been completed,
3. set state to true thereafter.

\section*{gdi.background (d, c)}

Sets the background colour on device d. c must be a number determined by gdi.ink, see Chapter 15.1.3. Note that in Windows, the image is also cleared so that the background is properly displayed, whereas in UNIX, the image is not reset.
```

gdi.circle (d, x, y, r [, colour])

```

Draws a circle around the centre [ \(\mathrm{x}, \mathrm{y}\) ] with radius r , on device d. A colour (an integer, see Chapter 15.1.3), may be given optionally.
```

gdi.circlefilled (d, x, y, r [, colour])

```

Draws a filled circle around the centre [ \(\mathrm{x}, \mathrm{y}\) ] with radius r , on device d. The circle is filled with either the default colour, or the one given by colour (an integer, see Chapter 15.1.3).
```

gdi.clearpalette (d)

```

Removes all inks on device d.
```

gdi.close (d)

```

Closes the window or file referred to by device id d. If d points to a file, all image contents is saved to it.
```

gdi.dash (d, s)

```

Sets the line dash on device id d. The sequence s includes a vector of dash lengths (black, white, black, ...). If \(s\) is the empty sequence, a solid line is restored.
```

gdi.ellipse (d, x, y, r1, r2 [, colour])

```

Draws an ellipse around the centre \([\mathrm{x}, \mathrm{y}\) ] with x radius r 1 , and y radius r 2 , on device d. A colour (an integer, see Chapter 15.1.3), may be given optionally.
```

gdi.ellipsefilled (d, x, y, r1, r2 [, colour])

```

Draws a filled ellipse around the centre \([x, y\) ] with \(x\) radius \(r 1\), and \(y\) radius \(r 2\), on device d. The ellipse is filled with either the default colour, or the one given by colour (an integer, see Chapter 15.1.3).
```

gdi.flush (d)

```

Writes all buffered contents to the window or file referred to by device id d .
See also: gdi.autoflush.
```

gdi.fontsize (d, s)

```

Sets the font size s for text written by gdi.text, for device d.
See also: gdi.text.
```

gdi.hasoption (t, o)

```

Iterates a table \(t\) and returns true if one of its keys is equal to o.

See also: gdi.options.
```

gdi.initpalette (d)

```

Sets up basic colours on device d.
gdi.ink (d, r, g, b)
Returns a palette colour value - an integer - for the colour given by its RGB values \(r\) (red), g (green), and b (blue), for device d. \(r\), \(g\), and b must be numbers \(x\) with \(0 \leq x\) \(\leq 1\). The palette colour value can be given as an optional argument in most of the gdi functions, or be used in the gdi.useink function. Subsequent calls with the same arguments return different palette values.
gdi.lastaccessed ()
Returns the id of the last accessed device as a number.
```

gdi.line (d, x1, y1, x2, y2 [, colour])

```

Draws a line from the first point \([x 1, y 1]\) to the second point \([x 2, y 2]\) on device d. A colour, an integer (see Chapter 15.1.3), may be given optionally.
```

gdi.lineplot (p [, options])
gdi.lineplot ([ p1 [, p2, \cdots.] ], [, options])

```

Takes one or more tables or sequences consisting of points \(x_{k}: y_{k}\) and generates a plot with all points connected by lines. \(x_{k}\) and \(y_{k}\) must be finite numbers. The function automatically determines the common proper borders automatically.

For more information see: gdi.pointplot, as gdi.lineplot is just a wrapper for the former with the 'connect' option set to true.
```

gdi.mouse (d [, offset])

```

Returns three numbers: the current horizontal and vertical positions of the mouse relative to the screen, and its button state button_state. The button state is coded as a positive integer.

By applying a bitmask to the button state, you can query whether the left or the right mouse button has been pressed:
- button_state \(\& \& 0 \times 0100=0 \times 0100\) : left button has been pressed,
- button_state \(\& \& 0 \times 0400=0 \times 0400\) : right button has been pressed.
```

gdi.open (width, height)
gdi.open (width, height, filename)

```

In the first form, opens a window with the given width and height and returns a device number (an integer) for later reference needed by all other gdi functions.

In the second form, creates the image file with name filename, the given width and height and returns a device number (an integer) for later reference needed by all other gdi functions.

The type of the image file format is determined by the suffix in filename:
\begin{tabular}{|l|l|l|}
\hline Suffix & Resulting image file format & Example \\
\hline .fig & FIG format & '/export/home/misc/fern.fig' \\
\hline .gif & GIF format & 'c:/images/fractal.gif' \\
\hline .jpg & JPEG format & 'c:/images/fractal.jpg' \\
\hline .png & PNG format & 'c:/images/circle.png' \\
\hline .ps & PostScript format (DIN A4 size) & 'output.ps' \\
\hline
\end{tabular}
```

gdi.options (...)

```

Checks the given plotting options for correctness and returns them in a new table, along with the defaults for options that have not been passed to this function. The function currently only works with the gdi.plot, gdi.pointplot, and gdi.plotfn functions.

Valid options (all key~value pairs) are:
\begin{tabular}{|c|c|c|}
\hline Option (key) & Meaning (value) & Example \\
\hline 'axes' & \begin{tabular}{l}
' none ' - do not print axes \\
'normal' - print axes with labels and tick marks \\
'boxed' - print axes at top and bottom, and at the left and the right side \\
'frame ' - print axes at the bottom and at the left side
\end{tabular} & 'axes':'normal' \\
\hline 'axescolour' & defines the colour of the axes (a colour string, see Chapter 15.1.3) & 'axescolour':'red' \\
\hline 'bgcolour' & sets the background colour (a colour string, see Chapter 15.1.3) & \[
\begin{aligned}
& \text { 'bgcolour': } \\
& \text { 'yellow }
\end{aligned}
\] \\
\hline 'colour' & sets the default colour (a string, see Chapter 15.1.3) for the objects to be plotted. Note that the individual colour of an object overrides the one given by this option & 'colour':'navy' \\
\hline 'colourfn' & sets a colouring function & \[
\begin{gathered}
\text { 'colourfn': } \\
\ll x->\text {. } . \text { >> }
\end{gathered}
\] \\
\hline 'file' & indicates the name of the file (a string) to be created & 'file':'image.png' \\
\hline 'labels' & if set to false, no labels are printed (default is true) & 'labels':false \\
\hline 'labelsize' & sets the font size (a positive number) for axis labels (gdi.plotfn function only) & 'labelsize':6 \\
\hline 'linestyle' & sets the dash style (a positive number) for the graph to be plotted (gdi.plotfn, gdi.lineplot, and gdi.pointplot functions only) & 'linestyle':10 \\
\hline 'maxtickmarks' & sets the maximum number of tickmarks on both axes, by default is (around) 20. & 'maxtickmarks':5 \\
\hline 'mouse' & prints the current position of the mouse to the console. Click the right mouse button to finish. Default is false. & 'mouse':true \\
\hline 'res' & resolution of the window or image file in pixels (pair of numbers) & 'res':(1024:768) \\
\hline 'square' & in a plot, uses the same scale for the y-axis as given for the x-axis & 'square':true \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Option (key) & Meaning (value) & Example \\
\hline 'thickness' & \begin{tabular}{l} 
sets the thickness (a positive number) of \\
the line to be plotted (gdi.plotfn, \\
gdi.lineplot, and gdi.pointplot functions \\
only)
\end{tabular} & 'thickness':2 \\
\hline 'title' & \begin{tabular}{l} 
sets the title (a string) for the plot \\
(gdi.plotfn function only)
\end{tabular} & \begin{tabular}{l} 
'title': \\
'Graph of sin(x) '
\end{tabular} \\
\hline 'titlecolour' & \begin{tabular}{l} 
sets the colour (a string, see Chapter \\
\(15.1 .3) ~ o f ~ t h e ~ t i t l e ~(g d i . p l o t f n ~ o n l y) ~\)
\end{tabular} & \begin{tabular}{l} 
'titlecolour': \\
'red'
\end{tabular} \\
\hline 'titlesize' & \begin{tabular}{l} 
sets the font size (a positive number) of \\
the title (gdi.plotfn function only)
\end{tabular} & 'titlesize':15 \\
\hline 'x' & \begin{tabular}{l} 
horizontal range (left and right border) \\
over which the plot is displayed
\end{tabular} & 'x':(-2):2 \\
\hline 'y' & \begin{tabular}{l} 
vertical range (lower and upper border) \\
over which the plot is displayed
\end{tabular} & 'y':0:5 \\
\hline 'xscale' & \begin{tabular}{l} 
sets the step size for the tick marks on the \\
horizontal axis
\end{tabular} & 'xscale':0.5 \\
\hline 'yscale' & \begin{tabular}{l} 
sets the step size for the tick marks on the \\
vertical axis
\end{tabular} & 'yscale':0.5 \\
\hline
\end{tabular}

The function is written in Agena and included in the lib/gdi.agn file.
See also: gdi.setoptions.
```

gdi.plot (p [, options])

```

Plots PLOT structures stored in p. PLOT structures are points, lines, circles, triangles, rectangles, arcs, and ellipses, along with the information given by its optional INFO structure.

A PLOT structure is created by a call to gdi.structure, and the respective gdi.set* functions.

The function accepts all plot options (see gdi.options).
Example:
```

> p := gdi.structure();
> gdi.setline(p, 0, 0, 1, 1, 'navy');
> gdi.setcircle(p, 0, 0, 1, 'red');
> gdi.plot(p);
> gdi.plot(p, axes='normal', square=true, x=-2:2, y=-2:2);

```

The function is written in Agena and included in the lib/gdi.agn file.
```

gdi.plotfn (f, a, b [ [ c, d], options])
gdi.plotfn (ft, a, b [ [ c, d], options])

```

Plots graphs of one or more functions, with a straight line drawn between neighbouring points, which are automatically computed.

In the first form, the graph of the function \(£\) is plotted.
In the second form, by passing a table ft of functions, the graphs of the functions are plotted on one device - to one file or window.

If the file option is missing, the graphs are plotted in a window (UNIX/Mac and Windows, only). If the file option is given, the file type is determined by the suffix of the file you pass to this option.
a and \(b\) (both numbers with \(a<b\) ) must be given explicitly and specify the horizontal range. If \(c\) and \(d\) are missing, the vertical range is determined automatically.

You may specify one or more options for proper layout of the graphs. See gdi.options for more details.

If a table of function is passed, you may specify an individual colour, line style, and the thickness for each of their graphs. Just pass a table of settings at the right-hand side of the respective option. See the examples below.

See gdi.autoflush if you experience performance problems while plotting.

\section*{Examples:}

Plot the graph of the sine function on the horizontal range a to b . The vertical range is computed automatically.
```

> import gdi;
> gdi.plotfn(<< x -> sin(x) >>, -10, 10);

```

Plot the graph of the sine function on the horizontal range a to b and the vertical range cto d.
```

> gdi.plotfn(<< x -> sin(x) >>, -10, 10, -2, 2);

```

Specify a colour other than black:
```

> gdi.plotfn(<< x -> sin(x) >>, -10, 10, colour='red');

```

Give a specific thickness for the line:
```

> gdi.plotfn(<< x -> sin(x) >>, -10, 10, thickness=3);

```

Combine the options - their order does not matter:
```

> gdi.plotfn(<< x -> sin(x) >>, -10, 10, thickness=3, colour='red');

```

Plot two and more functions:
```

> gdi.plotfn([<< x -> sin(x) >>, << x -> cos(x) >>], -10, 10);

```

Give options, too:
```

> gdi.plotfn([<< x -> sin(x) >>, << x -> cos(x) >>], -10, 10,
> colour='navy');

```

Specify individual colours. The graph of the sine function shall be red, the cosine function shall by cyan:

```

>gdi.plotfn([<< x - > Sin(x) >>, << x -> cos(x) >> ], -10, 10,
> colour=['red', 'cyan']);

```

Choose another colour for the axes and another axes style:
```

>gdi.plotfn([<< x -> sin(x) >>, << x -> cos(x) >> ], -10, 10,
> colour=['red', 'cyan'], axescolour='grey', axes='boxed'
> res=480:200);

```

Do not draw axes:
```

> gdi.plotfn([<< x -> sin(x) >>, << x -> cos(x) >>], -10, 10,
> colour=['red', 'cyan'], axes='none');

```

If you want to set default options that will always be used by plotfn and that do not need to be specified with each call to plotfn, use gdi.setoptions:
```

> gdi.setoptions(colour='red', axescolour='grey');
> gdi.plotfn([<< x -> sin(x) >>, << x -> cos(x) >>], -10, 10)

```

The function is written in Agena and included in the lib/gdi.agn file.
See also: calc.clampedspline, calc.nakspline.
```

gdi.point (d, x, y [, colour])

```

Plots a point with co-ordinates [x, y] on device d. A colour, an integer (see Chapter 15.1.3), may be given optionally.
gdi.pointplot (p [, options])
gdi.pointplot ([ p1 [, p2, ...] ], [, options])
Takes one or more tables or sequences consisting of points \(x_{k}: y_{k}\) and generates a plot with no points connected by lines. \(x_{k}\) and \(y_{k}\) must be finite numbers. The function automatically determines the common proper borders automatically.

By passing the option colour \(=\mathrm{c}\), where c is either a string denoting a colour, or a table of strings denoting colours, you can set individual colours for the distributions. The default is 'black'.

By passing the option symbol=s, where \(s\) is the name of a symbol or a table of strings denoting symbols, each point in a distribution is plotted accordingly. Supported symbols are: 'cross', 'circle', 'circlefilled', 'box', 'boxfilled', 'triangle', 'trianglefilled', 'crosscircle', and 'dot'. The default is 'dot'.

The size of the symbols can be controlled by the symbolsize option which denotes a radius in pixels. Only one common size can be set for all distributions passed. The default is 3 .

Alternatively, by passing the connect=true option, you can connect all points in each distribution with a line.

The function supports various plotting options, see gdi.options.

In the first form, only one distribution \(p\) is passed, in the second form you can pass various distributions p1, p2, etc. by putting them into a table.

The function ignores y-values if they evaluate to infinity or undefined.
Example:
```

> s := seq(0.1, 0.2, 0.1, 0.3, 1, 2, 5, -1, 0);
> p := sequences.new( << x -> x:s[x] >>, 1, size s);
> s1 := << x -> ln(x) >> @ s;
> p1 := sequences.new( << x -> x:s1[x] >>, 1, size s1);
> gdi.pointplot([p, p1], colour=['red', 'black'],
> symbol=['circle', 'cross'], symbolsize=5, connect=true);

```

The function is written in Agena and included in the lib/gdi.agn file.
See also: gdi.lineplot.
```

gdi.rectangle (d, x1, y1, x2, y2 [, colour])

```

Draws a rectangle with the lower left and upper right corners [x1, y1] and [x2, y2] on device d. A colour (an integer, see Chapter 15.1.3), may be given optionally for the lines.
```

gdi.rectanglefilled (d, x1, y1, x2, y2 [, colour])

```

Draws a filled rectangle with the lower left and upper right corners [x1, y1] and [x2, y2] on device d. The rectangle is filled with either the default colour, or the one given by colour (an integer, see Chapter 15.1.3).
gdi.reset (d)
Clears the entire window or image file contents of device \(d\).
```

gdi.resetpalette (d)

```

Clears the colour palette by removing all inks and reallocates basic colours, on device d.
```

gdi.setarc (s, x, y, r1, r2, a1, a2 [, colour [, thickness]])

```

Inserts an arc around the centre \([\mathrm{x}, \mathrm{y}\) ] with x radius \(\mathrm{r} 1, \mathrm{y}\) radius r 2 , and the starting and ending angles a1, a2, given in degrees [0 .. 360], to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1. thickness is the thickness of the arc, with 1 its default.
```

gdi.setarcfilled (s, x, y, r1, r2, a1, a2 [, colour])

```

Inserts a filled arc around the centre [ \(\mathrm{x}, \mathrm{y}\) ] with x radius \(\mathrm{r} 1, \mathrm{y}\) radius r 2 , and the starting and ending angles a1, a2, given in degrees [0 .. 360], to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black ', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1.
```

gdi.setcircle (s, x, y, r [, colour [, thickness]])

```

Inserts a circle around the centre \([x, y\) ] with radius \(r\), to PLOT structure \(s\). The optional colour argument may be either a string denoting a colour like 'black ', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1 . thickness is the thickness of the circle, with 1 its default.
```

gdi.setcirclefilled (s, x, y, r [, colour])

```

Inserts a filled circle around the centre \([x, y\) ] with radius \(r\), to PLOT structure \(s\). The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1.
```

gdi.setellipse (s, x, y, r1, r2 [, colour [, thickness]])

```

Inserts an ellipse around the centre [ \(\mathrm{x}, \mathrm{y}\) ] with x radius r 1 , and y radius r 2 , to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1. thickness is the thickness of the ellipse, with 1 its default.
```

gdi.setellipsefilled (s, x, y, r1, r2 [, colour])

```

Inserts a filled ellipse around the centre \([\mathrm{x}, \mathrm{y}\) ] with x radius r 1 , and y radius r 2 , to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1 .
gdi.setinfo (s, ...)
Inserts information on the minimum and maximum values ( \(x\) - and \(y\) values) and their scaling of all the geometric objects included in the PLOT data structure s into its INFO substructure. The INFO object always is the last element in s.

The options xdim=a:b and ydim=c:d set the \(x\)-range and \(y\)-range on which objects will be plotted, respectively, where \(a, b, c, d\) are numbers (i.e. borders). The square \(=\) true option scales the \(x\) and \(y\) dimensions equally, the square \(=\) false does not.

The information is useful so that gdi.plot can automatically determine the proper plotting ranges for s .

Example:
```

> gdi.setinfo(s, xdim = 0:10, ydim = -5:5, square = false);

```
gdi.setline (s, x1, y1, x2, y2 [, colour [, thickness]])
Inserts a line drawn from point \((x 1, y 1)\) to point \((x 2, y 2)\) with the optional colour into the PLOT structure s. x1, y1, x2, y2 should be numbers. colour may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1 . thickness is the thickness of the line, with 1 its default.
```

gdi.setoptions (...)

```

Checks the given plotting options (all key~value pairs) for correctness and sets them as the respective defaults for subsequent calls to the gdi.plot and gdi.plotfn functions.

For a list of valid plotting options, see gdi.options.
Internally, the function assigns the given options to the global environment variable environ.gdidefaultoptions which is checked by gdi.plot and gdi.plotfn.
```

gdi.setpoint (s, x, y [, colour])

```

Inserts a point with co-ordinates [x, y] to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1.
gdi.setrectangle (s, x1, y1, x2, y2 [, colour [, thickness]])
Inserts a rectangle with the lower left and upper right corners [x1, y1] and [x2, y2] to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1 . thickness is the thickness of the arc, with 1 its default.
gdi.setrectanglefilled (s, x1, y1, x2, y2 [, colour])
Inserts a filled rectangle with the lower left and upper right corners [x1, y1] and [x2, y2] to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1.
gdi.settriangle (s, x1, y1, x2, y2, x3, y3 [, colour [, thickness]])
Inserts a triangle with the corners [x1, y1], [x2, y2], and [x3, y3] to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1. thickness is the thickness of the arc, with 1 its default.
```

gdi.settrianglefilled (s, x1, y1, x2, y2, x3, y3 [, colour])

```

Inserts a filled triangle with the corners [x1, y1], [x2, y2], and [x3, y3] to PLOT structure s. The optional colour argument may be either a string denoting a colour like 'black ', 'red', etc., or a table with three RGB numeric values in the range 0 .. 1.
gdi.structure ([n])
Creates a PLOT data structure with n pre-allocated entries. Of course, the structure may contain less or more entries. If \(n\) is not given, no pre-allocation is done which may slow down inserting new objects into s later in a session. The return is the PLOT data structure (a sequence of user type 'PLOT').

See also: gdi.setinfo.
gdi.system (d, x, y, xs, ys)
Sets the user's co-ordinate system on device \(d\), where \(x, y, x s\), and \(y\) s are numbers. The pixel \([x, y]\) determines the origin. The horizontal unit is given in xs pixels, the vertical unit in ys pixels. The function returns nothing.
```

> d := open(640, 480);
> gdi.system(d, 320, 240, 320, 240);
> gdi.line(d, -1, 0, 1, 0);
> gdi.line(d, 0, -1, 0, 1);

```
```

gdi.text (d, x, y, str [, colour])

```

Prints the string str at [x,y] on device d. A text colour (an integer), may be given optionally.

See also: gdi.fontsize.
```

gdi.thickness (d, t)

```

Sets the default thickness for all lines to t pixels, on device d.
```

gdi.triangle (d, x1, y1, x2, y2, x3, y3 [, colour [, thickness]])

```

Draws a triangle with the corners [x1, y1], \([x 2, y 2]\), and \([x 3, y 3]\) on device \(d\). A colour (an integer, see Chapter 15.1.3), may be given optionally for the lines. thickness is the thickness of the triangle, with 1 its default.
gdi.trianglefilled (d, x1, y1, x2, y2, \(x 3, y 3\) [, colour])
Draws a filled triangle with the corners \([x 1, y 1],[x 2, y 2]\), and \([x 3, y 3]\) on device d. The triangle is filled with either the default colour, or the one given by colour (an integer, see Chapter 15.1.3).
```

gdi.useink (d, c)

```

Sets the default colour c (a number) for all subsequent drawings, on device d. c must be a number determined by gdi.ink.

\section*{15.2 fractals - Library to Create Fractals}

As a plus package, in Solaris, Linux, Mac OS X, and Windows, this library is not part of the standard distribution and must be activated with the import statement, e.g.
import fractals.
Since it needs gdi graphics functions, it is of no use in DOS. The OS/2 - ArcaOS version is still experimental. The package is not available in the 64-bit edition.

The library creates fractals and includes three types of functions:
1. escape-time iteration functions like fractals.mandel,
2. auxiliary mathematical functions lie fractals.flip,
3. fractals.draw to draw fractals using escape-time iteration functions.

See Chapter 15.2.3 for some examples.

\subsection*{15.2.1 Escape-time Iteration Functions}
```

fractals.amarkmandel (x, y, iter, radius)

```

This function computes the escape-time fractal created by Mark Peterson of the formula:
\[
z:=z^{2} * c^{0.1}+c
\]

It returns the number of iterations a point \([x, y]\) needs to escape radius. The maximum number of iterations conducted is given by iter.

See also: fractals.markmandel.
```

fractals.albea (x, y, iter, radius)

```

This function calculates the Julia set of the formula lambda * bea(z), where lambda is the point \(1!0.4\) and \(z=x!y\), and iter is the maximum number of iteration. Its return is the number of iterations the function needs to escape radius. The function is written in Agena (see lib/fractals.agn).

See also: fractals.lbea.
```

fractals.alcos (x, y, iter, radius)

```

This function calculates the Julia set of the formula lambda * \(\cos (z)\), where lambda is the point \(1!0.4\) and \(z=x!y\), and iter is the maximum number of iteration. Its return is the number of iterations the function needs to escape radius. The function is written in Agena (see lib/fractals.agn).
```

fractals.alcosxx (x, y, iter, radius)

```

This function calculates the Julia set of the formula lambda * cosxx(z), where lambda is the point \(1!0.4\) and \(z=x!y\), and iter is the maximum number of iteration. Its return is the number of iterations the function needs to escape radius. The function is written in Agena (see lib/fractals.agn).

The function implements FRACTINT's buggy \(\cos\) function till v16, and creates beautiful fractals.
```

fractals.alsin (x, y, iter, radius)

```

This function calculates the Julia set of the formula lambda * \(\sin (z)\), where lambda is the point 1!0.4 and \(z=x!y\), and iter is the maximum number of iteration. Its return is the number of iterations the function needs to escape radius. The function is written in Agena (see lib/fractals.agn).
```

fractals.anewton (x, y, iter, radius)

```

This function implements Newton's formula for finding the roots of \(z^{3}-1\), with \(z=x!y\), and returns the number of iterations it takes for an orbit to be captured by a root. The iteration formula itself is
\[
z:=z-\left(z^{3}-1\right) /\left(3 * z^{2}\right)
\]

The function stops if \(\left|z^{3}-1\right|\) < radius or the maximum number of iterations iter is reached. The function is written in Agena (see lib/fractals.agn).

See also: fractals.newton.
```

fractals.lbea (x, y, iter, radius)

```

This function calculates the Julia set of the formula lambda * bea(z), where lambda is the point \(1!0.4\) and \(z=x!y\), and iter is the maximum number of iteration. Its return is the number of iterations the function needs to escape radius. The function is implemented in C.

\section*{See also: fractals.albea.}
fractals.mandel (x, y, iter, radius)
This function computes the Mandelbrot set of the formula
\[
z:=z^{2}+c
\]
using complex arithmetic. It returns the number of iterations a point \([x, y\) ] needs to escape radius. The maximum number of iterations conducted is given by iter. The function is implemented in C .
```

fractals.mandelbrot (x, y, iter, radius)

```

Like fractals.mandel, but written in Agena and using complex arithmetic.
```

fractals.mandelbrotfast (x, y, iter, radius)

```

Like fractals.mandel, but written in Agena and using real arithmetic.
```

fractals.mandelbrottrig (x, y, iter, radius)

```

Like fractals.mandel, but written in Agena and using real arithmetic and trigonometric functions (see lib/fractals.agn).
fractals.markmandel (x, y, iter, radius)
Like fractals.amarkmandel, but implemented in C.
fractals.newton ( \(\mathbf{x}, \mathrm{y}\), iter, radius)
Like fractals.anewton, but implemented in C.

\subsection*{15.2.2 The Drawing Function fractals.draw}

The function takes an escape-time iterator, various other parameters, and creates either image files or windows of fractals. By default a window is opened (see file option on how to create image files).
fractals.draw (iterator, \(x_{\text {_centre, }}\) Y_centre, \(x_{\text {_width }}\) [, options])
Draws a fractal given by the escape-time iterator function iterator with image centre [x_centre, y_centre] and of the total length on the x-axis x_width. x_centre and \(y\) _centre are numbers whereas \(x\) _width is a positive number.

Options are:
\begin{tabular}{|c|c|c|}
\hline Option & Meaning & Example \\
\hline colour ~ f & a colouring function f of the form \(\mathrm{f}:=\) \(\ll x\)-> r, g, b \(\gg\). Predefined functions are: red, blue, violet, cyan, cyannew. & \begin{tabular}{l}
colour ~ \ll X -> \\
\(0,0,0.05 * x \gg\) \\
colour ~ blue
\end{tabular} \\
\hline file~'filename.suf' & creates a GIF, PNG, or JPEG file, if the file suffix is .gif, .png, or .jpg & file ~ 'mandel.gif' \\
\hline iter ~ n & maximum number of iterations with \(n\) a positive number; default is 128 & iter \(\sim 512\) \\
\hline lambda \(\sim \mathrm{p}\) & lambda value p, a complex number, for fractals.[a]|* functions like albea & lambda ~ 1 ! 0.4 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Option & Meaning & Example \\
\hline map ~ 'filename.map' & \begin{tabular}{l}
FRACTINT colour map to be used to draw the fractal. \\
The FRACTINT maps can be downloaded separately from: http://agena.sourceforge.net/ downloads.html\#fractintmaps \\
Put these files into the share folder of your Agena distribution, preserving the subfolder fractint. A valid path may thus be: /usr/agena/share/fractint. \\
Alternatively, set the environment variable environ.fractintcolourmaps to the folder where your map files reside.
\end{tabular} & map ~ 'basic.map' \\
\hline mouse ~ bool & display pointer co-ordinates on console after image has been finished, if bool = true. Default: bool = false. Click the right mouse button to quit printing co-ordinates. & mouse ~ true \\
\hline radius \(\sim\) r & iteration radius r, a positive number & radius \(\sim 2\) \\
\hline res ~ width:height & resolution of the window or image, with width and height positive numbers. Default is 640:480 & res \(\sim 1024: 768\) \\
\hline update \(\sim\) n & with \(n\) a non-negative number: determines the number of rows after an image is being flushed to a file or window during computation & \\
\hline
\end{tabular}

Notes on the update option:
On all operating systems the default is 1 . This behaviour can globally be changed in a session by assigning a non-negative integer to the environment variable environ.fractscreenupdates.

In Sun x86 Solaris and Linux, update \(\sim 0\) is the fastest, but when outputting to a window, it does not plot anything while the fractal is being computed (of course, if computation finishes, the fractal will be displayed).

Sparcs do not show any effect when changing the update rate, at least with XVR-1200 VGAs. The same applies to Microsoft Windows XP and 7, as well as Mac OS \(\times 10.5\).

\subsection*{15.2.3 Examples}
```

> import fractals alias
> draw(fractals.lbea, 1.75, 0.5, 0.001, map='grayish.map', radius=1024,
> iter=1024, lambda=1!0.4);

```


There are further examples at the bottom of the lib/fractals.agn file residing in the main Agena library folder.
```

> draw(mandel, -1.0037855135, 0.2770816775, 0.086686273, iter=255);
> draw(mandel, -1.0037855135, 0.2770816775, 0.086686273, file='out.png',
> iter=255, res=1024:768); \# create a PNG file of the Mandelbrot set

```

Chapter Sixteen
Utilities

\section*{16 Utilities}

\section*{16.1 utils - Utilities}

The utils package provides miscellaneous functions.
```

utils.calendar ([x])

```

Converts x seconds (an integer) elapsed since the beginning of an epoch to a table representing the respective calendar date in your local time. The table contains the following keys with the corresponding values:
- 'year' (integer)
- 'month' (integer)
- 'day' (integer)
- 'hour' (integer)
- 'min' (integer)
- 'sec' (integer)
- 'wday' (integer, day of the week)
- 'yday' (integer, day of the year)
- 'DST' (Boolean, is Daylight Saving Time)

If x is null or not specified, then the current system time will be returned. If x is invalid, the function will issue fail.

\section*{See also: os.now.}
```

utils.checkdate (obj)
utils.checkdate (year, month, day [, hour [, minute [, second]]])

```

In the first form, receives a date of the form year, month, date [, hour [, minute [, second]]], with these values in table or sequence obj being integers, and checks whether the given date and optionally time exists and returns true or false.

In the second form, receives the given integers, and conducts the same operation.
```

utils.decodea85 (str)

```

Decodes the ASClII85 encoded string str and returns the result as a string.
See also: utils.encodea85.
```

utils.decodeb64 (str)

```

Decodes the Base64 encoded string str and returns the result as a string.
See also: utils.encodeb64.
utils.decodeb85 (str [, option])
Decodes the Base85 Z85 encoded string str and returns the result as a string. If option is set to true, then the function determines which characters in str might be invalid. The default is false.

See also: utils.encodeb85.
utils.decodexml (str [, options])
Reads a string str containing an XML stream and converts it into a dictionary.
You can pass one or two options in any order:
If the Boolean option false is given, the function does not automatically try to convert strings representing numbers, complex numbers and the Booleans true, false, and fail into the proper Agena representation.

If the option ' nocomment ' is given, the function does not return XML comments.
The function provides some checking (basic syntax and balanced tags), and supports namespaces, XML and DOCTYPE declarations, comments and processing instructions. If a XML tag includes hyphens or colons, then they are converted to underscores in the corresponding Agena dictionary key.

Since the function does not return processing instructions, you may want to have a look at the auxiliary utils.aux.decoderawxml function included in the lib/library.agn file which returns a user-defined table containing processing instructions in the xarg tag.

The function is written in Agena and included in the libary.agn file.
Here is an example:
```

> xmlstr := '<?xml version="1.0"?>
> <Data>
<Name1>Agena</Name1>
<Name2>1</Name2>
<Name3>1.1</Name3>
<Name4>1.1+2.2*I</Name4>
</Data>
[Lang:Info-All](Lang:Info-All)
<Name action="interpret">Agena</Name>
<Version>1.6.1</Version>
</Lang:Info-All>
<!-- this is a comment -->
> <Motto>The Power of Procedural Programming</Motto>'
> utils.decodexml(xmlstr):
[Data ~ [Name1 ~ Agena, Name2 ~ 1, Name3 ~ 1.1, Name4 ~ 1.1+2.2*I],
Lang_Info_All ~ [Name ~ Agena, Version ~ 1.6.1], Motto ~ The Power of
Procedural Programming, header ~ <?xml version="1.0"?>]

```
```

> for i, j in ans do print(i, j) od
Lang_Info_All [Name ~ Agena, Version ~ 1.6.1]
Motto The Power of Procedural Programming
Data [Name1 ~ Agena, Name2 ~ 1, Name3 ~ 1.1, Name4 ~ 1.1+2.2*I]
header <?xml version="1.0"?>

```

The function is quite slow when parsing deeply nested XML structures, but it is more exact than xml.decodexml. If you need to parse only certain portions of an XML stream, just extract them from the string using the strings.match function before applying utils.decodexml.

See also: utils.encodexml, utils.readxml.
```

utils.encodea85 (str)

```

Encodes a string str into ASCll85 format and returns it as a string.
See also: utils.decodea85.
utils.encodeb64 (str)
Encodes a string str into Base64 format and returns it as a string.
See also: utils.decodeb64.
utils.encodeb85 (str)
Encodes a string str into Base85 \(Z 85\) format and returns it as a string.
See also: utils.decodeb85.
utils.encodexml (obj [, indent [, flag]])
Encodes a dictionary obj of the same format as created by utils.readxml into XML format.

If indent (a non-negative number) is not given the number of white space indentations is 3 .

If any value is given for flag , the return is a flat table of substrings, else the return is one concatenated string.

See also: utils.decodexml.
utils.findfiles (d, what [, options])
utils.findfiles (obj, what [, options])
Searches a single file - or searches a directory for all the files - that include a certain string or which satisfy a given condition.

In the first form, the directory to be searched is denoted by the first argument \(d\), \(a\) string, which may include file wildcards. a may also denote a single file. In the second form, obj is a table of a table with file names of type string, and the absolute path to the directory containing the given files. (os.list returns such a table.)

The second argument what can either be a string to be searched for, or a procedure of one argument that describes a satisfying condition and which should result in either true or false.

The returns are two lists: the first list includes all the names of the files where the search has been successful, and the second lists includes all files that could not be read due to errors, for example because of missing read permissions.

By default, the function searches all files line by line for a given search criterion. Pass the option 'whole' if the search criterion should be applied to the entire file, i.e. to search in the string concatenation of all the lines of a file, so that line breaks do not matter.

By passing the further option 'r', the function also searches recursively in all respective subfolders.

Options may be given in any order after the second argument what.

\section*{Examples:}
```

> utils.findfiles('*.c', '\#define'):
> utils.findfiles('*.c', << x -> '\#define' in x = 1 >>, 'whole'):
> utils.findfiles([['a.txt', 'b.txt'], 'c:/text'], 'hello'):

```

See also: io.infile, io.readfile.
```

utils.hexlify (str)

```

Converts a string str to its hexadecimal representation and returns a new string where each character in str is replaced by a two-digit hexadecimal value. The resulting string is twice as long as str.

See also: utils.unhexlify.
utils.posrelat (pos, len)
If pos represents a negative integer index, returns the respective positive index for the given number len of items in a structure, otherwise returns pos. The function is written in the Agena language and included in the lib/library.file.
utils.readcsv (filename [, options [, fn]])
Reads a comma-separated value (CSV) file and returns its contents in a sequence. The delimiter of the fields in a line by default is a semicolon.

If a line contains more than one field, then the respective fields are returned in a sequence \({ }^{29}\). If a line contains only one field, then it will be returned without including it in a sequence \({ }^{30}\). If a line contains nothing, i.e. ' \(\mid n\) ', it is by default ignored \({ }^{31}\).

Strings containing numbers are automatically converted to numbers.
Options can be passed as pairs:
\begin{tabular}{|c|c|c|}
\hline Left pair element & Right pair element & Example \\
\hline convert & true or false: If false, do not attempt to convert strings to numbers. Default: true. & convert = true \\
\hline comma & true or false: If a field contains a string recognised as a number by strings.iscenumeric decimal comma instead of a decimal dot - this option automatically transforms the value to an Agena number if the option evaluates to true. Default is false. This option is applied before checking for the 'convert' option. & comma = true \\
\hline delim & A string. Use this string as the delimiter instead of a semicolon which is the default. & delim = '|' \\
\hline dictionary & Returns a dictionary instead of a sequence with the dictionary keys defined by the values in the row passed with this new option, where the row can be depicted by a field number or field id (a string). The values in the `key` row should be unique. & \[
\begin{aligned}
& \text { dictionary = } 1 \\
& \text { dictionary = 'ID' }
\end{aligned}
\] \\
\hline
\end{tabular}

\footnotetext{
\({ }^{29}\) See the flat option to override this behaviour.
\({ }^{30}\) See the newseq option to override this behaviour.
\({ }^{31}\) See the skipemptylines option to override this behaviour.
}
\begin{tabular}{|c|c|c|}
\hline Left pair element & Right pair element & Example \\
\hline field & a positive integer: If given, only the given field in the CSV file is extracted, else all fields are returned. & field = \\
\hline fields & \begin{tabular}{l}
A table or sequence of positive integers. If given, only the fields given in this table or sequence are returned, and in the order of the elements in this table or sequence; if not given, all fields are returned. \\
If a CSV file contains a header, then column numbers or strings denoting the field name can be passed, and column numbers and field names can be mixed.
\end{tabular} & ```
fields = [3, 1, 5]
fields =
    ['name', 'phone']
fields =
    ['name', 2]
``` \\
\hline flat & true or false: If true, do not return values in each line in a new sequence. Default: false. & flat = true \\
\hline header & true or false: If true, ignore the very first line. Default: false. & header = true \\
\hline ignore & a procedure returning either true, false, or fail. If given, the procedure is applied to each line of the CSV file and if it evaluates to true, it does not process the line and proceeds with the next one. & ```
ignore =
    << x ->
        'text' in x
        <> null
    >>
``` \\
\hline ignorespaces & true or false: all spaces in a line are deleted before returning the fields. Default is false. & ignorespaces = true \\
\hline mapfields & \begin{tabular}{l}
A table or sequence of pairs of the form posint:procedure. Applies the given function to a specific field in the CSV file. \\
If a CSV file contains a header, then column numbers or strings denoting the field name can be passed along with the procedures, and column numbers and field names can be mixed.
\end{tabular} & ```
mapfields =
    [1:f, 3:g]
mapfields =
    ['name':f, 2:g]
``` \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Left pair element & Right pair element & Example \\
\hline newseq & true or false: if only one field, i.e. one value per line, is stored in the CSV file, always put this single value in each line into a new sequence (true), resulting in a sequence of sequences returned by readcsv; otherwise simply add it to the flat sequence returned by the function, which is the default (false). & newseq = true \\
\hline output & A string. If the right-hand side is 'record', then a dictionary will be returned, with its keys being defined by the tokens in the first line of the file (if the header=true option is also given), otherwise a table array will be returned. & output = 'record' \\
\hline remove & \begin{tabular}{l}
'quotes' or 'doublequotes', or both. \\
If 'quotes' is given, enclosing single quotes are removed from the CSV field. \\
If 'doublequotes' is given, enclosing double quotes are removed from the CSV field (the default, see removedoublequotes option to prevent this). You cannot remove both single and double quotes.
\end{tabular} & remove = 'quotes' \\
\hline removedoublequotes & If set to true, removes enclosing double quotes from a field if present (the default). If set to false, enclosing double quotes are not deleted. & \[
\begin{aligned}
& \text { removedoublequotes = } \\
& \text { false }
\end{aligned}
\] \\
\hline skipemptylines & true or false: If true, do not return empty lines. Default is true. & skipemptylines = true \\
\hline skipfaultylines & true or false; if set to true, ignores all lines in a CSV file that do not have the same number of fields as there are in the CSV header, or the first CSV line if a header is non-existent. Default is false. If set to true, the function also returns all skipped lines as a second result. & skipfaultylines = true \\
\hline skipspaces & true or false: If true, do not return lines consisting of spaces only. Default is false. & skipspaces = true \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Left pair element & Right pair element & Example \\
\hline subs & a pair, or a table or sequence of pairs \(x: y\). For each line read from the CSV file, replaces \(x\) with \(y\). If you pass a function as the last argument, substitution is done before finally mapping this function on the return. & \begin{tabular}{l}
subs = '':undefined \\
subs = ['':undefined, 'HUGE_VAL':infinity]
\end{tabular} \\
\hline
\end{tabular}

You may also optionally pass a function fn - at any position in the argument list - to be mapped on each value of the input to be returned, or mix options given as pairs and a function to be applied to each value to be returned, e.g.:
```

> L := utils.readcsv('data.dat', delim=' ', flat=true, << x -> x^2 >>);

```

The function is written in Agena and included in the libary.agn file.
See also: columns, descend, io.lines, io.readlines, utils.readxml, utils.writecsv, skycrane.readcsv.
utils.readini (filename [, options])
Reads a traditional initialisation file and returns its contents as a table. Initialisation files supported look like the following:
```


# 

# This is an example of an ini file

# 

; Pizzas
Taxi=Pizza Cab
Agena=
[Pizza] ; <- this is a section name
Ham = yes; <- and this is a key~value pair
Mushrooms = true ;
Capres = 0
Cheese = "Non" ;
Price = 3.99
Preis=3,99

```

A line beginning with a hash (\#), followed optionally by one or more characters, is completely ignored.

In a line, any text starting with a semicolon is also skipped. Key~value pairs may be separated by one or more white spaces.

The result is a table.

The file is parsed from top to bottom. As long as no section name has been given (here `[Pizza]'), any key~value pairs encountered are entered into the table as such.

If a section name is given, then a subtable of the form section \(\sim\) [key \(\sim\) value pairs] is stored to the resulting main table.

If a key is given, but now value, then the corresponding value will be the empty string. Values may also be enclosed in double quotes, but double quotes will be stripped of during import.

By default, any number values are automatically transformed to numbers, and the strings 'true', 'false', or 'fail' are converted to Booleans, and all other values are returned as strings. You may prevent any conversion by passing the convert=false Option.

If the option comma=true is given, then all floating point values containing a decimal comma are converted to a representation with a decimal dot. Default is comma=false.

The option sections=true reads only the section names in the ini file and returns them in the order of occurrence in a table array. Default is sections=false. The results of reading the above ini file will look as follows if no option is given:
```

[Agena ~ , Taxi ~ 'Pizza Cab', Pizza ~ [Capres ~ 0, Cheese ~ Non, Ham ~
yes, Mushrooms ~ true, Preis ~ 3,99, Price ~ 3.99]]

```

See also: utils.writeini.
utils.readxml (filename [, options])
Reads an XML file and returns its data in an Agena dictionary.
You can pass one or two options in any order:
If the Boolean option false is given, the function does not automatically try to convert strings representing numbers, complex numbers and the Booleans true, false, and fail into the proper Agena representation.

If the option ' nocomment ' is given, the function does not return XML comments.
For further information on how the function works, see utils.decodexml.

See also: utils.decodexml, utils.readcsv, xml.readxml.
utils.singlesubs (str, sp)
Substitutes individual characters in string str by corresponding replacements in sequence sp. The return is a new string. Note that the function tries to find a replacement for a single character in str by determining its integer ASCll value \(n\) and then accessing index \(n\) in sp. If an entry is found for index \(n\), then the character is replaced, otherwise the character remains unchanged.

For an example, check the strings.diamap procedure in the lib/library.agn file.
utils.speed ( n , f [, \(\cdot\) ] ])
Receives a positive integer \(n\), a function \(f\), and any optional arguments, and executes the function \(n\) times. The function returns the execution time in seconds.

If you want to check the speed of an operator, you have to enclose it in a function, e.g.:
> utils.speed(1k, << x -> sin x >>, 0):
See also: time.
utils.unhexlify (str)
Does the opposite of utils.hexlify.
utils.uuid ([x])
Creates a random version 4 universally unique identifier (UUID) by exclusively producing random numbers, and returns a string of 32 characters. If its argument x is null, the nil UUID will be returned (i.e. the template), otherwise, x has no effect.

See also: environ.ref, factory.count, math.random, sema.open.
utils.writecsv (obj, filename [, options])
Creates a comma-separated value (CSV) file. The function writes all values or keys and value(s) of a table, set, sequence or register obj to a text file given by filename. If obj includes a structure, then each element of the respective structure is written on the same line. Otherwise, each value or key ~ value pair is written on a separate line.

By default only values are written, the keys are ignored, but check the 'key' option below.

The following options can be passed as pairs:
\begin{tabular}{|l|l|l|}
\hline Left pair element & Right pair element & Example \\
\hline delim & \begin{tabular}{l} 
A string. Use this string as the \\
delimiter instead of a semicolon \\
which is the default.
\end{tabular} & delim = 'I' \\
\hline dot & \begin{tabular}{l} 
A single character of type string. \\
With numbers, a decimal dot is \\
replaces with the given character. \\
Default: no replacement.
\end{tabular} & dot \(=^{\prime} \prime^{\prime}\) \\
\hline enclose & \begin{tabular}{l} 
A string. Each value to be written is \\
enclosed with this string.
\end{tabular} & enclose = ' \(\backslash \prime^{\prime \prime}\) \\
\hline header & \begin{tabular}{l} 
A string written to the very first line. \\
Default: no header is written.
\end{tabular} & header = 'A;B;C' \\
\hline key & \begin{tabular}{l} 
A Boolean. If true, writes the \\
respective index of the structure at \\
the beginning of each line. Default: \\
false, i.e. indices are not written.
\end{tabular} & \\
\hline
\end{tabular}

The function returns nothing, is written in Agena and included in the lib/library.agn file.

Example:
```

> obj := seq(seq(1.1, 2, 3), seq(4, 5.1, 6), seq(7, 8, 9));
> utils.writecsv(obj, 'c:/out.csv', delim='|', dot=',');

```
creating a file with the contents:
```

1|1,1|2|3
2|4|5,1|6
3|7|8|9

```

See also: utils.readcsv, skycrane.readcsv.
utils.writeini (obj, filename [, options])
Creates a traditional initialisation file with name filename and writes a dictionary obj of key~value pairs to it. If values are not tables, they are written at the beginning of the file. If values are tables of key~value pairs, then they are written to the corresponding sections.

By default, the function writes the entries and sections in ascending order. You may change the order of the sections and the specific sections to be written by passing a table array of section names with the sections option, e.g. sections=['salad', 'Pizza'] first writes all entries of the Salad section, and then the Pizza section is written.

An optional spacer in front and behind the equals signs may be given by passing the spacer option which accepts any string, e.g. spacer=' \(\backslash t\) '. Default is the empty string.

A floating point value may be written with a decimal comma instead of a decimal dot by passing the comma=true option, default is comma=false.

The function returns nothing, is written in Agena and included in the lib/library.agn file.

See also: utils.readini
utils.writexml (obj, filename [, indent])
Creates an XML file with name filename from the dictionary obj which should be of the same format as the dictionary returned by utils.decodexml.

The function returns nothing, is written in Agena and included in the lib/library.agn file.

See also: utils.decodexml, utils.encodexml, utils.readxml.

\section*{16.2 skycrane - Auxiliary Functions}

As a plus package, the skycrane package is not part of the standard distribution and must be activated with the import statement, e.g. import skycrane.

The package contains functions that you might or might not find usefully.
```

skycrane.bagtable (o)

```

Creates a table of empty bags with its keys determined by the values in the sequence o. o may include values of any type. If o is empty, an error will be issued.

The function automatically loads the bags package if it has not yet been initialised.
The function is written in Agena and included in the lib/skycrane.agn file.
See also: bags.bag.
```

skycrane.dice ()

```

Returns random integers in the range [1 .. 6].
See also: math.random, math.randomseed.
```

skycrane.enclose (str [, d])

```

Encloses a string str with the given character or string d. If d is not given, the string is enclosed in double quotes. If str is a number, null or a Boolean, it is converted to a string before the operation starts. Otherwise it returns an error. It also returns an error if the optional second argument is not a string.

\section*{See also: skycrane.removedquotes.}
```

skycrane.fcopy (a, b [, verbose])

```

This function is an interface to os.fcopy but can also deal with directories. If \(a\) and \(b\) are file names, then the function works like os.fcopy. If b is a directory, then a is copied into it. If a is a directory, then all files in it are copied into b.

If verbose is true then the name of the file copied successfully is printed at stdout.
The function is written in Agena and included in the lib/skycrane.agn file.
See also: os.fcopy, skycrane.move.
skycrane.formatline (1 [, ...])
Similar to io.writeline, but all the strings, numbers or Booleans to be formatted must be passed in a table, sequence or register 1 . The function returns a string instead of writing the values to a file. The function accepts the following options:
- delim \(=\) <string \(>\)
the delimiter, a semicolon by default, can also be the empty string;
- enclose \(=<\) string \(>\)
each value will be enclosed by \(<\) string \(>\), double quotes by default, can also be the empty string.

\section*{Example:}
```

> skycrane.formatline([1, 'agena', true], delim = '|', enclose = '\''):
'1'|'agena'|'true'

```
skycrane.getlocales ()
Returns all locales available on your operating system. The return is a table with the keys being valid arguments to os.setlocale, and the entries the result of the respective call to os.setlocale.

The function is very, very slow, as os.setlocale is called around 460.000 times. In UNIX, it would be better to issue the command 'locale -a' in a shell to determine the locales supported on your system.

The function is written in Agena and included in the lib/skycrane.agn file.
See also: os.setlocale.
skycrane.isemail (str [, strict])
Checks whether a string str represents a valid E-mail address and returns true or false. The algorithm used does not cover all rules defined in RFC 3696, but should suffice with standard E-mail addresses of syntax "local-part@domain".

Note that the domain may not necessarily include a dot. You can override this rule by passing any non-null value for strict.
```

skycrane.iterate (o)

```

Returns an iterator function traversing a table, set, sequence or register o always in strict ascending order.

If \(\circ\) is a table, the function first sorts its keys and returns a function which if called, returns the table values of \(\circ\) in the ascending order of these sorted keys.

If \(\circ\) is a set, the function first sorts its entries and returns a function that if called, returns the elements one by one in ascending sorted order.

Although unnecessary: if o is a sequence or register, the function returns a function that if called, returns each value in o one by one in their original order.

The function is written in Agena and included in the lib/skycrane.agn file. For the order how keys or values will be sorted, see sorted.

A note: This function is utterly slow compared to the for/in statement. But there may be few situations demanding loops iterating in the strict ascending order of its (numeric or string) indices, or set, register, and sequence values.

See also: ipairs, next, sorted, factory.iterate, factory.count.
```

skycrane.move (a, b [, verbose])

```

This function is an interface to os.move but can also deal with directories. If a and \(b\) are file names, then the function works like os.move. If \(b\) is a directory, then \(a\) is moved into it. If a is a directory, then all files in it are moved into \(b\).

The function is written in Agena and included in the lib/skycrane.agn file.
If verbose is true then the file copied successfully moved is printed at stdout.
See also: os.move, skycrane.fcopy.
skycrane.readcsv (filename [, ...])
Like utils.readcsv, but with the following default options, which can be overridden:
convert=false, ignorespaces=false, remove='doublequotes'.
The function is written in Agena and included in the lib/skycrane.agn file.
```

skycrane.removedquotes (str)

```

Removes enclosing double quotes from the string str and returns the modified string. If \(s t r\) is not enclosed by double quotes, str will be returned unmodified.

See also: skycrane.enclose.
```

skycrane.replaceinfile (fn, oldstring, newstring [, true])
skycrane.replaceinfile (fn, subslist [, true])
In the first form, replaces all occurrences of string oldstring in file fn (a filename) in-place with string newstring. The function supports pattern matching.

```

In the second form, one or more substitutions can be given by passing a table or sequence sublist of pairs of the form oldstring : newstring.

By default, a backup of the file to be modified is created with the additional suffix ‘.bup`. You can suppress any backup by passing the Boolean value true as the very last argument.

The function is written in Agena and included in the lib/skycrane.agn file.
```

skycrane.scribe (fh, obj [, ...])
skycrane.scribe (obj [, ...])
skycrane.scribe (...)

```

Like io.write and io.writeline, but if a table, sequence or register obj is being passed, it writes the values in the structure to the file denoted by its handle fh (first form) or the console (second form) instead of throwing an exception. fh is a file handle, not a file name.

The values in the structure obj must either be numbers or strings.
The function accepts the following options of type pair:
- If the delim option (third to last argument) has been passed, all values are separated by the given string. Default is a semicolon. Examples: delim='। ': use a pipe instead of a semicolon, delim=' ' (i.e. the empty string): do not include a delimiter.
- If the newline or nl option has been passed, and if its value is false, then no newline is included after the elements have been written. (Include a trailing delimiter - if needed - by calling io.write.) Default is true. Example: newline=false.

If no structure has been passed (third form), the function just behaves like io.write or io.writeline.

Examples:
```

> import skycrane;
> skycrane.scribe('men ne cunnon hwyder helrunan hwyrftum scribað'):
men ne cunnon hwyder helrunan hwyrftum scripað
> fd := io.open('Depeche Mode','wb');
> skycrane.scribe(fd,
> 'Enjoy the silence,
> words are very unnecessary,
> they can only do harm.');
> io.close(fd);

```
```

> fd := io.open('c:/wulfila.txt', 'w');
> paternoster 32 := (/
> atta unsar pu in himinam
weihnai namo pein
qimai piudinassus peins
wairpai wilja peins
swe in himina jah ana airpai
hlaif unsarana pana sinteinan
gif uns himma daga \);
> skycrane.scribe(fd, paternoster, delim = ' ');
> io.close(fd);

```

The function is written in Agena and included in the lib/skycrane.agn file.

\section*{See also: print, printf, io.write, io.writeline, skycrane.tee.}
```

skycrane.sorted (obj [, f])

```

Sorts a table, sequence or register obj non-destructively but contrary to sort and sorted can cope with structures including values of different types. First, numbers are sorted, then strings, the others are not. The function, however, is slower than sorted.

If f is given, then it must be a function that receives two structure elements, and returns true when the first is less than the second (so that not f (obj[i+1], obj[i]) will be true after the sort). If f is not given, then the standard operator < (less than) is used instead.

The function is written in Agena and included in the lib/skycrane.agn file.
See also: sort, sorted, stats.issorted, stats.sorted.
skycrane.stopwatch ()
Implements a stopwatch. Just follow the instructions when calling skycrane.stopwatch(). The function returns nothing.

The function is written in Agena and included in the lib/skycrane.agn file.
See also: watch.
```

skycrane.tee (fh, x [,..]] [, 'delim':str])
skycrane.tee (fh, x [,\cdots], 'format':str)

```

In the first form, the function writes one or more numbers or strings x to both the console (stdout), and a file denoted by its handle fh to the current working directory. By default, the values are separated with a tabulator ( \(\backslash t\) ). It finally puts a

\footnotetext{
\({ }^{32}\) Taken from the Gothic Language Wulfila Bible edited by Wilhelm Streitberg.
}
line feed at the end of the output. By passing the option 'delim':str, as the last argument, the delimiter is given by the string str.

In the second form, one or more numbers or strings \(x\) are written to both the console (stdout), and a file denoted by its handle fh to the current working directory. The resulting string is formatted according to the printf-like template information in str passed with the format option. See strings.format for more information on the template string. It does not put a line feed at the end of the output, but to do so, you may add a \(\backslash \mathrm{n}\) control character to the end of the format string.

The function returns nothing.
The function is written in Agena and included in the lib/skycrane.agn file.
See also: print, printf, skycrane.scribe.

\section*{skycrane.timestamp (ts [, options])}

Transforms the timestamp string ts of the format 'dD.Mm.yYYy hH:MM:SS' or 'YYYY.MM.DD hh:MM:SS' into a numeric Lotus Serial Date (LSD, a number) and optionally - the time in DMS notation (a number, see math.dms for details).
ts does not need to include the number of minutes, hours and seconds. In this case, the missing digits are replaces by zeros. In ts, year and day may be swapped, and the month, day, hour, minute and second may be single integers, thus not necessarily preceded by a zero. Seconds can include fractional milliseconds.

If the option splitup=true is being passed, the function also returns the LSD as a string with a comma as the decimal separator, plus six integers depicting year, month, day, hour, minute and second. See third example below.

The function by default returns the time in Daylight Saving Time if active. You can switch this off (always returning Standard Time) by passing the option standardtime=true.

The delimiter in ts which separates year, month, day, a dot by default, can be changed to another delimiter by passing the datedelim=<any character> option, see example below.

The delimiter in ts which separates hour, minute and second, a colon by default, can be changed to another delimiter by passing the timedelim=<any character> option.

The delimiter in ts which separates date and time, a space by default, can be changed to another delimiter by passing the datetimedelim=<any character> option.

Optional delimiters may be preceded by a backslash so that the function can parse ts successfully.
```

> skycrane.timestamp('31.12.2017 23:59:01', datedelim='\.'):
43100.99931713 23.5901
> skycrane.timestamp('01/02/2017 23:59:01', datedelim='\/'):
42767.99931713 23.5901
> skycrane.timestamp('31-12-2017', datedelim='-'):
43100 0
> skycrane.timestamp('2017.2.1 23:59:01.999',
> datedelim='\.', splitup=true):
42767.99931713 23.5901 42767,99931713 2017 2 1 1 23 59 1.999

```

The function is written in Agena and included in the lib/skycrane.agn file.
See also: math.dms, os.Isd, skycrane.tocomma, skycrane.todate.

\section*{skycrane.tocomma (x)}

If \(x\) is a number, the function converts \(x\) to a string. If \(x\) is a float (containing \(a\) decimal dot), the dot is replaced by a comma. If \(x\) is a string and represents an integer or float, an optional decimal-dot is replaced by a comma.

The return is a string.
```

skycrane.todate (x)

```

Returns the calendar date and time represented by the number \(x\), which should hold the number of seconds (and optionally milliseconds) elapsed since the start of the given epoch. The return is a string of the format `YYYY/MM/DD \(\mathrm{hh}: \mathrm{mm}: \mathrm{ss}\) `.

If no argument is given, the current system date and time will be returned. You may pass an optional format string if you prefer another representation of the date and time.

See also: strings.format, os.now, os.time, skycrane.timestamp.
```

skycrane.tolerance (x, a)

```

Returns math.branch(ceil(a* \(\log 10(x+1)-1))\), a maximum tolerance value especially suited for comparing similar strings where \(x\) may denote the size of a string. A good value for a might be a number greater than 3 .

See also: strings.dleven, strings.diffs, strings.fuzzy.

\section*{skycrane.trimpath (str)}

Converts backslashes in the string str to slashes and then removes, if existing, one trailing slash, and returns the modified string. If str does not include backslashes or trailing slashes/backslashes, str will be returned unmodified.
skycrane.xmlmatch (str, tag [, \(\left.\operatorname{tag}_{2}, \cdots\right]\) )
Like strings.match, but returns the contents of the string str enclosed by the given XML search tag '<tag \(>(.-)</\) tag \(>\) '. If further tags \(\operatorname{tag}_{2}\).. tagk are given, then the
 be converted to a string before matching. If any tag is not a string or number, it will be ignored.

The function returns null if any tag could not be found.

Examples:
```

> data := '<data>
<name>abc</name>
<info>
<name>def</name>
</info>
</data>'
> skycrane.xmlmatch(data, 'name'):
abc
> skycrane.xmlmatch(data, 'info', 'name'):
def

```

\section*{16.3 factory - Iterators}

As a plus package, the factory package is not part of the standard distribution and must be activated with the import statement, i.e. import factory.

The package provides functional programming-style iterators.
factory. count ([start [, step [, stop [, method]]]])
Returns an iterator function that, each time it is called, returns a new number.
If no argument is given, the first number returned by the iterator is 0 , the next call returns 1, the next one 2, and so forth. This means that the number returned with each call is increased by 1.

If only start is given, the first number returned by the iterator is start, the next call returns start +1 , the next one start +2 , and so forth. This means that the number returned with each call is increased by 1 .

If start and step are given, the first number returned by the iterator is start, the next call returns start + step, the next one start \(+2{ }^{*}\) step, and so forth. This means that the number returned with each call is increased by step, which may be negative. In the latter case the next number returned will be less than the current returned number.

If stop is given, the iterator returns null if the counter value exceeds stop. Default is + infinity.

If start or step are not numbers, the factory issues an error.
If start or step is a non-integer, the function by default automatically applies Kahan-Babuška summation to avoid round-off errors. You can choose between the following summation methods:
\begin{tabular}{|l|l|}
\hline method & algorithm \\
\hline 'babuska' & Kahan-Babuška summation, highest accuracy but slowest (default) \\
\hline 'kbn' & \begin{tabular}{l} 
Kahan-Babuška-Neumaier compensated summation, used in the \\
Julia programming language
\end{tabular} \\
\hline 'neumaier' & Neumaier summation, good accuracy and performance \\
\hline 'ozawa' & Kahan-Ozawa summation \\
\hline
\end{tabular}

The generator automatically adds hEps to the stop value to avoid the iterator from leaving prematurely. If the absolute value of the step size is less than or equal to hEps, the generator will issue an error. You can entirely switch off this feature by setting math.Eps to zero, but only by calling environ.kernel:
```

> environ.kernel(hEps = 0);

```

The current setting of hEps can be queried by:
```

> environ.kernel('hEps'):
0

```

Note that hEps also controls numeric for loops with fractional step sizes. You might want to reset its value after generating the iterator to its default.

Example:
```

> import factory;
> f := factory.count(1, -0.1, -1, 'ozawa'); \# count down
> while c := f() do print(c) od;

```

See also: factory.reset, math.accu, skycrane.iterate, utils.uuid.
```

factory.cycle (obj [, firstkey [, sentinel]])

```

Like factory.iterate, but when sentinel is encountered during traversal or the end of the structure has been reached, it does not return null but simply restarts iteration with the first element in obj.

See also: next, factory.reset.
factory.iterate (obj [, firstkey [, sentinel]])
Creates a function that when called, starting with index firstkey, iterates each element in a table, sequence or register obj, or each character in a string obj one by one, returning the respective index and value as two results.
firstkey and sentinel by default are null. With tables, firstkey may be any value and should be null if the table is to be iterated from its beginning. With any other data type, firstkey is a positive integer. If sentinel is encountered during traversal, the iterator returns null.

If there is nothing left, the function returns null and if called again re-starts iteration.
With strings, sequences and registers, if firstkey is out of range, the iterator simply returns null. With tables, if firstkey is a non-existent key, an error will be issued.

See also: next, factory.cycle, factory.reset, skycrane.iterate.

\section*{factory.reset (f, index)}

Sets the current index of the iterator f created by factory.cycle, factory.iterate or factory.count to index.

If you want to re-iterate an object from its beginning, pass null for index if you traverse tables, and number 1 with every other object.

Chapter Seventeen

\section*{C API Functions}

\section*{17 C API Functions}

As already noted in Chapter 1, Agena features the same C API as Lua 5.1 so you are able to easily integrate your \(C\) packages and functions written for Lua 5.1 in Agena. Actually, Agena's C API is a superset of Lua's C API \({ }^{33}\). For a description of the API functions taken from Lua, see its Lua 5.1 manual. C API compatibility functions for Lua 5.2, 5.3 and 5.4 have also been added to facilitate porting \(C\) functions from these Lua editions to Agena.

The functions listed cannot be used in your Agena procedures - they have been created to access Agena's features from within C code. It generally supports GCC 3.4.6 and above.

If you would like to compile a Lua C package for Agena, usually only the names of following header files have to be changed:
\begin{tabular}{|l|ll|}
\hline Lua Header File & \begin{tabular}{l} 
Corresponding Agena Header \\
File
\end{tabular} \\
\hline lua.h & agena.h & \\
\hline lauxlib.h & agnxlib.h & \\
\hline lualib.h & agenalib.h & \\
\hline luaconf.h & agnconf.h & \\
\hline
\end{tabular}

The following Agena-specific header files exist:
\begin{tabular}{|l|l|}
\hline Agena Header & \begin{tabular}{l} 
Functionality \\
agncfg.h
\end{tabular} \\
\hline \begin{tabular}{l} 
This file will be created when executing `make config`, It \\
determines the Endianness of your system, extends C long ints \\
to eight bytes, and determines the date and time for the Agena \\
build. It is advised to not change the contents of this header file.
\end{tabular} \\
agncmpt.h & \begin{tabular}{l} 
Establishes cross-platform compatibility for certain \\
mathematical C functions, a few 64-bit C types, and functions \\
to work with files beyond the 2 GBytes size limit. Applicable \\
primarily to Solaris, but also Linux, OS/2, Windows, and GCC.
\end{tabular} \\
\hline agnhlps.h & \begin{tabular}{l} 
Provides C helper functions and definitions, primarily for file \\
access, further 64-bit types, quicksort, IEEE, Endian, \\
mathematical operations \& constants, cross-platform keyboard \\
access, and fast and secure string concatenation and \\
search-and-replace functions. Useful to compile Agena on \\
SPARCs, PPCs, other RISC systems, and also on Little Endian
\end{tabular} \\
architectures, since the binio package, read, and save work in \\
Big Endian mode.
\end{tabular}

\footnotetext{
\({ }^{33}\) Full compatibility to Lua's API has been established with Agena 1.6.0 in May 2012.
}
\begin{tabular}{|l|l|}
\hline Agena Header & Functionality \\
\hline interp.h & \begin{tabular}{l} 
Interface to Professor Brian Bradie's various interpolation and \\
spline functions.
\end{tabular} \\
\hline sofa.h & \begin{tabular}{l} 
Interface to the IAU Standards of Fundamental Astronomy (SOFA) \\
Libraries.
\end{tabular} \\
\hline \begin{tabular}{l} 
moon.h, \\
sunriset.h
\end{tabular} & Miscellaneous astronomical C functions \\
\hline xbase.h & Interface to dBASE III file support of the Shapelib library. \\
\hline charbuf.h & Small string character buffer library \\
\hline luasys.h & Nodir Temirkhodjaev's Lua System (LuaSys v1.8) \\
\hline
\end{tabular}

Agena features a macro agn_Complex which is a shortcut for complex double.

The following API functions have been added (see files lapi.c and agena.h):

\section*{agn_absindex}

LUA_API int agn_absindex (lua_State *L, int index, int gettop)
Returns the absolute positive stack index number for a given non-zero index i and the number of arguments gettop passed to a function.

\section*{agn_arrayborders}
```

void agn_arraytoseq (lua_State *L, int idx, size_t a[])

```

Returns the lowest and highest indices in the array part of the table at idx, where the lowest index may start at 1 (not 0 as in C). a must be an array of 2 slots. If a[0], a[1] are 0 , there is no array part in the table.

\section*{agn_arraypart}
void agn_arraypart (lua_State *L, int idx)
Pushes a table with all the values in the array part of the table at index idx onto the top of the stack.

\section*{agn_arraytoseq}
```

void agn_arraytoseq (lua_State *L, lua_Number *a, size_t n)

```

Converts a numeric array a with \(n\) elements to a sequence and pushes it on the top of the stack.

\section*{agn_asize}
```

size_t agn_asize (lua_State *L, int idx);

```

Returns the number of items actually currently stored to the array part of the table at stack index idx, using a linear method. See also: agn_size.

\section*{agn_borders}
```

void agn_borders (lua_State *L, int idx, size_t a[]);

```

Returns the smallest and largest assigned index - in this order - in the array and hash part of a table, in two-element array a. If zeros are returned, the array and hash parts of the table are empty.

\section*{agn_ccall}
```

agn_Complex agn_ccall (lua_State *L, int nargs); (Non-ANSI)
agn_Complex agn_ccall (lua_State *L, int nargs,
lua_Number *real, lua_Number *imag); (ANSI)

```

There are two different versions of this API function available. The first form supports Non-ANSI versions of Agena, e.g. Solaris, OS/2, etc. The second form can be used in the ANSI versions of Agena (compiled with the LUA_ANSI option).

Non-ANSI version: Exactly like lua_call, but returns a complex value as its result, so a subsequent conversion to a complex number via stack operation is avoided. If the result of the function call is not a complex value, an error will be issued. agn_ccall pops the function and its arguments from the stack.

ANSI version: Like lua_call, but returns the real and imaginary parts of the complex result through the parameters real and imag. If the result of the function call is not a complex value, an error will be issued. agn_ccall pops the function and its arguments from the stack.

The function always returns the first result of the function call.
The function does not reserve its own stack space so you must call lua_checkstack or luaL_checkstack before.
```

agn_checkboolean
int agn_checkboolean(lua_State *L, int idx);

```

Checks whether the value at index idx is a Boolean and returns 1 for true, and 0 for false or fail. An error will be raised if the value at idx is none of them.

\section*{agn_checkcomplex}
```

LUALIB_API agn_Complex agn_checkcomplex (lua_State *L, int idx)

```

Checks whether the value at index idx is a complex value and returns it. An error is raised if the value at \(i d x\) is not of type complex.

\section*{agn_checkinteger}
```

lua_Integer agn_checkinteger (lua_State *L, int idx);

```

Checks whether the value at index idx is a number and an integer and returns this integer. An error is raised if the value at idx is not a number, or if it is a float.

See also: agn_checknonposint, agn_checkposint.

\section*{agn_checklstring}
```

const char *agn_checklstring (lua_State *L, int idx, size_t *len);

```

Works exactly like luaL_checklstring but does not perform a conversion of numbers to strings.

\section*{agn_checknonnegint}
```

lua_Integer agn_checknonnegint (lua_State *L, int idx);

```

Checks whether the value at index idx is a number and a non-negative integer and returns this integer. An error is raised if the value at idx is not a number, or if it is a float or is negative.

See also: agn_checkinteger, agn_checkposint, agn_checkuint16_t, agn_checkuint32_t.

\section*{agn_checknonnegative}
```

lua_Number agn_checknonnegative (lua_State *L, int idx);

```

Like agn_checknumber, but checks whether the number at idx is non-negative.
See also: agn_checkpositive.
```

agn_checknumber
lua_Number agn_checknumber (lua_State *L, int idx);

```

Checks whether the value at index idx is a number and returns this number. An error is raised if the value at idx is not a number. This procedure is an alternative to luaL_checknumber for it is around 14 \% faster in execution while providing the same functionality by avoiding different calls to internal Auxiliary Library functions.

See also: agn_checkpositive, agn_checknonnegative.

\section*{agn_checkposint}
```

lua_Integer agn_checkposint (lua_State *L, int idx);

```

Checks whether the value at index idx is a number and a positive integer and returns this integer. An error is raised if the value at idx is not a number, or if it is a float or is non-positive.

See also: agn_checkinteger, agn_checknonnegint.

\section*{agn_checkpositive}
```

lua_Number agn_checkpositive (lua_State *L, int idx);

```

Like agn_checknumber, but checks whether the number at idx is positive.
See also: agn_checknonnegative.
```

agn_checkuint16_t
uint16_t agn_checkuint16_t (lua_State *L, int idx);

```

Checks whether its argument at stack position idx is an unsigned integer and whether it fits into the range \(0 . .2^{16}-1\).

See also: agn_checknonnegint, agn_checkuint32_t, agnL_optuint32_t.
agn_checkuint32_t
```

uint32_t agn_checkuint32_t (lua_State *L, int idx);

```

Checks whether its argument at stack position idx is an unsigned integer and whether it fits into the range \(0 . .2^{32}-1\).

See also: agn_checknonnegint, agn_checkuint16_t.
```

agn_checkstring

```
```

const char *agn_checkstring (lua_State *L, int idx);

```
```

const char *agn_checkstring (lua_State *L, int idx);

```

Works exactly like luaL_checkstring but does not perform a conversion of numbers to strings. An error is raised if \(i d x\) is not a string.

If idx is negative: due to garbage collection, there is no guarantee that the pointer returned will be valid after the corresponding value is removed from the stack.

\section*{agn_cleanse}
```

LUA_API void agn_cleanse (lua_State *L, int idx, int gc)

```

Empties the entire contents of the table at index idx, but does not delete it. If gc is 1 , then a garbage collection is performed, as well. Set it to 0 of no garbage collection shall be triggered. The function does not change the stack.

\section*{agn_cleanseset}
```

LUA_API void agn_cleanseset (lua_State *L, int idx, int gc)

```

Empties the entire contents of the set at index idx, but does not delete it. If gc is 1 , then a garbage collection is performed, as well. Set it to 0 of no garbage collection shall be triggered. The function does not change the stack.

\section*{agn_complexgetimag}
```

LUA_API void agn_complexgetimag (lua_State *L, int idx)

```

Pushes the imaginary part of the complex value at position idx onto the stack.

\section*{agn_complexgetreal}
```

LUA_API void agn_complexgetreal (lua_State *L, int idx)

```

Pushes the real part of the complex value at position idx onto the stack.

\section*{agn_compleximag}
```

lua_Number agn_compleximag (lua_State *L, int idx)

```

Returns the imaginary part of the complex value at stack index idx as a lua_Number. See also: agn_complexreal.
```

agn_complexreal
lua_Number agn_complexreal (lua_State *L, int idx)

```

Returns the real part of the complex value at stack index idx as a lua_Number. See also: agn_compleximag.

\section*{agn_copy}
```

LUA_API void agn_copy (lua_State *L, int idx, int mode)

```

Returns a true copy of the table, set, or sequence at stack index idx. The copy is put on top of the stack, but the original structure is not removed. mode controls what to do with tables: mode \(=1\) : copy array part only; mode \(=2\) : copy hash part only; mode \(=3\) : copy both array and hash part. With all structures, if mode \(=7\) then no metatables or user-defined types are copied. The function performs a garbage collection.

\section*{agn_createcomplex}
```

LUA_API void agn_createcomplex (lua_State *L, agn_Complex c)

```

Pushes a value of type complex onto the stack with its complex value given by c.

\section*{agn_createpair}
```

void agn_createpair (lua_State *L, int idxleft, int idxright);

```

Pushes a pair onto the stack with the left operand determined by the value at index idxleft, and the right operand by the value at index idxright. The left and right values are not popped from the stack. The function performs a garbage collection.

\section*{agn_createpairnumber}
```

void agn_createpairnumbers (lua_State *L, lua_Number l, lua_Number r);

```

Pushes a pair onto the stack with the left operand set to number 1 , and the right operand set to number \(r\). The function performs a garbage collection.

\section*{agn_createreg}

LUA_API void agn_createreg (lua_State *L, int nrec)
Pushes a register onto the top of the stack with nrec pre-allocated places (nrec may be zero).

\section*{agn_creatertable}
```

LUA_API void agn_creatertable (lua_State *L, int idx)

```

Creates an empty remember table for the function at stack index idx. It does not change the stack.

\section*{agn_createseq}
```

void agn_createseq (lua_State *L, int nrec);

```

Pushes a sequence onto the top of the stack with nrec pre-allocated places (nrec may be zero).

\section*{agn_createset}
```

void agn_createset (lua_State *L, int nrec);

```

Pushes an empty set onto the top of the stack. The new set has space pre-allocated for nrec items.

\section*{agn_createtable}
```

LUA_API void agn_createtable (lua_State *L, int narray, int nrec)

```

Like lua_createtable, but marks the new table such that the size operator will always return the correct number of elements stored in its array part. Note that size is slower on these special tables (arrays) since it has to conduct a linear count instead of a binary one - on its array part.

\section*{agn_deletefield}
```

LUA_API void agn_deletefield (lua_State *L, int idx, const char *key)

```

Deletes the field key from the table at index idx without invoking metamethods. The function leaves the stack unchanged.

\section*{agn_deletertable}
```

LUA_API void agn_deletertable (lua_State *L, int objindex)

```

Deletes the remember table of the procedure at stack index idx. If the procedure has no remember table, nothing happens. The function leaves the stack unchanged.

\section*{agn_equalref}
```

int lua_equalref (lua_State *L, int idx1, int idx2);

```

Compares any two values at stack indices idx1 and idx2, and returns 0 if they are different and 1 if they are equal. See environ.isequal for more information. The function does not change the stack.

\section*{agn_entries}
```

void agn_entries (lua_State *L, int idx, int *flag);

```

Returns all the values stored to the table at stack index idx in a new table and sets it to the top of the stack. flag is set to 0 if no value are residing in the hash part, and to 1 if there is at least one element in the hash part.

\section*{agn_fnext}
```

int agn_fnext (lua_State *L, int indextable, indexfunction, int mode);

```

Pops a key from the stack, and pushes three or four values in the following order: the key of a table given by indextable, its corresponding value (if mode \(=1\) ), the function at stack number indexfunction, and the value from the table at the given indextable. If there are no more elements in the table, then agn_fnext returns 0 (and pushes nothing).

The function is useful to avoid duplicating values on the stack for lua_call and the iterator to work correctly.

A typical traversal looks like this:
```

/* table is in the stack at index 't', function is at stack index 'f' */
lua_pushnil(L); /* first key */
while (lua_fnext(L, t, f, 0) != 0) {
/* 'key' is at index -3, function at -2, and 'value' at -1 */
lua_call(L, 1, 1); /* call the function with one arg \& one result */
lua_pop(L, 1); /* removes result of lua_call;
keeps 'key' for next iteration */
}

```

While traversing a table, do not call lua_tolstring directly on a key, unless you know that the key is actually a string. Recall that lua_tolstring changes the value at the given index; this confuses the next call to lua_next.

\section*{agn_getbitwise}
```

int agn_getbitwise (lua_State *L)

```

Returns the current mode for bitwise arithmetic: 0 if the bitwise operators (\&\&, \|, \(\wedge \wedge\), \(\sim \sim\), and shift), internally calculate with unsigned integers, and 1 if signed integers are used.

\section*{See also: agn_setbitwise.}

\section*{agn_getcmplxparts}
```

void agn_getcmplxparts (lua_State *L, int idx,
lua_Number *re, lua_Number *im)

```

Expects a number or complex number at stack position idx and returns its real and imaginary part in re and im. If the value at idx is a number or complex number, returns 1 and 0 otherwise. With numbers, im will always be 0 .

\section*{agn_getconstants}
```

int agn_getconstants (lua_State *L)

```

Returns a non-zero if constant declarations are active, and 0 otherwise.
See also: agn_setconstants.

\section*{agn_getdblepsilon}
```

lua_Number agn_getdblepsilon (lua_State *L)

```

The macro returns the setting of the double-accuracy threshold epsilon, i.e. system variable "DoubleEps". See also: agn_getepsilon, agn_setdblepsilon.

\section*{agn_getduplicates}
```

int agn_getduplicates (lua_State *L)

```

Returns a non-zero if parser duplicate declaration warnings are turned on, and 0 otherwise.

See also: agn_setduplicates.

\section*{agn_getemptyline}
int agn_getemptyline (lua_State *L)
Returns the current setting for two input prompts always being separated by an empty line and pushes a Boolean on the stack.

See also: agn_setemptyline.

\section*{agn_geteps}
```

lua_Number agn_geteps (lua_State *L, const char *varname)

```

Returns the value of the Agena system variable eps (epsilon) if varname is "Eps", and that of DoubleEps if varname is "DoubleEps", without changing the stack.

\section*{agn_getepsilon}
```

lua_Number agn_getepsilon (lua_State *L)

```

The macro returns the setting of the accuracy threshold epsilon used by the \(\sim=\) operator and the approx function. See also: agn_getdblepsilon, agn_setepsilon.

\section*{agn_getfunctiontype}
```

LUA_API int agn_getfunctiontype (lua_State *L, int idx)

```

Returns 1 if the function at stack index idx is a \(C\) function, 0 if the function at idx is an Agena function, and -1 of the value at idx is no function at all.

\section*{agn_gethepsilon}
```

lua_Number agn_gethepsilon (lua__State *L)

```

The macro returns the setting hEps. See also: Chapter 5.2.2 and agn_sethepsilon.

\section*{agn_getinumber}
```

lua_Number agn_getinumber (lua_State *L, int idx, int n);

```

Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a table at the given valid index idx. If \(t[n]\) is not a number, the return is 0 . The access is raw; that is, it does not invoke metamethods.

\section*{agn_getistring}
```

const char *agn_getistring (lua_State *L, int idx, int n);

```

Returns the value \(\dagger[n]\) as a const char *, where \(\dagger\) is a table at the given valid index idx. If \(\mathrm{t}[\mathrm{n}]\) is not a string, the return is NULL. The access is raw; that is, it does not invoke metamethods.

\section*{agn_getlibnamereset}
```

int agn_getlibnamereset (lua_State *L)

```

Returns the current setting for the restart statement to also reset libname and either pushes a non-zero integer (= true) or zero (= false).

\section*{See also: agn_setlibnamereset}

\section*{agn_getlongtable}
```

int agn_getlongtable (lua_State *L)

```

Returns the current setting for key~value pairs in tables being output line by line instead of just a single line and puts a Boolean on the stack. A non-zero integer denotes the feature is switched on, and 0 it is switched off.

See also: agn_setlongtable.

\section*{agn_getround}
```

LUA_API void agn_getround (lua_State *L)

```

Gets the current rounding mode. Pushes the string "downward" for FE_DOWNWARD, "upward" for FE_UPWARD, "nearest" for FE_TONEAREST, and "towardzero" for FE_TOWARDZERO onto the stack. If the rounding mode could not be determined, undefined is pushed. If any other \(\mathrm{FE}_{-}\)* value is determined, fail will be pushed. Not available in DOS.

See also: agn_setround.

\section*{agn_getrtable}
```

LUA_API int agn_getrtable (lua_State *L, int idx)

```

Pushes the remember table of the function at stack index idx onto the stack and returns 1. If the function does not have a remember table, it pushes nothing and returns 0 . See also: agn_getstore.

\section*{agn_getrtablewritemode}
```

int agn_getrtablewritemode (lua_State *L, int idx)

```

Returns 0 if the remember table of the function at stack index idx cannot be updated by the return statement (i.e. if it is an rotable), 1 if it can (i.e. if it is an rtable), 2 if the function at idx has no remember table at all, and -1 if the value at idx is not a function.

\section*{agn_getseqlstring}
```

const char *agn_getseqlstring (lua_State *L, int idx, int n, size_t *l);

```

Gets the string at index \(n\) in the sequence at stack index idx. The length of the string is stored to 1 .

\section*{agn_getstore}
```

LUA_API int agn_getstore (lua_State *L, int idx)

```

Pushes the internal 'store' table of the function at stack index idx onto the stack and returns 1 . If the function does not have a store, it pushes nothing and returns 0 . See also: Chapter 6.25 and agn_getrtable.

\section*{agn_getutype}
```

int agn_getutype (lua_State *L, int idx);

```

Returns the user-defined type of a procedure, table, sequence, set, userdata, or pair at stack position idx as a string, pushes it onto the top of the stack and returns 1. If no user-defined type has been defined, the function returns 0 and pushes nothing onto the stack.

See also: agn_isutype, agn_setutype.

\section*{agn_hashpart}
```

void agn_hashpart (lua_State *L, int idx)

```

Pushes a table with all the values in the hash part of the table at index idx onto the top of the stack.

\section*{agn_integerindices}
```

void agn_integerindices (lua_State *L, int idx, int *flag);

```

Returns all integer indices of the table \(\dagger\) at stack index idx in a new table and puts it onto the top of the stack. It also sets flag to 0 if there are no integer indices in hash part of \(t\), and flag to 1 if there is at least one integer index in the hash part.

\section*{agn_isfail / lua_isfail}
```

int agn_isfail (lua_State *L, int idx);
int lua_isfail (lua_State *L, int idx);

```

Returns 1 if the Boolean value at the given acceptable index results to fail, 0 otherwise (true and false). lua_fail first checks whether the value at the index is a

Boolean to avoid crashes if it is not, and then whether it represents fail. The functions actually are C macros. See also: agn_istrue, agn_isfail, lua_istrue, lua_isfalse.

\section*{agn_isfalse / lua_isfalse}
```

int agn_isfalse (lua_State *L, int idx);
int lua_isfalse (lua_State *L, int idx);

```

Returns 1 if the Boolean value at the given acceptable index results to false, 0 otherwise (true and fail). lua_false first checks whether the value at the index is a Boolean to avoid crashes if it is not, and then whether it represents false. The function actually are C macros. See also: agn_istrue, agn_isfail, lua_istrue, lua_isfail.
```

agn_isfloat
agn_isfloat (lua_State *L, int idx);

```

Returns 1 if the value at the given acceptable index is a number but not an integral, and 0 otherwise. See also: agn_isinteger, agn_isnumber.

\section*{agn_isinteger}
```

agn_isinteger (lua_State *L, int idx);

```

The function returns 1 if the value at the given acceptable index is a number representing an integer, and 0 otherwise. See also: agn_isnumber.

\section*{agn_islinalgvector}
int agn_islinalgvector (lua_State *L, int idx, size_t *dim)
Tests if a value at the given acceptable index is a vector created with the linalg package, and returns 1 if true and 0 otherwise. It also stores the dimension of the vector in dim.

\section*{agn_isnumber}
```

agn_isnumber (lua_State *L, int idx);

```

This macro returns 1 if the value at the given acceptable index is a number, and 0 otherwise. See also: agn_isfloat, agn_isinteger.
```

agn_issequtype
int *agn_issequtype (lua_State *L, int idx, const char *str);

```

Checks whether the type at stack index idx is a sequence and whether the sequence has the user-defined type denoted by str. It returns 1 if the above condition is true, and 0 otherwise.

\section*{agn_issetutype}
```

int *agn_issetutype (lua_State *L, int idx, const char *str);

```

Checks whether the type at stack index idx is a set and whether this set has the user-defined type denoted by str. It returns 1 if the above condition is true, and 0 otherwise.

\section*{agn_isstring}
```

agn_isstring (lua_State *L, int idx);

```

This macro returns 1 if the value at the given acceptable index idx is a string, and 0 otherwise.

\section*{agn_istableutype}
```

int *agn_istableutype (lua_State *L, int idx, const char *str);

```

Checks whether the type at stack index idx is a table and whether the table has the user-defined type denoted by str. It returns 1 if the above condition is true, and 0 otherwise.

\section*{agn_istrue / lua_istrue}
```

int agn_istrue (lua_State *L, int idx);
int lua_istrue (lua_State *L, int idx);

```

Returns 1 if the Boolean value at the given acceptable index idx results to true, 0 otherwise (false and fail). lua_true first checks whether the value at the index is a Boolean to avoid crashes if it is not, and then whether it represents true. The functions actually are C macros. See also: agn_isfalse, agn_isfail, lua_isfalse, lua_isfail.
```

agn_isutype
int *agn_isutype (lua_State *L, int idx, const char *str);

```

Checks whether a user-defined type str has been set for the given table, set, sequence, pair, or procedure at stack position idx. It returns 1 if the user-defined type has been set, and 0 otherwise.

\section*{agn_isułypeset}
```

int *agn_isutypeset (lua_State *L, int idx, const char *str);

```

Checks whether a user-defined type has been set for the given object at stack position idx. It returns 1 if a user-defined type has been set, and 0 otherwise. The function accepts any Agena types. By default, if the object is not a table, sequence, a pair, set, or procedure, it returns 0.

\section*{agn_malloc}
```

void *agn_malloc (lua_State *L, size_t size, const char *procname, ...);

```

Allocates size bytes of memory and returns a pointer to the newly allocated block. In case memory could not be allocated, it returns an error message including procname that called agn_malloc. The function optionally can free one or more objects referenced by their pointers in case memory allocation failed.

In all cases, the last argument must be NULL.
See also: agn_free.

\section*{agn_ncall}
```

lua_Number agn_ncall (lua_State *L, int nargs, *int error, int quit);

```

Exactly like lua_call, but returns a numeric result as an Agena number, so a subsequent conversion to a number via stack operations is avoided. If the result of the function call is not numeric, an error will be issued. agn_ncall pops the function, its arguments and the result from the stack, leaving it leveled. It always returns the first result of the function call.

If the function call does not evaluate to a number, error is set to 1 and 0 otherwise. If quit is 1 , the function will automatically issue an error if the result is not a number; otherwise quit should be set to 0 . The function does not allocate its own stack space, so you must call lua_checkstack or luaL_checkstack before.

\section*{agn_nops}
```

size_t agn_nops (lua_State *L, int idx);

```

Determines the number of actual table, set, sequence or register entries of the structure or the size of a string at stack index idx. If the value at idx is not one of the mentioned data types, it returns 0 . With tables, this procedure is an alternative to lua_objlen if you want to get the size of a table since lua_objlen does not return correct results if there are holes in the table or if the table is a dictionary.

\section*{agn_onexit}
```

LUA_API void agn_onexit (lua_State *L)

```

Pushes the function environ.onexit if it exists, and calls it. The function leaves the stack unchanged.

\section*{agn_optcomplex}
agn_Complex agn_optcomplex (lua_State *L, int narg, agn_Complex z);

If the value at index narg is a complex number, it returns this number. If this argument is absent or is null, the function returns complex z. Otherwise, raises an error.

\section*{agn_pairgeti}
```

void agn_pairgeti (lua_State *L, int idx, int n);

```

Returns the left operand of a pair at stack index idx if \(n\) is 1 , and the right operand if n is 2 , and puts it onto the top of the stack. You have to make sure that n is either 1 or 2.

\section*{agn_pairrawget}
```

void agn_pairrawget (lua_State *L, int idx);

```

Pushes onto the stack the left or the right hand value of a pair \(t\), where \(t\) is the value at the given valid index \(i d x\) and the number \(k(k=1\) for the left hand side, \(k=2\) for the right hand side) is the value at the top of the stack. It does not invoke any metamethods. This function pops both k from the stack.

\section*{agn_pairrawset}
```

void agn_pairrawset (lua_State *L, int idx);

```

Does the equivalent to \(p[k]:=v\), where \(p\) is a pair at the given valid index \(i d x, v\) is the value at the top of the stack, and \(k\) is the value just below the top.

This function pops both the key and the value from the stack. It does not invoke any metamethods. See also: agn_pairset, agn_pairseti.

\section*{agn_pairset}
```

LUA_API void agn_pairset (lua_State *L, int idx, int idxleft, int idxright)

```

Sets the two values at indices idxleft and idxright to the pair at index idx. The function does not pop the values.

See also: agn_pairrawset, agn_pairseti.

\section*{agn_pairseti}
```

LUA_API void agn_pairseti (lua_State *L, int idx, int pos)

```

Sets the value at the stack top to the pair at index idx and pops the value. If pos is 1 , then the value is put into the left part of the pair, if pos is 2 , then the right part is set.

See also: agn_pairrawset, agn_pairset.

\section*{agn_pairstate}
```

LUA_API void agn_pairstate (lua_State *L, int idx, size_t a[])

```

Returns a flag indicating whether a metatable has been assigned to the pair at index idx in a, a C array with one entry, where 1 indicates that the pair features a metatable, and 0 means it does not.

\section*{agn_parts}
```

void agn_parts (lua_State *L, int idx)

```

Pushes two tables onto the top of the stack: one with all the values in the array part of the table at index idx, and one with the values in its hash part.
```

agn_poptop
void agn_poptop (lua_State *L);

```

Pops the top element from the stack. The function is more efficient than lua_pop(L, 1).

\section*{agn_poptoptwo}
```

void agn_poptoptwo (lua_State *L);

```

Pops the top element and the value just below the top from the stack. The function is more efficient than lua_pop(L, 2).

\section*{agn_pushboolean}
```

void agn_pushboolean (lua_State *L, int b);

```

Pushes true onto the stack if b is 1 or larger, and pushes false onto the stack if b is 0 . If \(b\) is -1 , it pushes fail onto the stack.

\section*{agn_pushcomplex}
```

void agn_pushcomplex (lua_State *L, lua_Number re, lua_Number im);

```

Pushes the complex value re \(+1{ }^{*}\) im onto the stack. The macro can be used both with Agena versions using standard complex.h complex functions and those using proprietary complex arithmetic.

\section*{agn_rawgetfield}
```

LUA_API void agn_rawgetfield (lua_State *L, int idx, const char *field)

```

Returns \(\dagger[f\) field], where table \(\dagger\) resides at stack index idx.

\section*{agn_rawgetifield}
```

LUA_API void agn_rawgetifield (lua_State *L, int idx, int kidx)

```

Returns \(\dagger[i]\), where table \(\dagger\) resides at stack index idx and the key i at stack index kidx .

\section*{agn_rawgetinumber}
```

lua_Number agn_rawgetinumber (lua_State *L, int idx, int n, int *rc);

```

Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a table at the given valid index idx. If \(\mathrm{t}[\mathrm{n}]\) is not a number, the return is 0 . The access is raw; that is, it does not invoke metamethods. \(r\) c includes the result of the retrieval and is 1 on success and 0 otherwise, i.e. \(\dagger[n]\) is not a number or a string convertible to a number.
```

agn_rawinsert
LUA_API void agn_rawinsert (lua_State *L, int idx)

```

Inserts the value at the top of the stack to the table at index idx, more precisely, it is added to the end of the array part of the table. The value is popped from the stack.

\section*{agn_rawinsertfrom}
```

LUA_API void agn_rawinsertfrom (lua_State *L, int tidx, int vidx)

```

Inserts the value at stack index vidx to the table residing at index idx, more precisely, it is added to the end of the array part of the table.

If vidx \(=-1\), then the value is popped from the stack, otherwise the stack is left untouched.

\section*{agn_rawreggetinumber}
```

lua_Number agn_rawreggetinumber (lua_State *L, int idx, int n, int *rc);

```

Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a register at the given valid index idx. If \(t[n]\) is not a number, the return is 0 . The access is raw; that is, it does not invoke metamethods. rc includes the result of the retrieval and is 1 on success and 0 otherwise, i.e. \(\dagger[n]\) is not a number or a string convertible to a number.

\section*{agn_rawseqgetinumber}
```

lua_Number agn_rawseqgetinumber (lua_State *L, int idx, int n, int *rc);

```

Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a sequence at the given valid index idx. If \(\dagger[n]\) is not a number, the return is 0 . The access is raw; that is, it does not invoke metamethods. rc includes the result of the retrieval and is 1 on success and 0 otherwise, i.e. \(\dagger[n]\) is not a number or a string convertible to a number.

\section*{agn_rawsetfield}
```

LUA_API void agn_rawsetfield (lua_State *L, int idx, const char *field)

```

Does the equivalent to \(\dagger[\) field \(]:=v\), where \(\dagger\) is a table at the given valid index \(i d x\), and \(v\) is the value at the top of the stack, without invoking metamethods.

This function pops the value from the stack. It does not invoke any metamethods.
See also: agn_deletefield.

\section*{agn_regextend}
```

LUA_API int agn_regextend (lua_State *L, int idx, size_t newsize)

```

Extends the size of the register at stack position idx to newsize elements and fills the newly created slots with null. If newsize is less than the current size, it simply returns 0 and does not change the size of the register, otherwise the function returns 1 . If the current top pointer already refers to the total size of the register, it is set to newsize, otherwise it is left unchanged.

\section*{agn_reggeti}

LUA_API void agn_reggeti (lua_State *L, int idx, size_t n)
Pushes the value stored at position \(n\) of the register located at stack index idx to the top of the stack. If \(n\) is out-of-range, or larger than the position of the top pointer, it issues an error.

\section*{agn_reggetinumber}

LUA_API lua_Number agn_reggeti (lua_State *L, int idx, size_t n)
The function the number stored at position \(n\) of the register located at stack index idx. If \(n\) is out-of-range, or larger than the position of the top pointer, it issues an error. It returns infinity if the value at n is non-numeric.

\section*{agn_reggettop}

LUA_API size_t agn_reggettop (lua_State *L, int idx)
Returns the position of the top pointer of a register at stack index idx. See also: agn_regsettop.

\section*{agn_regpurge}

LUA_API void agn_regpurge (lua_State *L, int idx, int n)

Removes the value at position \(n\) of the register at stack index idx and shifts down all values beyond \(n\) if necessary. The function does not reduce the size of the register, but decrements the top pointer by 1.

\section*{agn_regrawget}
```

LUA_API void agn_regrawget (lua_State *L, int idx)

```

Pushes onto the stack the value \(\dagger[k]\), where \(\dagger\) is the register at the given valid index \(i d x\) and \(k\) is the value at the top of the stack.

This function pops the key from the stack (putting the resulting value in its place). It does not invoke metamethods.

\section*{agn_regreduce}
```

LUA_API int agn_regreduce (lua_State *L, int idx, size_t newsize, int nil)

```

Reduces the size of the register residing at stack index idx to newsize entries. If nil is 1, then all values residing at positions larger then newindex, are null'ed, otherwise set nil to 0 . The function returns 0 if newindex is less than 0 , and 1 otherwise. See also: agn_regextend.

\section*{agn_regset}
```

LUA_API void agn_regset (lua_State *L, int idx)

```

Assumes that the value to be set to a register residing at stack position idx is at the top of the stack and the numeric key just below the stack and conducts the assignment.

\section*{agn_regseti}

LUA_API void agn_regseti (lua_State *L, int idx, int n)
Sets the value residing at the top of the stack to position \(n\) of the register at index idx and pops the inserted value from the stack.

\section*{agn_regsettop}
```

LUA_API int agn_regsettop (lua_State *L, int idx)

```

Sets the current top pointer of a register residing at index idx to the number stored at the top of the stack. The number at the top of the stack is popped therafter. See also: agn_reggettop.

\section*{agn_regstate}
```

LUA_API void agn_regstate (lua_State *L, int idx, size_t a[])

```

Returns the current top pointer, the total number of items, and a flag indicating whether a metatable has been assigned to the register at index idx in a, a C array with three entries. The position of the top pointer is stored to a[0], the total number of entries to \(a[1]\). The metatable flag is stored to \(a[2]\), where 1 indicates that the sequence features a metatable, and 0 means it does not.

\section*{agn_seqrawgetinumber}
lua_Number agn_seqrawgetinumber (lua_State *L, int idx, int n);
Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a sequence at the given valid index idx. If \(\dagger[n]\) is not a number, the return is 0 . The access is raw; that is, it does not invoke metamethods.

\section*{See also: lua_seqrawgetinumber.}

\section*{agn_seqresize}
int agn_seqresize (lua_State *L, int idx, size_t newsize);
Shrinks or expands the sequence at stack index idx, i.e. adds or deletes the number of pre-allocated slots to exactly newsize. The function takes care to nullify all surplus values before shrinking the sequence or adding nulls when expanding it.

\section*{agn_seqsize}
```

size_t agn_seqsize (lua_State *L, int idx);

```

Returns the number of items currently stored to the sequence at stack index idx.

\section*{agn_seqstate}
```

void agn_seqstate (lua_State *L, int idx, size_t a[])

```

Returns the actual number of items, the maximum number of items assignable to, and a flag indicating whether a metatable has been assigned to the sequence at index idx in a, a C array with three entries. The actual number of items is stored to \(a[0]\), the maximum number of entries to \(a[1]\). If \(a[1]\) is 0 , then the number of possible entries is infinite. The metatable flag is stored in a[2], where 1 indicates that the sequence features a metatable, and 0 means it does not.

\section*{agn_setbitwise}
void agn_setbitwise (lua_State *L, int value)
Sets the mode for bitwise arithmetic. If value is greater than 0 , the bitwise functions (\&\&, ||, ^ ^, ~~, and shift) internally calculate with signed integers, otherwise Agena calculates with unsigned integers.

See also: agn_getbitwise.

\section*{agn_setconstants}
```

void agn_setconstants (lua_State *L, int value)

```

Switches on constants mode if value is non-zero, and switches it off if 0 .

See also agn_getconstants.

\section*{agn_setdblepsilon}
```

lua_Number agn_setdblepsilon (lua_State *L, lua_Number x)

```

Sets the double-accuracy threshold epsilon to system variable "DoubleEps". See also: agn_setepsilon.

\section*{agn_setduplicates}
```

void agn_setduplicates (lua_State *L, int value)

```

Switches on duplicate declaration warnings (shadowing) if value is non-zero, and switches it off if 0 .

See also agn_getduplicates.

\section*{agn_setemptyline}
void agn_setemptyline (lua_State *L, int value)
If value is greater than 0 , then two input prompts are always separated by an empty line. If set false, no empty line is inserted.

See also: agn_getemptyline.

\section*{agn_setepsilon}
```

lua_Number agn_setepsilon (lua_State *L, lua_Number x)

```

Sets the accuracy threshold epsilon used by the \(\sim=\) operator and the approx function to the number \(x\). See also: agn_getepsilon.

\section*{agn_sethepsilon}
lua_Number agn_sethepsilon (lua_State *L, lua_Number x)
Sets the hEps constant. See also: Chapter 5.2.2 and agn_gethepsilon.

\section*{agn_setlibnamereset}
```

void agn_setlibnamereset (lua_State *L, int value)

```

If value is greater than 0 , then the restart statement resets libname to its default. If value is non-positive, then libname is not changed with a restart.

\section*{See also: agn_getlibnamereset.}

\section*{agn_setlongtable}
```

void agn_setlongtable (lua_State *L, int value)

```

If value is greater than 0 , then the print function outputs key~value pairs in tables line-by-line. If value is non-positive, then the print function prints all pairs in a single consecutive line.

See also: agn_getlongtable.

\section*{agn_setreadlibbed}
```

int agn_setreadlibbed (lua_State *L, const char *name)

```

Inserts name into the global set package.readlibbed.

\section*{agn_setresize}
```

void agn_setresize (lua_State *L, int idx, size_t newsize, int protect)

```

Resizes the set at stack index idx to newsize pre-allocated slots. protect controls whether to allow only a set to be shrunk without dropping any elements (protect \(==1\) ), shrunk or enlarged without dropping any elements (protect \(==2\) ), or
whether to have full control what may happen: shrinking or expanding, dropping or not dropping any elements (protect \(==0\) ). With protect \(==0\), it is advised that the set is empty.

\section*{agn_setround}
```

int agn_setreadlibbed (lua_State *L, const char *name)

```

Sets the rounding mode. what may be "downward" for FE_DOWNWARD, "upward" for FE_UPWARD, "nearest" for FE_TONEAREST, and "towardzero" for FE_TOWARDZERO. Returns 1 on success, and 0 otherwise. In case of failure, the former rounding mode is re-established. Not available in DOS.

See also: agn_getround.

\section*{agn_setrtable}
```

LUA_API void agn_setrtable (lua_State *L, int find, int kind, int vind)

```

Sets argument~return values to the function at stack index find. The argument list reside at a table array at stack index kind, the return list are in another table at stack index vind. See the description for the ret function for more information.

\section*{agn_setudmetatable}
```

LUA_API void agn_setudmetatable (lua_State *L, int idx)

```

Expects a valid userdata metatable at the top of the stack, assigns it to the userdata residing at stack index idx, and pops the value at the top of the stack thereafter. If the value at the top of the stack is null, then a metatable assigned to a userdatum is deleted, and null is popped from the stack.

\section*{agn_setutype}
```

void agn_setutype (lua_State *L, int idxobj, int idxtype);

```

Sets a user-defined type of a procedure, table, sequence, set, userdata, or pair. The object is at stack index idxobj, the type (a string) is at position idxtype. The function leaves the stack unchanged.

If null is at idxtype, the function deletes the user-defined type.
Setting the type of a sequence, set, table, procedure, or pair also causes the pretty printer to display the string passed to the function instead of the usual output at the console. See also: agn_getutype.

\section*{agn_size}
```

int agn_size (lua_State *L, int idx);

```

Returns the number of items currently stored to the array and the hash part of the table at stack index idx. See also: agn_asize.

\section*{agn_ssize}
```

int agn_ssize (lua_State *L, int idx);

```

Returns the number of items currently stored to the set at stack index idx.

\section*{agn_sstate}
```

void agn_sstate (lua_State *L, int idx, size_t a[])

```

Returns the actual number of items and the current maximum number of items allocable to the set at index idx in a, a C array with three entries. The actual number of items is stored to a[0], the current allocable size to a[1]. a[2] indicates whether a metatable has been assigned to the set, where 0 means it does not, and 1 that it does.

\section*{agn_stralloc}
```

char *agn_stralloc (lua_State *L, size_t l, const char *procname, ...);

```

Allocates a string buffer by internally determining its most efficient size, aligned along the "long" boundary. The return is a char* pointer to the beginning of the string. The function zeros only the last few bytes and assumes that the `trailing` rest will be filled by real characters later on. Just pass 1 as the number of characters, excluding the terminating \(\backslash 0\), and do not multiply it by sizeof(char). The function automatically adds a terminating \(\backslash 0\).

The function can optionally free variables passed after procname in case memory allocation fails internally. In case of an error, the function issues the name of the procedure procname from which it was called.

In any case, the last argument must always be NULL.

\section*{agn_strmatch}
```

const char *agn_strmatch (lua_State *L, const char *s, size_t s_len,
const char *p, ptrdiff_t init, ptrdiff_t *start, ptrdiff_t *end)

```

Searches string s of size s_len for pattern p. init is the position from where to start the search and by default is 1, the first character in s. start and end will include the start and end position in case of a match, always counting from 1. The return is the string starting at position start in case of a match, or NULL if there was no hit.

\section*{agn_structinsert}
```

void agn_structinsert (lua_State *L, int idxs,int idxv)

```

Inserts the object at stack index idxv into the table, set, sequence or register at stack index idxs. The function does not change the stack.

\section*{agn_tablesize}
```

void agn_tablesize (lua_State *L, int idx, size_t a[])

```

Returns a guess on the number of elements in a table at stack index idx in a [0], an indicator on whether a table contains an allocated hash part a[1], and an indicator on whether null has been assigned to a table (a [2]).

The function is useful to determine the size of a table much more quickly than the size operator does, using a logarithmic instead of linear method, but may return incorrect results if the array part of a table has holes, so the programmer should make sure that the array part of a table has no holes. It also does not count the number of elements in the hash part of a table.

See also: agn_tablestate.

\section*{agn_tablestate}
```

void agn_tablestate (lua_State *L, int idx, size_t a[], int mode)

```

Returns the number of key~value pairs allocable and actually assigned to the respective array and hash sections of the table at index idx by storing the result in \(a\), a \(C\) array with nine entries.

The number of key~value pairs currently stored in the array part is stored to a[0], the number of pairs currently stored in the hash part to \(a[1]\). a[2] contains the information whether the array part has holes (1) or not (0). The number of allocable key~value pairs to the array part is stored to \(a[3]\), and the number of allocable key~value pairs to the hash part is stored to \(a[4]\). a[5] indicates whether null has been set to the table, where \(0=\) false, and \(1=\) true. If \(a[6]\) is 0 , then the table does
not feature a metatable, if it is 1 then a metatable has been assigned. a[7] contains information on whether the hash part of a table does not have an allocated node (no dummynode), a[8] contains a guess on the number of elements in the array part of a table (see agn_tablesize for further information). a[9] contains the smallest integral index, and a[10] the largest integral index of the table.

If mode is not 1 , then the number of pairs actually assigned is not determined, which may save time. In this case \(a[0]=a[1]=a[2]=0\).

\section*{agn_tabresize}
```

LUA_API void agn_tabresize (lua_State *L, int idx, size_t newsize,
int checkholes)

```

Resizes the array part of a table at stack index idx to the given number newsize of pre-allocated slots.

If you do not know whether there are still non-null values beyond the new size in the array part, then set checkholes to 1 instead of 0 as otherwise Agena will crash in such situations. If set to 1 , the function will not resize the table if there are any excess non-null values.

\section*{agn_tocomplex (non-ANSI versions only)}
```

agn_Complex agn_tocomplex (lua_State *L, int idx)

```

Assumes that the value at stack index idx is a complex value and returns it as a lua_Number. It does not check whether the value is a complex number.

\section*{agn_tointeger}
```

lua_Integer agn_tointeger (lua_State *L, int idx)

```

Assumes that the value at stack index idx is a number and returns it as an integer, not a float. It does not check whether the value is a number.

The function does not change the stack.

\section*{agn_tonumber}
```

lua_Number agn_tonumber (lua_State *L, int idx)

```

Assumes that the value at stack index idx is a number and returns it as a lua_Number. It does not check whether the value is a number. The values undefined and infinity are recognised properly.

The function does not change the stack.

\section*{agn_tonumberx}
```

lua_Number agn_tonumberx (lua_State *L, int idx, int *exception)

```

If the value at stack index idx is a number or a string containing a number, it returns it as a lua_Number. The strings or names 'undefined' and 'infinity' are recognised properly. If successful, exception is assigned to 0 .

If the value could not be converted to a number, 0 will be refurned, and exception is assigned to 1 .

\section*{agn_tostring}
```

const char *agn_tostring (lua_State *L, int idx)

```

Assumes that the value at stack index idx is an Agena string and returns it as a C string of type const char *. It does not check whether the value is a string.

If idx is negative: due to garbage collection, there is no guarantee that the pointer returned will be valid after the corresponding value is removed from the stack.

\section*{agn_usedbytes}

LUAI_UMEM agn_usedbytes (lua_State *L)
Returns the number of bytes used by the interpreter.

\section*{agnL_checkoption}
```

LUALIB_API int agnL_checkoption (lua_State *L, int idx, const char *def,
const char *const lst[], int ignorecase)

```

Like luaL_checkoption, but returns an error if a given option at index idx is not a string. Returns the index of the option found in 1st, which may be the position of the default def if there is no value at idx. Otherwise issues an error if the option at idx is not part of lst[], or if def is not in lst[]. def must not be NULL. If ignorecase is 1 , the function compares option names case-insensitively, and case-sensitively if it is 0 . Example:
```

static const char *const datatypes[] = {"uchar", "double", "int32", NULL};
position = agnL_checkoption(L, 2, "double", datatypes, 0);

```

\section*{agnL_createpairofnumbers}
```

void agnL_createpairofnumber (lua_State *L, lua_Number l, lua_Number r);

```

Deprecated, see agn_createpairnumbers.

\section*{agnL_datetosecs}
```

LUA_API Time64_T agnL_datetosecs (lua_State *L, int idx,
const char *procname)

```

\section*{Takes either}
- a table, register, or a sequence of date time values of the form [yy, mm, dd, hh, mm , seconds], or
- six numbers yy, mm, dd, hh, mm, seconds,
and returns the number of seconds elapsed since the begin of the epoch (usually January 01, 1970) as a Time64_† value; idx must be a _positive_index number.

\section*{agnL_fncall}
```

lua_Number agnL_fncall (lua_State *L, int idx, lua_Number x,
int optstart, int optstop);

```

Pushes the mathematical function at index idx and number \(x\) onto the stack, optionally pushes the numbers at stack positions optstart through optstop (including) and then calls the function with the values pushed. It always returns the first result of the function call.

The function does not change the stack and reserves its own stack space, so you do not have to call lua_checkstack or luaL_checkstack.

The function at idx should return one number, otherwise an error will be issued. If the function at idx is not multivariate, then pass values for optstart and optstop such that optstart > optstop. See also: agnL_fnunicall.

\section*{agnL_fneps}
```

lua_Number agnL_fneps (lua_State *L, int fidx, lua_Number x, int n, int p,
int q, lua_Number *origh, lua_Number *abserr);

```

Determines an epsilon value by taking the function value \(f(x)\) into account, using a divided difference table. Also returns original epsilon estimate before correction in parameter origh, and the absolute error in parameter abserr.

The function must be at index position idx. n is the number of iterations and must be positive. p is the first index of further arguments to \(\mathrm{f}, \mathrm{q}\) the last index of further arguments to \(f\). if \(p>q\), no further arguments are evaluated.

\section*{agnL_fnunicall}
```

lua_Number agnL_fnunicall (lua_State *L, int idx, lua_Number x);

```

Pushes the mathematical function at index idx and number x onto the stack, and then calls the function. It returns one result and leaves the stack unchanged.

The function reserves its own stack space, so you do not have to call lua_checkstack or luaL_checkstack.

See also: agnL_fncall.
agnL_geti
```

int agnL_geti (lua_State *L, int idx, int i);

```

Returns the \(i\) 'th entry in the string, table array, pair, register, sequence or numarray at index idx and pushes it onto the top of the stack. The index i counts from 1.

\section*{agnL_getmetafield}
```

agnL_getmetafield (lua_State *L, int idx, const char *event);

```

Pushes onto the stack the metamethod event from the metatable of the object at index idx. If the object does not have a metatable, or if the metatable does not have this field, or - unlike luaL_getmetafield - if the field does not refer to a procedure, returns 0 and pushes nothing. Examples for event are the metamethods '__index', '__tostring', etc.

\section*{agnL_getsetting}
```

agnL_getsetting (lua_State *L, int idx,
const char * const *modenames, const int *mode, const char *procname);

```

For a given string in modenames at stack index idx, returns the respective integral representation in mode. If the string passed cannot be found in modenames, issues an error.

\section*{Example:}
```

static const int mode[] =
{OP_ADD, OP_SUB, OP_MUL, OP_DIV, OP_INTDIV, OP_MOD, OP_POW, OP_IPOW};
static const char *const modenames[] =
{"+", "-", "*", "/", "<br>", "%", "^", "**", NULL};

```
```

int op = agnL_getsetting(L, 1, modenames, mode, "zip");

```

\section*{agnL_gettablefield}
```

agnL_gettablefield (lua_State *L, const char *table, const char *field,
const char *procname, int issueerror);

```

Determines the entry from the table field <table>. <field> and puts it on top of the stack. procname is the name of the function that calls agnL_gettablefield.

If issueerror is set to 1 , then an error will be issued if table is not a table. If issueerror is set to 0 and table is not a table, then no such error will be issued and the global value found is pushed on the stack. In the latter case, the function returns LUA_TNONE-1.

The function returns the Lua/Agena type, an integer (e.g. LUA_TBOOLEAN), in case of success. If the field does not exist, LUA_TNIL will be returned and the function instead pushes null on top of the stack. See the agena.h source file for the proper type mapping (grep "basic types").

A typical call might look like this:
```

type = agnL_gettablefield(L, "environ", "infolevel",
"environ.userinfo", 1);
if (type != LUA_TTABLE) {
/* do something */
}

```

\section*{agnL_gettop}
```

LUALIB_API agnL_gettop (lua_State *L, const char *message, const char
*procname);

```

Returns the number of arguments passed to a function, or issues an error with the given message if no argument has been passed.

\section*{agnL_isdlong}

LUALIB_API int agnL_isdlong (lua_State *L, int idx)
Checks whether the value at stack index idx is a longdouble (see the long package) and returns 1 if it is and 0 otherwise.

\section*{agnL_optboolean}
```

LUALIB_API int agnL_optboolean (lua_State *L, int narg, int def)

```

If the value at stack index narg is a Boolean, returns this Boolean as an integer: -1 for fail, 0 for false, and 1 for true. If there is no value at index narg or if it is null, returns def. Otherwise, raises an error.

\section*{agnL_optinteger}
```

lua_Integer agnL_optinteger (lua_State *L, int narg, lua_Integer def)

```

If the function argument narg is a number, returns this number cast to a lua_Integer. If this argument is absent or is NULL, returns def. Otherwise, raises an error.

The function internally uses agn_checknumber which avoids internal calls to other C API auxiliary library functions and thus is somewhat faster than luaL_optinteger.

See also: agnL_optposint, agnL_optnonnegint, agnL_optuint32_t.

\section*{agnL_optnonnegative}
```

lua_Number agnL_optnonnegative (lua_State *L, int narg, lua_Integer def)

```

If the function argument narg is a non-negative number (integer or float), returns this number cast to a lua_Number. If this argument is absent or is NULL, returns def. Otherwise, raises an error.

See also: agnL_optpositive.

\section*{agnL_optnonnegint}
```

lua_Integer agnL_optnonnegint (lua_State *L, int narg, lua_Integer def)

```

If the function argument narg is a positive integer or zero, returns this number cast to a lua_Integer. If this argument is absent or is NULL, returns def. Otherwise, raises an error.

See also: agnL_optinteger, agnL_optposint.

\section*{agnL_optnumber}
```

LUALIB_API agnL_optnumber(lua_State *L, int narg, lua_Number d)

```

If the value at stack index narg is a number, returns this number. If this stack value is absent or is NULL, returns d. Otherwise, raises an error. Contrary to luaL_optnumber, agnL_optnumber does not try to convert a string to a number.

\section*{agnL_optposint}
lua_Integer agnL_optposint (lua_State *L, int narg, lua_Integer def)
If the function argument narg is a positive integer, returns this number cast to a lua_Integer. If this argument is absent or is NULL, returns def. Otherwise, raises an error.

See also: agnL_optinteger, agnL_optnonnegint, agnL_optuint32_t.

\section*{agnL_optpositive}
```

lua_Number agnL_optpositive (lua_State *L, int narg, lua_Integer def)

```

If the function argument narg is a positive number (integer or float), returns this number cast to a lua_Number. If this argument is absent or is NULL, returns def. Otherwise, raises an error.

See also: agnL_optnonnegative, agnL_optuint32_t.

\section*{agnL_optstring}
```

LUALIB_API const char *agnL_optstring (lua_State *L, int narg,
const char *def)

```

Similar to luaL_optstring, but returns an error if a given option is not a string. The length of the optional string is not determined.

\section*{agnL_optuint32_t}
```

lua_Integer agnL_optuint32_t (lua_State *L, int narg, uint32_t def)

```

Checks for an optional argument at stack position narg and returns it if it is a non-negative number; if the given argument is not a non-positive number, issues an error. If narg is null, returns def.

\section*{See also: agn_checkuint32_t, agnL_optinteger, agnL_optnonnegint, agnL_optposint.}

\section*{agnL_paircheckbooloption}
```

agnL_paircheckbooloption (lua_State *L, const char *procname, int idx,
const char *option)

```

For the given Agena procedure procname, checks whether the value at index idx is a pair, and whether its left operand is equals to option (of type string), and whether the right operand is a Boolean.

Returns -2 if the value at idx is not a pair, or the result of the call to the lua_toboolean C API function.

The function issues an error if the left operand of the pair is not equals to option, or if the right operand is not a Boolean.

The function does not pop the pair at idx.

\section*{agnL_pairgetinumber}
lua_Number agnL_pairgetinumber (lua_State *L, const char *procname, int idx, int place)

For the given Agena procedure procname, checks whether the value at stack index idx is a pair. It then checks whether the left-hand ( \(\mathrm{pOs=1}=1\) ) or right-hand side ( \(\mathrm{pos}=2\) ) is annumber and returns itthese numbers in x and y . The function leaves the stack unchanged otherwise.

If the value at \(i_{d x}\) is not a pair, or if at least one of its operands is not a number, it issues an error.

\section*{agnL_pairgetinumbers}
```

void agnL_pairgetinumbers (lua_State *L, const char *procname, int idx,
lua_Number *x, lua_Number *y)

```

For the given Agena procedure procname, checks whether the value at stack index idx is a pair. It then checks whether the left-hand and right-hand side are numbers and returns these numbers in \(x\) and \(y\). Finally, if idx is negative, the function pops the pair from the stack, and leaves the stack unchanged otherwise.

If the value at \(i d x\) is not a pair, or if at least one of its operands is not a number, it issues an error.

\section*{agnL_pexecute}
```

int agnL_pexecute (lua_State *L, const char *str, const char *procname)

```

Executes the operating system command represented by string str and puts the output - a string - onto the top of the stack.

The string procname indicates the name of the function from which it is called. The function also removes any carriage returns(' \(\backslash\) r') from the output.

\section*{agnL_readlines}
```

void agnL_readlines (lua_State *L, FILE *f,
const char *procname, int ispipe)

```

Reads in the file or pipe depicted by its handle f and pushes its entire contents or output as a string onto the top of the stack. The string procname indicates the name of the function from which it is called. The function also removes any carriage returns (' \(\backslash\) r') from the output.

If you read from a pipe, pass 1 for ispipe, and 0 otherwise.

Note that you have to open the file or pipe before, and that the function does not close the file or pipe automatically.

\section*{agnL_tonumarray}
```

lua_Number *agnL_tonumarray (lua_State *L, int idx, size_t *size,
const char *procname)

```

Creates a C double array and puts all numbers in the table, sequence or register at index idx into it. If a non-number is part of the structure, an error will be issued for function procname. size will contain the number of elements in the C array after returning. Free the array after usage. See also agnL_fillarray.

\section*{agnL_tostringx}
```

const char *(agnL_tostringx) (lua_State *L, int idx, const char *procname);

```

Converts the number, Boolean, null or string at index idx to a string. If a wrong argument has been passed, the function issues an error with the name of the procedure causing the exception given by procname.

\section*{lua_absindex}
```

int lua_absindex (lua_State *L, int idx);

```

Converts the acceptable index idx into an equivalent absolute index (that is, one that does not depend on the stack top).

\section*{lua_arith}
```

void lua_arith (lua_State *L, int op);

```

Performs an arithmetic operation op over the two values (or one, in the case of negations) at the top of the stack, with the value at the top being the second operand, pops these values, and pushes the result of the operation. The function follows the semantics of the corresponding Agena operator (that is, it may call metamethods).

The value of op must be one of the following constants:
- OP_ADD: performs addition (+)
- OP_SUB: performs subtraction (-)
- OP_MUL: performs multiplication (*)
- OP DIV: performs float division (/)
- OP_INTDIV: performs integer division ( I )
- OP_MOD: performs modulo (\%)
- OP_POW: performs exponentiation ( \(\wedge\) )
- OPIPOW: performs integer exponentiation (**)
- \(\mathrm{OP}_{-}^{-}\)UNM: performs mathematical negation (unary -)

See also: lua_compare.

\section*{lua_compare}
void lua_compare (lua_State *L, int idx1, int idx2, int op);
Compares two Agena values. Returns 1 if the value at index idx1 satisfies op when compared with the value at index idx2, following the semantics of the corresponding Agena operator (that is, it may call metamethods). Otherwise returns 0 . Also returns 0 if any of the indices is not valid.
The value of op must be one of the following constants:
- OP_EQ: compares for equality (==),
- OP LT: compares for less than ( \(<\) ),
- OP_LE: compares for less or equal ( \(<=\) ).

See also: lua_arith.
```

lua_copy
void lua_copy (lua_State *L, int fromidx, int toidx);

```

Copies the element at index fromidx into the valid index toidx, replacing the value at that position. Values at other positions are not affected.

\section*{lua_geti}
```

int lua_geti (lua_State *L, int idx, lua_Integer i);

```

Pushes onto the stack the value \(\dagger[i]\), where \(\dagger\) is the value at the given index. This function may trigger a metamethod for the '__index' event. Returns the type of the pushed value. See also: lua_seti.

\section*{lua_getiuservalue}
```

void lua_getiuservalue (lua_State *L, int idx, int n);

```

Pushes onto the stack the n-th user value associated with the full userdata at the given index and returns the type of the pushed value.

If the userdata does not have that value or the value at idx is not a userdata, pushes null and returns LUA_TNONE.
n should always be 1 as the function would always return LUA_TNONE otherwise.

\section*{lua_getwarnf}
```

int lua_setwarnf (lua_State *L);

```

Returns the current warning state:
- 0 - warning system is off;
- 1 - ready to start a new message;
- 2 - previous message is to be continued.

See also: lua_setwarnf.

\section*{lua_hasfield}
```

void lua_hasfield (lua_State *L, int idx, const char *k);

```

Checks whether a table at index idx includes a given field, a string key, and returns 0 (false) or 1 (true). Metamethods are ignored. The stack is left unchanged.

See also: lua_getfield, lua_shas.

\section*{lua_iscomplex}
```

void lua_iscomplex (lua_State *L, int idx);

```

This macro checks whether the value at stack index idx is a complex number. It returns 1 if the value is a complex number, and 0 otherwise. It does not pop anything.
```

lua_newuserdatuv
void *lua_newuserdatauv (lua_State *L, size_t size, int nuvalue);

```

This function creates and pushes on the stack a new full userdata, with nuvalue associated Agena values, called user values, plus an associated block of raw memory with size bytes. (The user values can be set and read with the functions lua_setiuservalue and lua_getiuservalue.) In Agena, nuvalue should always be 1, otherwise the function will issue an error to avoid segmentation faults.

The function returns the address of the block of memory.

\section*{lua_isnone}
```

void lua_isnone (lua_State *L, int idx);

```

This macro returns 1 if the given index is acceptable, but not valid, and 0 otherwise.

\section*{lua_isreg}
```

void lua_isreg (lua_State *L, int idx);

```

This macro checks whether the value at stack index idx is a register. It returns 1 if the value is a pair, and 0 otherwise. It does not pop anything.

\section*{lua_ispair}
```

void lua_ispair (lua_State *L, int idx);

```

This macro checks whether the value at stack index idx is a pair. It returns 1 if the value is a pair, and 0 otherwise. It does not pop anything.
```

lua_isseq
void lua_isseq (lua_State *L, int idx);

```

This macro checks whether the value at stack index idx is a sequence. It returns 1 if the value is a sequence, and 0 otherwise. It does not pop anything.

\section*{lua_isset}
```

void lua_isset (lua_State *L, int idx);

```

This macro checks whether the value at stack index idx is a set. It returns 1 if the value is a set, and 0 otherwise. It does not pop anything.

\section*{lua_isyieldable}
```

void lua_isyieldable (lua_State *L);

```

This macro returns 1 if the given coroutine can yield, and 0 otherwise.

\section*{lua_numbertointeger}
```

int lua_numbertointeger (lua_Number n, lua_Integer *p);

```

Tries to convert a float to an integer; the floating-point value \(n\) must have an integral value. If that value is within the range of integers, it is converted to an integer and assigned to *p. The macro results in a boolean indicating whether the conversion was successful. (Note that this range test can be tricky to do correctly without this macro, due to rounding.)

This macro may evaluate its arguments more than once.

\section*{lua_pushchar}
```

void lua_pushchar (lua_State *L, char c);

```

Pushes character cas a string of length 1 onto the stack.

\section*{lua_pushfail}
```

void lua_pushfail (lua_State *L);

```

This macro pushes the Boolean value fail onto the stack.
```

lua_pushfalse

```
```

void lua_pushfalse (lua_State *L);

```
```

void lua_pushfalse (lua_State *L);

```

This macro pushes the Boolean value false onto the stack.

\section*{lua_pushglobaltable}
```

void lua_pushglobaltable (lua_State *L);

```

Pushes the global environment onto the stack.

\section*{lua_pushundefined}
```

void lua_pushundefined (lua_State *L);

```

Pushes the value undefined onto the stack.

\section*{lua_pushunsigned}
```

LUA_API void lua_pushunsigned (lua_State *L, lua_Unsigned u);

```

Pushes an unsigned int (if you do not change the defaults) onto the stack.

\section*{lua_pushtrue}
```

void lua_pushtrue (lua_State *L);

```

This macro pushes the Boolean value true onto the stack.

\section*{lua_rawaequal}
```

int lua_rawaequal (lua_State *L, int index1, int index2);

```

Returns 1 if the two values in acceptable indices index1 and index2 are primitively approximately equal (that is, without calling metamethods, see also approx, \(\sim=\) ). Otherwise returns 0 . Also returns 0 if any of the indices are non valid.

\section*{lua_rawgetp}
```

int lua_rawgetp (lua_State *L, int index, const void *p);

```

Pushes onto the stack the value \(t[k]\), where \(\dagger\) is the table at the given index and \(k\) is the pointer \(p\) represented as a light userdata. The access is raw; that is, it does not use the \(\qquad\) index metavalue.

Returns the type of the pushed value.

\section*{lua_rawset2}
```

void lua_rawset2 (lua_State *L, int idx);

```

Similar to lua_settable, but does a raw assignment (i.e., without metamethods).
Contrary to lua_rawset, only the value is deleted from the stack, the key is kept, thus you save one call to lua_pop. This makes it useful with lua_next which needs a key in order to iterate successfully.

\section*{lua_rawsetiboolean}
```

void lua_rawsetiboolean (lua_State *L, int idx, int n, int num);

```

This macro does the equivalent of \(\dagger[n]:=\) fail, if num is \(-1, \dagger[n]:=\) false, if num is 0 , and \(\dagger[n]:=\) true, if num is \(1 . \dagger\) is the table at the given valid index idx, \(n\) is an integer, and num an integer.
This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetilstring}
```

void lua_rawsetilstring (lua_State *L, int idx, int n, const char *str,
int len);

```

This macro does the equivalent of \(\dagger[\mathrm{n}]:=\) string, where \(\dagger\) is the table at the given valid index idx, \(n\) is an integer, str the string to be inserted and len the length of then string.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetikey}
```

void lua_rawsetikey (lua_State *L, int idx, int n);

```

Does the equivalent of \(\dagger[\mathrm{n}]:=\mathrm{k}\), where \(\dagger\) is the table at the given valid index idx and \(k\) is the value just below the top of the stack.

This function pops the topmost value from the stack and leaves everything else untouched. The assignment is raw; that is, it does not invoke metamethods.
```

lua_rawsetinumber
void lua_rawsetinumber (lua_State *L, int idx, int n, lua_Number num);

```

This macro does the equivalent of \(\dagger[n]:=\) num, where \(\dagger\) is the table at the given valid index idx, \(n\) is an integer, and num an Agena number (a C double).

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetistring}
```

void lua_rawsetistring (lua_State *L, int idx, int n, const char *str);

```

This macro does the equivalent of \(\dagger[n]=\) str, where \(\dagger\) is the table at the given valid index idx, \(n\) is an integer, and str a string.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetp}
```

void lua_rawsetp (lua_State *L, int index, const void *p);

```

Does the equivalent of \(\dagger[p]=v\), where \(\dagger\) is the table at the given index, \(p\) is encoded as a light userdata, and \(v\) is the value on the top of the stack.

This function pops the value from the stack. The assignment is raw, that is, it does not use the \(\qquad\) newindex metamethod.

\section*{lua_rawsetstringboolean}
```

void lua_rawsetstringboolean
(lua_State *L, int idx, const char *str, int n);

```

This macro does the equivalent of \(t[s t r]:=(n==1)\), where \(\dagger\) is the value at the given valid index idx, str a string, and \(n\) an integer.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetstringchar}
```

void lua_rawsetstringchar
(lua_State *L, int idx, const char *str, int v);

```

This macro does the equivalent of \(\dagger[s t r]:=\mathrm{v}\), where \(\dagger\) is the value at the given valid index idx, str a string, and \(v\) is an integer.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods. See also lua_rawsetstringstring.

\section*{lua_rawsetstringnumber}
```

void lua_rawsetstringnumber
(lua_State *L, int idx, const char *str, lua_Number n);

```

This macro does the equivalent of \(\dagger[\) str \(]:=n\), where \(\dagger\) is the value at the given valid index idx, str a string, and \(n\) a number.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetstringpairnumbers}
```

void lua_rawsetstringpairnumbers
(lua_State *L, int idx, const char *str, lua_Number x, lua_Number y);

```

This macro does the equivalent of \(\mathrm{t}[\mathrm{str}]:=\mathrm{x}: \mathrm{y}\), where \(\dagger\) is the value at the given valid index idx, str a string, and x:y is a pair of the numbers \(x\) and \(y\).

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua_rawsetstringstring}
```

void lua_rawsetstringstring
(lua_State *L, int idx, const char *str, const char *text);

```

This macro does the equivalent of \(\dagger[s t r]:=\) text, where \(\dagger\) is the value at the given valid index idx, str a string, and text is a string.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods. See also lua_rawsetstringchar.

\section*{lua_reginsert}
```

void lua_reginsert (lua_State *L, int idx);

```

Puts the element on top of the Lua stack into the register at stack index idx. on the first slot that is currently set to null. If there is no free slot, an error will be issued. The value added to the register is popped from the stack thereafter.

\section*{lua_regnext}
```

int lua_regnext (lua_State *L, int idx);

```

Pops a key from the stack, and pushes the next key~value pair from the register at the given index idx. If there are no more elements in the register or the position of the top pointer has been exceeded, then lua_regnext returns 0 (and pushes nothing). To access the very first item in a register, put null on the stack before (with lua_pushnil).

While traversing a register, do not call lua_tolstring directly on the key. Recall that lua_tolstring changes the value at the given index; this confuses the next call to lua_regnext.

\section*{lua_regsetinumber}
void lua_regsetinumber (lua_State *L, int idx, int n, lua_Number num);
This macro sets the given Agena number num to the non-zero and positive index \(n\) of the register at stack index idx.

\section*{lua_rotate}
```

void lua_rotate (lua_State *L, int idx, int n);

```

Rotates the stack elements between the valid index idx and the top of the stack. The elements are rotated \(n\) positions in the direction of the top, for a positive \(n\), or \(-n\) positions in the direction of the bottom, for a negative \(n\).

The absolute value of \(n\) must not be greater than the size of the slice being rotated.
This function cannot be called with a pseudo-index, because a pseudo-index is not an actual stack position.
```

lua_sdelete
void lua_sdelete (lua_State *L, int idx);

```

Deletes the element residing at the top of the stack from the set at stack position idx. The element at the stack top is popped thereafter.

Note that you should not delete a value while traversing a set with lua_usnext. This code, however, works:
```

lua_pushvalue(L, idx);
if (lua_isset(L, -1)) {
lua_pushnil(L);
while (lua_usnext(L, -2) != 0) {
lua_sdelete(L, -3); /* delete value in the set and pop it */
agn_poptop(L); /* pop the key from stack, too, since it cannot
be used for next iteration as it has been
purged from the set */
lua_pushnil(L); /* restart iteration */
}
}
agn_poptop(L);

```

See also: lua_sinsert.

\section*{lua_seqgeti}
```

void lua_seqgeti (lua_State *L, int idx, int n);

```

Gets the n-th item from the sequence at stack index idx and pushes it onto the stack. You have to make sure that the index is valid, otherwise there may be segmentation faults.

See also: lua_seqseti.

\section*{lua_seqrawgetinumber}
```

lua_Number lua_seqrawgetinumber (lua_State *L, int idx, int n);

```

Returns the value \(\dagger[n]\) as a lua_Number, where \(\dagger\) is a sequence at the given valid index idx. If \(\dagger[n]\) is not a number, the return is huge_val. The access is raw; that is, it does not invoke metamethods.

See also: agn_seqgetinumber.

\section*{lua_seqinsert}
```

void lua_seqinsert (lua_State *L, int idx);

```

Inserts the element on top of the Lua stack into the sequence at stack index idx. The element is inserted at the end of the sequence. The value added to the sequence is popped from the stack thereafter.

\section*{lua_seqnext}
```

int lua_seqnext (lua_State *L, int idx);

```

Pops a key from the stack, and pushes the next key~value pair from the sequence at the given index idx. If there are no more elements in the sequence, then lua_seqnext returns 0 (and pushes nothing). To access the very first item in a sequence, put null on the stack before (with lua_pushnil).

While traversing a sequence, do not call lua_tolstring directly on the key. Recall that lua_tolstring changes the value at the given index; this confuses the next call to lua_seqnext.

\section*{lua_seqrawget}
```

void lua_seqrawget (lua_State *L, int idx, int pushnil);

```

Pushes onto the stack the sequence value \(\dagger[k]\), where \(\dagger\) is the sequence at the given valid index idx and \(k\) is the value at the top of the stack. If t[k] does not exist, an error will be issued if pushnil \(=0\), and null will be pushed if pushnil is non-zero.

This function pops the key from the stack (putting the resulting value in its place). The function does not invoke any metamethods.

\section*{lua_seqrawgeti}
```

void lua_seqrawgeti (lua_State *L, int idx, size_t n);

```

Pushes onto the stack the sequence value \(t[n]\), where \(\dagger\) is the sequence at the given valid index idx.

The function does not invoke any metamethods. Contrary to lua_rawgeti, it issues an error if \(n\) is out of range.

\section*{lua_seqrawset}
```

void lua_seqrawset (lua_State *L, int idx);

```

Does the equivalent to \(s[k]:=v\), where \(s\) is a sequence at the given valid index idx, \(v\) is the value at the top of the stack, and \(k\) is the value just below the top.

This function pops both the key and the value from the stack. It does not invoke any metamethods.

\section*{lua_seqrawsetilstring}
```

void lua_seqrawsetilstring (lua_State *L, int idx, int n, const char *str,
int len);

```

This macro does the equivalent of \(s[n]=\) string, where \(s\) is the sequence at the given valid index idx, \(n\) is an integer, str the string to be inserted and len the length of then string.

This function leaves the stack unchanged. The assignment is raw; that is, it does not invoke metamethods.

\section*{lua seqseti}
```

void lua_seqseti (lua_State *L, int idx, int n);

```

Sets the value at the top of the stack to the non-zero and positive index \(n\) of the sequence at stack index idx.

If the value added is null, the entry at sequence index \(n\) is deleted and all elements to the right of the value deleted are shifted to the left, so that their index positions get changed, as well.

The function pops the value from the top of the stack.
If there is already an item at position \(n\) in the sequence, it is overwritten.
If you want to extend a current sequence, the function allows to add a new item only at the next free index position. Larger index positions are ignored, but the value to be added is popped from the stack, as well.

See also: lua_seqgeti.

\section*{lua_seqsetinumber}
```

void lua_seqsetinumber (lua_State *L, int idx, int n, lua_Number num);

```

The function sets the given Agena number num to the non-zero and positive index \(n\) of the sequence at stack index idx.

\section*{lua_seqsetistring}
```

void lua_seqsetistring (lua_State *L, int idx, int n, const char *str);

```

This macro sets the given string str to the non-zero and positive index index \(n\) of the sequence at stack index idx.

\section*{lua_seti}
```

void lua_seti (lua_State *L, int idx, lua_Integer n);

```

Does the equivalent to \(t[n]=v\), where \(t\) is the value at the given index idx and \(v\) is the value at the top of the stack.

This function pops the value from the stack. This function may trigger a metamethod for the '__writeindex' event.

See also: lua_geti.

\section*{lua_setmetatabletoobject}
```

void lua_setmetatabletoobject (lua_State *L, int idx, const char *k,
int settype);

```

Sets metatable \(k\) to the structure at index position idx. The function does not change the stack. If settype is 1 the user-defined type \(k\) will also be set, if settype is 0 no user-defined type will be set. If \(k\) is NULL, the metatable will be deleted and if settype is 1 , the user-defined type will also be removed.

\section*{lua_setwarnf}
```

void lua_setwarnf (lua_State *L, lua_WarnFunction f, void *ud);

```

Sets the warning function to be used by Lua to emit warnings (see lua_WarnFunction). The ud parameter sets the value ud passed to the warning function. See also: lua_getwarnf.
```

lua_sinsert
void lua_sinsert (lua_State *L, int idx);

```

This macro to lua_srawset inserts an item into a set. The set is at the given index idx, and the item is at the top of the stack.

This function pops the item from the stack. See also: lua_sdelete.

\section*{lua_sinsertlstring}
```

void lua_sinsertlstring (lua_State *L, int idx, const char *str, size_t l);

```

This macro sets the first I characters of the string denoted by str into the set at the given index idx.

\section*{lua_sinsertnumber}
```

void lua_sinsertnumber (lua_State *L, int idx, lua_Number n);

```

This macro sets the number denoted by n into the set at the given index idx.

\section*{lua_shas}
```

void lua_shas (lua_State *L, int idx, int pop);

```

Checks whether the value at the stack top exists in the set at stack index idx. Returns 0 or 1 . If pop is 1, pops the value, otherwise leaves the stack unchanged.

\section*{See also lua_hasfield.}

\section*{lua_sinsertstring}
```

void lua_sinsertstring (lua_State *L, int idx, const char *str);

```

This macro sets the string denoted by str into the set at the given index idx.

\section*{lua_srawget}
```

int lua_srawget (lua_State *L, int idx);

```

Checks whether the set at index idx contains the value at the top of the stack. The function pops the value from the stack putting the Boolean value true or false in its place. It returns 1 if the element has been found, and 0 otherwise.

It does not invoke any metamethods.

\section*{lua_srawset}
```

void lua_srawset (lua_State *L, int idx);

```

Does the equivalent to insert \(v\) into \(s\), where \(s\) is the set at the given valid index idx, \(v\) is the value at the top of the stack.

This function pops the value from the stack. It does not invoke any metamethods. To delete entries, see lua_sdelete.

\section*{lua_stringtonumber}
void lua_stringtonumber (lua_State *L, const char *s);

Converts the zero-terminated string s to a number, pushes that number into the stack, and returns the total size of the string, that is, its length plus one. The conversion can result in an integer or a float, according to the lexical conventions of Agena. The string may have leading and trailing whitespaces and a sign. If the string is not a valid numeral, returns 0 and pushes nothing. (Note that the result can be used as a Boolean, true if the conversion succeeds.)

\section*{lua_toboolean}
int lua_toboolean (lua_State *L, int idx)
Converts the value at the given acceptable index to an integer value ( \(-1,0\) or 1 ).
If the value at \(i d x\) is null or false, the functions returns 0 .
If the value at \(i d x\) is fail, the function returns -1 .
If the value at idx is different from false, fail, and null, the function returns 1 .
The function also returns 0 when called with a non-valid index. (If you want to accept only actual Boolean values, use lua_isboolean to test the value's type.)

\section*{lua_toint32_t}
```

int32_t lua_toint32_t (lua_State *L, int idx)

```

Converts the value at the given acceptable index to the signed integral type int32_t. The value must be a number or a string convertible to a number; otherwise, lua_toint32_t returns 0 .

If the number is not an integer, it is truncated in some non-specified way.
See also: agnL_optuint32_t.

\section*{lua_usnext}
```

int lua_usnext (lua_State *L, int idx);

```

Pops a key from the stack, and pushes the next item twice (!) from the set at the given idx. If there are no more elements in the set, then lua_usnext returns 0 (and pushes nothing). To access the very first item in a set, put null on the stack before (with lua_pushnil).

While traversing a set, do not call lua_tolstring directly on an item, unless you know that the item is actually a string. Recall that lua_tolstring changes the value at the given index; this confuses the next call to lua_usnext.

\section*{lua_warning}
```

int lua_warning (lua_State *L, const char *msg, int tocont);

```

Emits a warning with the given message. A message in a call with tocont true should be continued in another call to this function.

\section*{luaL_addgsub}
```

const void luaL_addgsub (luaL_Buffer *B, const char *s,
const char *p, const char *r);

```

In string \(s\), replaces any occurrence of the string \(p\) with the string \(r\) and adds the resulting string to buffer в. Search patterns are ignored.
```

luaL_argexpected
void luaL_argexpected (lua_State *L, int cond, int arg, const char *tname);

```

Checks whether cond is true. If it is not, raises an error about the type of the argument arg with a standard message (see lual_typeerror).

\section*{lual_checkint32_†}
```

int32_t luaL_checkint32_t (lua_state *L, int narg)

```

Checks whether the function argument narg is a number and returns this number cast to an int32_t.

\section*{luaL_checksetting}
```

int luaL_checksetting (lua_State *L, int idx,
const char *const lst[], const char *errmsg);

```

Checks whether the string at stack index idx is included in the list lst, and returns its position in lst, counting from 0 . If it does not find the string in the list, issues the error errmsg.

\section*{luaL_clearbuffer}
```

void luaL_clearbuffer (luaL_Buffer *B)

```

Clears a luaL_Buffer and resets it, does not leave anything on the stack

\section*{luaL_isudata}
```

int luaL_isudata (lua_State *L, int ud, const char *tname);

```

Checks whether the object at stack position ud is a userdata object. If ud depicts the position of a userdata, the function also checks whether the metatable - if available - attached to it complies with metatable tname which the programmer originally intended to be used by the specific userdata.

The function returns 1 if all checks have been successful, and 0 otherwise.
See also: luaL_getudata.

\section*{luaL_getsubtable}
```

int luaL_getsubtable (lua_State *L, int idx, const char *fname);

```

Ensures that the value t[fname], where \(\dagger\) is the value at index idx, is a table, and pushes that table onto the stack. Otherwise creates a new table, assigned to \(\dagger[\) fname \(]\), and pushes it onto the top of the stack. Returns true (1) if it finds a previous table and false \((0)\) if it creates a new table.

\section*{luaL_getudata}
```

void *luaL_getudata (lua_State *L, int narg, const char *tname,
int *result);

```

Checks whether the function argument narg is a userdata of the type tname. Contrary to luaL_checkudata, it does not issue an error if the argument is not a userdata, and also stores 1 to result if the check was successful, and 0 otherwise.

\section*{lual_setfuncs}
```

void luaL_setfuncs (lua_State *L, const luaL_Reg *l, int nup);

```

Registers all functions in the array 1 (see lual_Reg) into the table on the top of the stack (below optional upvalues, see next).

When nup is not zero, all functions are created with nup upvalues, initialized with copies of the nup values previously pushed on the stack on top of the library table. These values are popped from the stack after the registration.

The following functions have originally been written by Rici Lake for Lua 5.x:
luaL_newref
luaRef *luaL_newref (lua_State *L, int idx);

Creates a new C reference to the object at stack index idx.

\section*{luaL_pushref}
```

void luaL_pushref (lua_State *L, luaRef *r)

```

Pushes a referenced object onto the stack.

\section*{luaL_pushref}
```

void luaL_freeref (lua_State *L, luaRef *r)

```

Frees a reference.

\section*{Appendices}

\section*{Appendix A}

\section*{A1 Operators}

Unary operators are:
\&\&, ~~, ||, ^^, abs, antilog2, antilog10, arccos, arcsec, arcsin, arctan, assigned, atendof, bea, char, cis, conjugate, copy, cos, cosh, cosxx, cube, empty, entier, even, exp, filled, finite, first, flip, float, lngamma, gethigh, getlow, imag, infinite, inrange, instr, int, integral, join, last, left, ln, lower, nan, nargs, nonzero, not, odd, qmdev, qsumup, real, recip, reg, replace, right, sumup, seq, sign, signum, sin, sinc, sinh, size, square, sqrt, tan, tanh, trim, type, unassigned, unique, upper, times, typeof, values, zero, - (unary minus), ~~ (bitwise complement).

Binary operators are:
and, in, intersect, minus, nand, nor, or, roll, split, squareadd, subset, symmod, union, xor, xnor, xsubset, + (addition), - (subtraction), * (multiplication), / (division), *\% (percentage) \(/ \%\) (ratio), +\% (add percentage), -\% (subtract percentage), \%\% (percentage change), \ (integer division), \% (modulus), ^ (exponentiation), ** (integer exponentiation), \& (concatenation), = (equality), ~= (approximate equality), ~<> (approximate inequality), < (less than), <= (less or equal), > (greater than), >= (greater or equal), e (mapping), \$ (selection), \$\$ (fulfillment), : (pair constructor), ! (complex constructor), \&\& (bitwise and), ।। (bitwise or), ^^ (bitwise xor), <<< (bitwise left-shift), >>> (right-shift), <<<< (bitwise left-rotation), >>>> (right-rotation), \&+ (add 4 -byte integer), \&- (subtract 4-byte integer), \&* (multiply 4-byte integer), and \&/ (devide 4-byte integer), । (comparison), ~। (approximate comparison), । - (absolute difference).

\section*{A2 Metamethods}

The following metamethods were inherited from Lua 5.1:
\begin{tabular}{|c|c|}
\hline Index to metatable & Meaning \\
\hline '__index' & read operation using indices, e.g. if n[1] = 0 then ... or if n[2 to 3] = 'JP' then ... \\
\hline '__gc' & Garbage collection, for userdata only \\
\hline '__mode' & Sets weakness of a table \\
\hline '__add' & Addition of two values \\
\hline '__sub' & Subtraction of two values \\
\hline '-_mul' & Multiplication of two values \\
\hline '__div' & Division of two values \\
\hline '__mod' & Modulus \\
\hline '__pow' & Exponentiation \\
\hline '__unm' & Unary minus \\
\hline '__eq' & Equality operation \\
\hline '__lt' & Less-than operation \\
\hline '__le' & Less-than or equals operation \\
\hline '__concat' & Concatenation \\
\hline '__call' & See Lua 5.1 manual \\
\hline '__tostring' & Method for pretty printing values at stdout \\
\hline '__metatable' & Protection for metatables \\
\hline '__weak' & Declaration of weak tables, sets, and sequences \\
\hline
\end{tabular}

Table 20: Metamethods taken from Lua
The __len metamethod in Lua 5.1 to determine the size of an object was replaced with the __size metamethod. Lua's __mode metamethod has been renamed weak.

The following methods are new in Agena:
\begin{tabular}{|c|c|}
\hline Index to metatable & Meaning \\
\hline '__abs' & abs operator \\
\hline '__aeq' & approximate equality operator ( \(\sim=\) ) \\
\hline '__arccos' & arccos operator \\
\hline '__arcsin' & arcsin operator \\
\hline '__arctan' & arctan operator \\
\hline '__cis' & cis operator \\
\hline '__cos' & cos operator \\
\hline '__cosh' & cosh operator \\
\hline '__cube' & cube operator \\
\hline '__eeq' & strict equality operator ( \(==\) ) \\
\hline '__empty' & empty operator \\
\hline '__even' & even operator \\
\hline '__exp' & exp operator \\
\hline '_-filled' & filled operator \\
\hline '__float' & float operator \\
\hline
\end{tabular}
\begin{tabular}{l|l|}
\hline Index to metatable & Meaning \\
\hline '__imag' & imag operator \\
\hline '__in' & in binary operator \\
\hline '__intdiv' & integer division \\
\hline '__intersect' & intersect operator \\
\hline '__integral' & integral operator \\
\hline '__ipow' & exponentiation with an integer power \\
\hline '__ln' & In operator \\
\hline '__log' & log operator \\
\hline '__minus' & minus operator \\
\hline '__nonzero' & nonzero operator \\
\hline '__notin' & notin operator \\
\hline '__oftype' & \begin{tabular}{l} 
self-defined type check for \(::, ~:-, ~ a n d ~ p a r a m e t e r ~ l i s t s ~\) \\
of procedures
\end{tabular} \\
\hline '__qsumup' & \begin{tabular}{l} 
qsumup operator for table or sequence-based \\
user-defined types
\end{tabular} \\
\hline '__real' & real operator \\
\hline '__recip' & recip operator \\
\hline '__sumup' & sumup operator for table or sequence based \\
\hline \hline user-defined types
\end{tabular}

Table 21: Metamethods introduced with Agena

\section*{A3 Mathematical Constants}
\begin{tabular}{l|l|}
\hline Constant & Meaning \\
\hline degrees & Factor \(1 / \pi^{*} 180\) to convert radians to degrees \\
\hline DoubleEps & Equals \(2.2204460492503131 \mathrm{E}-16\) \\
\hline Eps & Equals \(1.4901161193847656 \mathrm{e}-08\) \\
\hline hEps & Equals 1.4901161193847656 e -12 \\
\hline EulerGamma & Euler-Mascheroni constant, equals 0.57721566490153286061 \\
\hline E, Exp & Constant e \(=\) exp( 1 ) \(=2.71828182845904523536\) \\
\hline I & Imaginary unit \(\sqrt{-1}\) \\
\hline infinity & Infinity \(\infty\) \\
\hline Pi & Constant \(\pi=3.14159265358979323846\) \\
\hline Pi2 & Constant \(2 \pi=6.283185307179586476926\) \\
\hline PiO2 & Constant \(\pi / 2=1.570796326794896619232\) \\
\hline PiO4 & Constant \(\pi / 4=0.785398163397448309616\) \\
\hline radians & Factor \(\pi / 180\) to convert degrees to radians \\
\hline undefined & An expression stating that it is undefined, e.g. a singularity \\
\hline Phi & Golden ratio \((1+\sqrt{5}) / 2\) \\
\hline math.largest & Largest representable number; the smallest negative one \\
nearest to \(-\infty\) is the negative of this constant \\
\hline math.smallest & Smallest positive representable number \\
\hline math.smallest- & Smallest positive normal number \\
\hline normal & \(L\) Largest integer i representable on the floating-point system with \\
\hline math. & enough precision, such that \(\mathrm{i}-1<>\) i \\
\hline lastcontint & \(10^{18}\) \\
\hline math.exa & \(10^{15}\) \\
\hline math.peta & \(10^{12}\) \\
\hline math.tera & \(10^{9}\) \\
\hline math.giga & \(10^{6}\) \\
\hline math.mega & \(10^{3}\) \\
\hline math.kilo & \(10^{1}\) \\
\hline math.deka & \(10^{-1}\) \\
\hline math.deci & \(10^{-2}\) \\
\hline math.centi & \(10^{-3}\) \\
\hline math.milli & \(10^{-6}\) \\
\hline math.micro & \(10^{-9}\) \\
\hline math.nano & \(10^{-12}\) \\
\hline math.pico & \(10^{-15}\) \\
\hline math.femto & \(10^{-18}\) \\
\hline math.atto & \\
\hline
\end{tabular}

\section*{A4 System Variables}

Agena lets you configure the following settings, where `n/e` means `no effect`.
\begin{tabular}{|c|c|c|}
\hline System variable & Meaning & Write \\
\hline libname & The paths to Agena libraries. & yes \\
\hline mainlibname & The path to the main Agena directory. & yes \\
\hline environ.cpu & Contains the name of the CPU in use as a lower-case string, e.g. 'sparc', 'ppc' for PowerPC, or 'x86' for Intel 386-compatible processors. See also system variable environ.os. & no \\
\hline environ.homedir & The path to the user's home directory. & yes \\
\hline environ.gdidefaultoptions & A table with all default plotting options for some functions in the gdi package. This table is set by gdi.setoptions. & no \\
\hline environ.libpatchlevel & The update version of the main Agena library (in lib/library.agn). Mostly defaults to null. & no \\
\hline environ.maxpathlength & The maximum number of characters for a file path (excluding C's 10 character). & no \\
\hline environ.more & The number of entries in tables and sets printed by print and the end-colon functionality before issuing the `press any key` prompt. Default is 40 . & yes \\
\hline environ.os & Contains the name of the operating system in use as a lower-case string, e.g. 'windows', 'macosx','solaris', 'os/2', 'haiku','dos', or 'linux'. Do not change this value. See also system variable environ.cpu. & no \\
\hline environ.release & A sequence containing the string 'AGENA' the main interpreter version as a number, the subversion as a number, and the \(C\) patch number as a number, as well. The lib/library.agn patch level is denoted by the fourth entry, or 0 if non-existent. Do not change environ.release. See also system variables _RELEASE and environ.version. & no \\
\hline environ.version & Similar to environ.release, but contains version information represented by a float, not including the lib/library.agn patch level. & no \\
\hline environ.withprotected & A set of names (passed as strings) that cannot by overwritten by the with function. Currently the names ‘next’, ‘print`, ‘with`, `write`, `read`, ‘writeline` have been assigned. & yes \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline System variable & Meaning & Write \\
\hline environ.withverbose & If set to false, the with function will not display warnings, the initialisation string, and the short names assigned. Default is true. & yes \\
\hline _G & A table holding all currently assigned global names and their values, and itself. You can add or delete entries by simple table assignment or unassignment, e.g. to delete the print function in the current session, just enter:
```

> delete print from _G
> print('Klöße !')
Error in stdin, at line 1:
attempt to call global `print` (a null
value)

``` & yes \\
\hline _PROMPT & Defines the prompt Agena displays at the console. If unassigned, by default the prompt is ' \(>\) '. & yes \\
\hline _RELEASE & Release information on the installed Agena release, returned as a string, e.g. 'AGENA \(\gg 2.2 .0\) '. See also system variables environ.release and environ.version. & no \\
\hline nargs & Number of arguments actually passed in a function call, including varargs & no \\
\hline procname & Refers to the function currently invoked, can be used in recursive calls & no \\
\hline
\end{tabular}

Table 22: System variables
All environ.* settings are reset by the restart statement to their original defaults, whereas those settings the user defines with the environ. kernel function will never be modified or deleted by a restart.

Some of the default settings can be found at the bottom of the lib/library.agn file.
See also:
- Chapter 14.2 for a description of the kernel functions for other settings.
- Appendix A5 for settings that control how Agena outputs data at the console.

\section*{A5 Command-Line Usage \& Scripting}

Agena can be used in the command line as follows:
```

agena [options] [script [arguments]]

```

This means that any option, a script name, and the arguments are all optional. If you just enter
```

shell> agena

```

Agena is started in interactive mode immediately.
There are two ways to run an Agena script with some arguments and then return to the command line immediately without entering interactive mode:

\section*{A5.1 Using the -e Option}

We may write a script with a text editor, e.g. one to print the sine of a number, for example the following two lines:
```

n := n or Pi; \# if n is not set from the shell, just assign Pi to n
writeline(sin(n));

```

When using the -e option, we first assign the desired number to a variable and then call the script by its name:
```

shell> agena -e "n := Pi/2" sin.agn
I

```

Note that you first have to enter the -e option along with the assignment statement, and then the name of the script.

A much better alternative is this:

\section*{A5.2 Using the Internal args Table and Exit Status}

Everything you pass to the interpreter from the command line is stored in the args table.

The name of the script is always stored at index 0 , the arguments are stored at the positive indices 1, 2, etc., in the order given by the user. The name of the Agena binary and any options are accessible via negative keys. The name of the interpreter binary is always at the smallest index.

Consider the following script called 'args.agn':
```

for i, j in args do
writeline(i, j, delim='\t')
od;

```

If you run it, the output will be:
```

shell> agena -m args.agn 1.1 2.2 3.3
4'194'303 KBytes of physical RAM free.
1
3 3.3
-2 agena
-1 -m
0 args.agn

```

Just play around with this a little bit.
Let us use our new knowledge: The script 'In.agn' requires at least one number and calculates the corresponding natural logarithm. The numbers entered at the command line are put into the args table as strings, so you should convert them back into numbers first. The number of actual arguments - without script name, options and Agena binary file name - are stored in nargs. os.exit passes an exit code to the shell, if needed.
```


# Evaluate the natural logarithm of given numbers

if nargs < 1 then
print('Error, need at least one number');
os.exit(-1) \# just return error exit code
fi
rc := 0; \# exit/return code of the script
for i to nargs do \# iterate each argument at the command line
x := tonumber(args[i]);
if x :- number then x := 0 fi; \# if conversion failed, set x to 0
r := ln(x);
if r = undefined then rc := 1 fi; \# there was an arithmetic error
writeline('ln(', x, ') = ', r)
od;
/* clear interpreter state, perform garbage collection \& return exit code:
-1 = no arguments given
0 = okay
1 = domain error or wrong type of argument */
os.exit(rc, true);

```

Use it:
```

shell> agena ln.agn 0 1 2
ln(0) = undefined
ln(1)}=
ln(2) = 0.69314718055995

```

You will find sample scripts in the 'share/scripting' directory of your Agena distribution. The folder also includes batch files to start the scripts from a shell in OS/2 Warp 4.5 (e.g. 'whereis.cmd'), DOS and Windows (e.g. 'whereis.bat').

\section*{A5.3 Running a Script and then Entering Interactive Mode}

The -i option allows you to enter the interactive level after running a script or passing other options to Agena. The position of the -i option is free. The following shell statement resets the Agena prompt and starts the interpreter:
```

shell> agena -i -e "_PROMPT := 'AGENA> '"

```
AGENA>

\section*{A5.4 Running Scripts in UNIX and Mac OS X}

If you use Agena in UNIX and Mac OS X, then you can execute Agena scripts directly by just entering the name of the script followed by any arguments (if needed).

Just insert the following line at the head, i.e. the very first line, of each script:
```

\#!/usr/local/bin/agena

```
and set the appropriate rights for the script file (e.g. chmod \(a+x\) scriptname). An example:
```

bash> ./sin.agn 1

```
0.8414709848079

In all other operating systems, the first line is ignored by the interpreter, so you do not have to delete the first line of the script in order to use scripts you have originally written under UNIX or Mac.

Please make sure that the file is stored in UNIX line break format - and not Windows line breaks.

\section*{A5.5 Command Line Switches}

The available switches are:
\begin{tabular}{|c|c|}
\hline Option & Function \\
\hline -e "stat" & execute string "stat" (double quotes needed) \\
\hline -h & help information \\
\hline -i & enter interactive mode after executing `script` or other options \\
\hline -1 & print licence information \\
\hline -m & print the amount of free RAM at start-up \\
\hline -n & do not run initialisation file(s) agena.ini / .agenainit at start-up or restart \\
\hline -p path & sets <path> to libname, overriding the standard initialisation procedure for this environment variable. The path does not need to be put in quotes if it does not contain spaces. \\
\hline -r name & readlib library <name>. The name of the library does not need to be put in quotes. \\
\hline -a & ignore AGENAPATH environment variable, setting libname by searching the file system. \\
\hline -s "text" & issue the slogan "text" at start-up \\
\hline -V & show version information and compilation time \\
\hline -x & does not read the main library file lib/library.agn art start-up or restart \\
\hline -- & stop handling options \\
\hline - & execute stdin and stop handling options \\
\hline
\end{tabular}

Table 23: Command line options
Instead of a preceding hyphen you can also use a slash, e.g. `agena /d` and `agena -d` for debugging mode are accepted.

\section*{A6 Define Your Own Printing Rules for Types}

You can tell Agena how to output strings, tables, sets, sequences, pairs, and complex values at the console.

With each call to the internal printing routine, the interpreter uses the respective environ.aux.print* function or settings defined in the lib/library.agn file. You may change these functions or settings according to your needs.
\begin{tabular}{l|l|l|}
\hline Table index & Type & Functionality \\
\hline environ.aux.printtable & function & \begin{tabular}{l} 
defines how to print a table, overriding \\
the built-in default
\end{tabular} \\
\hline environ.aux.printlongtable & function & \begin{tabular}{l} 
defines how to print a table if \\
kernel/longtable has been set true
\end{tabular} \\
\hline environ.aux.printset & function & \begin{tabular}{l} 
defines how to print a set, overriding the \\
built-in default
\end{tabular} \\
\hline environ.aux.printsequence & function & \begin{tabular}{l} 
defines how to print a sequence, \\
overriding the built-in default
\end{tabular} \\
\hline environ.aux.printpair & function & \begin{tabular}{l} 
defines how to print a pair, overriding the \\
built-in default
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Table index & Type & Functionality \\
\hline environ.aux.printcomplex & function & \begin{tabular}{l} 
defines how to print a complex value, \\
overriding the built-in default
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{l|l|l|}
\hline Table index & Type & Functionality \\
\hline \begin{tabular}{l} 
environ.aux. \\
printenclosestrings
\end{tabular} & string & \begin{tabular}{l} 
if set, Agena outputs strings with the \\
prepending and appending string that is \\
assigned to \\
environ.aux.printenclosestrings
\end{tabular} \\
\hline environ.aux.printprocedure function & \begin{tabular}{l} 
defines how to print a procedure, \\
overriding the built-in default
\end{tabular} \\
\hline
\end{tabular}

Table 24: Printing functions
Alternative environ.aux.print* functions might look like the following one:
```

> environ.aux.printset := proc(s) is
write('set(');
if size s > 0 then
for i in s do
write(i, ', ');
od;
write('\b\b');
fi;
write(')');
end;
environ.aux.printcomplex := proc(s) is
write('cmplx(', real(s), ', ', imag(s), ')');
end;
> {1, 2}:
set(1, 2)
> 1*2*I:
cmplx(1, 2)

```

\section*{A7 The Agena Initialisation File}

You can customise your personal Agena environment via special initialisation files.
The initialisation files may include code written agena and will always be executed when Agena is started or restarted. They can include definitions or redefinitions of predefined (environment) variables, and feature self-written procedures or statements to be executed at start-up.

Two kinds of initialisation files are supported:
1. a global initialisation file, and
2. a personal initialisation file for the current user.

Agena first tries to read the global initialisation file, and then the user's initialisation file. If the initialisation files do not exist, nothing happens and Agena starts without errors.

The global initialisation file should reside in the lib folder of your Agena installation and is always named agena. ini for all operating systems. You may find your Agena
installation in /usr/agena on UNIX platforms, and usually in <drive:>/Program Files/Agena Or <drive:>/Program Files(x86)/Agena On Windows systems.

In Solaris, Linux, Mac OS X, the personal initialisation file resides in the folder pointed to be the нome environment variable. The personal Agena initialisation file on UNIX machines is called .agenainit (not agena.ini). Thus the path is \$Home/.agenainit.

In Windows, the system environment variable userProfile points to the user's home folder, and the personal initialisation file is called agena.ini, (not .agenainit), thus the file path is \%UserProfile\%/agena.ini.

On Windows platforms, the user's initialisation file should be put into the user's respective home folder:
\begin{tabular}{|l|l|}
\hline Windows version & Path to user's home directory \\
\hline NT 4.0 & <drive:>\WINNT\Profiles\<username> \\
\hline 2000, XP, 2003 & <drive:>\Documents and Settings\<username> \\
\hline Vista and later & <drive:>\Users\<username> \\
\hline
\end{tabular}

Table 25: Windows' ‘home` paths
In OS/2 and DOS, Agena tries to find the user's personal agena.ini file in the directory pointed to by the environment variable номе, if it has been defined. If HOME has not been defined, it searches in the folder pointed to by the environment variable uSER, if the latter has been defined. Otherwise, the personal file is not read.

Agena is shipped with a file called agena.ini. sample that resides in the lib folder of your installation. You can rename it to agena.ini Or . agenainit and play with it - but beware not to overwrite the initialisation which you may already have created.

Here is a sample file:
```

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# 

# Agena initialisation file

# 

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# assign short names for the following library functions:

execute := os.execute;
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# Extend libname to include paths to additional libraries (but only

# if directories exist)

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
if os.isWin() or os.isOS2() or os.isDOS() then
addpaths := seq(
'd:/agena/phq',
'd:/agena/pcomp'
)
elif os.isSolaris() then
addpaths := seq(
'/export/home/proglang/agena/phq',
'/export/home/proglang/agena/pcomp'

```
```

    )
    elif os.isLinux() then
addpaths := seq(
'~/agena/phq',
'~/agena/pcomp'
)
fi;
for i in addpaths do
if os.exists(i) and i in libname = null then
libname := libname \& ';' \& i
fi
od;
clear addpaths;
writeline('Have fun with Agena !\n');

```
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
\# Set default plotting options for gdi.plotfn
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
import gdi;
gdi. setoptions(colour~'red', axescolour~'grey');

\section*{A8 Escape Sequences}

Agena supports the following escape sequences known from ANSI C:
\begin{tabular}{|l|l|}
\hline Sequence & Meaning \\
\hline la & alert \\
\hline Ib & backspace \\
\hline If & formfeed \\
\hline In & new line \\
\hline Ir & carriage return \\
\hline It & horizontal tabulator \\
\hline IV & vertical tabulator \\
\hline XAB & hex escape \\
\hline Iz & \begin{tabular}{l} 
lkips subsequent white-space characters, including line breaks; it is \\
particularly useful to break and indent a long literal string into \\
multiple lines without adding the newlines and spaces into the string \\
contents
\end{tabular} \\
\hline
\end{tabular}

Table 26: Escape sequences
```

> print('{\n\z
> \x20 \"\104ello\": \"world\"\n\z
}')
"hello": "world"
}

```

\section*{A9 Backward Compatibility}

Aliases for deprecated functions in Agena versions prior to 1.0 are no longer automatically initialised at start-up. However, by entering
```

> import compat;

```
you can activate them in your current session if you prefer compatibility to Agena 1.0. For all other cases, please consult the change. log file distributed with the source and binary editions.

This concerns all deprecated function names in the base library, in the math, package, strings, tables, utils packages, as well as the former _Env* environment control variables.

Deprecated names of functions in the linalg package can only be used by uncommenting the alias assignments at the bottom of the lib/linalg.agn file.

Users of the mapm package should first import the mapm package and then load the compat.agn file.

\section*{A10 Some Few Technical Notes}

All Solaris and RedHat binaries of Agena have been created with GCC 4.4.5, the Debian x86 binaries with GCC 6.3.0 and the AMD64 binaries with GCC 11.2.

All OS/2 binaries have been created with Paul Smith's GCC 4.4.6.

All Windows binaries of Agena have been created with MinGW/GCC 6.3.0.
All Mac OS X binaries of Agena have been created with Apple's GCC 4.2.1.
The DOS version is being compiled with DJGPP/GCC 12.1.0.
The C Sources should be ANSI C99 compatible, mostly due to Agena's support of complex arithmetic.

\section*{Appendix B}

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Although their code does not appear in gd, the authors wish to thank David Koblas, David Rowley, and Hutchison Avenue Software Corporation for their prior contributions.

\section*{Appendix C}

\section*{Cl : Further Reading}

A selection of books that helped a lot in recent years when developing Agena:
- Niklaus Wirth: Algorithmen und Datenstrukturen mit Modula-2
- Roberto lerusalimschy: Programming in Lua
- Roberto lerusalimschy, Luiz Henrique de Figueirido, Waldemar Celes: Lua 5.1 Reference Manual
- Kurt Jung \& Aaron Brown: Beginning Lua Programming
- Jürgen Wolf: C von A bis Z
- Brian W. Kernighan \& Dennis M. Ritchie: The C Programming Language
- Federico Biancuzzi \& Shane Warden (Ed.): Masterminds of Programming
- Michael. B. Monagan, Keith O. Geddes, K. M. Heal, G. Labahn, S. M. Vorkoetter, J. McCarron, P. DeMarco: Maple 7 Programming Guide
- Brian "Beej Jorgensen" Hall, Beej's Guide to Network Programming, Using Internet Sockets
- Jan Jones: QL SuperBASIC - The Definitive Handbook
- Frank G. Pagan: A Practical Guide to Algol68

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[^0]:    ${ }^{19}$ For an excellent introduction on implementing linked lists, see "Linked List Basics", Copyright © 1998-2001, Nick Parlante. This quote has been taken from his manual, page 4.

[^1]:    ${ }^{20}$ Please note that for $-5 \leqslant x<0$, the result is an approximation.

[^2]:    ${ }^{21}$ The = operator just checks whether an element in one structure is residing at any position in the other structure, whereas the $==$ and $\sim=$ operators check elements place-by-place. Developers who would like to extend the linalg package may also have a look at the _eeq and _aeq metamethod. to influence the behaviour of the $==$ and $\sim=$ operators, respectively.

[^3]:    ${ }^{22}$ See also io.readfile to read a file entirely.

